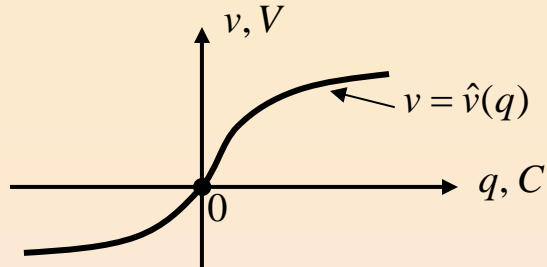


CAPACITOR

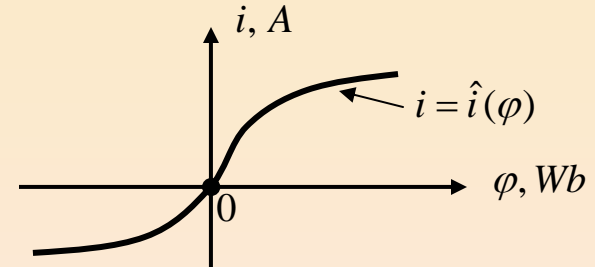
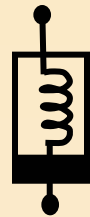


Element Law : $v = \hat{v}(q)$

where **charge**

$$q(t) \triangleq \int_{-\infty}^t i(\tau) d\tau$$

INDUCTOR

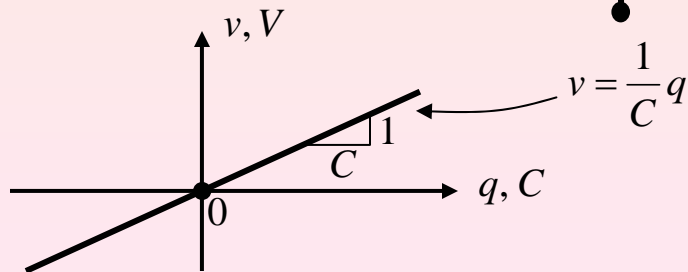
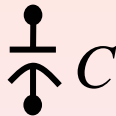


Element Law : $i = \hat{i}(\varphi)$

where **flux**

$$\varphi(t) \triangleq \int_{-\infty}^t v(\tau) d\tau$$

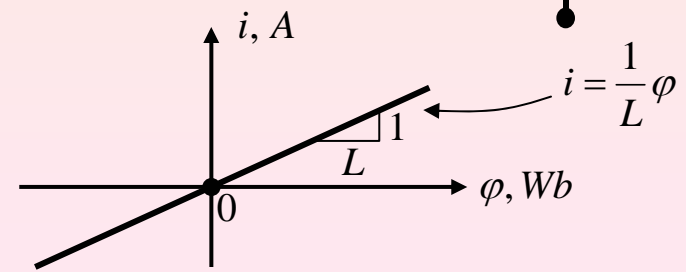
Special case : Linear Capacitor



Element Law : $q = C v$

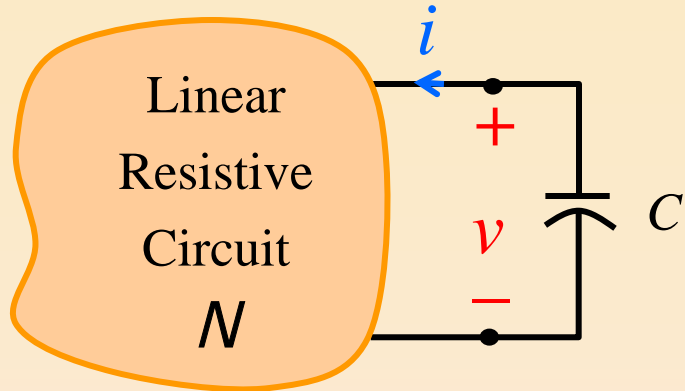
$$i(t) = C \frac{dv(t)}{dt}$$

Special case : Linear Inductor

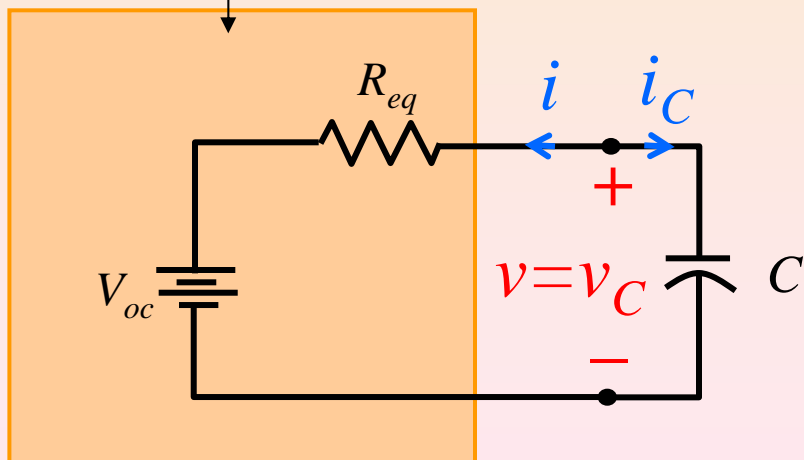


Element Law : $\varphi = L i$

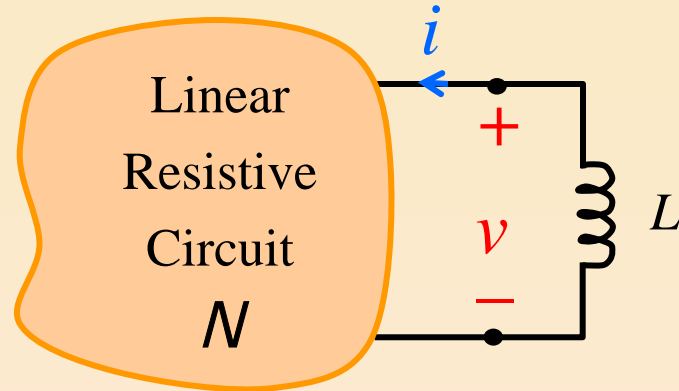
$$v(t) = L \frac{di(t)}{dt}$$



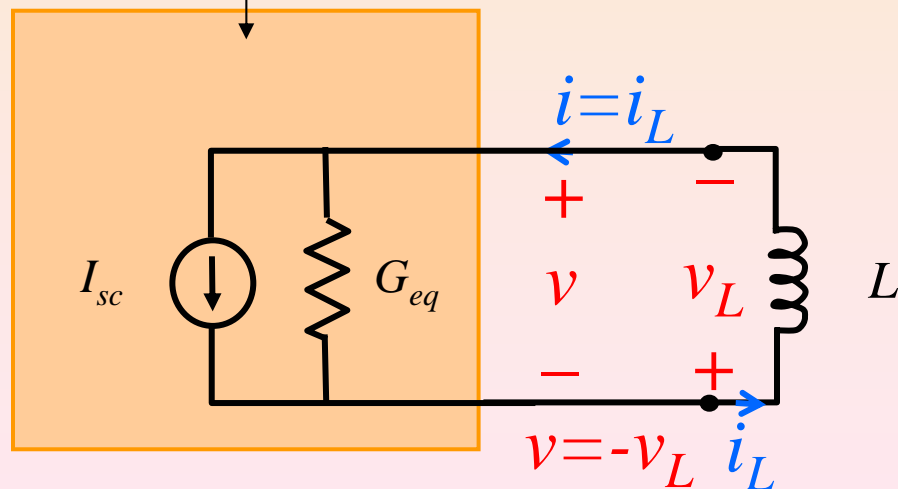
Thevenin Equivalent Circuit of N



$$\frac{dv_C}{dt} = -\frac{v_C}{R_{eq}C} + \frac{V_{oc}}{R_{eq}C}$$

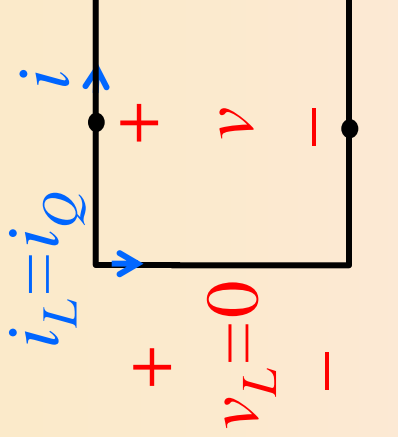


Norton Equivalent Circuit of N



$$\frac{di_L}{dt} = -\frac{i_L}{G_{eq}L} + \frac{I_{sc}}{G_{eq}L}$$

Equilibrium Points

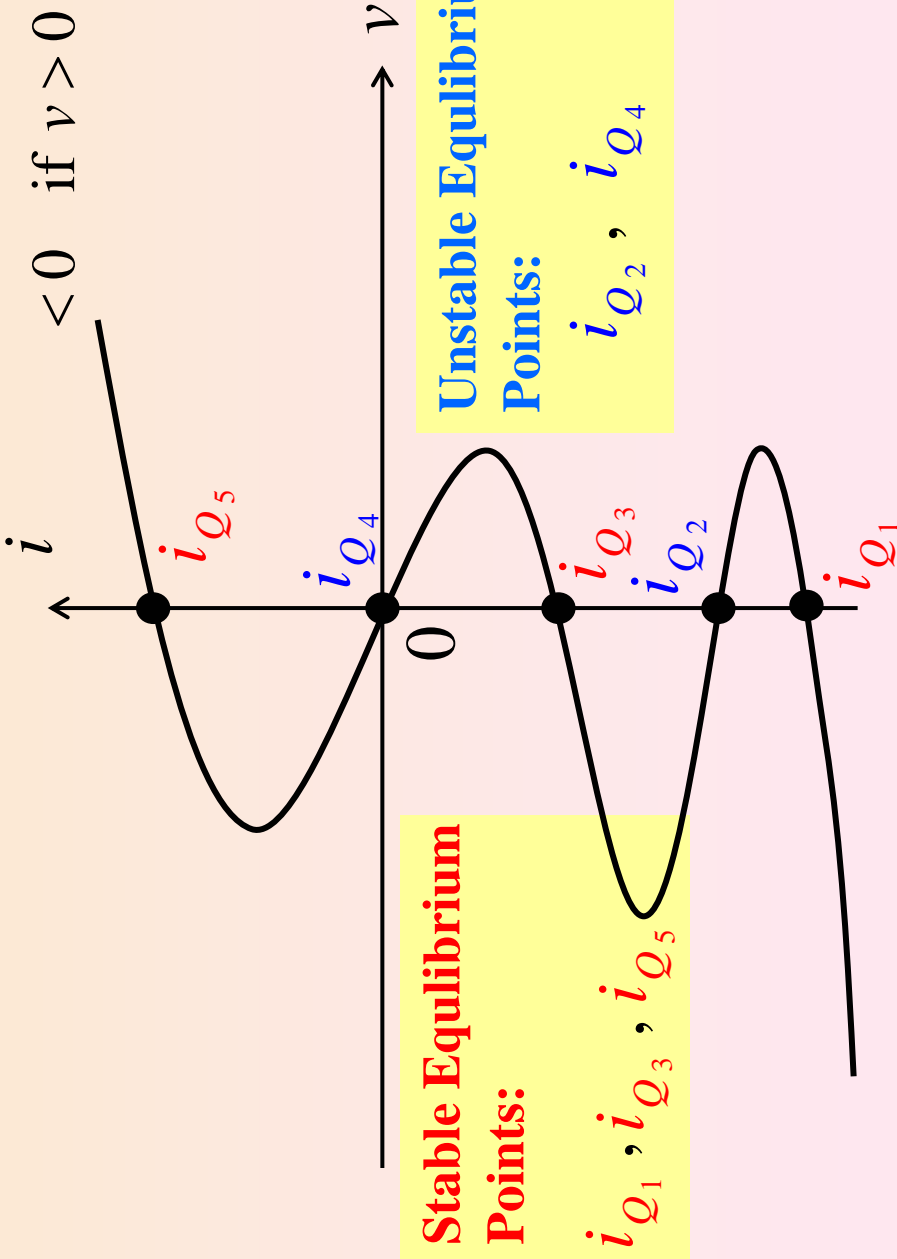


$$\frac{di}{dt} = \frac{-v}{L}$$

$$> 0 \quad \text{if } v < 0$$

$$= 0 \quad \text{if } v = 0$$

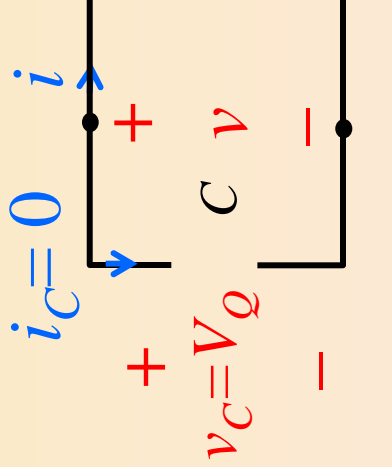
$$i < 0 \quad \text{if } v > 0$$



Conclusion

Each short-circuit inductor current i_{Q_j} is an **Equilibrium Point** of this RL circuit.

Equilibrium Points

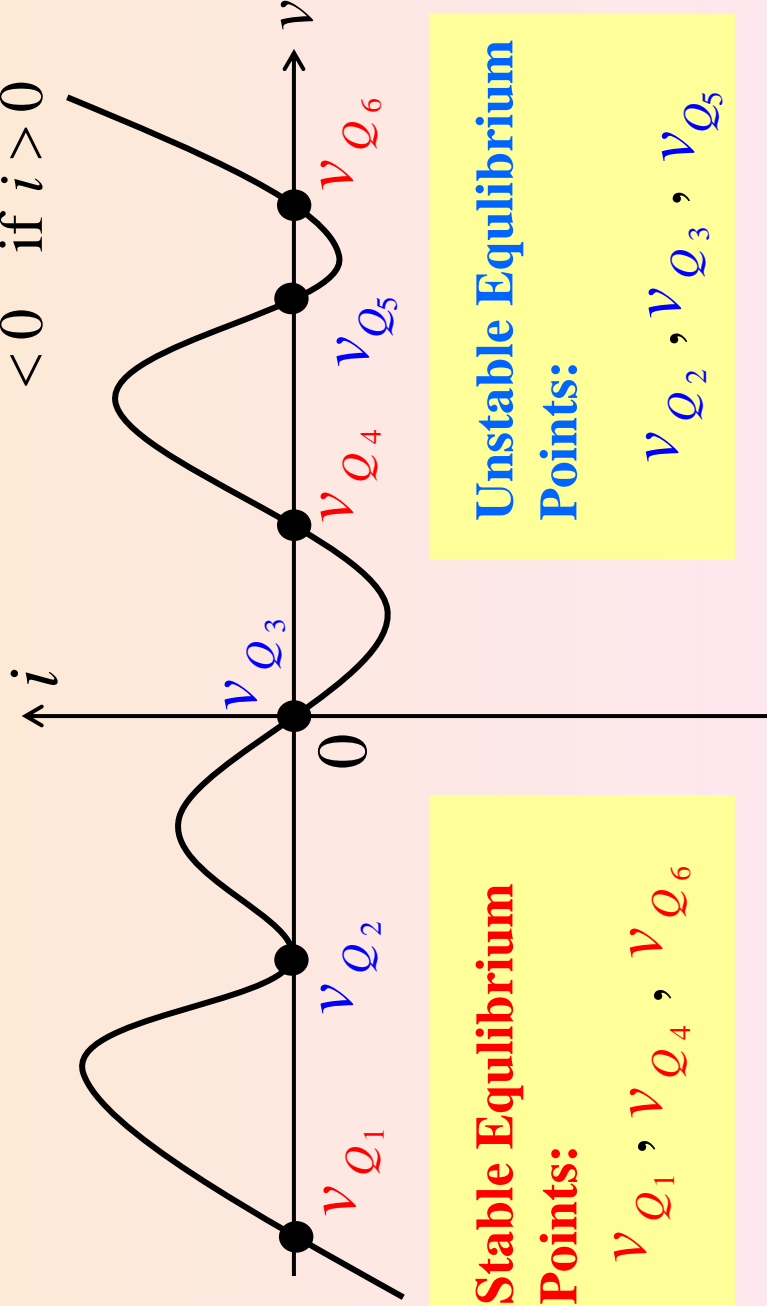


$$\frac{dv}{dt} = \frac{-i}{C}$$

$$> 0 \quad \text{if } i < 0$$

$$= 0 \quad \text{if } i = 0$$

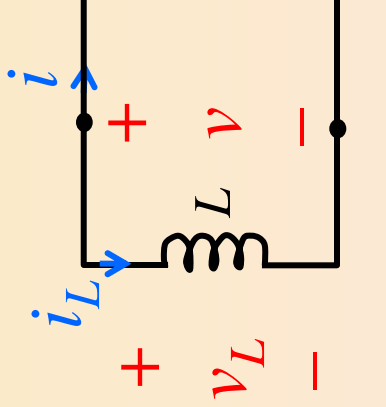
$$< 0 \quad \text{if } i > 0$$



Conclusion

Each open-circuit capacitor voltage v_{Q_j} is an **Equilibrium Point** of this RC circuit.

Equilibrium Points

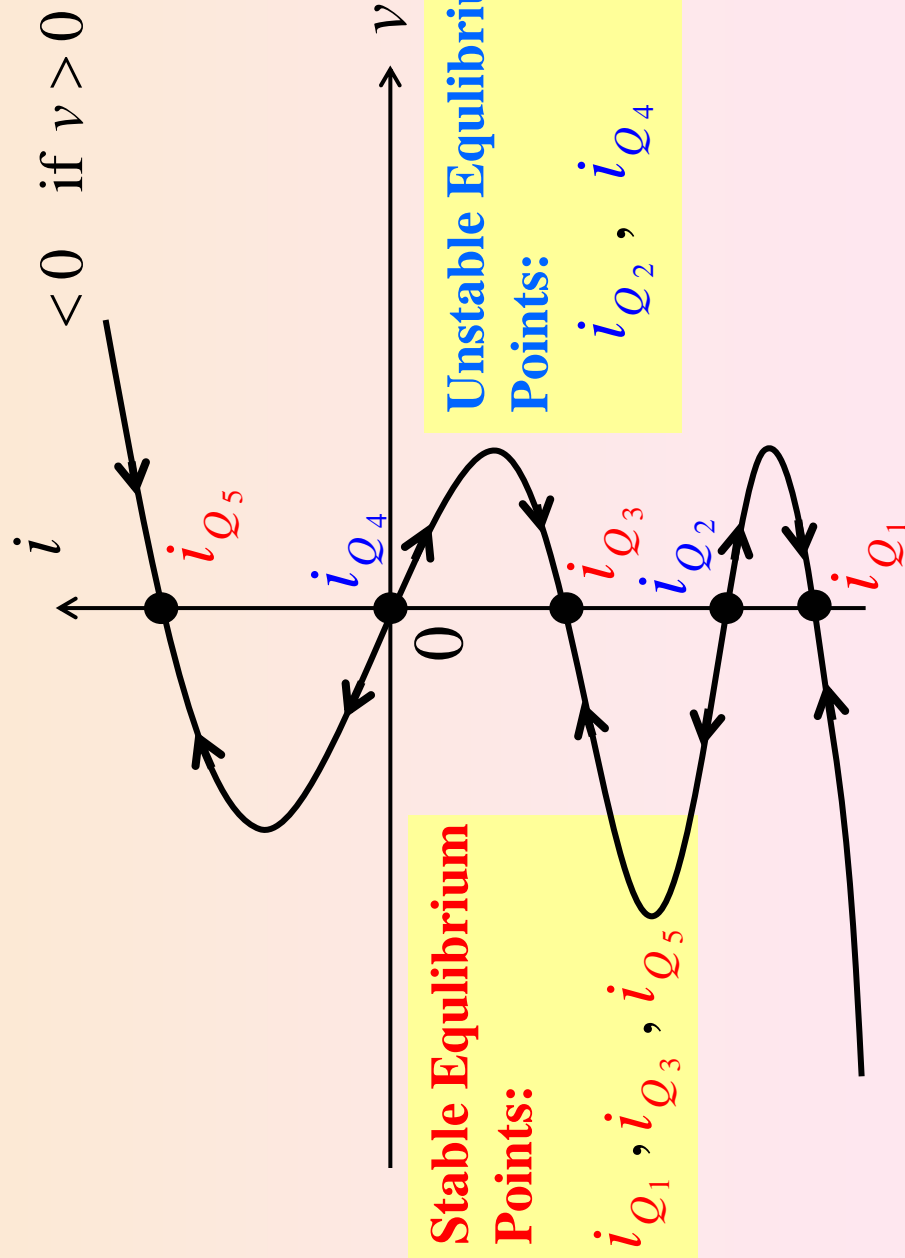


$$\frac{di}{dt} = \frac{-v}{L}$$

$$> 0 \quad \text{if } v < 0$$

$$= 0 \quad \text{if } v = 0$$

Resistive
One-Port



Stable Equilibrium Points:

$$i_{Q_1}, i_{Q_3}, i_{Q_5}$$

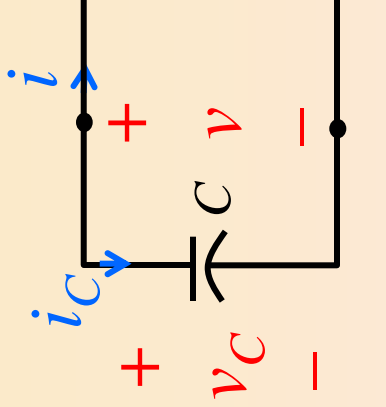
Unstable Equilibrium Points:

$$i_{Q_2}, i_{Q_4}$$

Conclusion

Each short-circuit inductor current i_{Q_j} is an **Equilibrium Point** of this RL circuit.

Equilibrium Points

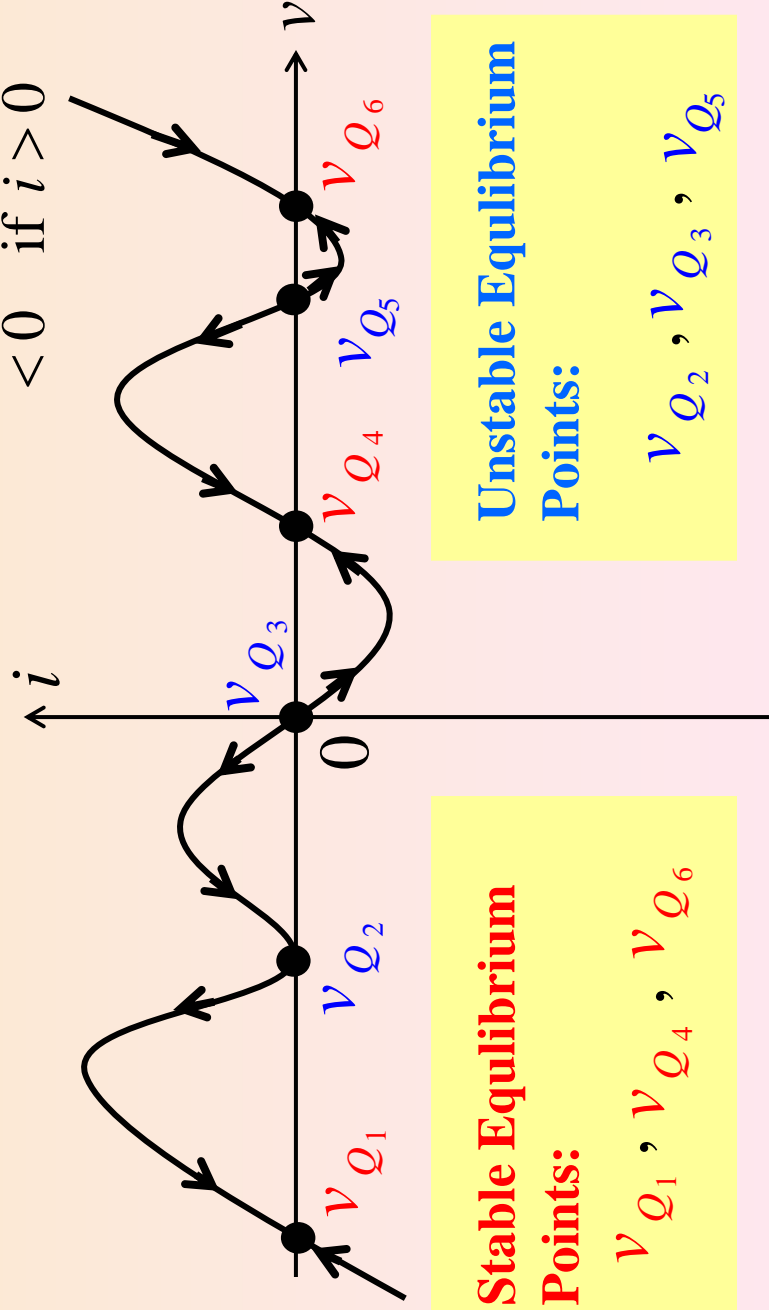


$$\frac{dv}{dt} = \frac{-i}{C}$$

$$> 0 \quad \text{if } i < 0$$

$$= 0 \quad \text{if } i = 0$$

$$< 0 \quad \text{if } i > 0$$



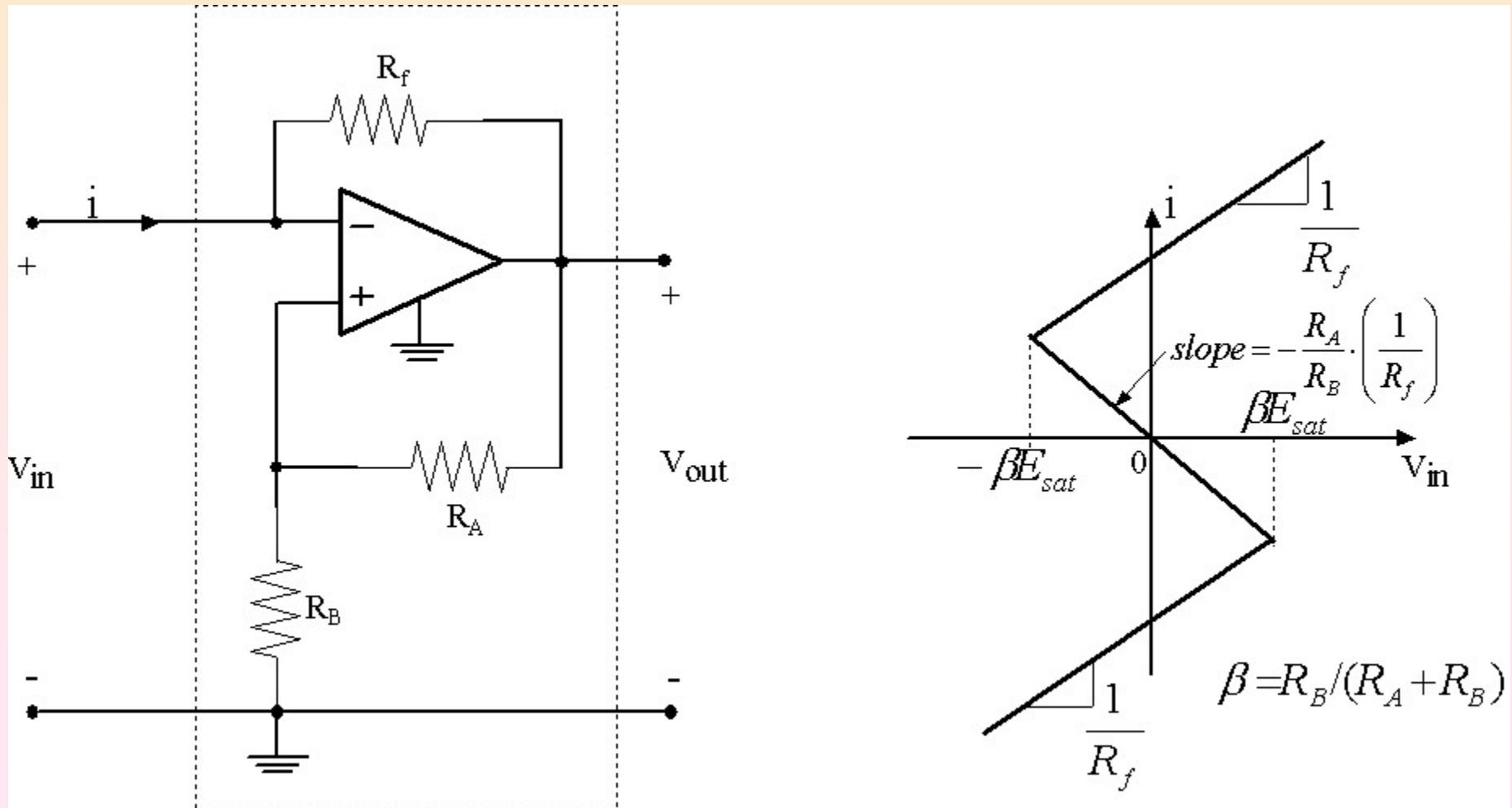
Stable Equilibrium Points:
 $v_{Q_1}, v_{Q_4}, v_{Q_6}$

Unstable Equilibrium Points:
 $v_{Q_2}, v_{Q_3}, v_{Q_5}$

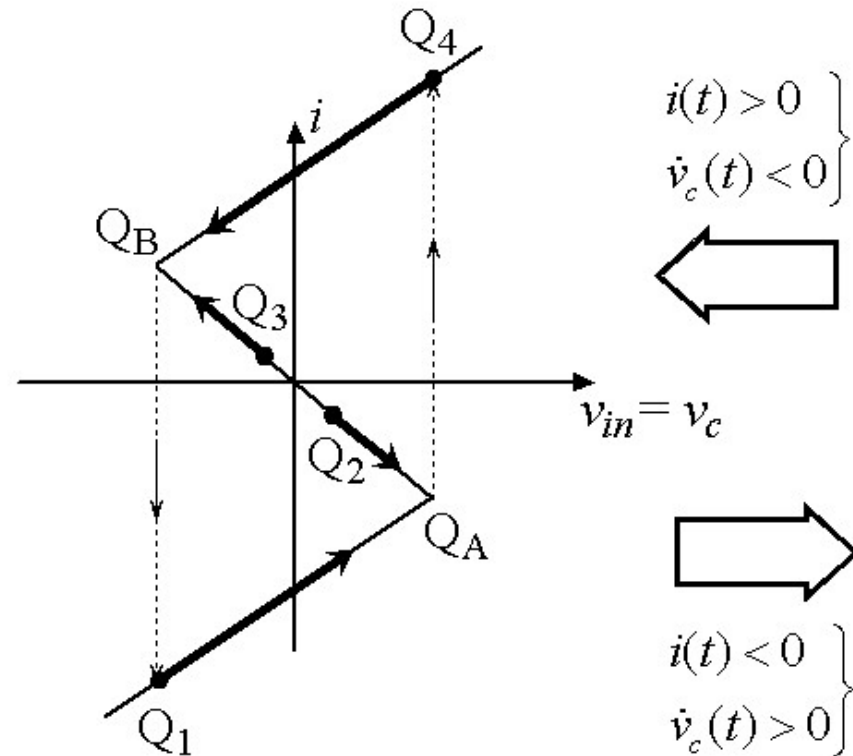
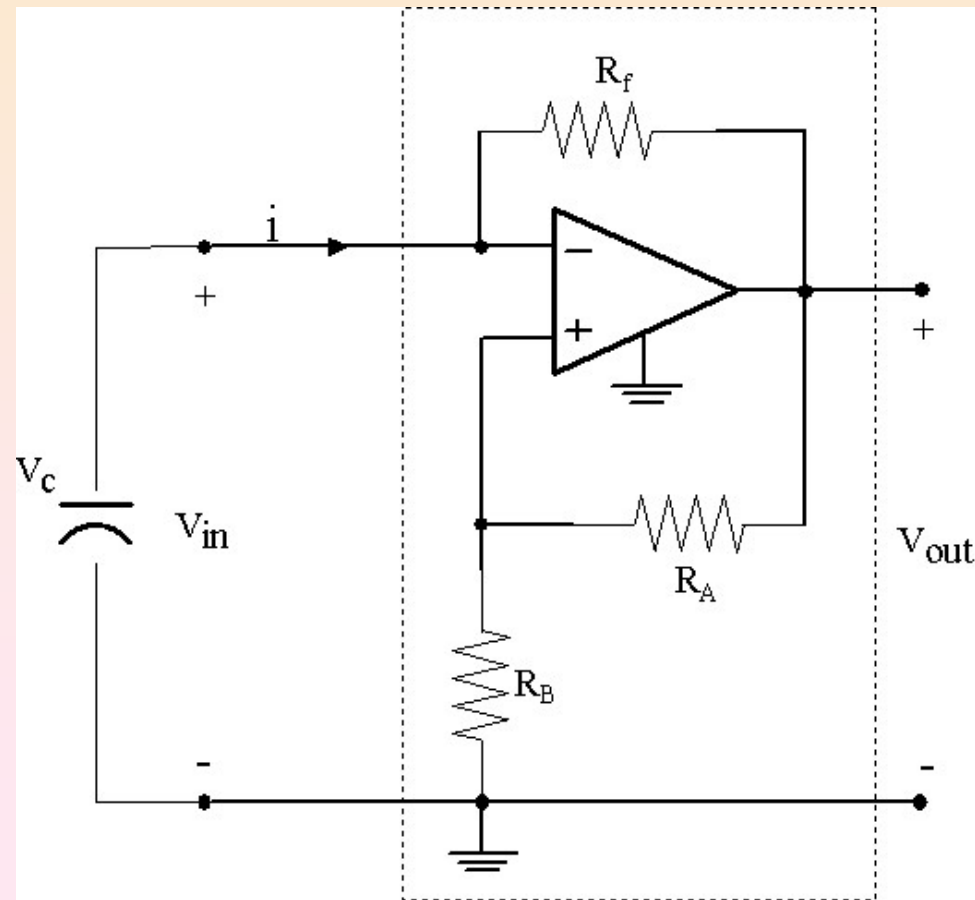
Conclusion

Each open-circuit capacitor voltage v_{Q_j} is an **Equilibrium Point** of this RC circuit.

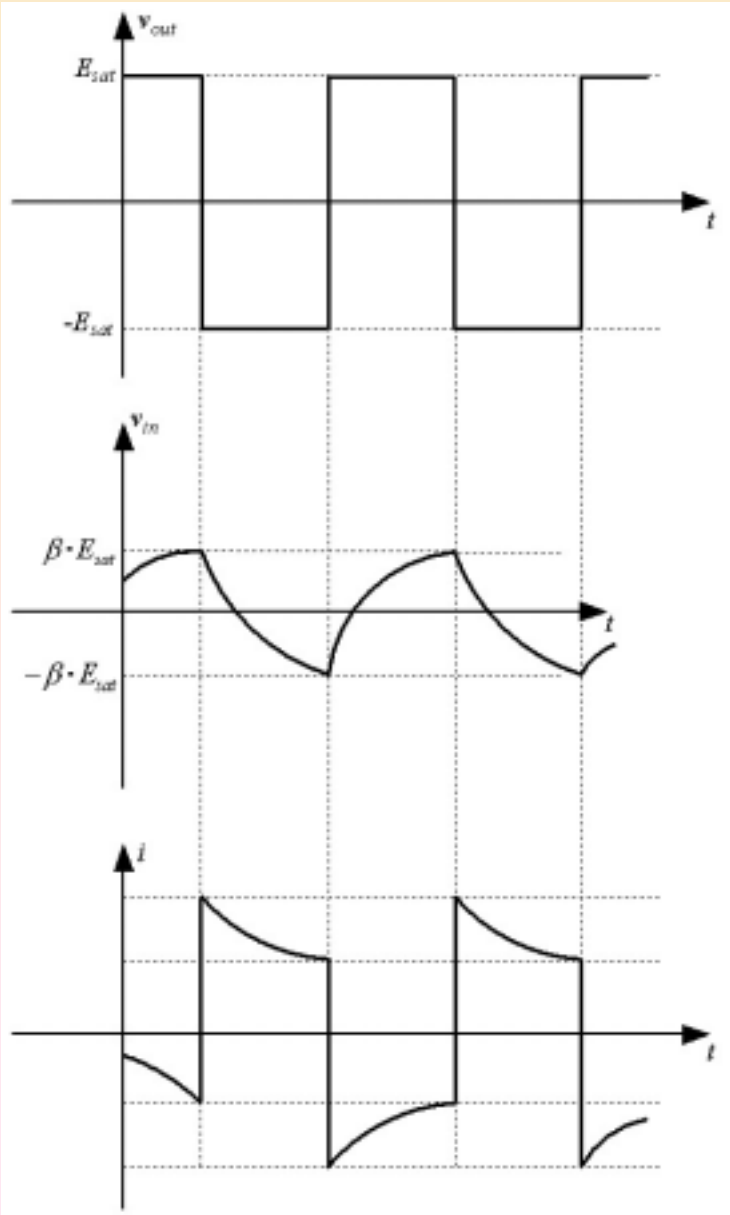
Negative Resistance Converter and its Driving-Point Characteristic



An Astable RC op-amp Circuit and its Driving-Point Characteristic



Waveforms of the Astable RC op-amp Circuit

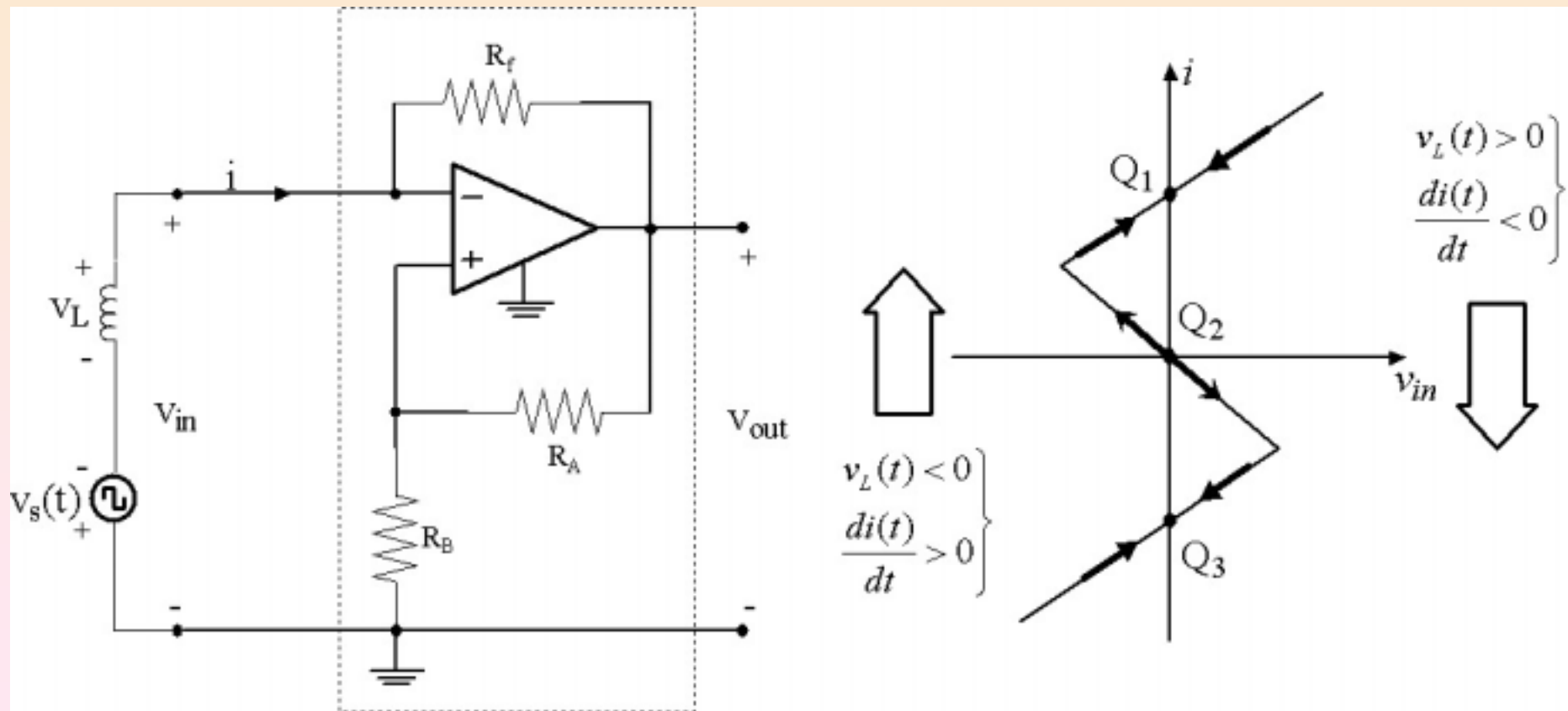


Output Voltage

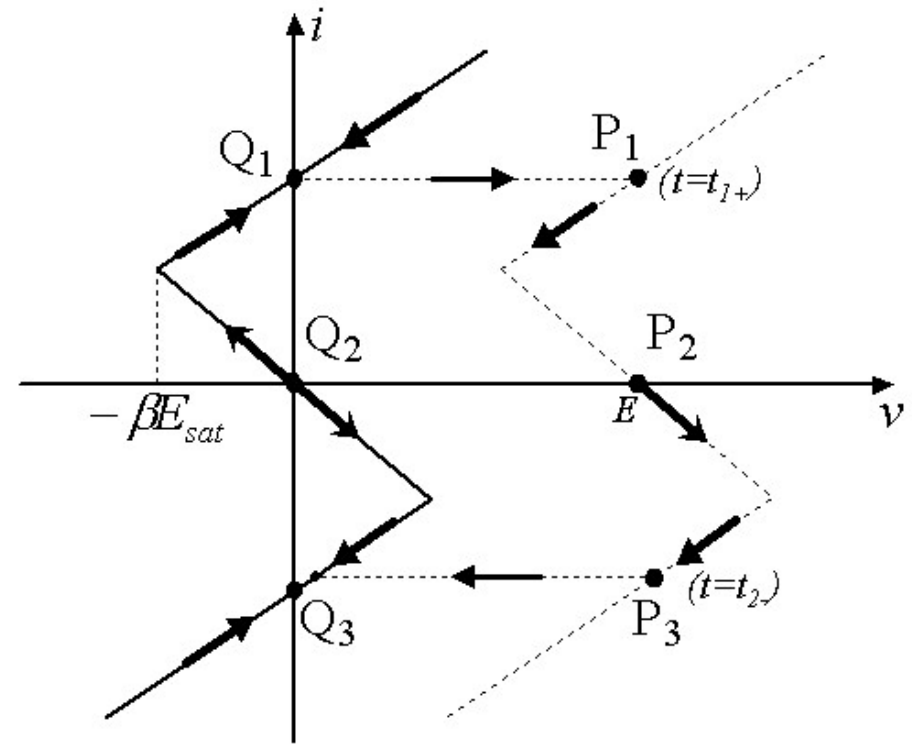
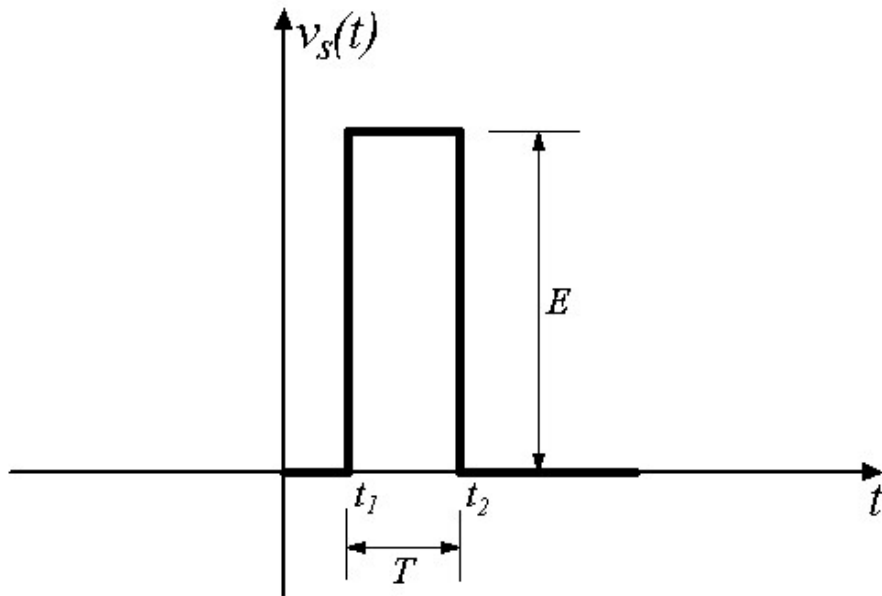
Input Voltage

Input Current

A Bi-stable op-amp Circuit and its Driving Point Characteristic

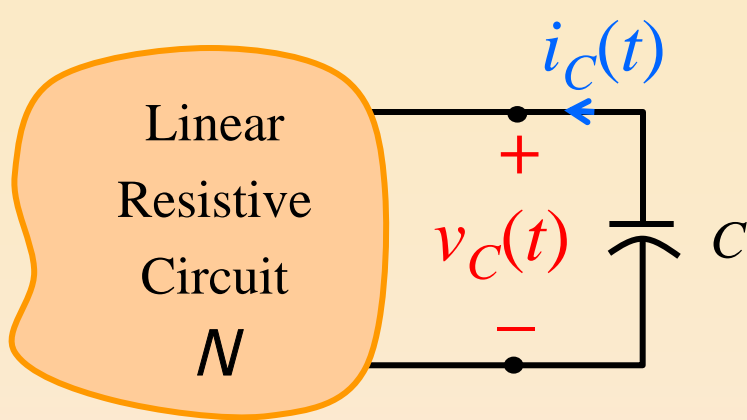


Dynamic Route of the Bi-stable op-amp Circuit Corresponding to a Square Pulse Triggering Signal



Impasse Point

A point Q is called an **impasse point** whenever a **dynamic route** starting from $t = t_j$ reaches Q at some **finite** time $t = t_k > t_j$ and can *not* be continued for $t > t_k$ without violating the capacitor (resp., inductor) element law.



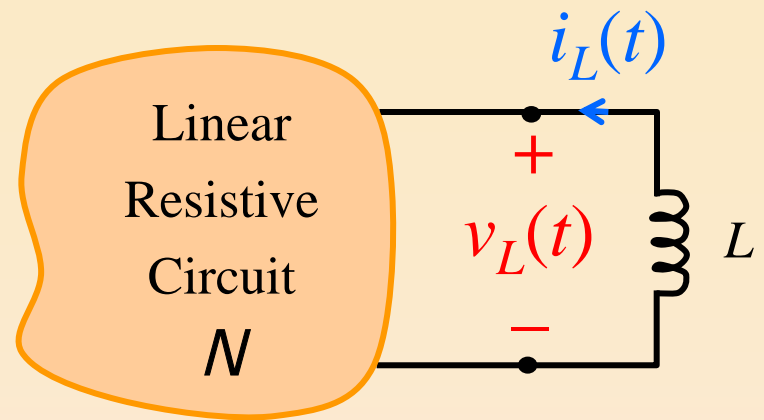
Capacitor Voltage Continuity Theorem

The **voltage** $v_C(t)$ across a **capacitor** can *not* change abruptly at any time $t = t_k$, provided

$$i_C(t_k) \neq \pm \infty$$

namely,

$$v_C(t_k^+) = v_C(t_k^-)$$



Inductor Current Continuity Theorem

The **current** $i_L(t)$ through an **inductor** can *not* change abruptly at any time $t = t_k$, provided

$$v_L(t_k) \neq \pm \infty$$

namely,

$$i_L(t_k^+) = i_L(t_k^-)$$

Proof.

$$i_C(t) = C \frac{dv_C(t)}{dt}$$

$$\Rightarrow v_C(t) = \frac{1}{C} \int_{-\infty}^t i_C(\tau) d\tau$$

$$v_C(t_k^- + \Delta t) = \underbrace{\frac{1}{C} \int_{-\infty}^{t_k^-} i_C(\tau) d\tau}_{v_C(t_k^-)} + \underbrace{\frac{1}{C} \int_{t_k^-}^{t_k^- + \Delta t} i_C(\tau) d\tau}_{A_\Delta}$$

$$= v_C(t_k^-) + \frac{1}{C} (A_\Delta)$$

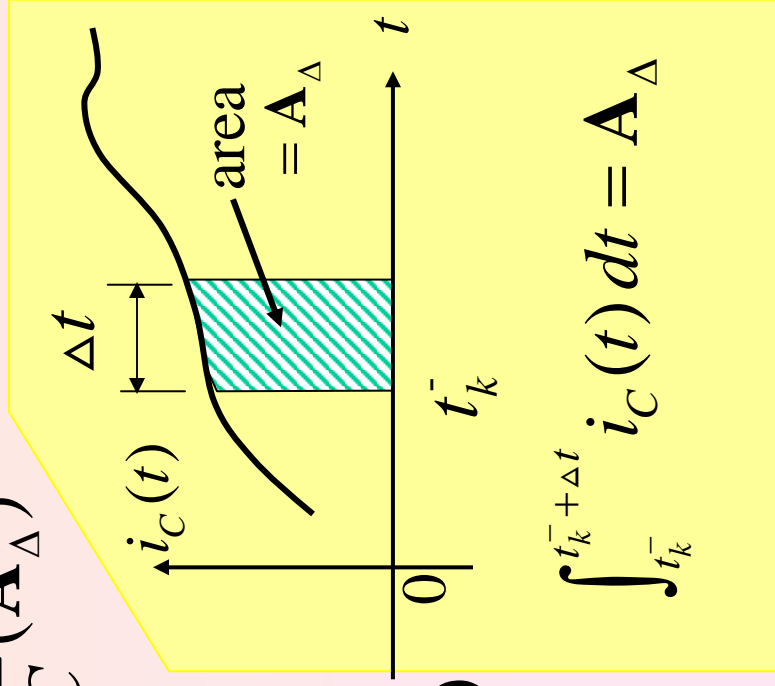
as $\Delta t \rightarrow 0$,

$t_k^- + \Delta t \rightarrow t_k^+$ and

$A_\Delta \rightarrow 0$

(provided $i_C(t_k) \neq \pm\infty$)

$$\therefore v_C(t_k^+) = v_C(t_k^-)$$



Jump Rule

Capacitor Current Jump Rule

Upon reaching an **impasse point** Q at $t = t_k^-$ in an **RC circuit**, the **dynamic route jumps abruptly** to a point on the v - i curve at $t = t_k^+$ such that

$$v_C(t_k^+) = v_C(t_k^-)$$

Inductor Voltage Jump Rule

Upon reaching an **impasse point** Q at $t = t_k^-$ in an **RL circuit**, the **dynamic route jumps abruptly** to a point on the v - i curve at $t = t_k^+$ such that

$$i_L(t_k^+) = i_L(t_k^-)$$