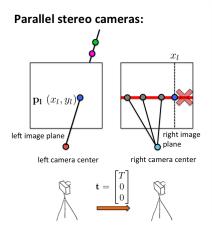
Stereo Epipolar Geometry for General Cameras

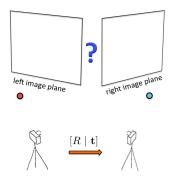
Stereo

Epipolar geometry

- Case with two cameras with parallel optical axes
- General case \leftarrow **Now this**







• If I can always mount two cameras parallel to each other, why do I need to learn math for the general case?

• Let's say that you want to reconstruct a CN tower in 3D

- Let's say that you want to reconstruct a CN tower in 3D
- One out of endless possibilities of why you would do that:
 - You can print it with a 3D printer to get a nice pocket or not-so-pocket edition (better than those that are sold in Chinatown)
 - Give it to your mum for Christmas (say it's a present from CSC420)



- Let's say that you want to reconstruct a CN tower in 3D
- You obviously can't get a good 360 shot of the CN tower with just parallel cameras. Particularly not the top of the CN tower which is very high up.

- Let's say that you want to reconstruct a CN tower in 3D
- You obviously can't get a good 360 shot of the CN tower with just parallel cameras. Particularly not the top of the tower.
- But you can download great images of the tower from the web without even needing to leave the house.

• But these images are not taken from parallel cameras...



Photosynth

• You could even do part of Venice...

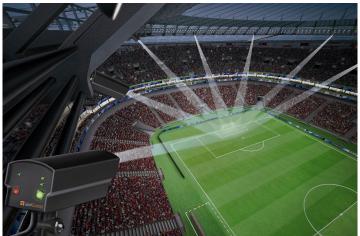


Figure: https://www.youtube.com/watch?v=HrgHFDPJHXo

Noah Snavely, Steven M. Seitz, Richard Szeliski, "Photo tourism: Exploring photo collections in 3D", SIGGRAPH 2006, https://photosynth.net/

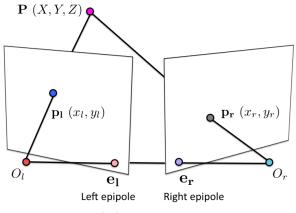
World Cup 2014 - High Tech 3D

- Last World Cup was monitored with 14 high-speed cameras, capturing 500 frames per second, and could accurately detect ball motion to within 5mm.
- 2,000 tests performed, all successful. By German company Goal Control.



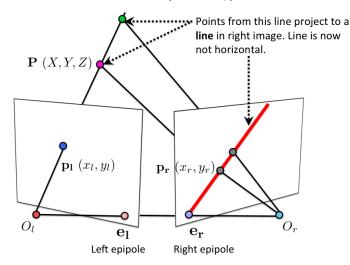
Stereo – General Case Ready for the math?

• Some notation: the left and right epipole

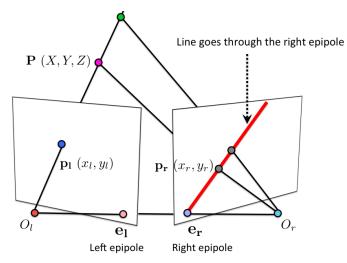


Where line $O_l O_r$ intersects the image planes

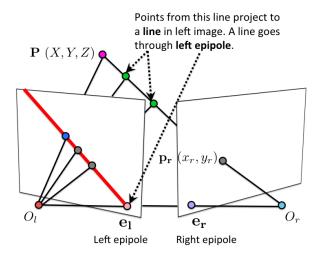
• All points from the projective line **O**₁**p**₁ project to a line on the right image plane. This time the line is not (necessarily) horizontal.



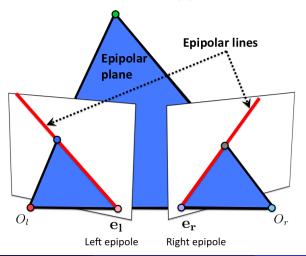
• The line goes through the right epipole.



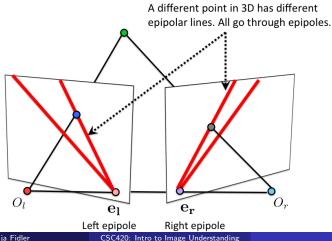
• Similarly, All points from the projective line **O**_r**p**_r project to a line on the left image plane. This line goes through the left epipole.



• The reason for all this is simple: points **O**_I, **O**_r, and a point **P** in 3D lie on a plane. We call this the **epipolar plane**. This plane intersects each image plane in a line. We call these lines **epipolar lines**.

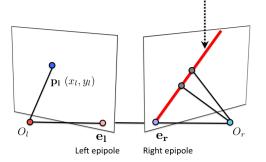


• Obviously a different point in 3D will form a different epipolar plane and therefore different epipolar lines. But these epipolar lines go through epipoles as well.



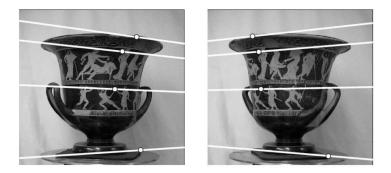
• Why are we even dumping all this notation? Are epipolar lines, epipoles, etc somehow useful?

- Remember what we did for parallel cameras? We were matching points in the left and right image, giving us a point in 3D. We want the same now.
- Epipolar geometry is useful because it constrains our search for the matches:
 - For each point p_l we need to search for p_r only on a epipolar line (much simpler than if I need to search in the full image)
 - All matches lie on lines that intersect in epipoles. This gives another constraint.



Epipolar geometry: Examples

• Example of epipolar lines for converging cameras



[Source: J. Hays, pic from Hartley & Zisserman]

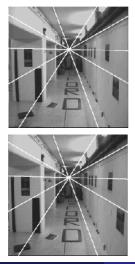
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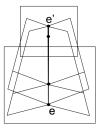
• How would epipolar lines look like if the camera moves directly forward?

[Source: J. Hays]

Epipolar geometry: Examples

• Example of epipolar lines for forward motion





Epipole has same coordinates in both images.

Points move along lines radiating from e: "Focus of expansion"

[Source: J. Hays, pic from Hartley & Zisserman]

- $\bullet\,$ We first need to figure out on which line we need to search for the matches for each \mathbf{p}_{l}
- Each point in left image maps to a line in right image. We will see that this mapping can be described by a single 3 × 3 matrix **F**, called the **fundamental matrix**

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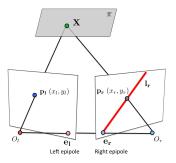
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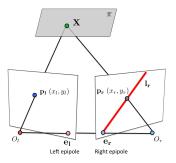
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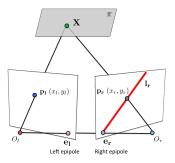
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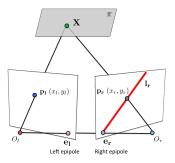


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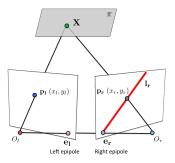
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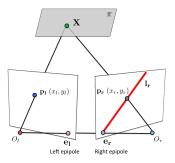
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[Adopted from: R. Urtasun]

Sanja Fidler



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=0, because \mathbf{p}_r lies on a line \mathbf{I}_r

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- Then you can get the parameters $\mathbf{f} := [F_{11}, F_{12}, \dots, F_{33}]$ by solving:

$$\begin{bmatrix} x_{r,1} & x_{l,1} & x_{r,1} & y_{l,1} & x_{r,1} & y_{r,1} & x_{l,1} & y_{r,1} & y_{l,1} & y_{l,1} & 1 \\ \vdots & & & & \\ x_{r,n} & x_{l,n} & x_{r,n} & y_{l,n} & x_{r,n} & y_{r,n} & x_{l,n} & y_{r,n} & y_{l,n} & y_{l,n} & 1 \end{bmatrix} \mathbf{f} = \mathbf{0}$$

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- See Zisserman & Hartley's book for details.

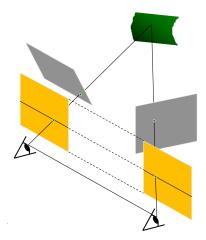
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Rectification

- Once we have F we can compute homographies that transform each image plane such that they are parallel (see Zisserman & Hartley's book)
- Once they are parallel, we know how to proceed (matching, etc)



[Source: J. Hays]

Rectification Example



[Source: J. Hays]

Sanja Fidler

The Fundamental Matrix: One Last Thing

Once you have F you can even compute camera projection matrices
 P₁ and P_r (under some ambiguity). You may choose the camera projection matrices like this:

- This means that I don't need the relative poses of the two cameras, I can compute it!
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w

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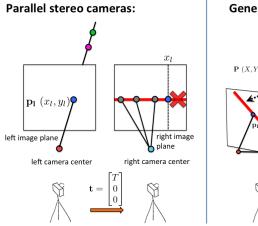
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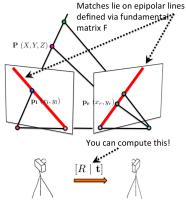
Stereo: Summary

Epipolar geometry

- Case with two cameras with parallel optical axes
- General case







Summary – Stuff You Need To Know

Cameras with parallel optics and known intrinsics and extrinsics:

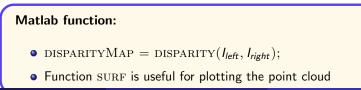
- You can search for correspondences along horizontal lines
- The difference in x direction between two correspondences is called disparity:

disparity
$$= x_l - x_r$$

• Assuming you know the camera intrinsics and the baseline (distance between the left and right camera canter in the world) you can compute the depth:

$$Z = \frac{f \cdot T}{\text{disparity}}$$

- Once you have Z (depth), you can also compute X and Y, giving you full 3D
- Disparity and depth are inversely proportional

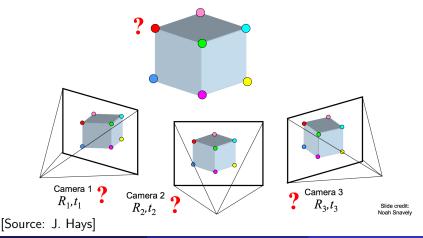


General cameras:

- You first find matches in both images without any restriction. You need at least 7 matches, but the more (reliable) matches the better
- Solve a homogeneous linear system to get the fundamental matrix F
- Given *F*, you can compute homographies that can rectify both images to be parallel.
- Given *F*, you can also compute the relative pose between cameras.

Structure From Motion

- What if you have more than two views of the same scene?
- This problem is called structure-from-motion



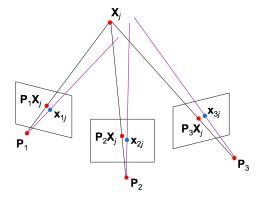
Sanja Fidler

Structure From Motion

• Solve a non-linear optimization problem minimizing re-projection error:

$$E(\mathbf{P}, \mathbf{X}) = \sum_{i=1}^{\#cameras} \sum_{j=1}^{\#points} \operatorname{dist}(\mathbf{x_{ij}}, P_i X_j)$$

• This can be done via technique called bundle adjustment



[Source: J. Hays]

Sanja Fidler

OFRONT Nisamits. • Imagine you are driving a car somewhere in Tokyo

Imagine you are driving a cat somewhere in Tokyo
 You have a phone with GPS, but with tall buildings around you the GPS stops working (*retrieving satellites* appears). You are lost.

Sanja Fidler

CSC420: Intro to Image Understanding

Imagine you are driving a car somewhere in Tokyo
You have a phone with GPS, but with tall buildings around you the GPS stops working (*retrieving satellites* appears). You are lost.
You have a map, but all the signs around you have unrecognizable characters

RONI

Sanja Fidler



What can you do?

HMV

RONI

Imague you are driving a car st new fete in Tokyo
 You have a phone with GPS, but with tall buildings around you have GPS stops working (*retrieving satellites* appears). You are lost
 You have a map, but all the signs around you have unrecognizable characters

• You stop to ask, but most people don't speak English

Take out your phone, start recording the road and $\mathsf{Drive!}$

M. Brubaker, A. Geiger and R. Urtasun Lost! Leveraging the Crowd for Probabilistic Visual Self-Localization CVPR 2013

Paper & Code: http://www.cs.toronto.edu/~mbrubake/projects/map/



[M. Brubaker, A. Geiger and R. Urtasun, CVPR13]

• From consecutive frames you can compute relative camera poses

• The recorded video stream therefore gives you a trajectory you are driving



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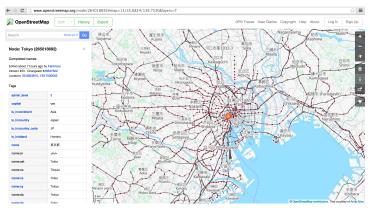


Figure: OpenStreetMap are free downloadable maps (with GPS) of the world

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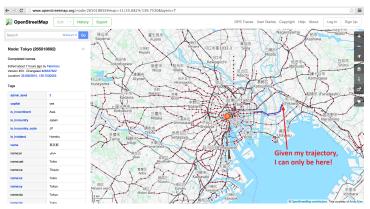


Figure: The shape of my trajectory reveals where I am

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- The recorded video stream therefore gives you a trajectory you are driving
- Probabilistic model reasons where you can be on a map given your trajectory
- This gives you the GPS location!
- With 1 camera up to 18m accuracy, 2 cameras up to 3m accuracy

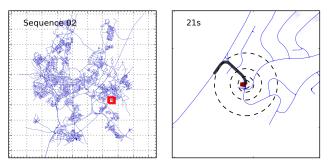


Figure: https://www.youtube.com/watch?v=4Z3shNPOdQA&feature=youtu.be

Vision for Visually Impaired

• You can imagine a more complex version of the system for visually impaired



Pic from: http://www.blogcdn.com/www.engadget.com/media/2012/05/wxzfdgrs.jpg

Vision for Visually Impaired

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- How else could depth / 3D help me?



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Vision for Visually Impaired

- You can imagine a more complex version of the system for visually impaired
- How else could depth / 3D help me?
- What else do we need to solve to make a vision system for visually impaired functional?



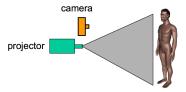
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Another Way to get Stereo: Stereo with Structured Light



Project "structured" light patterns onto the object

- Simplifies the correspondence problem
- Allows us to use only one camera



L. Zhang, B. Curless, and S. M. Seitz. Rapid Shape Acquisition Using Color Structured Light and Multi-pass Dynamic Programming. 3DPVT 2002 [Source: J. Hays]

Kinect: Structured infrared light

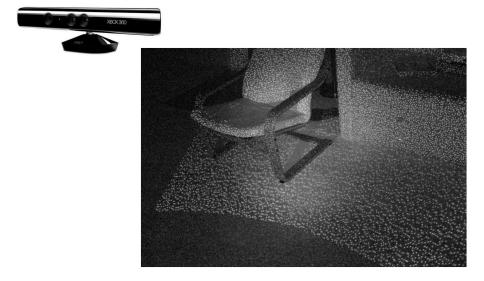


 Figure:
 https://www.youtube.com/watch?v=uq9SEJxZiUg

 ISource:
 Havel

 Sanja Fidler
 CSC420:

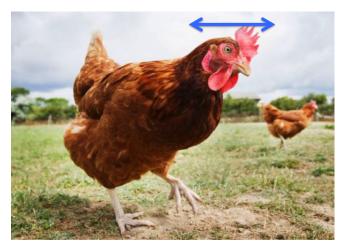
• Humans and a lot of animals (particularly cute ones) have stereoscopic vision



- Most birds don't see in stereo (each eye gets its own picture, no overlap)
- How do these animals get depth? E.g., how can a chicken beak the corn without smashing the head against the floor?



- Most birds don't see in stereo (each eye gets its own picture, no overlap)
- How do these animals get depth? E.g., how can a chicken beak the corn without smashing the head against the floor? **Structure-from-motion**



• Owls are one of the exceptions (they see stereo)



Birdseye View on What We Learned So Far

Problem	Detection	Description	Matching
Find Planar	Scale Invariant	Local feature:	All features to all features
Distinctive Objects	Interest Points	SIFT	+ Affine / Homography
Panorama Stitching	Scale Invariant	Local feature:	All features to all features
	Interest Points	SIFT	+ Homography
Stereo	Compute in	Intensity or	For each point search
	every point	Gradient patch	on epipolar line

Towards Semantics

- 3D and Projective Geometry can explain a lot of things in the image.
- However, some of the most valuable images cannot be explained by 3D at all.

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100 million \$

"Dora Maar au Chat" Pablo Picasso, 1941



1 cent

"La Picture" Sanja Fidler, yesterday

[Adopted from: A. Torralba]

Sanja Fidler

Towards Semantics

- We shouldn't only look at the 3D behind the image but also at the **story** behind it.
- We need to also understand the image semantics.





It's Fine Without Depth Too



https://www.youtube.com/watch?v=_dPlkFPowCc

It's Fine Without Depth Too

• Chickens don't want depth, they want story ;)



https://www.youtube.com/watch?v=_dPlkFPowCc

Next Time: Recognition