## 7.7

Consider the investment project with the following net cash flows: What would be the value of X if the project's IRR is $23 \%$ ?

| End of Year (n) | Net Cash Flow |
| :---: | ---: |
| 0 | $-\$ 12,000$ |
| 1 | $\$ 2,500$ |
| 2 | $\$ 5,500$ |
| 3 | X |
| 4 | X |

$$
\begin{aligned}
\mathrm{PW}(23 \%) & =-\$ 12,000+\$ 2,500(P / F, 23 \%, 1)+\$ 5,500(P / F, 23 \%, 2) \\
& +X(P / A, 23 \%, 2)(P / F, 23 \%, 2) \\
& =0 \\
\$ 6,332= & 0.9743 X \\
X= & \$ 6,498.93
\end{aligned}
$$

### 7.27

A manufacturing firm is considering the following mutually exclusive alternatives:

Determine which project a better choice is at MARR $=15 \%$, on the basis of the IRR criterion.

| $(\mathrm{n})$ | Project A | Project B |
| :---: | ---: | ---: |
| 0 | $-\$ 2,000$ | $-\$ 3,000$ |
| 1 | $\$ 1,400$ | $\$ 2,400$ |
| 2 | $\$ 1,650$ | $\$ 2,000$ |

Determine the cash flow on incremental investment:

| Net Cash Flow |  |  |  |
| :--- | ---: | ---: | ---: |
| $n$ | Project A | Project B | B A |
| 0 | $-\$ 2,000$ | $-\$ 3,000$ | $-\$ 1,000$ |
| 1 | $\$ 1,400$ | $\$ 2,400$ | $\$ 1,000$ |
| 2 | $\$ 1,640$ | $\$ 2,000$ | $\$ 360$ |

$$
i_{B-A}^{*}=28.11 \%>15 \%
$$

Select project B.

### 7.28

Consider the following two mutually exclusive alternatives:
(a) Determine the IRR on the incremental investment in the amount of \$2,000
(b) If the firm's MARR is $10 \%$, which alternative is the better choice?

## SOLUTION

| (n) | Project A1 | Project A2 |
| :---: | ---: | ---: |
| 0 | $-\$ 10,000$ | $-\$ 12,000$ |
| 1 | $\$ 5,000$ | $\$ 6,100$ |
| 2 | $\$ 5,000$ | $\$ 6,100$ |
| 3 | $\$ 5,000$ | $\$ 6,100$ |

(a) IRR on the incremental investment:

| Net Cash Flow |  |  |  |
| :---: | ---: | ---: | ---: |
| $n$ | Project A1 | Project A2 | A2 -A 1 |
| 0 | $-\$ 10,000$ | $-\$ 12,000$ | $-\$ 2,000$ |
| 1 | $\$ 5,000$ | $\$ 6,100$ | $\$ 1,100$ |
| 2 | $\$ 5,000$ | $\$ 6,100$ | $\$ 1,100$ |
| 3 | $\$ 5,000$ | $\$ 6,100$ | $\$ 1,100$ |

$$
i_{A 2-A 1}^{*}=29.92 \%
$$

(b) Since it is an incremental simple investment, $\mathrm{IRR}_{\mathrm{A} 2-\mathrm{A} 1}=29.92 \%>10 \%$.

Therefore, select project A2.

### 7.29

Consider the following two mutually exclusive investment alternatives: (a) Determine the IRR on the incremental investment in the amount of $\$ 4,000$. (Assume that MARR $=10 \%$.) (b) If the firm's MARR is $10 \%$. Which alternative is the better choice?

## SOLUTION

(a)

| (n) | Project A1 | Project A2 |
| :---: | ---: | ---: |
| 0 | $-\$ 16,000$ | $-\$ 20,000$ |
| 1 | $\$ 7,500$ | $\$ 5,000$ |
| 2 | $\$ 7,500$ | $\$ 15,000$ |
| 3 | $\$ 7,500$ | $\$ 8,000$ |
| IRR | $19.19 \%$ | $17.65 \%$ |


| $n$ | A 1 | A 2 | $\mathrm{~A} 2-\mathrm{A} 1$ |
| :---: | ---: | ---: | ---: |
| 0 | $-\$ 16,000$ | $-\$ 20,000$ | $-\$ 4,000$ |
| 1 | $\$ 7,500$ | $\$ 5,000$ | $-\$ 2,500$ |
| 2 | $\$ 7,500$ | $\$ 15,000$ | $\$ 7,500$ |
| 3 | $\$ 7,500$ | $\$ 8,000$ | $\$ 500$ |

$$
\operatorname{IRR}_{A 2-A 1}=13.08 \%
$$

(b) Select Project A2.

Consider the following two investment alternatives:
The firm's MARR is known to be $15 \%$.
(a) Compute the IRR of Project B.
(b) Compute the PW of Project A.
(c) Suppose that Projects A and B are mutually exclusive. Using the IRR, which project would you select?

| $(\mathrm{n})$ | Project A1 | Project A2 |
| :---: | ---: | ---: |
| 0 | $-\$ 10,000$ | $-\$ 20,000$ |
| 1 | $\$ 5,500$ | $\$ 0$ |
| 2 | $\$ 5,500$ | $\$ 0$ |
| 3 | $\$ 5,500$ | $\$ 40,000$ |
| IRR | $30 \%$ | $?$ |
| PW (15\%) | $?$ | $\$ 6,300$ |

## SOLUTION

(a) $\mathrm{IRR}_{B}=25.99 \%$
(b) $\mathrm{PW}(15 \%)_{A}=-\$ 10,000+\$ 5,500(P / A, 15 \%, 3)=\$ 2,558$
(c) Incremental analysis:

| Net Cash Flow |  |  |  |
| :--- | ---: | ---: | ---: |
| $n$ | Project A | Project B | B - A |
| 0 | $-\$ 10,000$ | $-\$ 20,000$ | $-\$ 10,000$ |
| 1 | $\$ 5,500$ | 0 | $-\$ 5,500$ |
| 2 | $\$ 5,500$ | 0 | $-\$ 5,500$ |
| 3 | $\$ 5,500$ | $\$ 40,000$ | $\$ 34,500$ |

Since $\operatorname{IRR}_{B-A}=24.24 \%>15 \%$, select project B.

