

## Overview

• Fluid Kinematics deals with the motion of fluids without considering the forces and moments which create the motion.

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What is a fluid ?

Tension: Force per unit area • Normal tension: perpendicular to the surface Shear tension: parallel to the surface

Solids deform non-permanently
 Plastics deform permanently

• Fluids do not resist: they flow

Materials respond differently to shear stresses:











Acceleration Field  
• Consider a fluid particle and Newton's second law,  

$$\vec{F}_{particle} = m_{particle}\vec{a}_{particle}$$
  
• The acceleration of the particle is the time derivative of the  
particle's velocity.  
 $\vec{a}_{particle} = \frac{d\vec{V}_{particle}}{dt}$   
• However, particle velocity at a point is the same as the fluid  
velocity,  
 $\vec{V}_{particle} = \vec{V} \left( x_{particle}(t), y_{particle}(t), z_{particle}(t) \right)$   
• To take the time derivative of  $V_{particle}$  the chain rule must be  
used.  
 $\vec{a}_{particle} = \frac{\partial \vec{V}}{\partial t} \frac{dt}{dt} + \frac{\partial \vec{V}}{\partial x} \frac{dx_{particle}}{dt} + \frac{\partial \vec{V}}{\partial y} \frac{dy_{particle}}{dt} + \frac{\partial \vec{V}}{\partial z} \frac{dz_{particle}}{dt}$ 

## Material Derivative

• The total derivative operator is called the **material derivative** and is often given special notation, D/Dt.

$$\frac{D\vec{V}}{Dt} = \frac{d\vec{V}}{dt} = \frac{\partial\vec{V}}{\partial t} + \left(\vec{V} \cdot \vec{\nabla}\right)\vec{V}$$

- Advective acceleration is nonlinear: source of many phenomena and primary challenge in solving fluid flow problems.
- Provides ``transformation'' between Lagrangian and Eulerian frames.
- Other names for the material derivative include: total, particle, and substantial derivative.

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• A Streamline is a curve that is everywhere tangent to the instantaneous local velocity vector.

Consider an arc length







































































