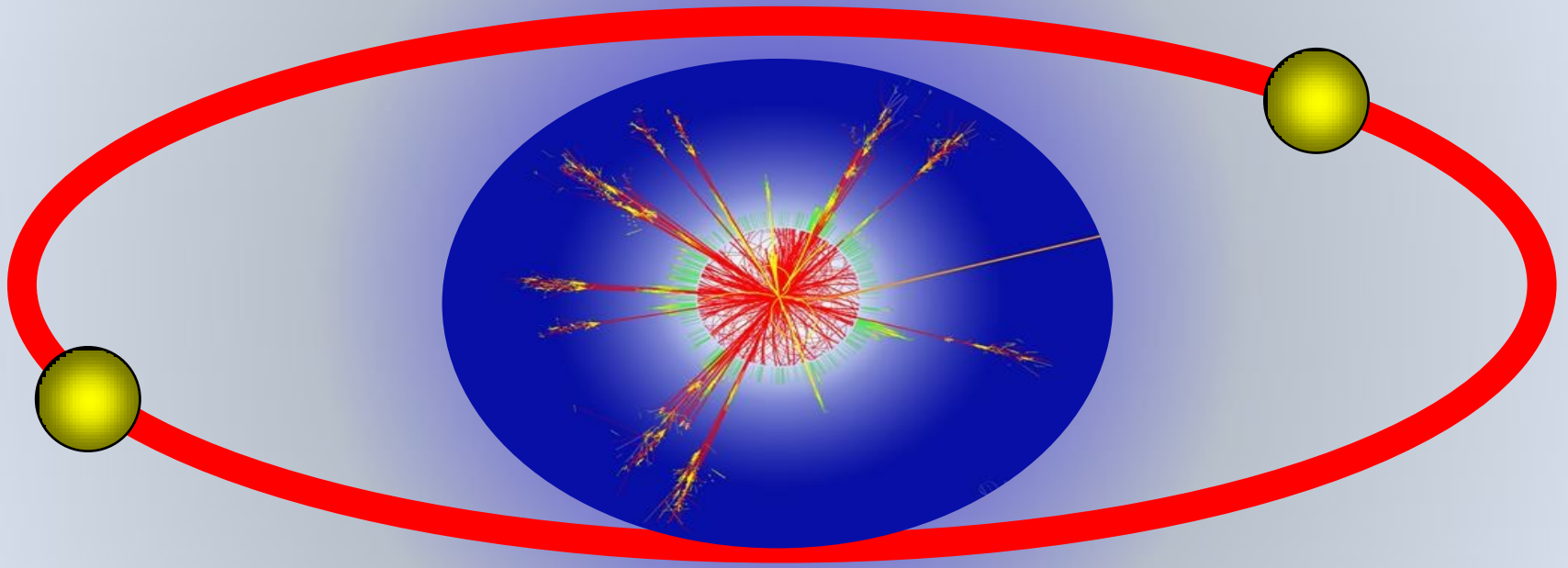


# *Particle Accelerators*



*Prof. Glenn Patrick*

# Last Week - Recap

Nuclear Reactions, Conservation Laws

Reaction Energy, Q Value

Cross-section

Nuclear Fission: Induced and Spontaneous

Neutron Reactions, Fission Energy Release

Chain Reaction

Uranium Fuel Cycle

Fission Reactor Designs

Thorium

ADSR

Nuclear Fusion

Magnetic Confinement and Inertial Confinement

# Today's Plan

## 06 November Accelerators

Voltage Multiplier

Van de Graaff Generator

Tandem Accelerators

Linear Accelerator (LINAC)

Cyclotron

Relativistic Effects

Synchro-Cyclotron Iso-Cyclotron

Synchrotron

Synchrotron Radiation

Large Hadron Collider (LHC)

Beyond the LHC

Super LHC

International Linear Collider and CLIC

## BOOKS

Edmund Wilson, *An Introduction to Particle Accelerators*, OUP

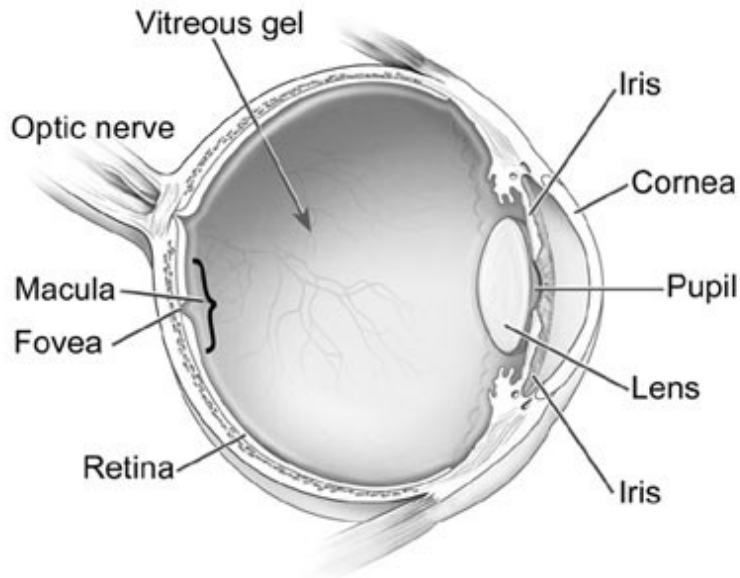
Klaus Wille, *The Physics of Particle Accelerators*, OUP

## Copies of Lectures:

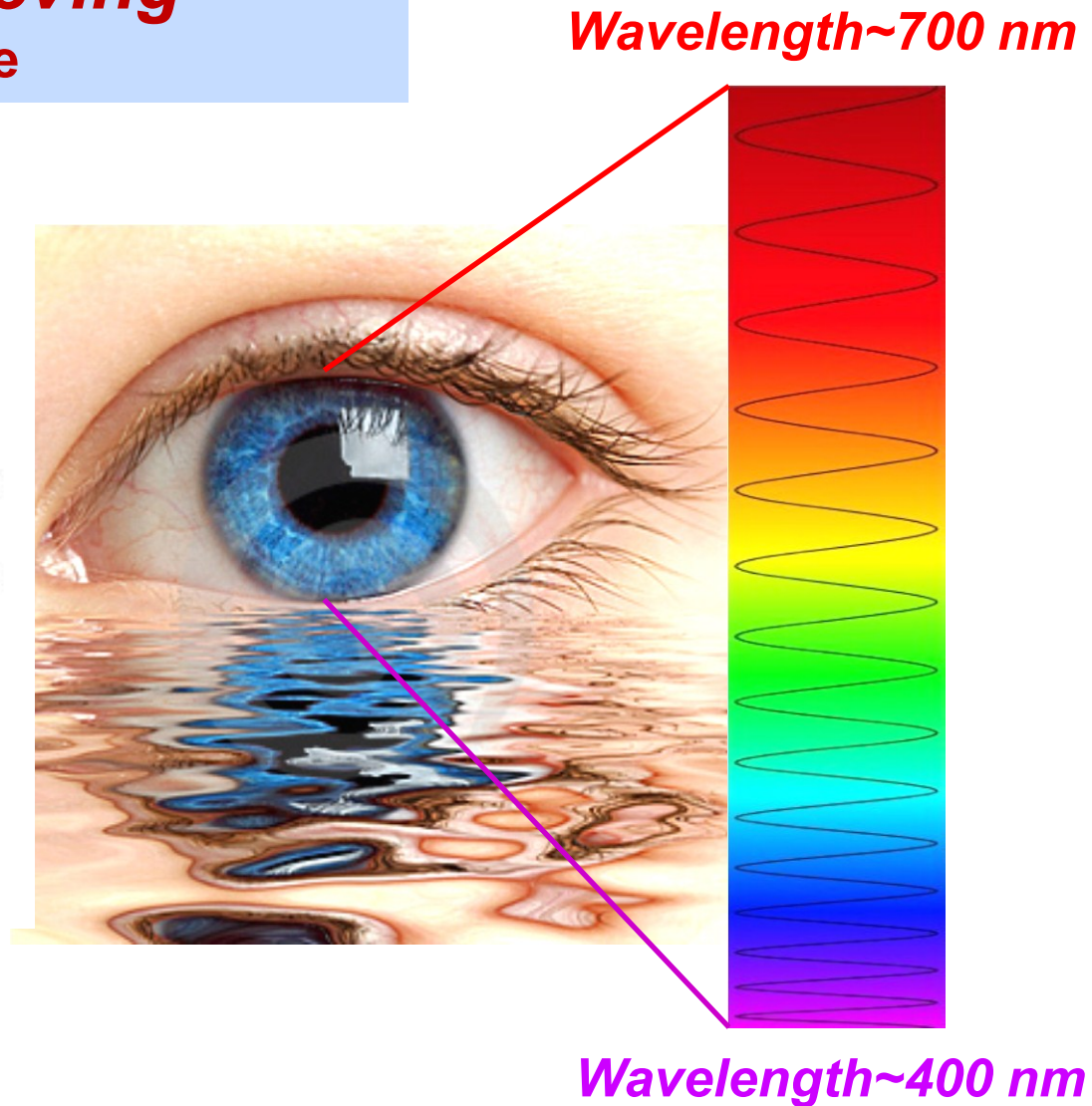
<http://hepwww.rl.ac.uk/gpatrick/portsmouth/courses.htm>

# Visible/Optical Spectrum

*“Seeing is beleeving”*  
1639, J. Clarke



The eye is the **detector**

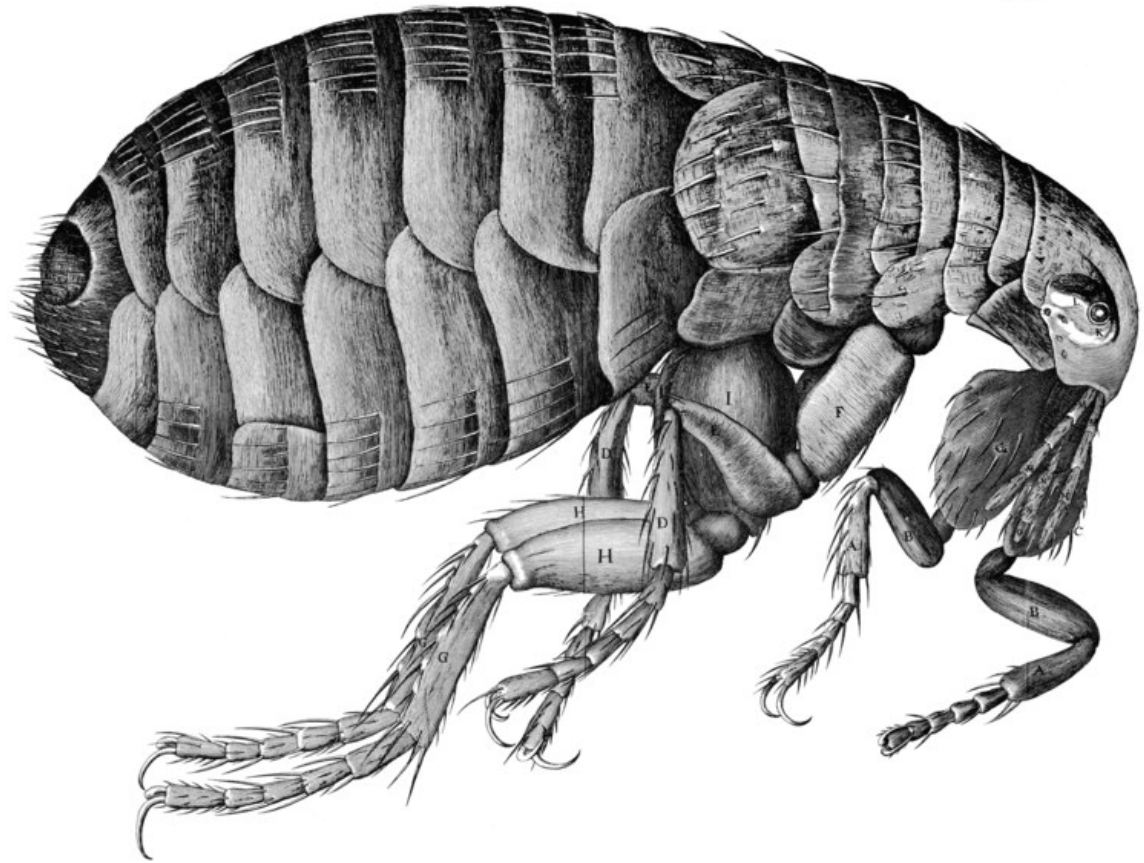




# The Very Small ~ 400 years Ago



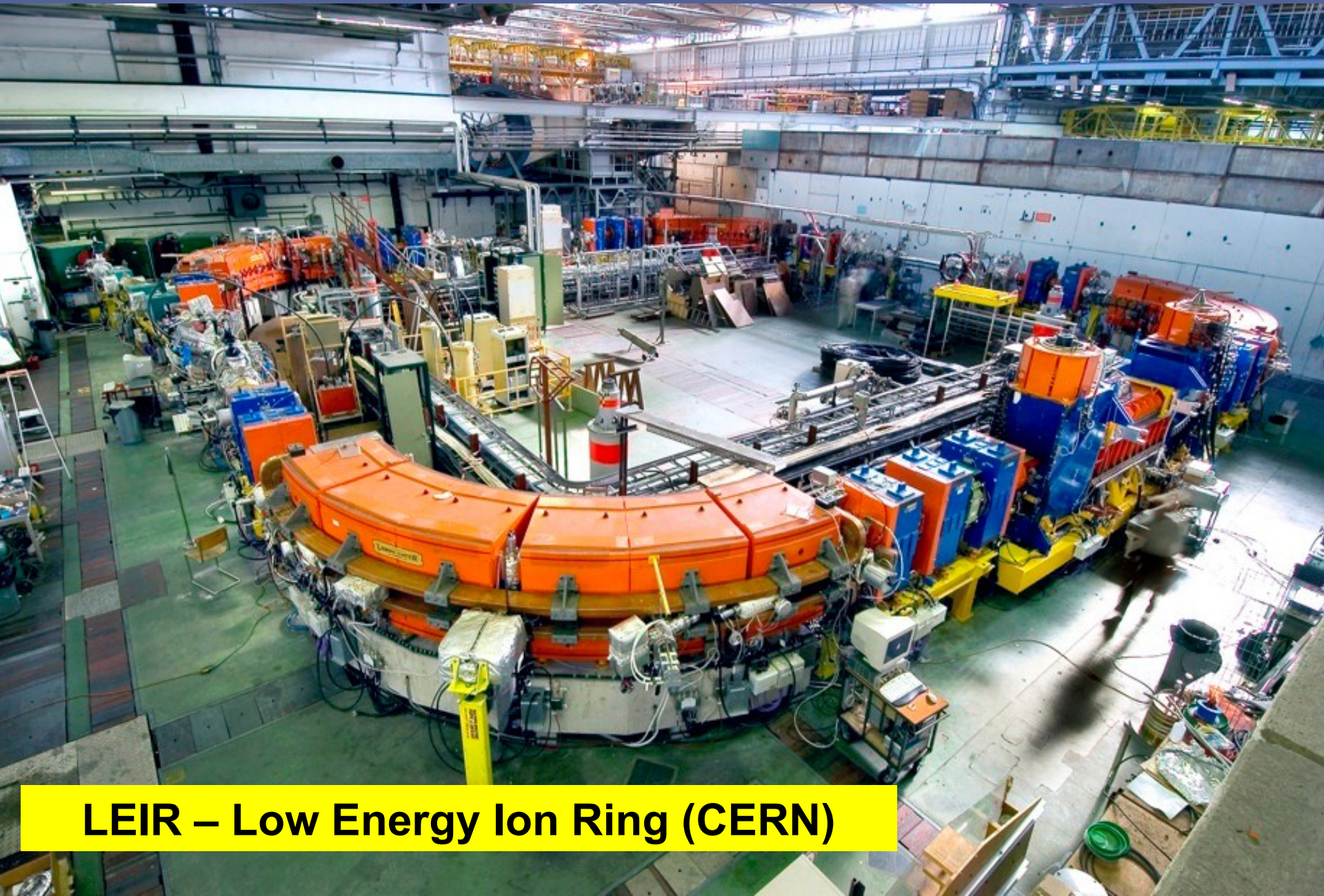
Compound Microscope, ~1670, Glasgow  
*Magnification ~30*



*Micrographia, Robert Hooke, 1665*  
*"Cell" appears for the first time.*



# Modern Microscope?

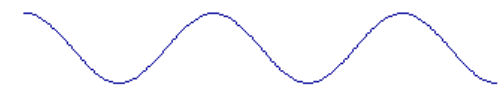


**LEIR – Low Energy Ion Ring (CERN)**





# Wave Particle Duality

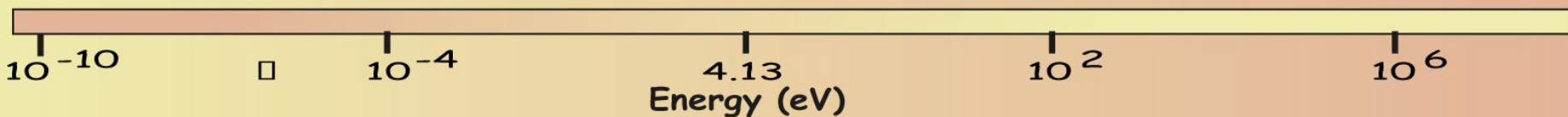
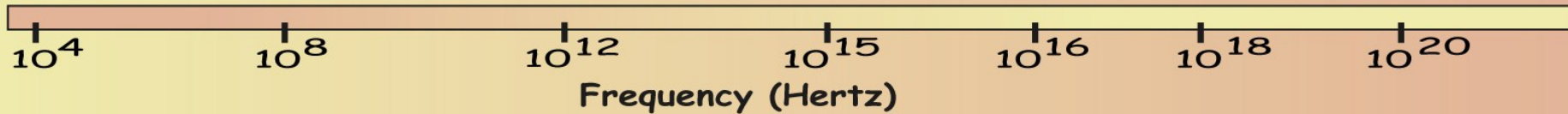
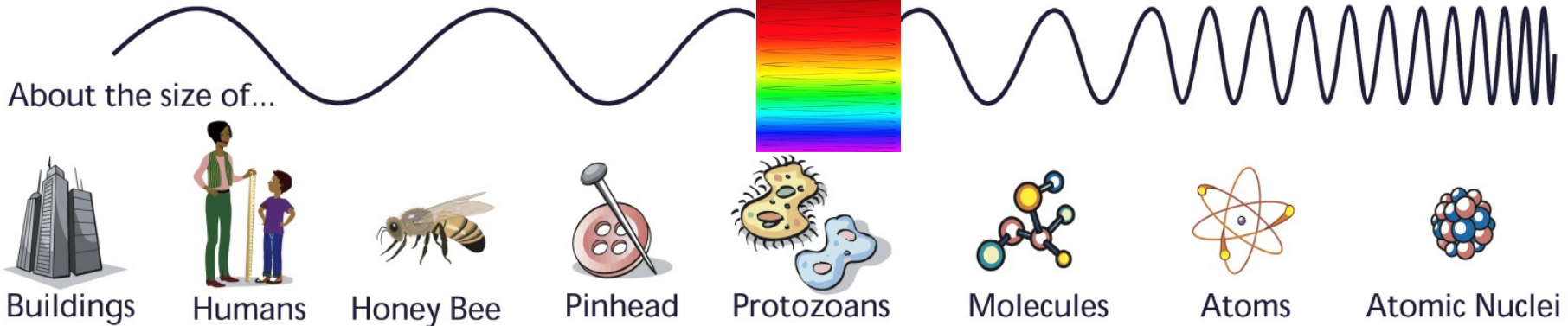
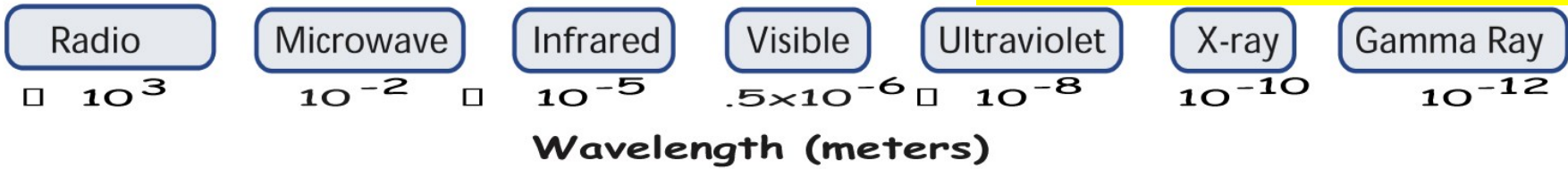


Visible light can probe down to ~1 micron



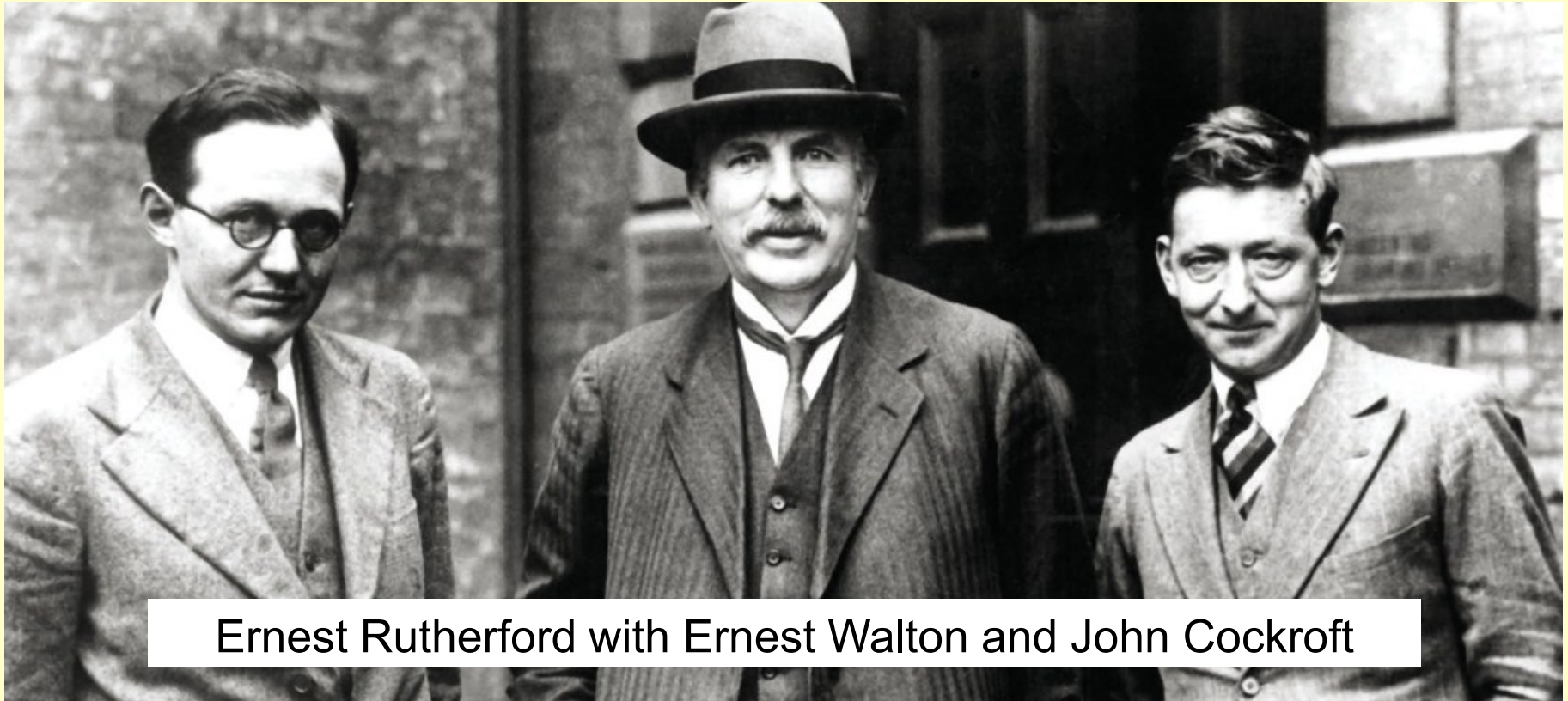
Higher energies mean shorter wavelengths.

$$\lambda = \frac{h}{p}$$



# The Quest for Higher Energies

In the early 20<sup>th</sup> century, the only known sources of particles that could induce nuclear reactions were the natural alpha particle emitters (usually radium). The only type of nuclear reaction was an  $\alpha$  particle interacting with a nucleus.



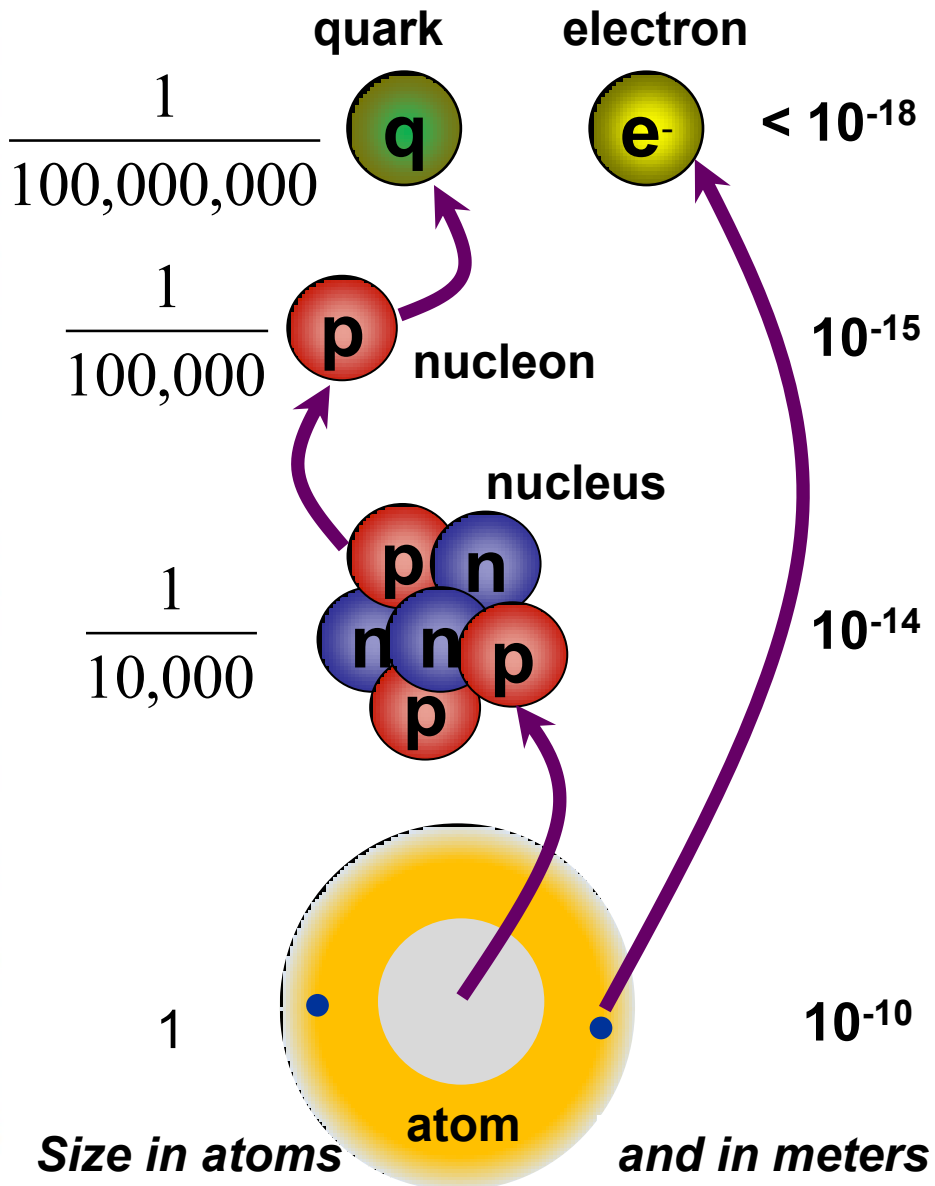
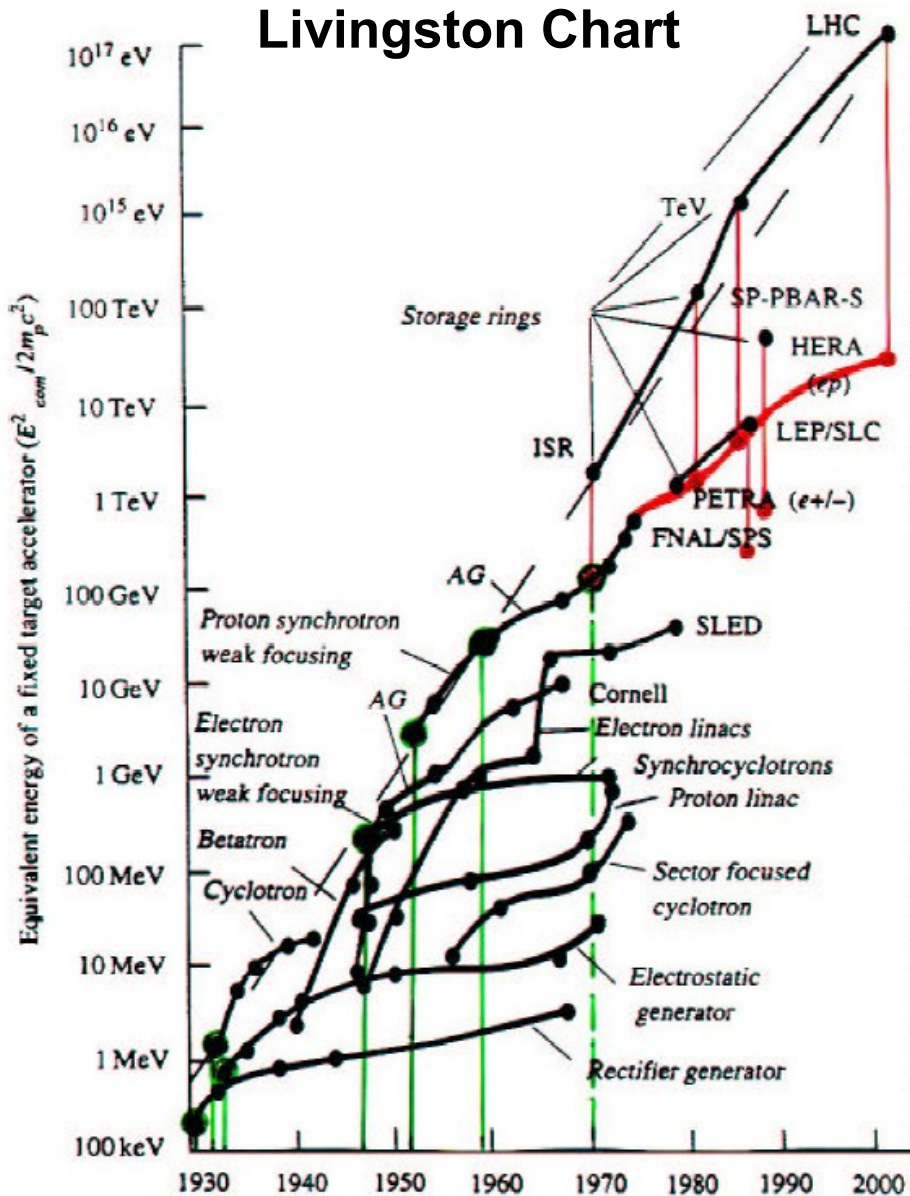
Ernest Rutherford with Ernest Walton and John Cockcroft

Need for a device – an **accelerator** – to accelerate charged particles to higher energies.

The way to do this was to create large electric fields.

# Energy Growth of Accelerators

Livingston Chart



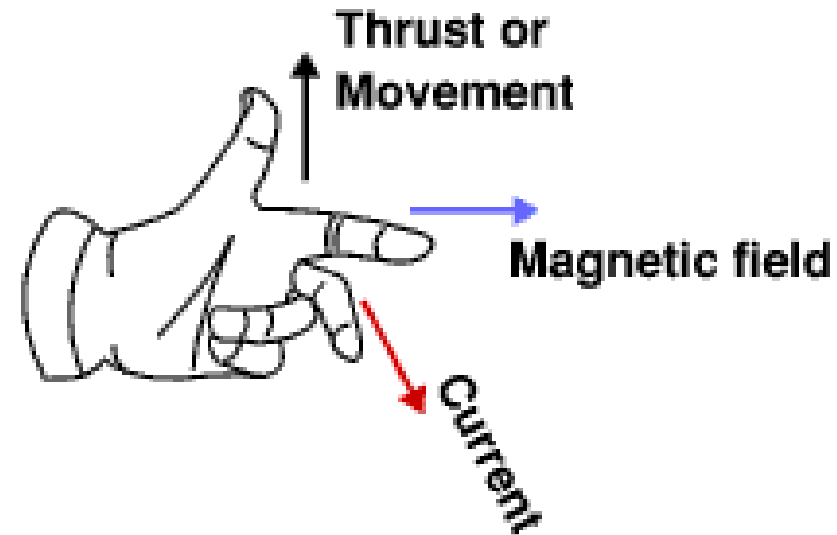
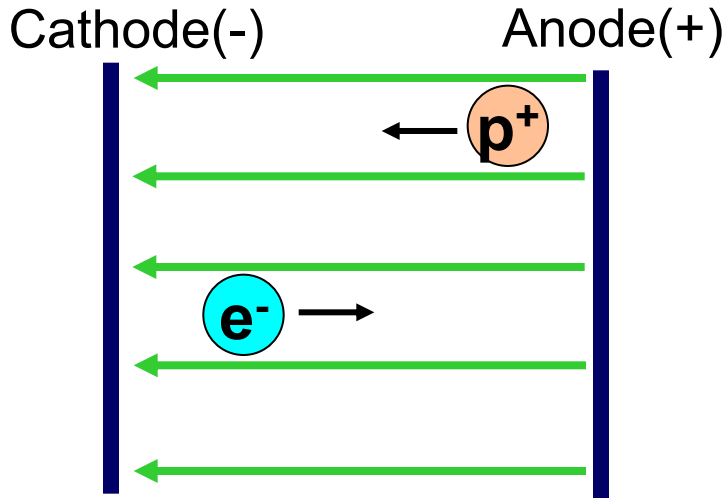
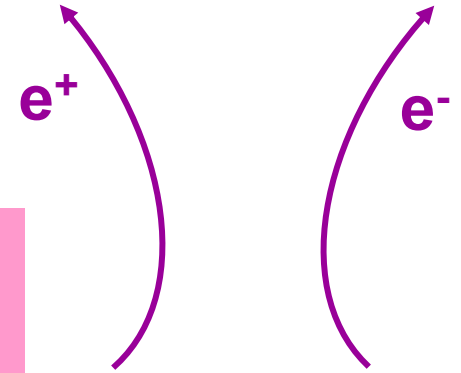
# Charged Particle Beams

Force on charged particle is given by the **Lorentz Force**

$$\vec{F} = q\vec{E} + q\vec{v} \times \vec{B}$$

**Electric Field**  
*Acceleration*

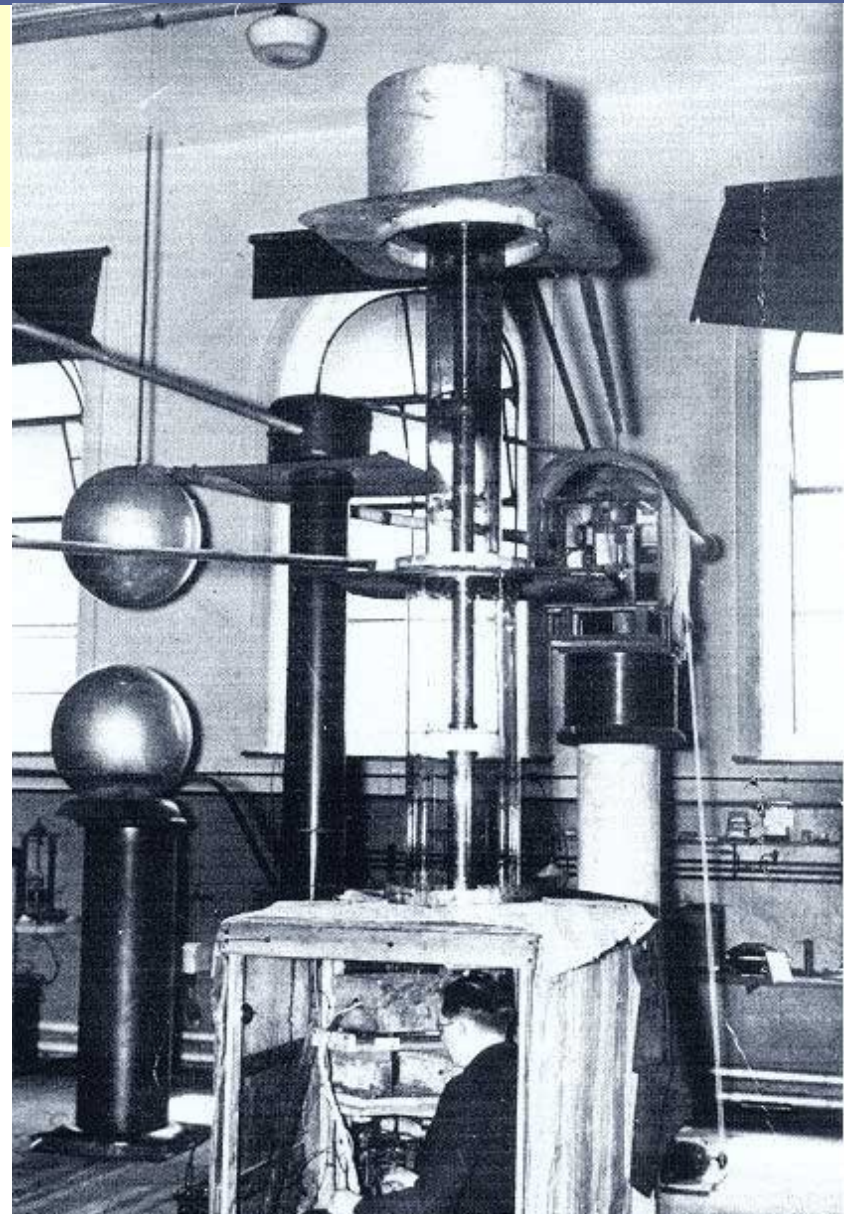
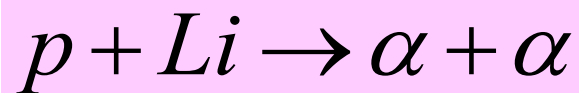
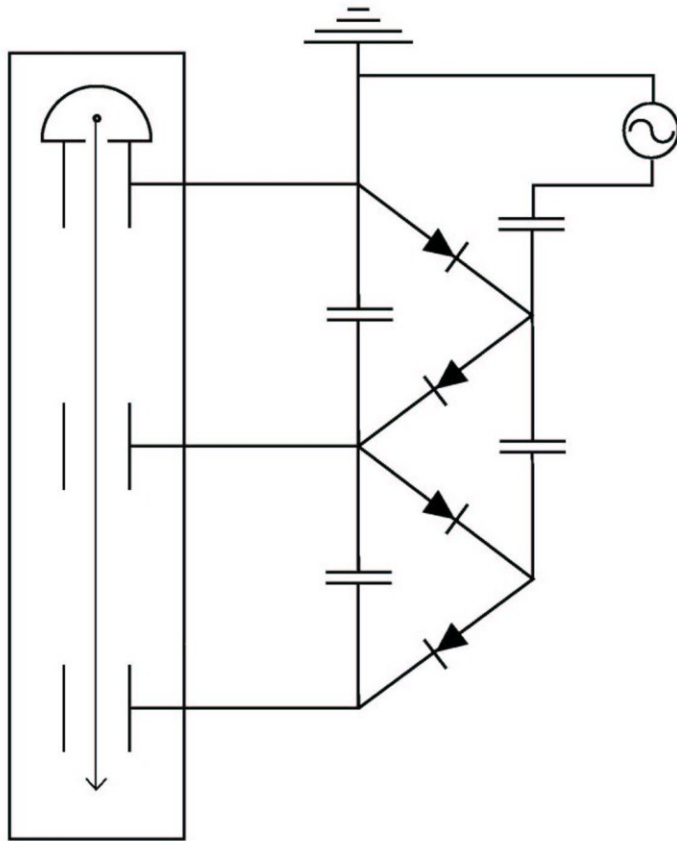
**Magnetic Field**  
*Bending*





# Splitting the Nucleus (1932)

John Cockroft & Ernest Walton  
Voltage Multiplier (800 kV)  
Cavendish Laboratory, 1932.



Max. accelerating voltage  $\sim 1\text{MV}$

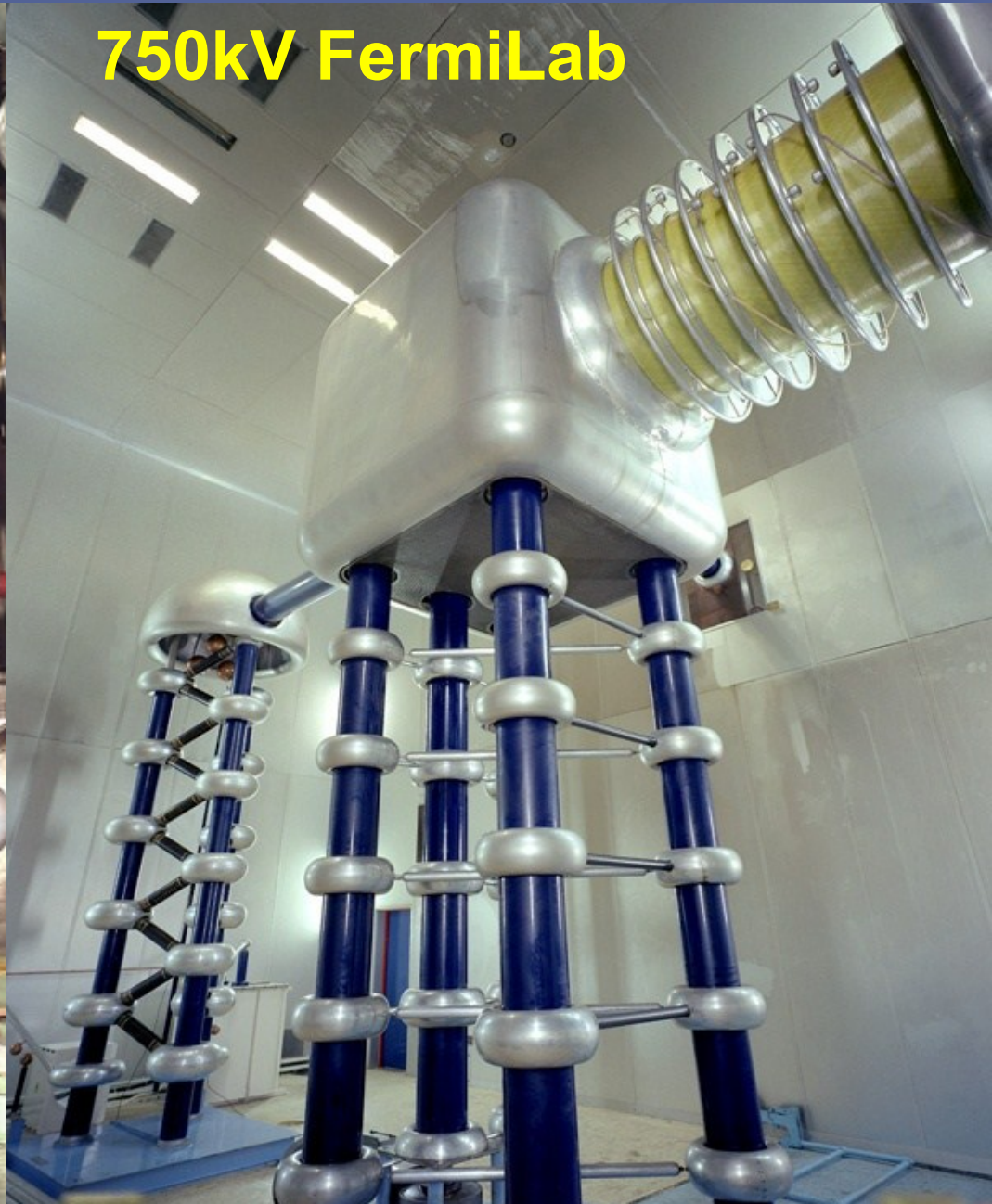


# Cockroft/Walton Pre-Injectors

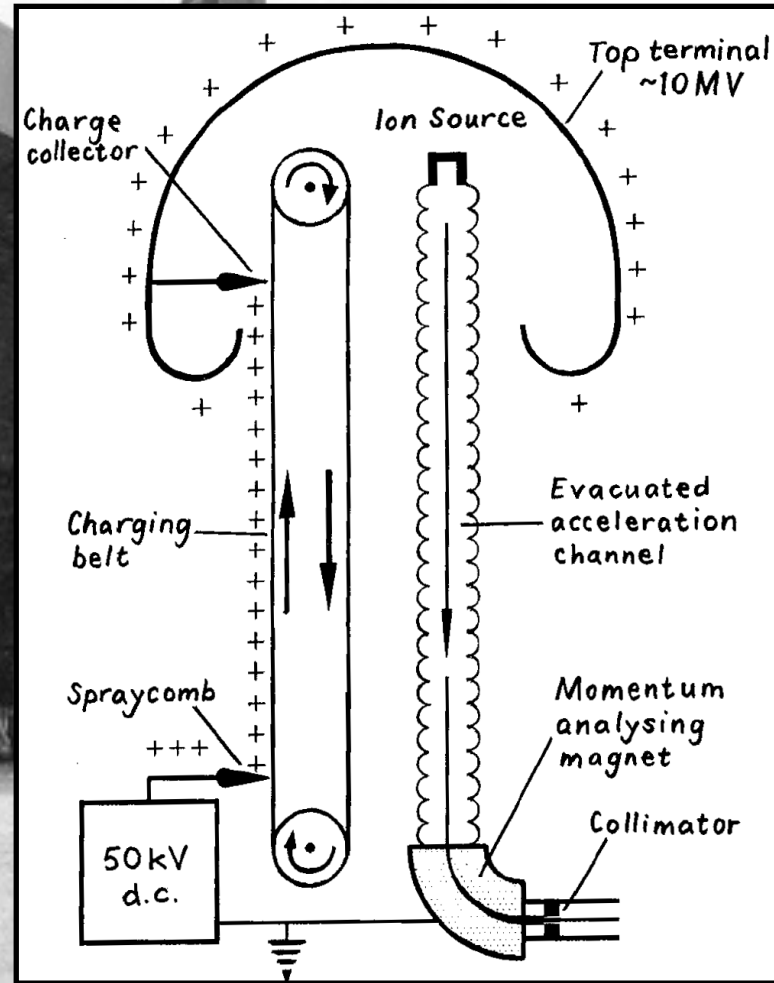
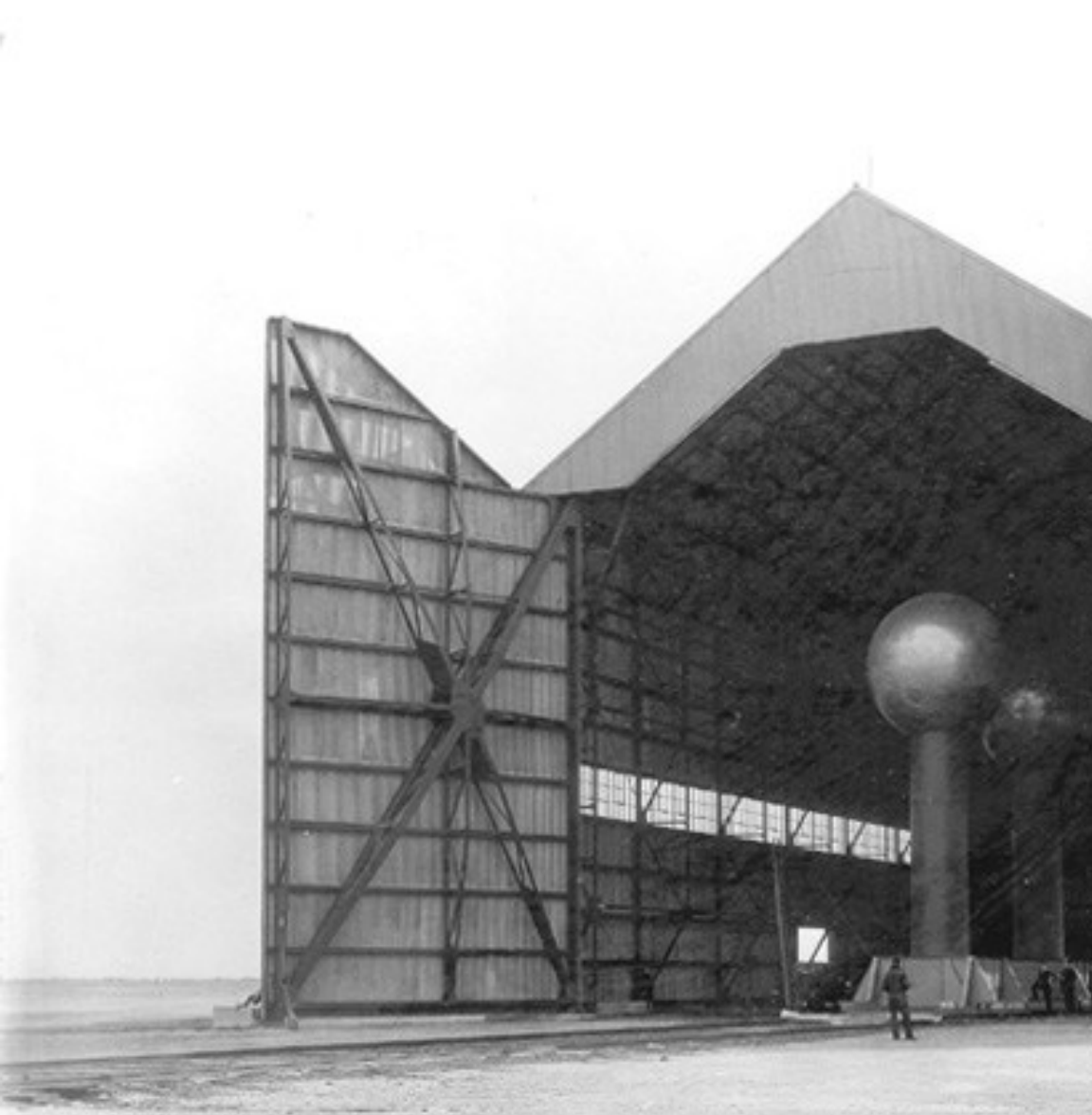
665 kV ISIS, RAL  
(replaced 2004)



750kV FermiLab

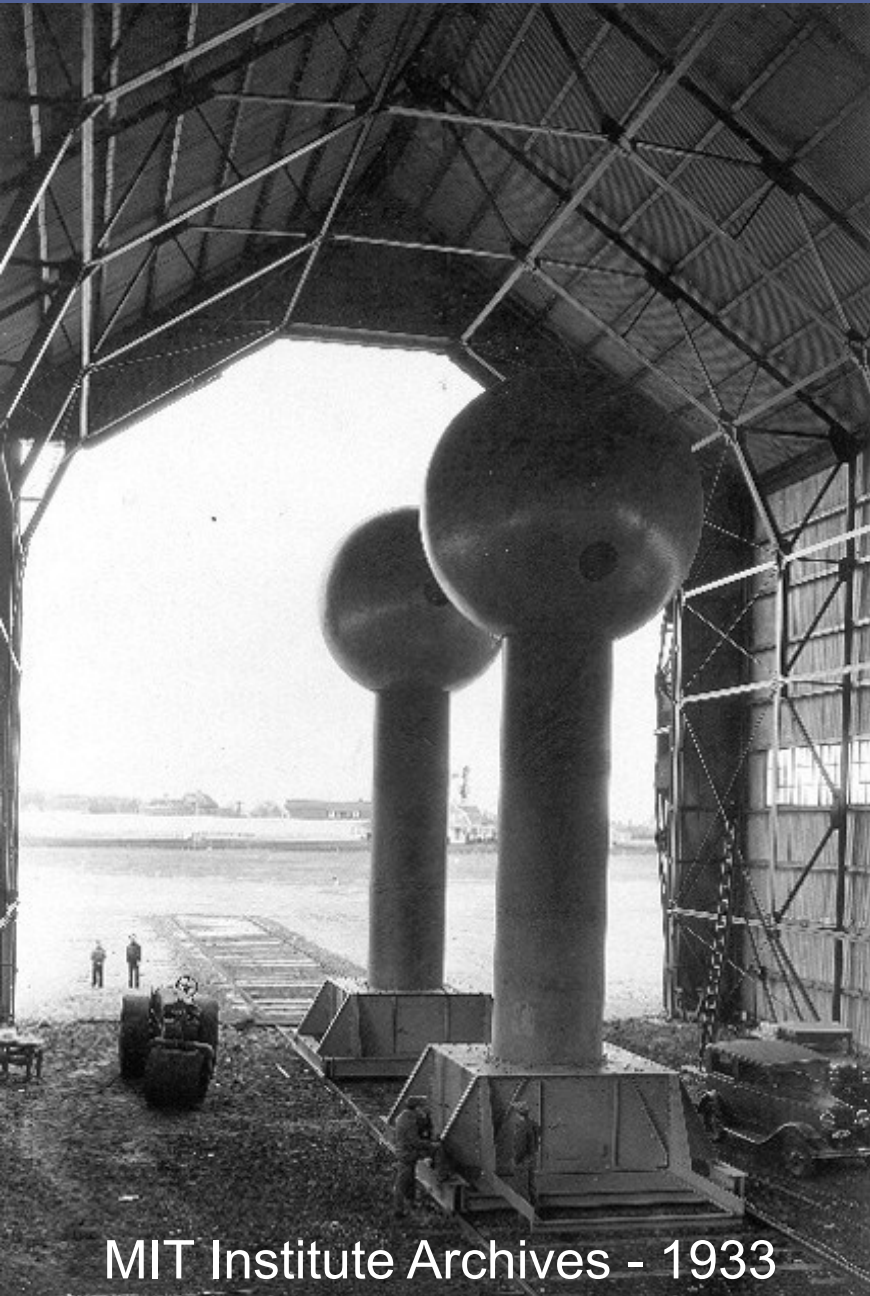


# Van de Graaff High Voltage Generator





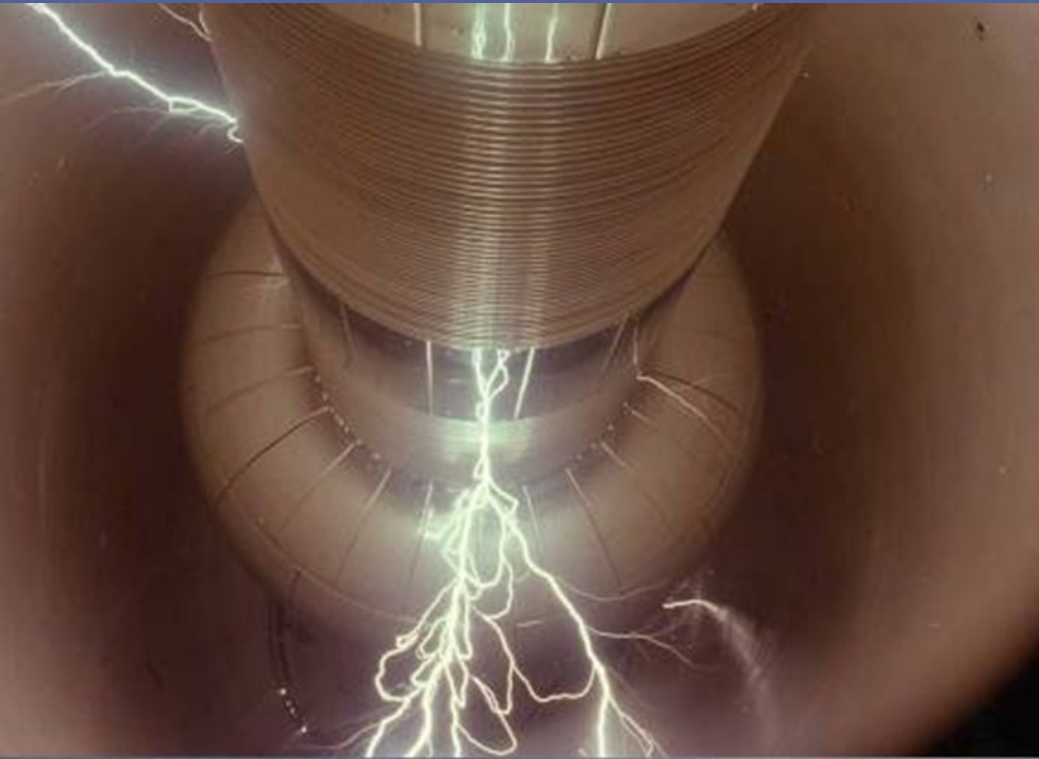
# Breakdown!



MIT Institute Archives - 1933

Max. accelerating voltage  $\sim 1$  MV

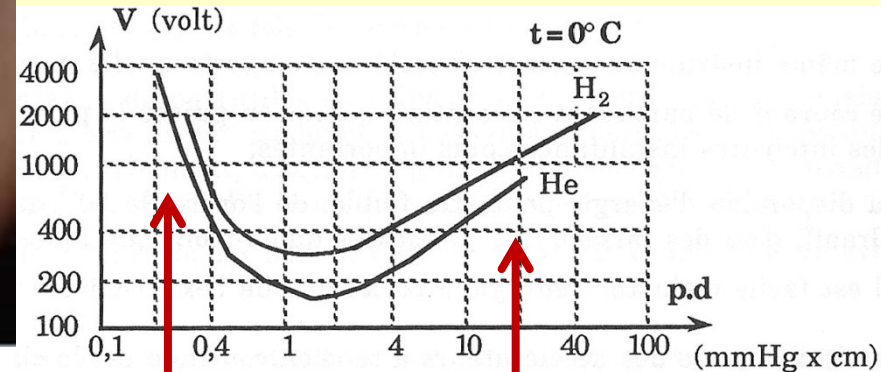
# High Voltage Limit!



Can reach ~10MV if high voltage parts under high pressure gas instead of air.

**Sulphur Hexafluoride, SF<sub>6</sub> used**

**Limit set by Paschen's Law:**  
*The breaking voltage between two parallel electrodes depends only on the **pressure** of the gas between the electrodes and their distance.*



Low pressure: gas not too dense, long mean path of electrons between collisions.

High pressure: dense gas, more collisions reduce electron energy making it more difficult to ionise.

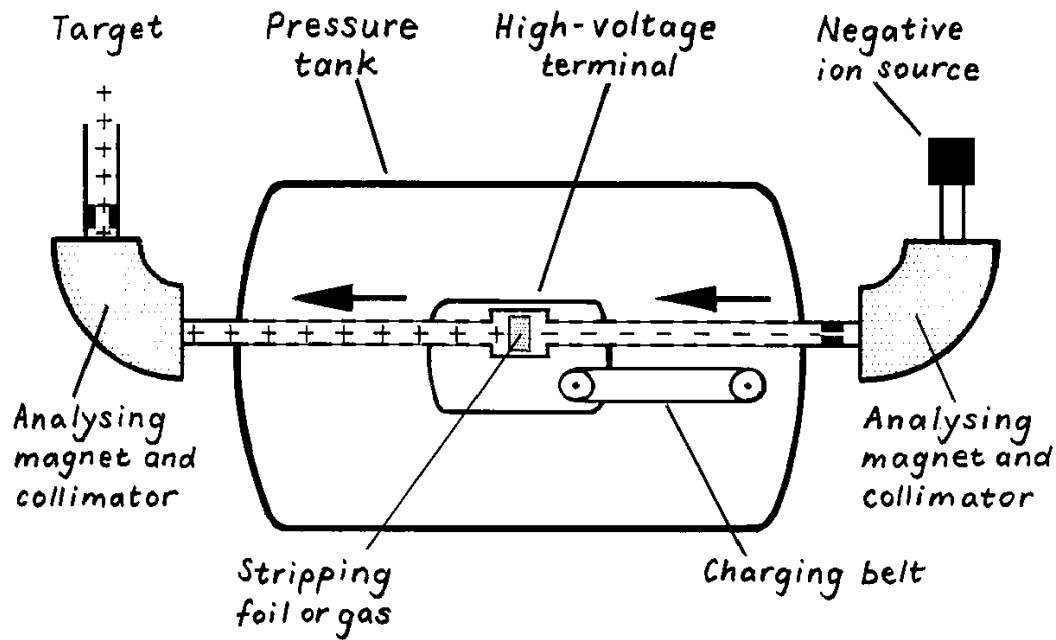
# Tandem Accelerator

Problem with single Van de Graaff is that voltage only applied once per particle.

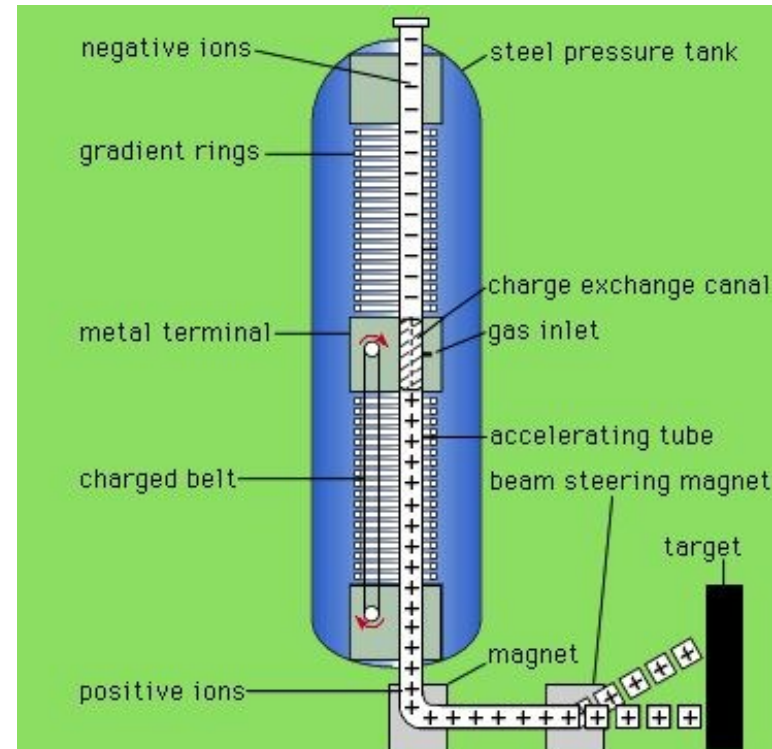
Can double the energy by using the **tandem** approach.

Start with **negative ions** (e.g.  $\text{H}^-$ ) and then **strip the electrons** in the centre to get a second stage of acceleration.

## Horizontal tandem



## Vertical tandem

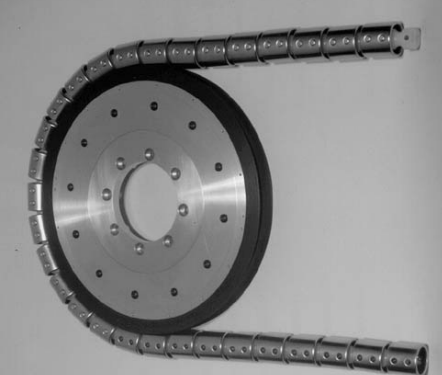
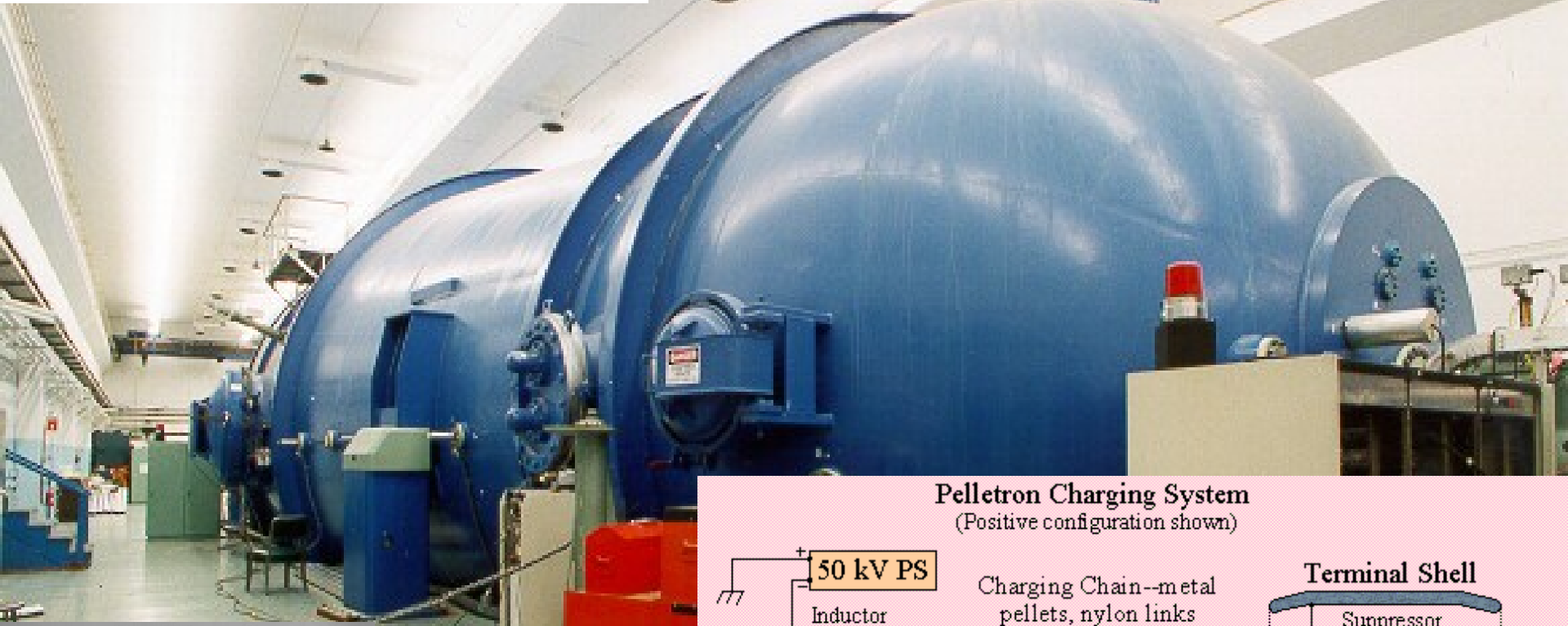


Can also have a **folded tandem** (e.g. Oxford) where two accelerator tubes are placed side-by-side and a  $180^\circ$  magnet deflects the beam between them.



# Tandem Accelerator

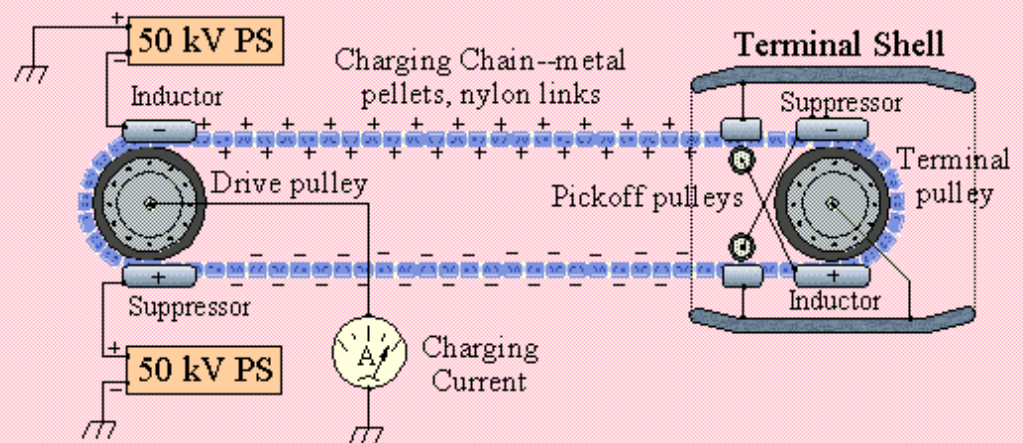
Yale University, ESTU, 21 MV



**Pelletron Chain**

**Metal pellets with nylon links**

**Pelletron Charging System**  
(Positive configuration shown)





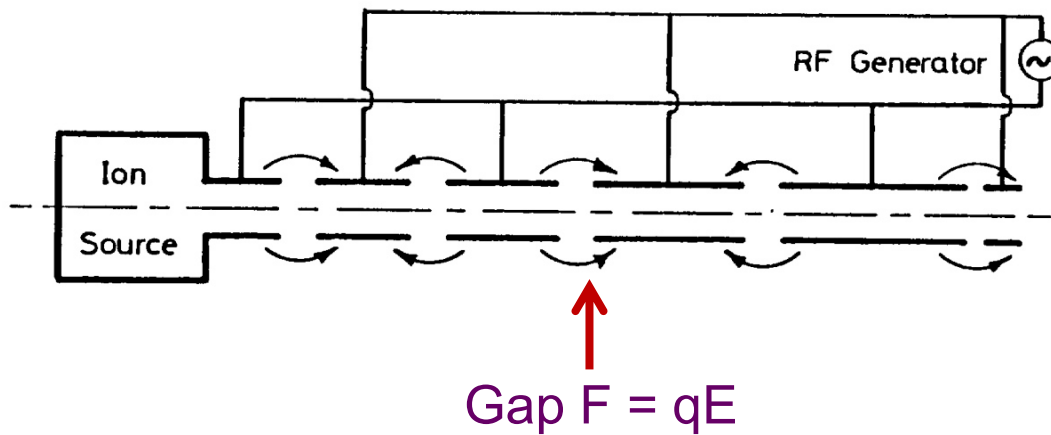
# UK - Nuclear Structure Facility (NSF)



***Daresbury Laboratory  
Tandem Van de Graaff (1983-1992)  
20-30 MV, 70m high***

# Linear Accelerator (LINAC)

Wideröe LINAC (1927): First successful test of using **rapidly changing high frequency voltage** instead of direct voltage.



25kV  
1 MHz oscillator

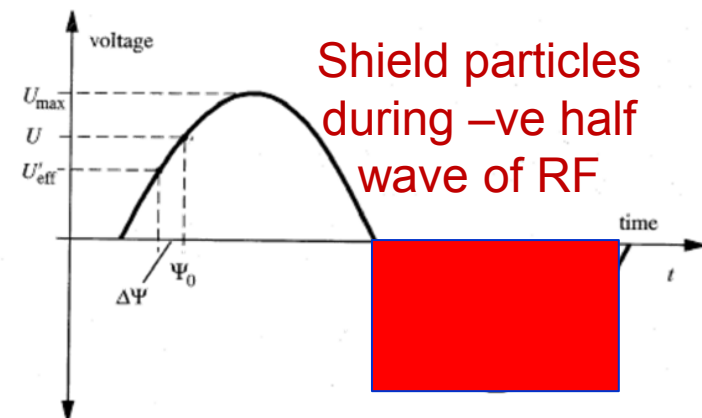
$$\text{Voltage } U(t) = U_{\max} \sin \omega t$$

Alvarez drift tube LINAC (1946): First serious proton LINAC. High frequency RF oscillators (klystrons) become available because of radar.

After the  $n$ th tube, the particles have energy  $E_n$ , where  $\Psi$  is average phase of RF voltage that particles "see".

$$E_n = nqU_0 \sin \Psi_0$$

Distance between gaps has to increase to allow for increase in velocity.





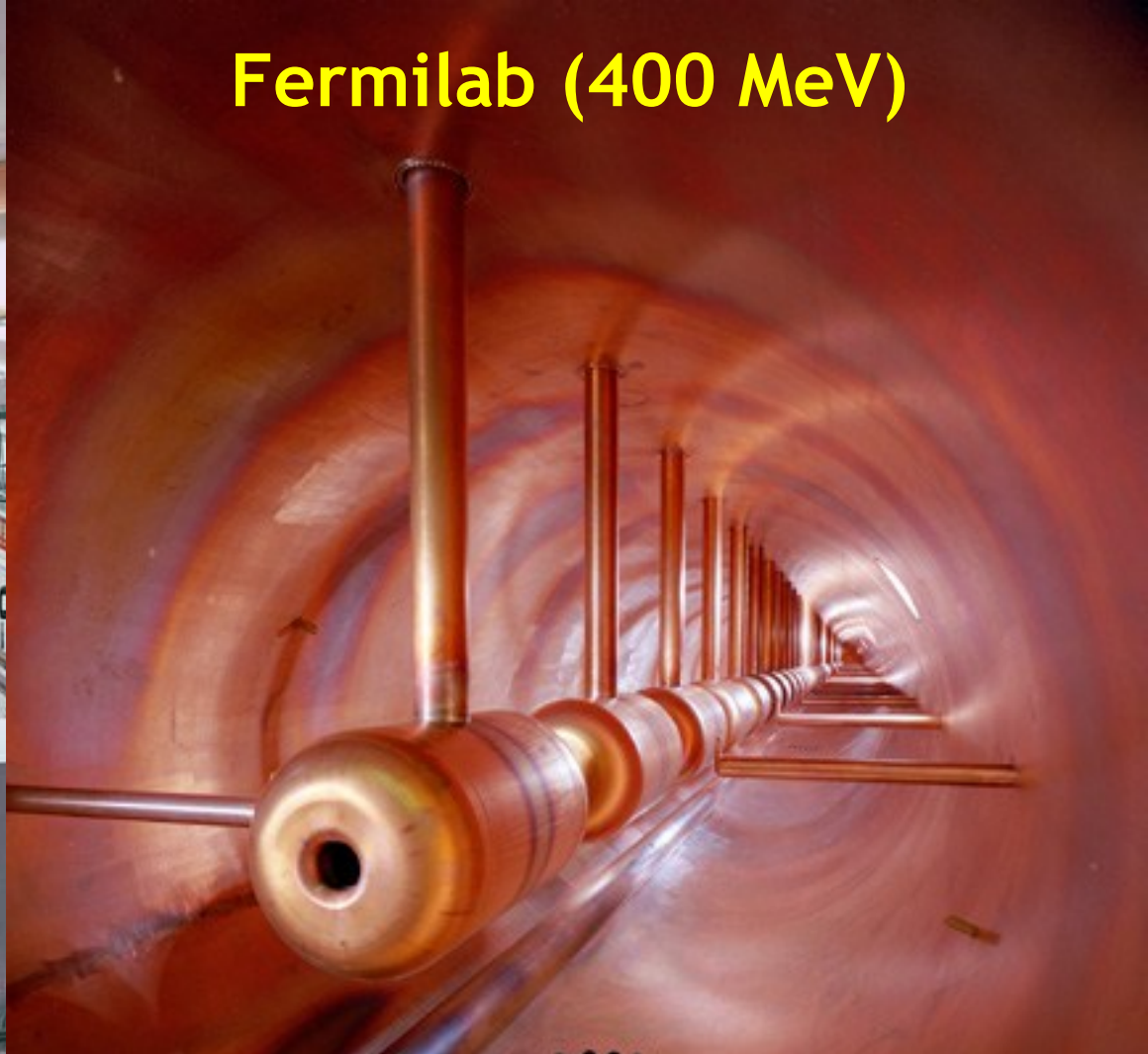
# ISIS LINAC (RAL)







Fermilab (400 MeV)



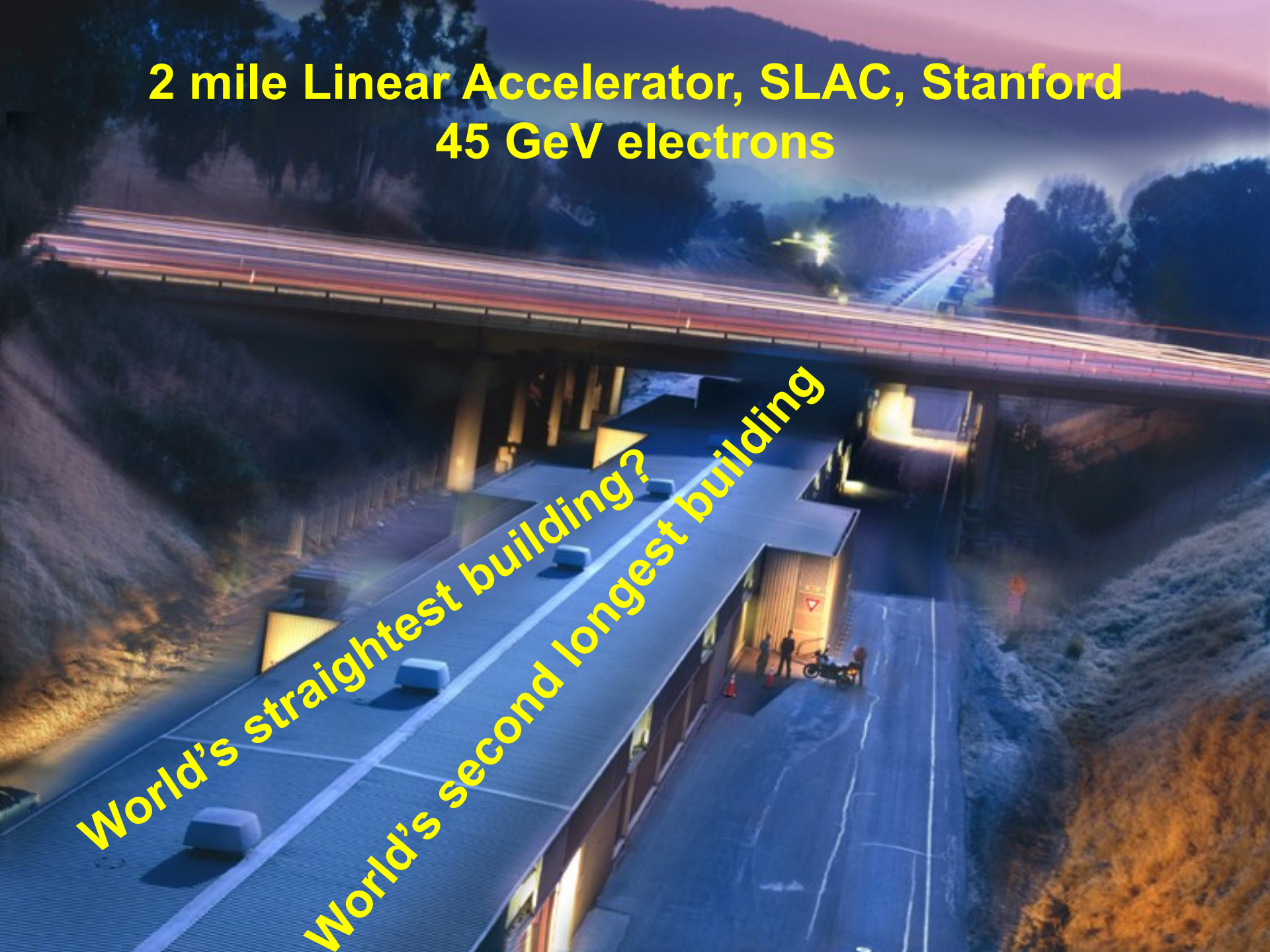
## LINEAR ACCELERATORS



Alternating RF voltage. Each step gives a small energy increase to the particle.

# 2 mile Linear Accelerator, SLAC, Stanford 45 GeV electrons

World's straightest building?  
World's second longest building





# Circular Accelerators

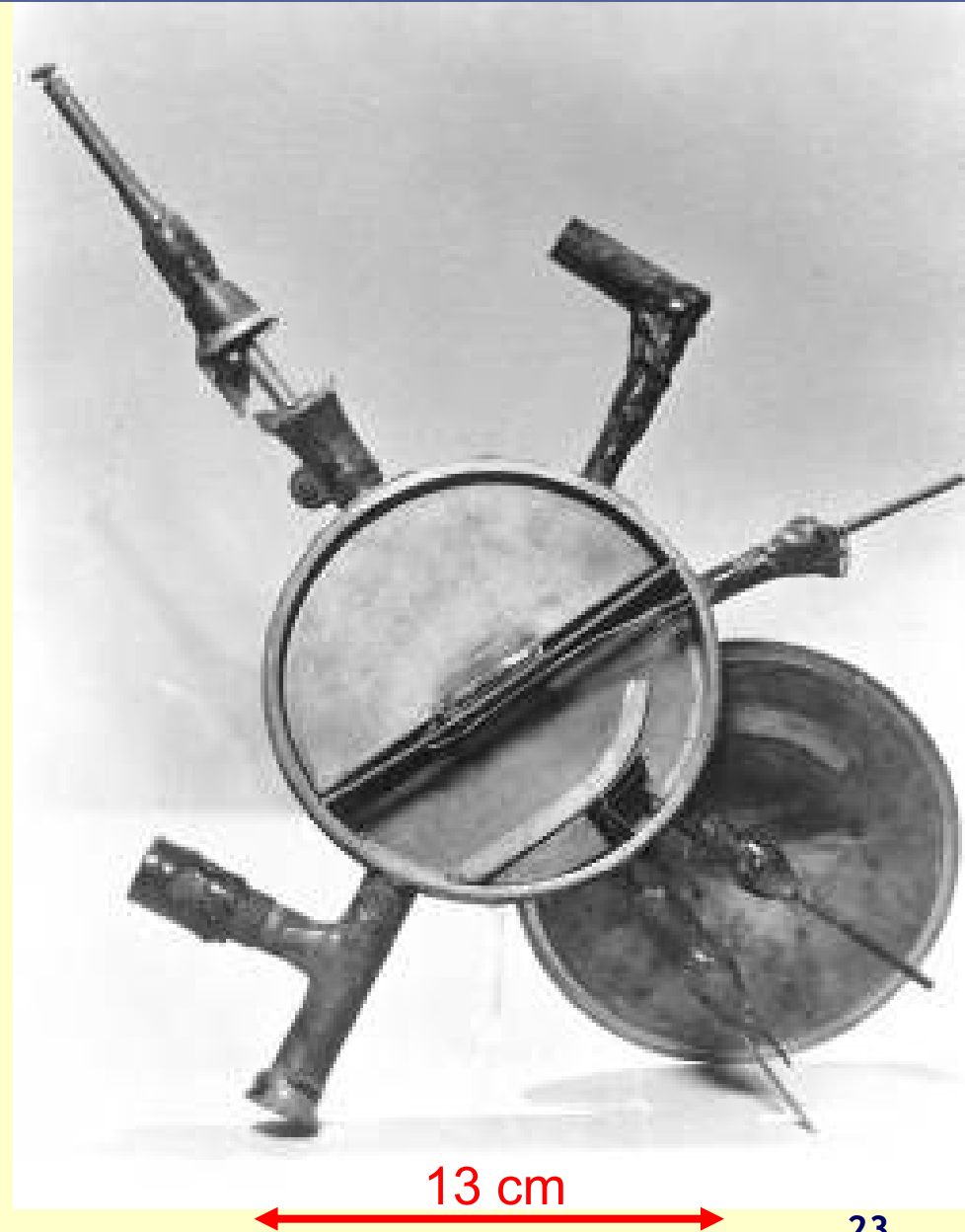
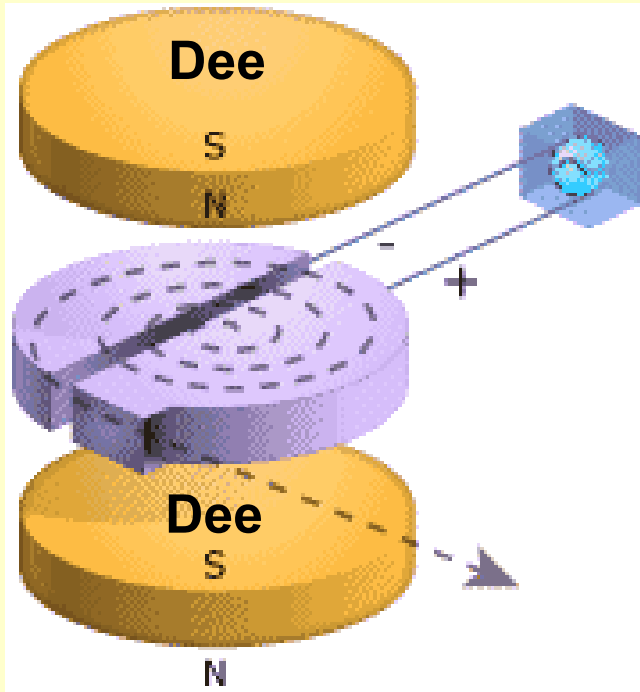
## CYCLOTRON

First circular particle accelerator built by Ernest O. Lawrence & Stanley Livingston at Berkeley in 1930.

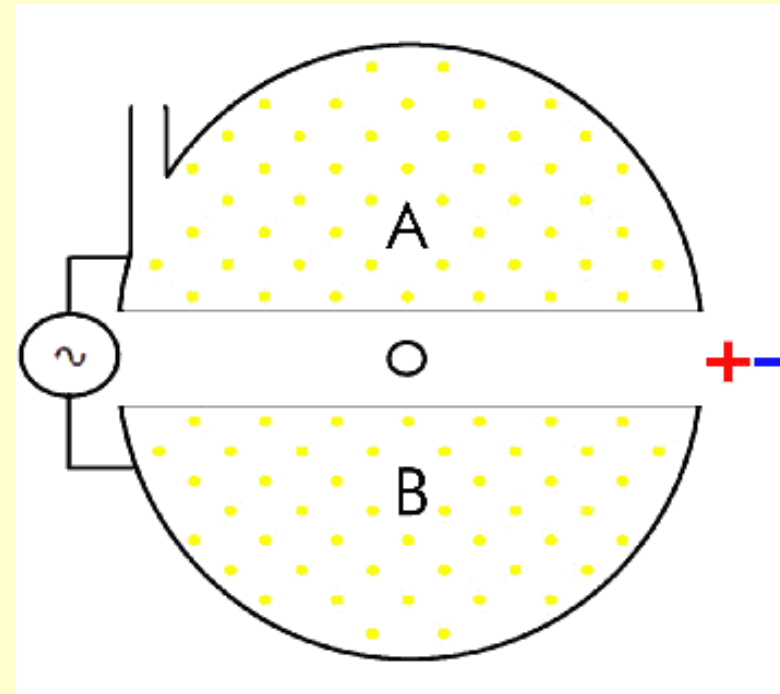
Energy = 80 keV

Diameter = 13cm

Bend beam round in a circle using **fixed** magnetic field and **constant** RF.



# The Cyclotron



Lorentz  
Force

$$\vec{F} = q(\vec{v} \times \vec{B}) = qvB_z$$

Classically:  
Magnetic = centripetal

$$qvB_z = \frac{mv^2}{R}$$

**Magnetic rigidity**  
(resistance of particle  
to deflection)

$$B_z R = \frac{p}{q}$$

$$R[m] = 3.33 p[GeV] / B[T]$$

*Increasing radius from increasing momentum → spiral trajectory.*

Frequency of revolution:

$$f = \frac{v}{2\pi R} = \frac{v}{2\pi} \cdot \frac{qB_z}{mv} = \frac{qB_z}{2\pi m}$$

**Cyclotron  
frequency**

$$\omega = 2\pi f = \frac{qB_z}{m}$$

*independent of particle momentum*

# Relativistic Mass Increase

**Classical cyclotrons** can accelerate protons, deuterons and alpha particles up to **~22 MeV per charge**.

At these energies, the motion is still sufficiently non-relativistic ( $\sim 0.15c$ ) for the revolution frequency to remain  $\sim$ constant.

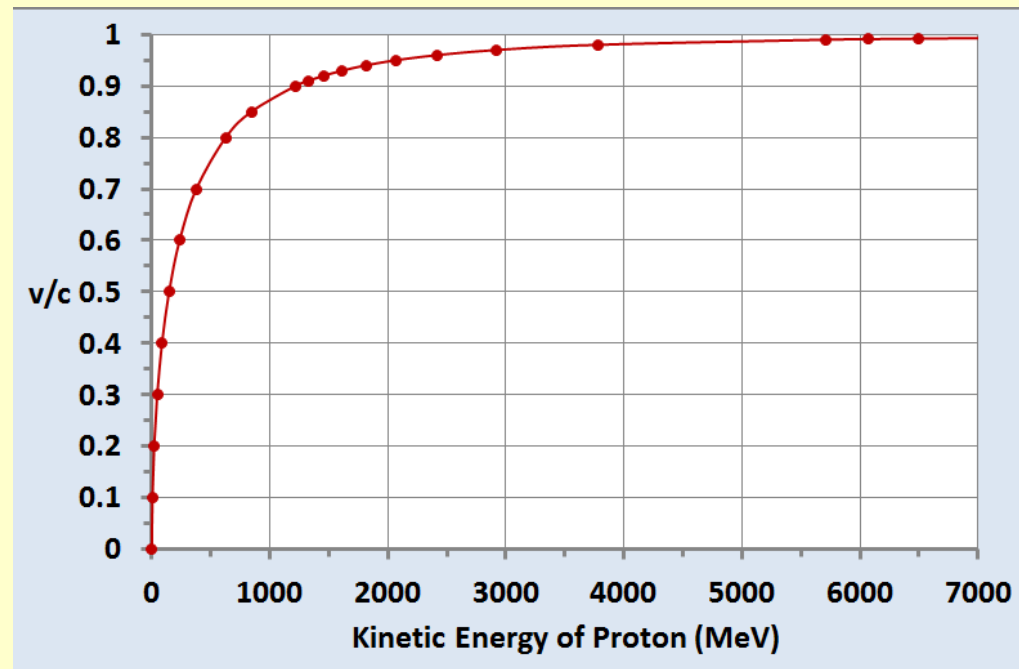
To go beyond, have to take account of relativistic Effects.

$$\omega = 2\pi f = \frac{qB_z}{m_0\gamma}$$

$$\gamma = \frac{1}{\sqrt{1 - v^2/c^2}}$$

$$E_{total} = \frac{m_0c^2}{\sqrt{1 - v^2/c^2}}$$

Machine	$\gamma$
26 MeV	26
LHC 7 TeV	7460



# Cyclotron Variations

## SYNCHRO-CYCLOTRON (Edwin McMillan, 1945)

$$\omega = 2\pi f = \frac{qB_z}{m_0\gamma}$$

Frequency of the **RF acceleration voltage decreased** so that it adjusts to changes in particle orbit due to relativistic effects.

Particles have to be bunched, beam capture → low intensity.

Can reach up to **~700 MeV**.

## ISO-CYCLOTRON

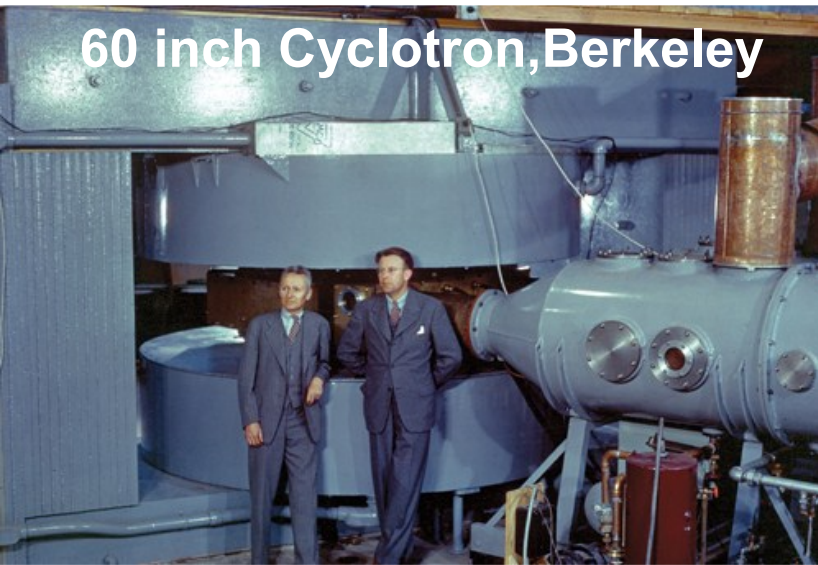
$$\omega = 2\pi f = \frac{qB_z(r(E))}{m_0\gamma} = \text{constant}$$

Keep RF frequency the same, but **increase the radial magnetic field** to compensate for mass increase.

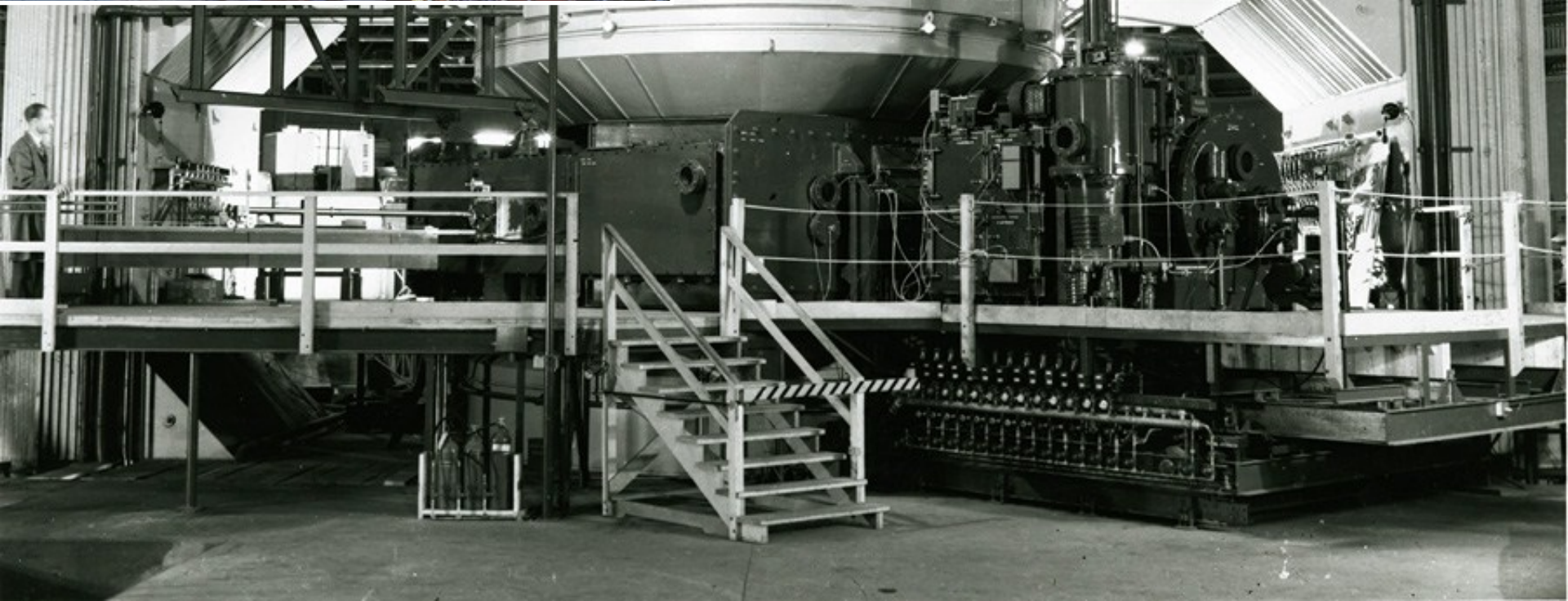
Greater beam current than synchro-cyclotron.

# Huge Magnets Needed

60 inch Cyclotron, Berkeley

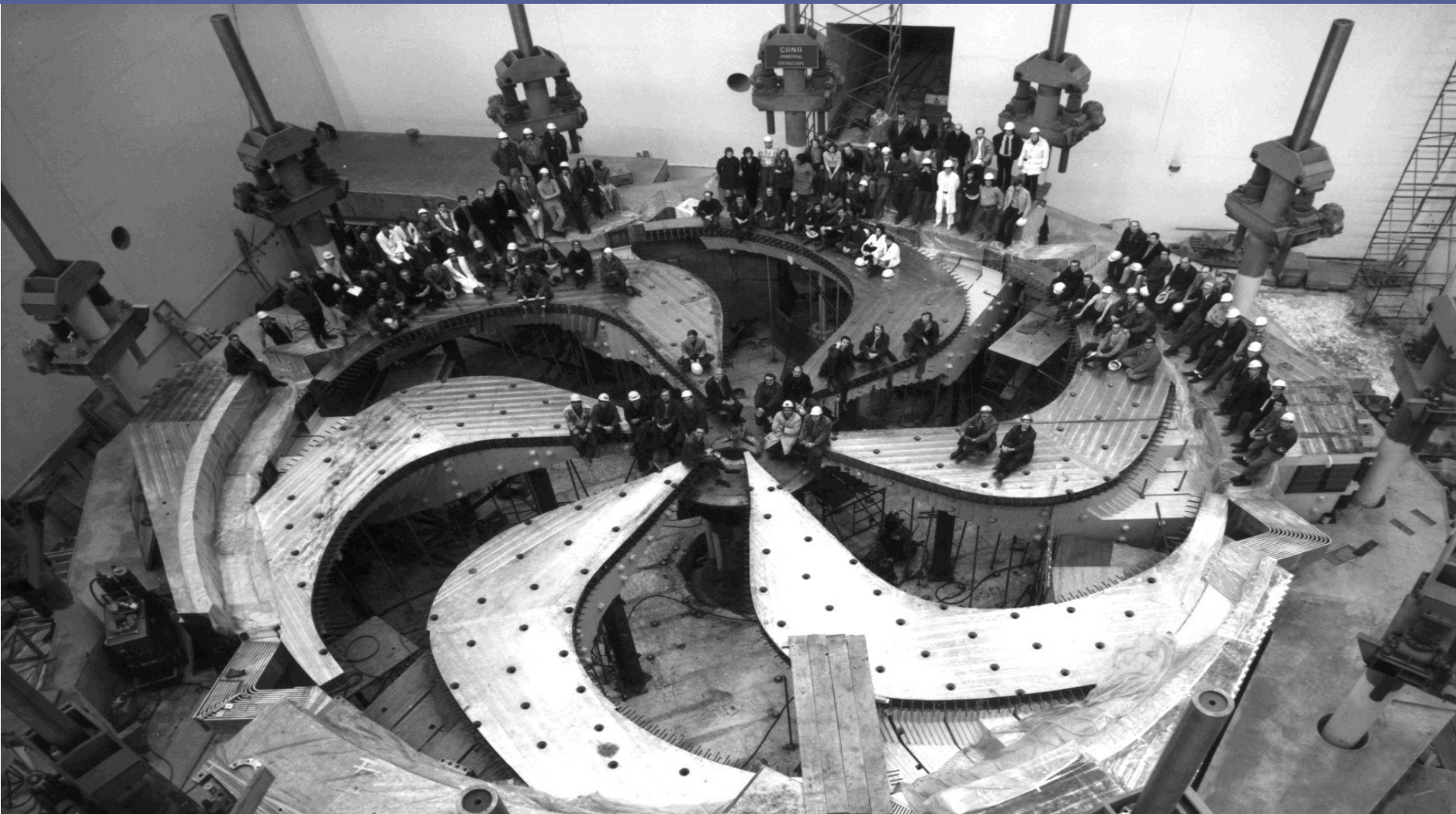


184 inch Synchrocyclotron  
Berkeley





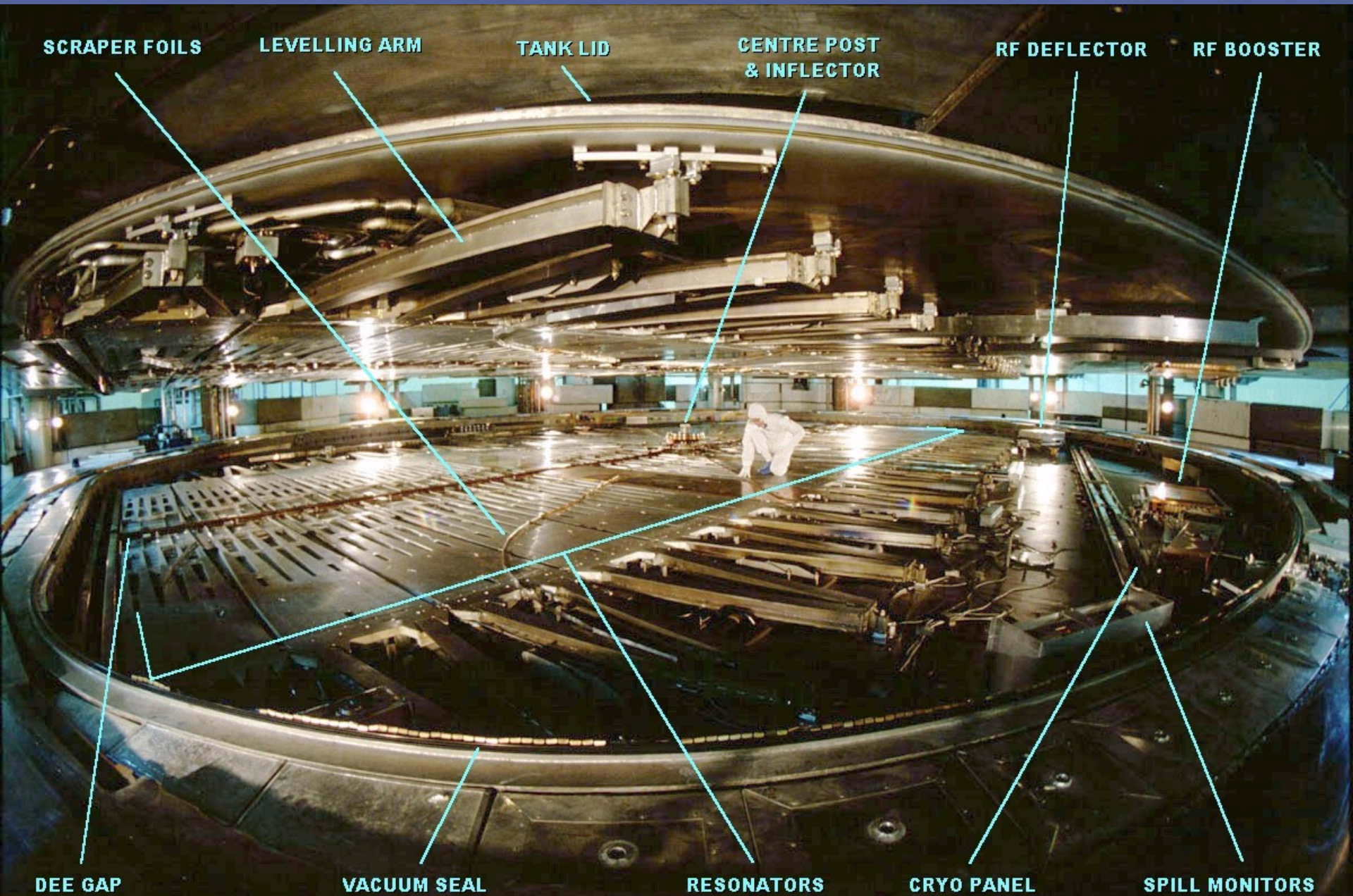
# TRIUMF Cyclotron - 500 MeV



One of the world's largest cyclotrons  
Lower six sectors of electromagnet (weight 4000 tonnes).  
Field = 0.56T, Current = 18,500 A



# TRIUMF Cyclotron - 500 MeV





# Superconducting Ring Cyclotron (SRC)

Riken, 2007 -



**Part of Radioactive Isotope Beam Factory (RIBF) at Riken  
World's highest intensity beam, 8,300 tons, 18.4m, diameter, Field=3.8 T,  
Accelerate uranium up to 350 MeV/nucleon**



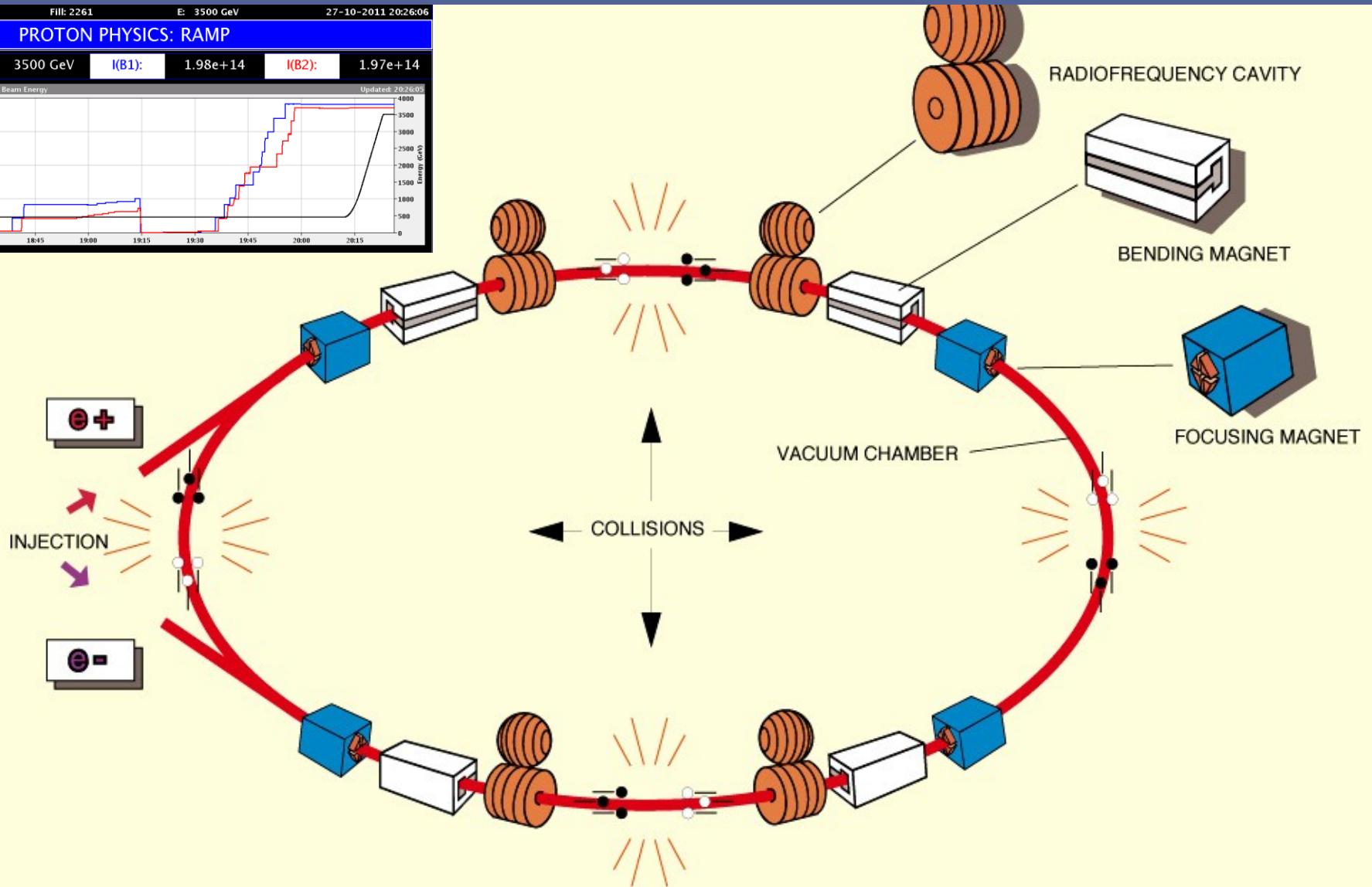
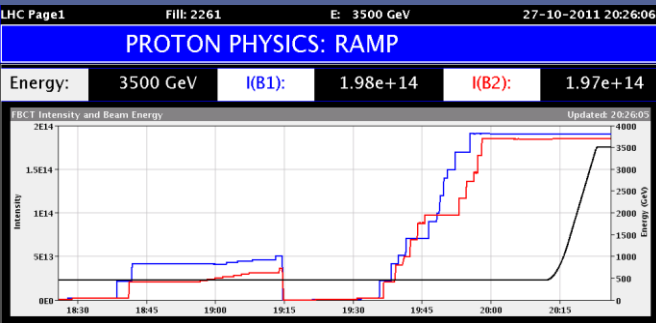
# The March of the Synchrotrons



**Bevatron, LBL (1954 – 1993)**  
**Discovered anti-proton and anti-neutron**



# Principal Components of a Synchrotron



In a **Collider**, bunches of particles/antiparticles circulate in opposite directions.



# Super Proton Synchrotron (CERN)

*6km circumference*  
*450 GeV*



**Beam pipe**

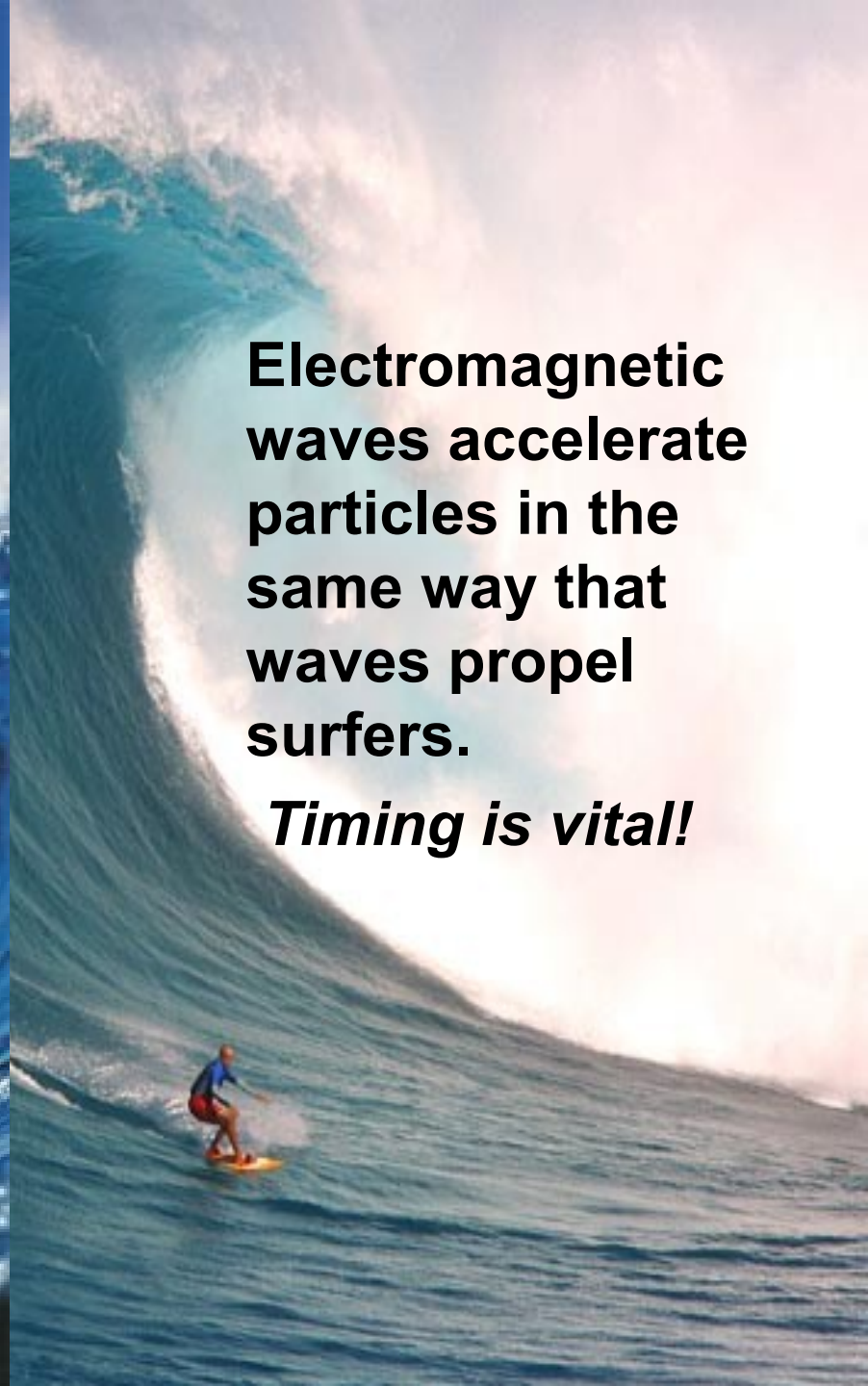
*High vacuum!*



# Bending Magnets



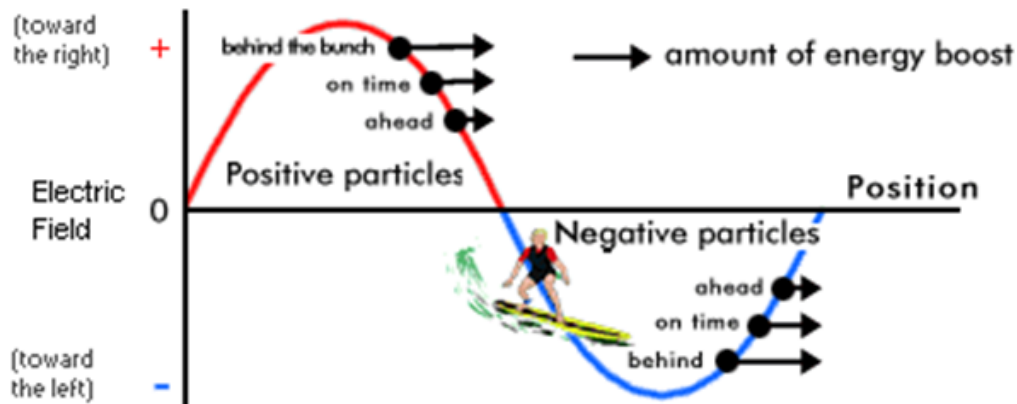




**Electromagnetic waves accelerate particles in the same way that waves propel surfers.**

***Timing is vital!***

# RF and Phase Stability



## Phase stability

Cavity set up so that particle at centre of bunch acquires just the right amount of energy.

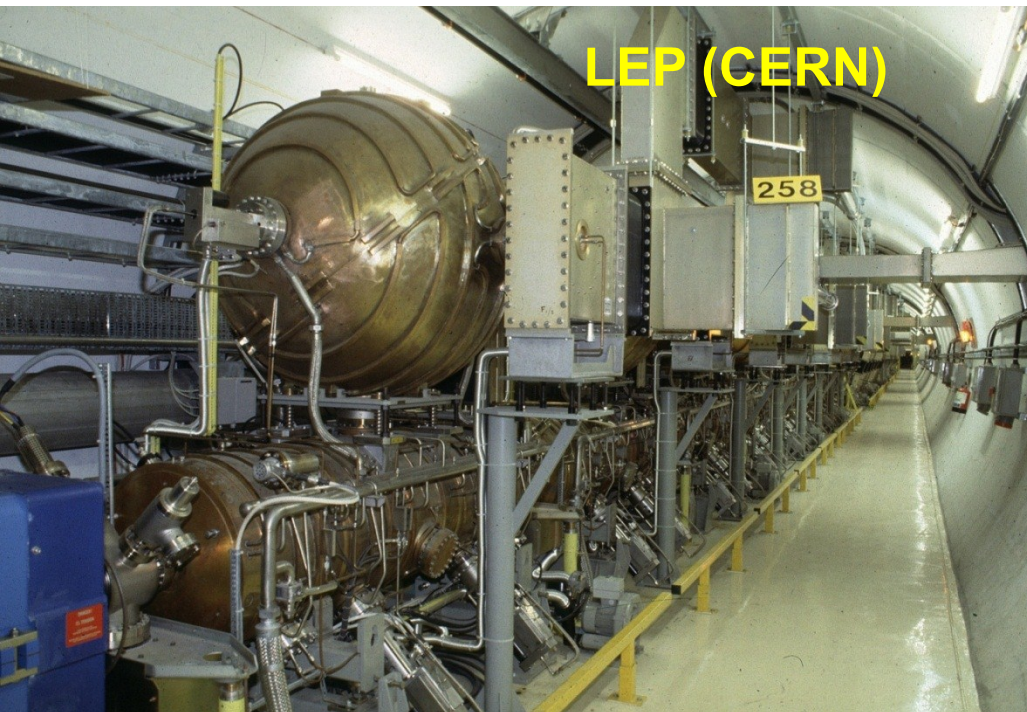
Particles see voltage:

$$V_0 \sin 2\pi\omega_{rf}t = V_0 \sin \varphi(t)$$

In case of **no acceleration**, synchronous particle has  $\varphi_s = 0$   
Particles arriving early see  $\varphi < \varphi_s$   
Particles arriving late see  $\varphi > \varphi_s$   
Energy of those arriving early is decreased and vice-versa.

To **accelerate** make  $0 < \varphi_s < \pi$  so that synchronous particle gains energy.

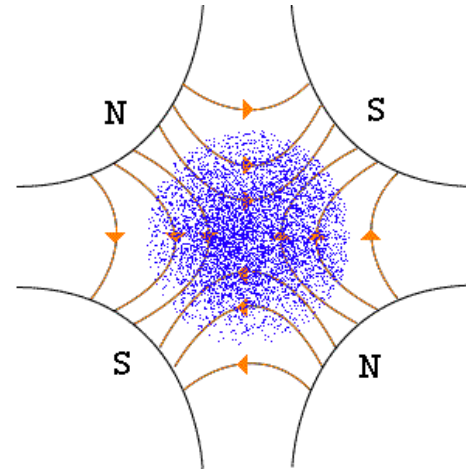
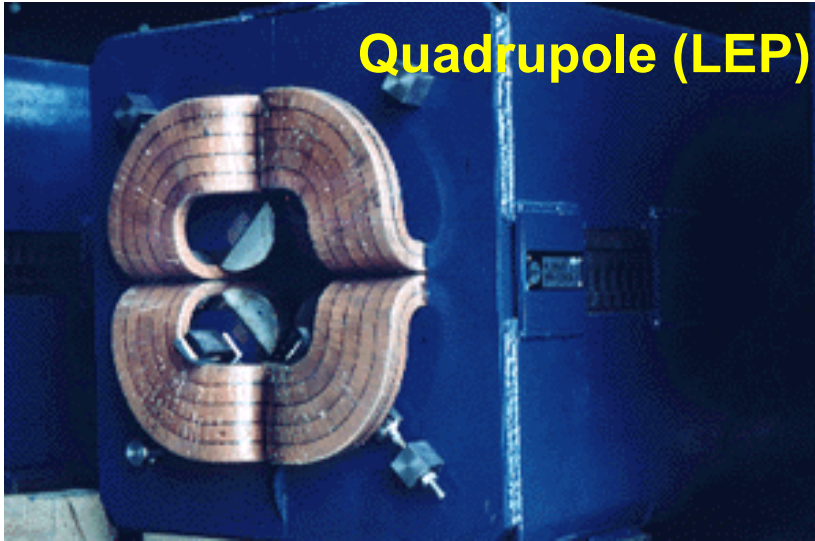
$$\Delta E = qV_0 \sin \varphi_s$$





# Focussing Magnets

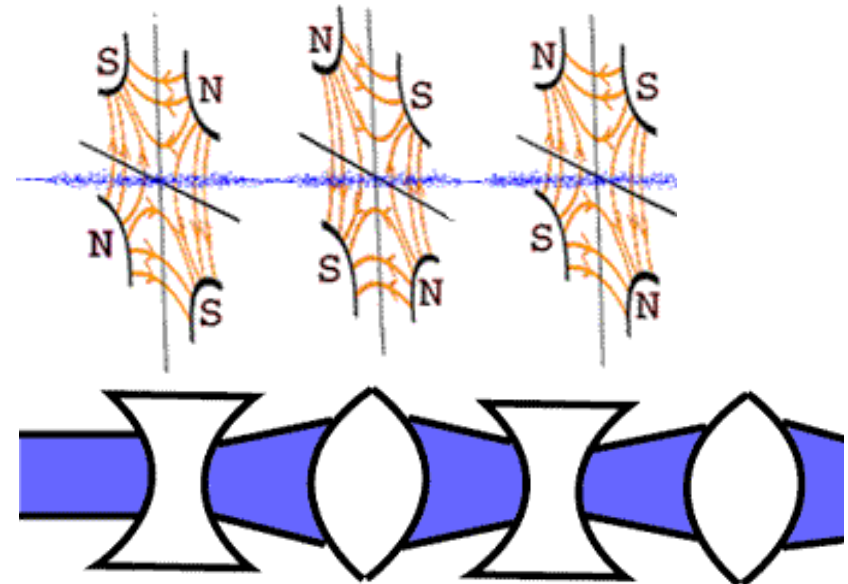
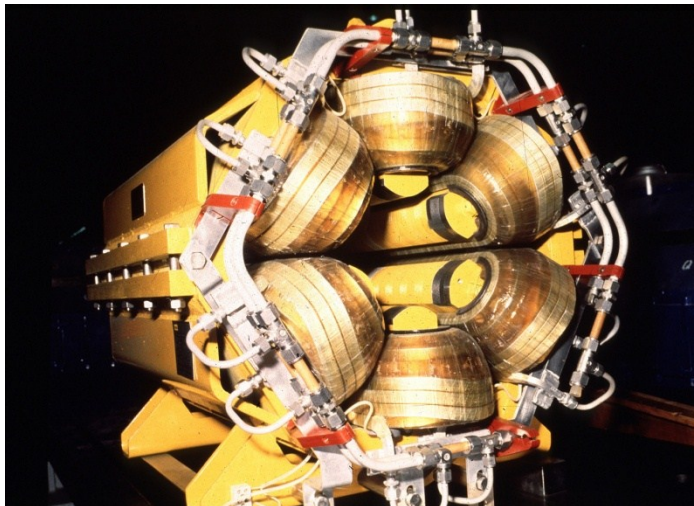
**Quadrupole (LEP)**



**Strong Focussing**  
Beam alternately  
focussed in horiz  
and vert planes.

**Sextupole (LEP)**

Correction of chromatic spread.



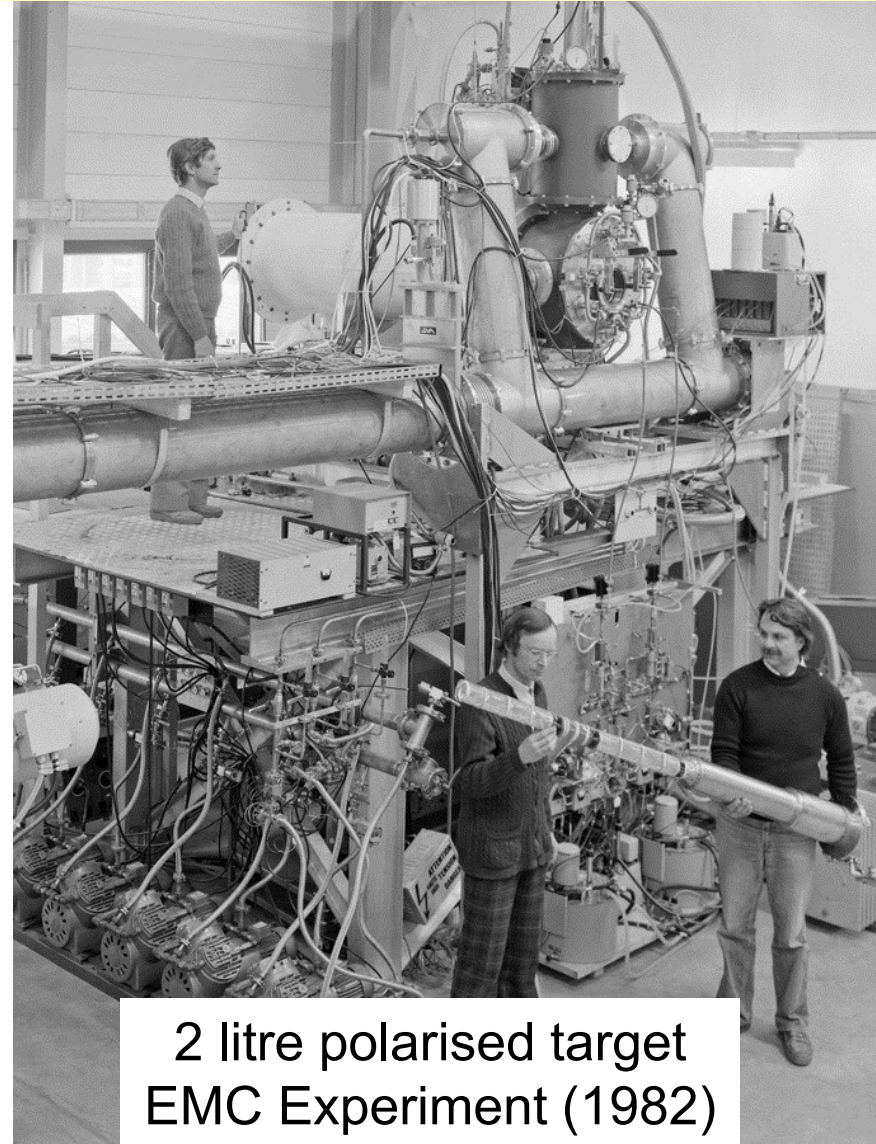


# Fixed Target Experiments

Rutherford used a fixed target of gold foil. Same idea used up to the 1980s with liquid hydrogen (lots of protons) commonplace as the target.



Hydrogen target  
EMC Experiment (1978)



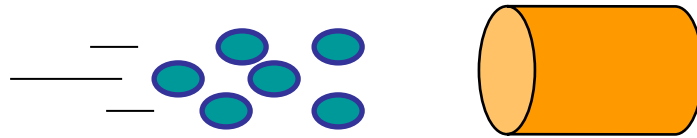
2 litre polarised target  
EMC Experiment (1982)

# Colliding Beam Machines

Rolf Wideroe (Norway) first had the idea of colliding two beams of particles head-on in order to maximise the energy available.

Bruno Touschek applied the idea.

Fixed target

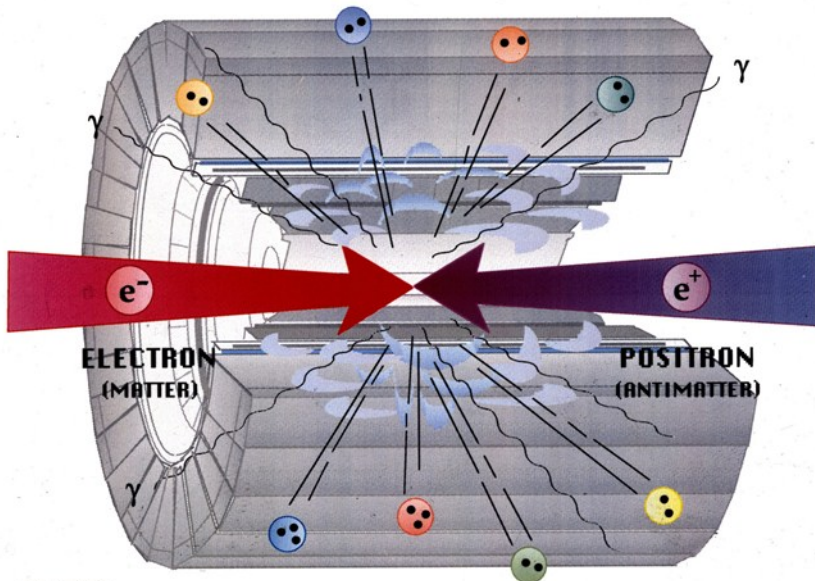


$$E_{CM} \approx \sqrt{(2m_T E_b)}$$

Collider

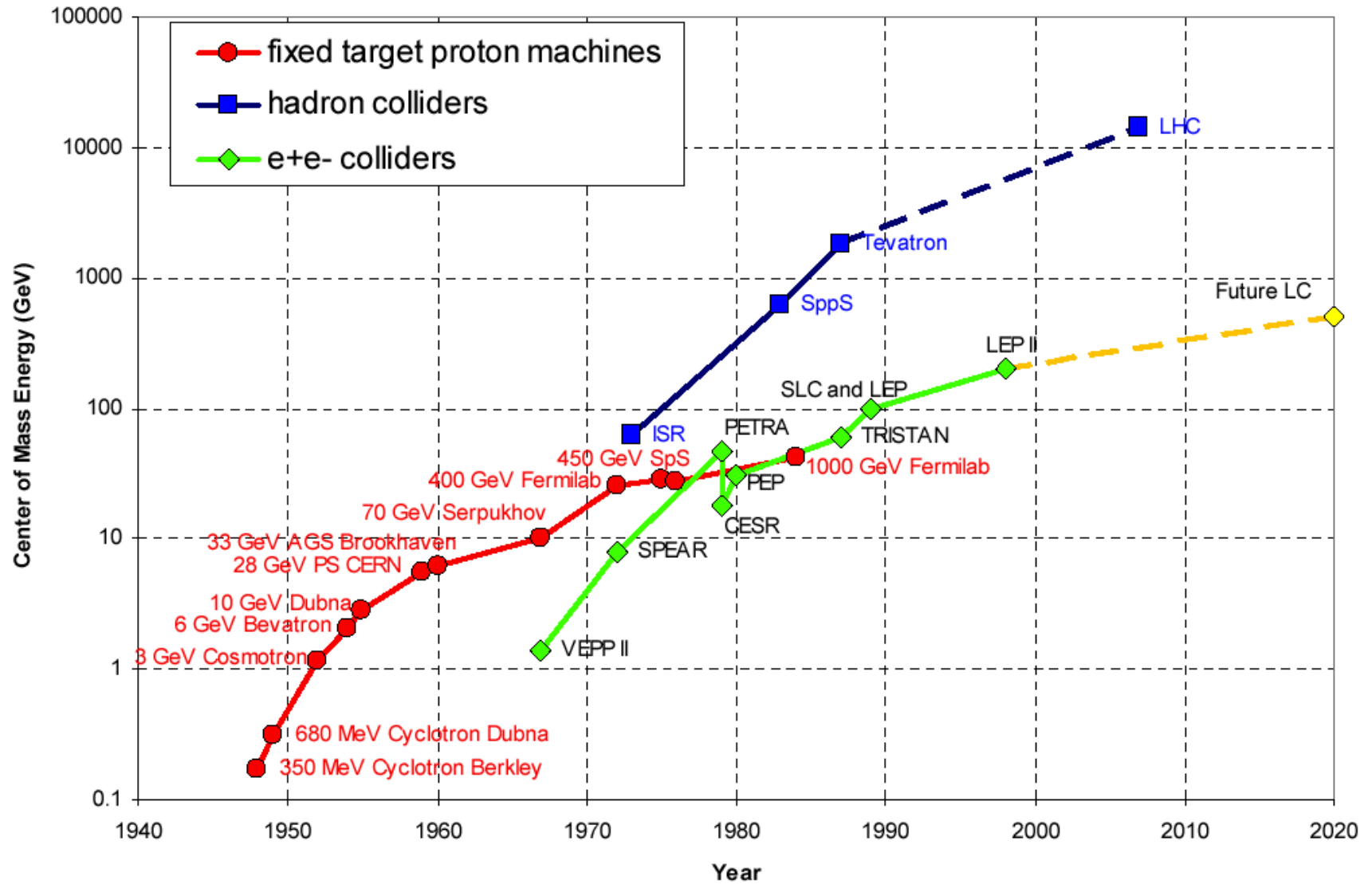


$$E_{CM} \approx 2E_b$$



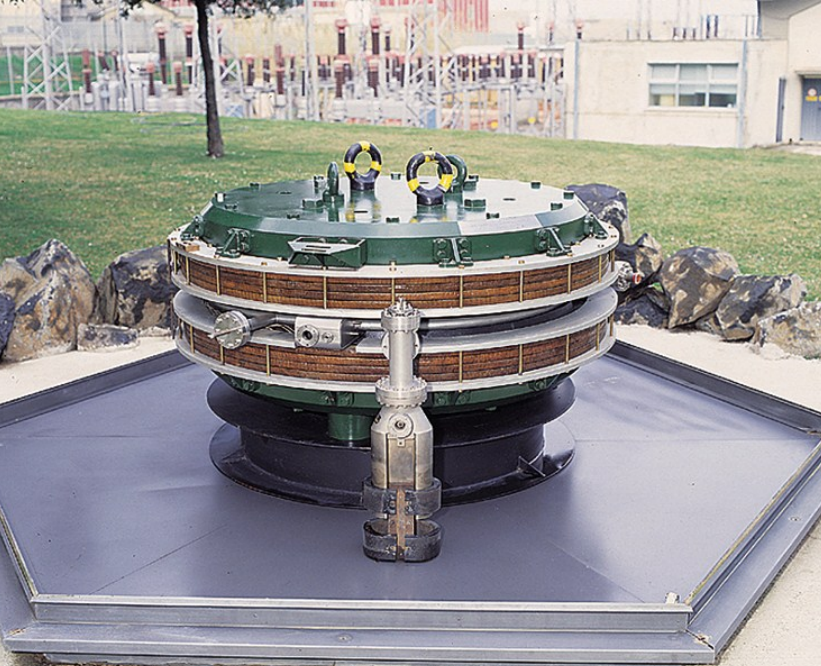
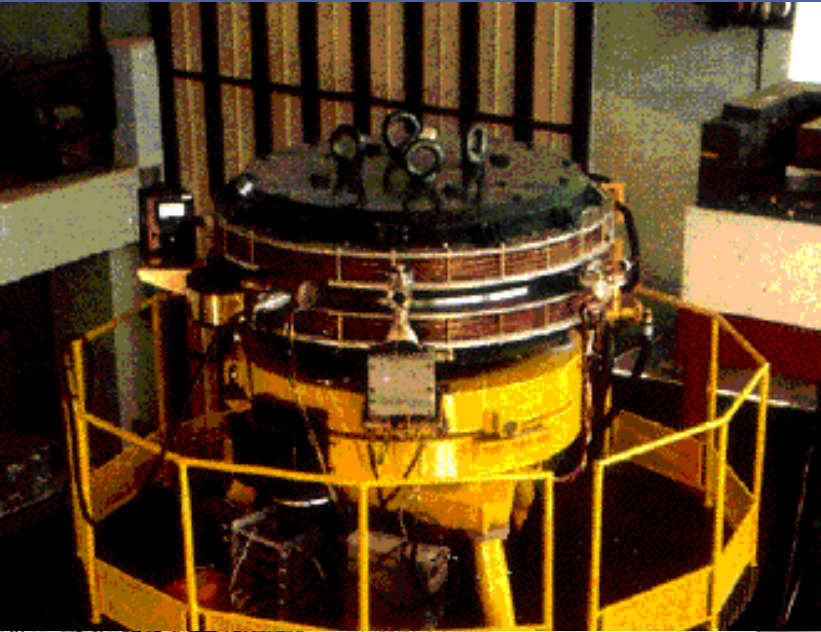
- $E_b = 100 \text{ GeV}$
- $E_{CM} = 200 \text{ GeV}$  in  $e^+e^-$  collider.
- $E_{CM} = 0.32 \text{ GeV}$  for  $e^+$  beam hitting an atomic electron.

# Energy Frontier





# Colliding Electrons and Positrons



First electron-positron collider:  
**AdA, Frascati, Italy (1961-1964).**



- Shipped to LAL, Orsay, France to locate alongside a better injector - a high intensity linear accelerator.
- First electron-positron interactions observed in 1964.
- Spawned a series of  $e^+e^-$  colliders: ADONE (Italy), VEPII (Russia) and most notably SPEAR (USA). Later PETRA, PEP, LEP...

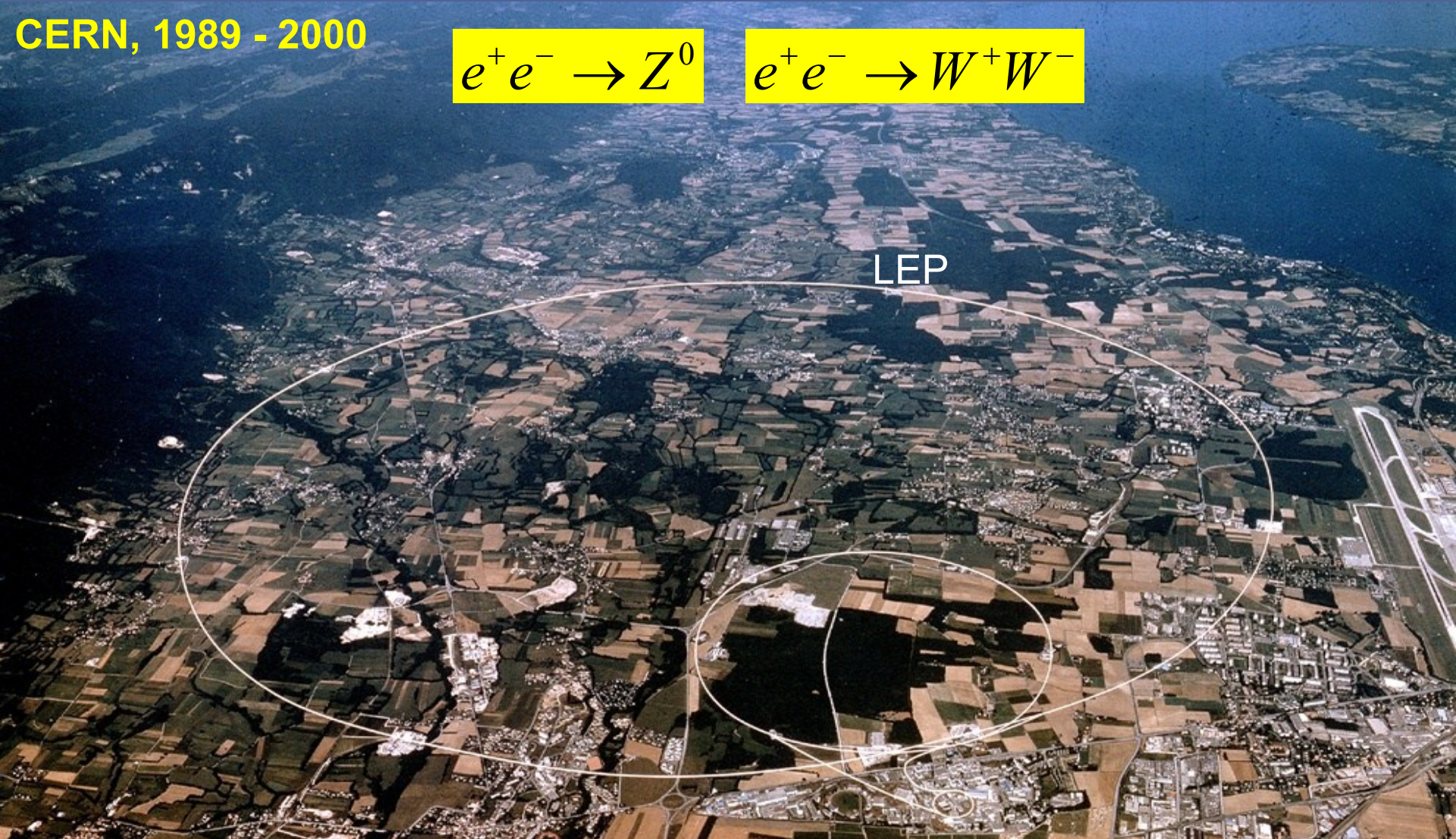


# Large Electron Positron Collider (LEP)

CERN, 1989 - 2000

$$e^+e^- \rightarrow Z^0$$

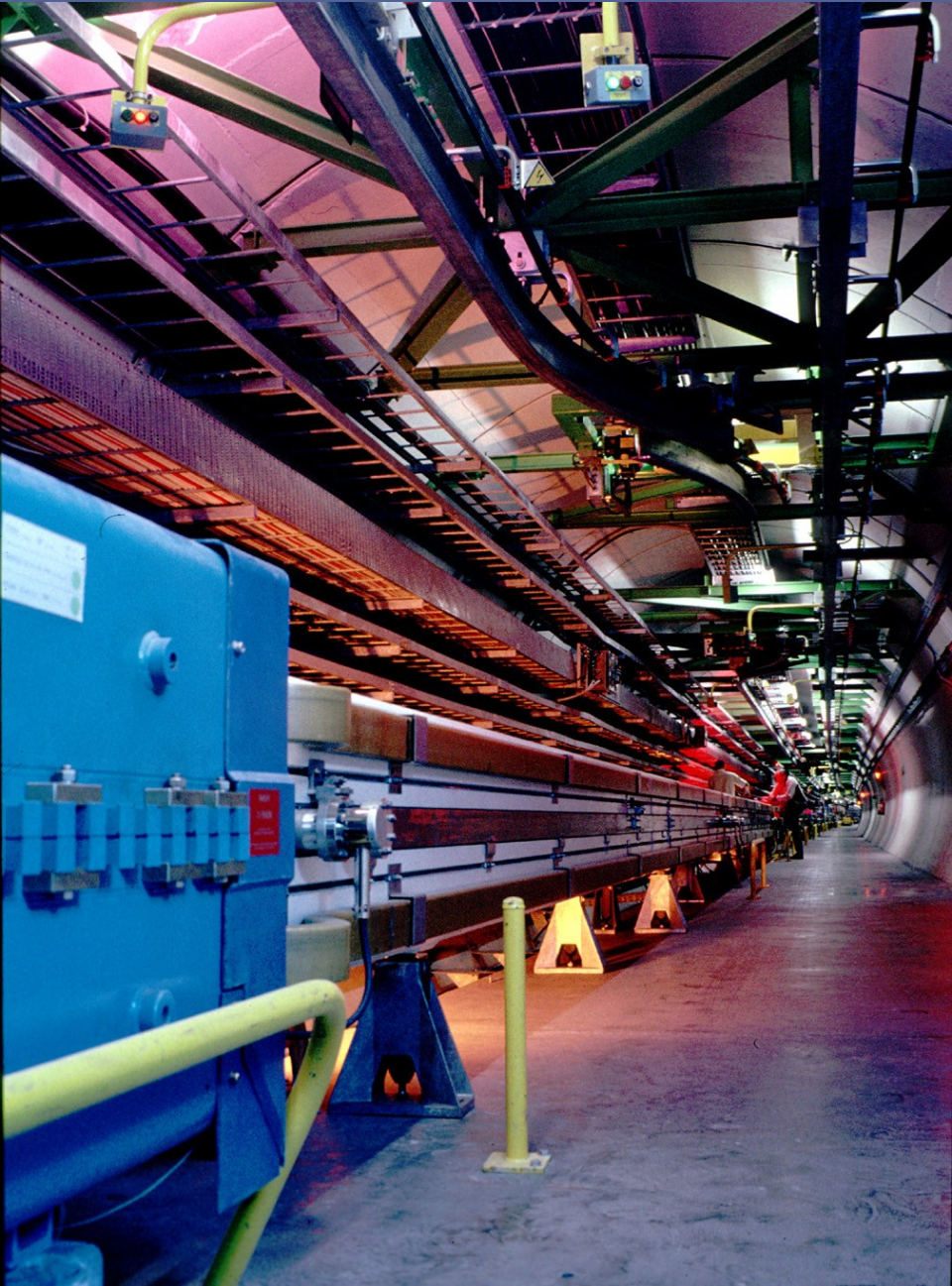
$$e^+e^- \rightarrow W^+W^-$$



**27km circumference , CM energy = 209 GeV, 3,368 dipoles  
revolution frequency = 11,245.5 Hz,  $10^{11}$  particles/bunch**



# LEP - Z Factory





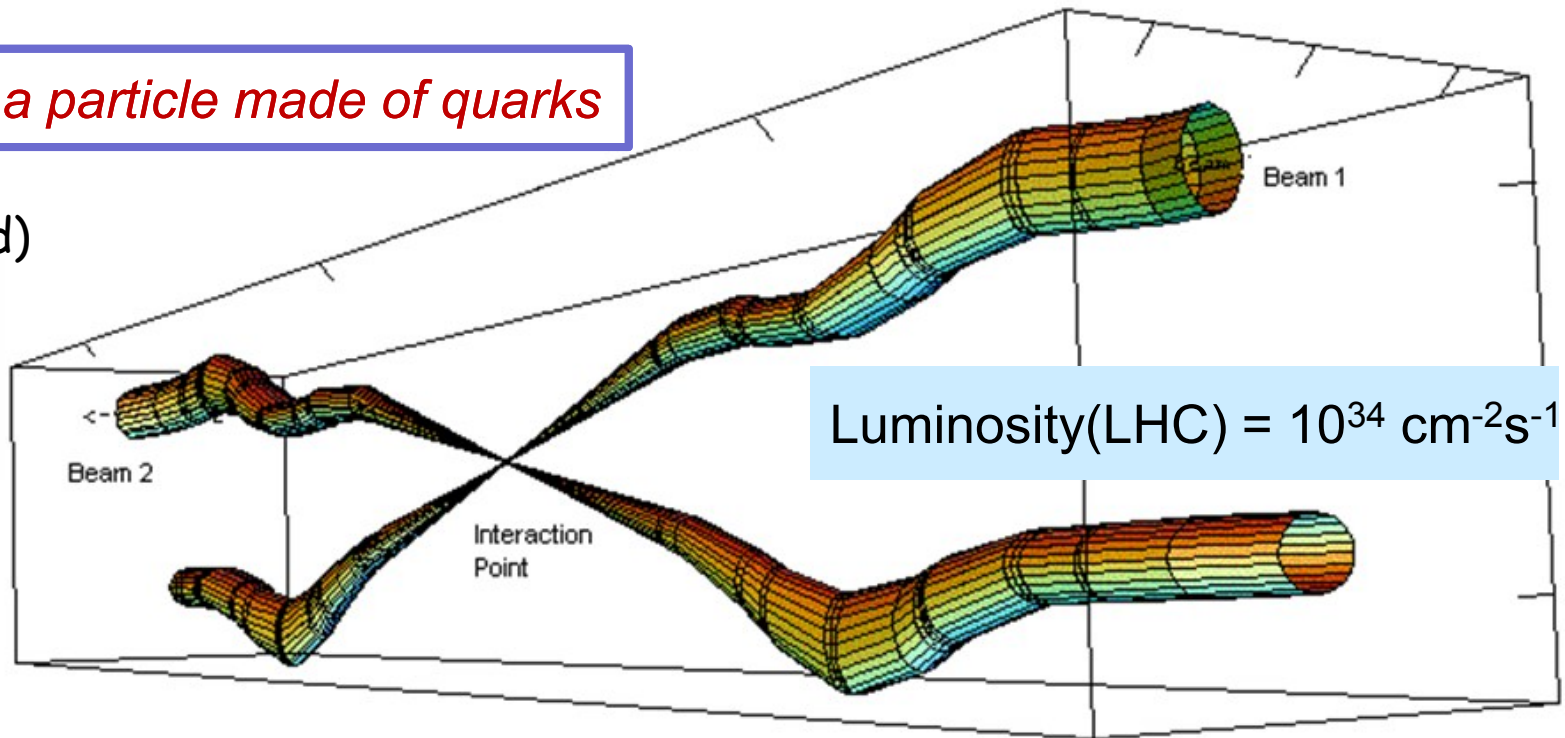
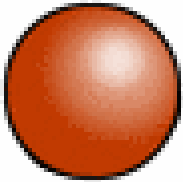
# Hadron Colliders - Quark Machines

*“Splitting the atom by bombardment is something like shooting sparrows in the dark in a place where there are only few birds”.*

Albert Einstein (1934)

**Hadron** – a particle made of quarks

proton (uud)



*The Large Hadron Collider has to collide bunches of 100 billion protons squeezed to 16 microns in diameter around a 27km ring!*



# Intersecting Storage Rings (1971-1984)

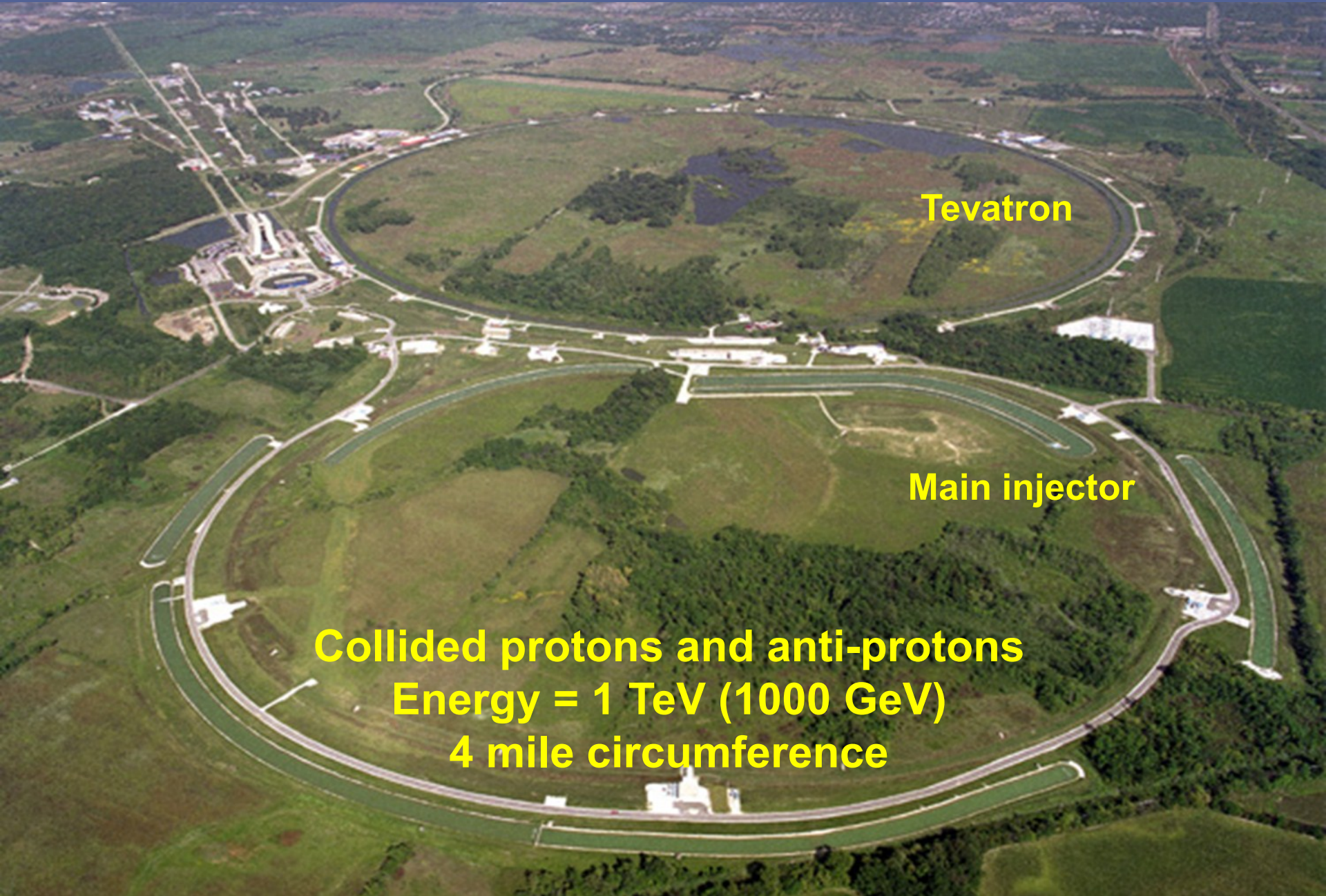
**27 January 1971:** Two beams of protons collided in the *Intersecting Storage Rings (ISR)* at CERN for the first time. World's first hadron collider paving the way for the LHC.



- Important for research in accelerator physics.
- Necessary technical step to SPS ppbar, LEP and LHC colliders.
- Stochastic cooling invented .
- No major discovery of historical importance.
- Missed out on Nobel prizes for  $J/\psi$  and  $Y$  particles.



# Tevatron (FermiLab, Chicago)



**Tevatron**

**Main injector**

**Collided protons and anti-protons**  
**Energy = 1 TeV (1000 GeV)**  
**4 mile circumference**



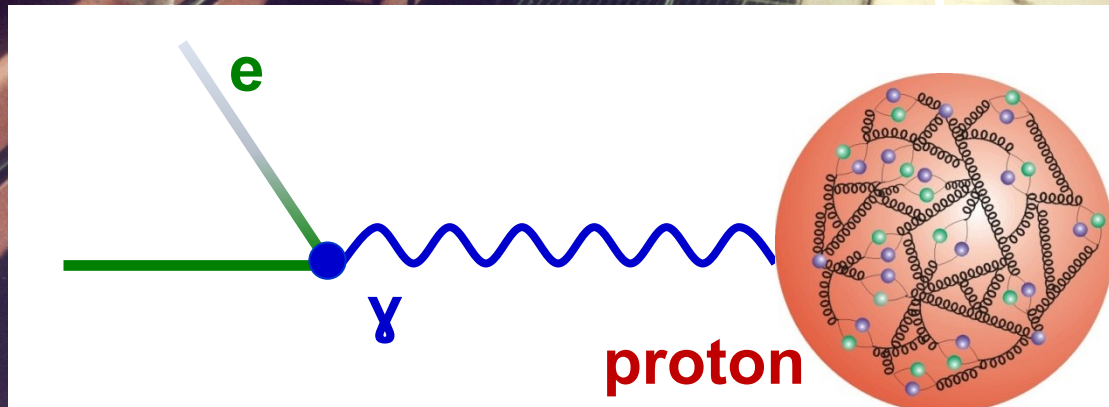
# Electron Proton Collider - HERA(6.3 km)

Hamburg, 1992-2007

920 GeV protons

27.5 GeV electrons/positrons

E.ZANEN  
ANSALDO  
EUROPAMETALLI - LMI





# Large Hadron Collider (LHC)



***27km circumference , ~100m underground***

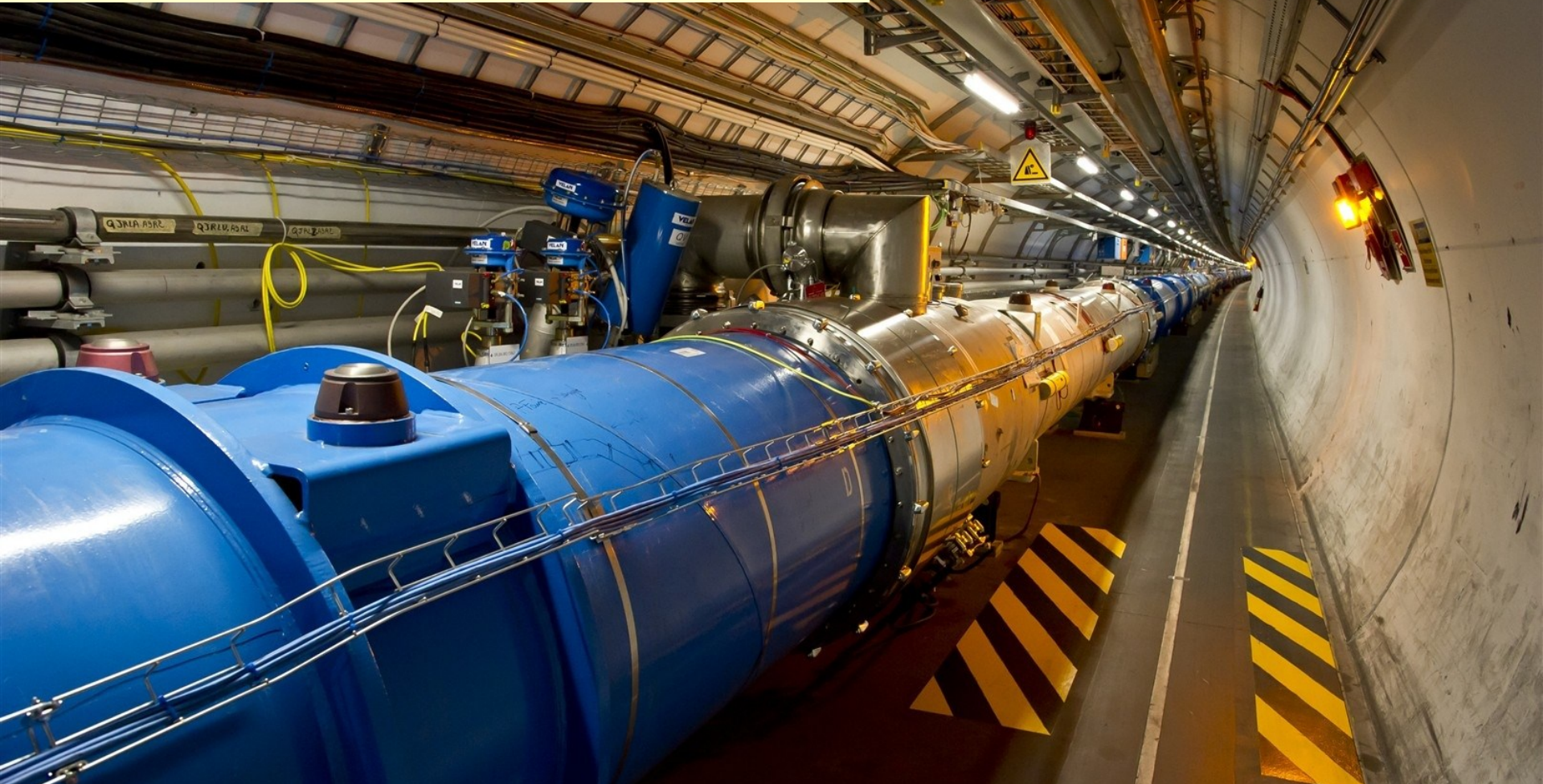


# Large Hadron Collider (LHC)

**Crossing rate = 40 MHz**

**800 million proton-proton collisions/sec**

**Velocity(proton) =  $0.999999991c$**

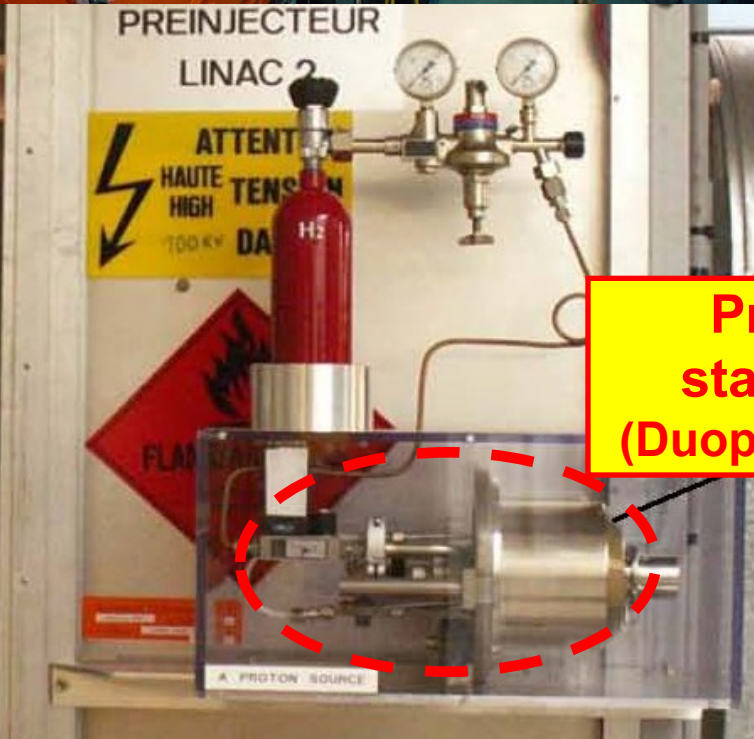


***The most energetic sub-atomic particles on the planet.***

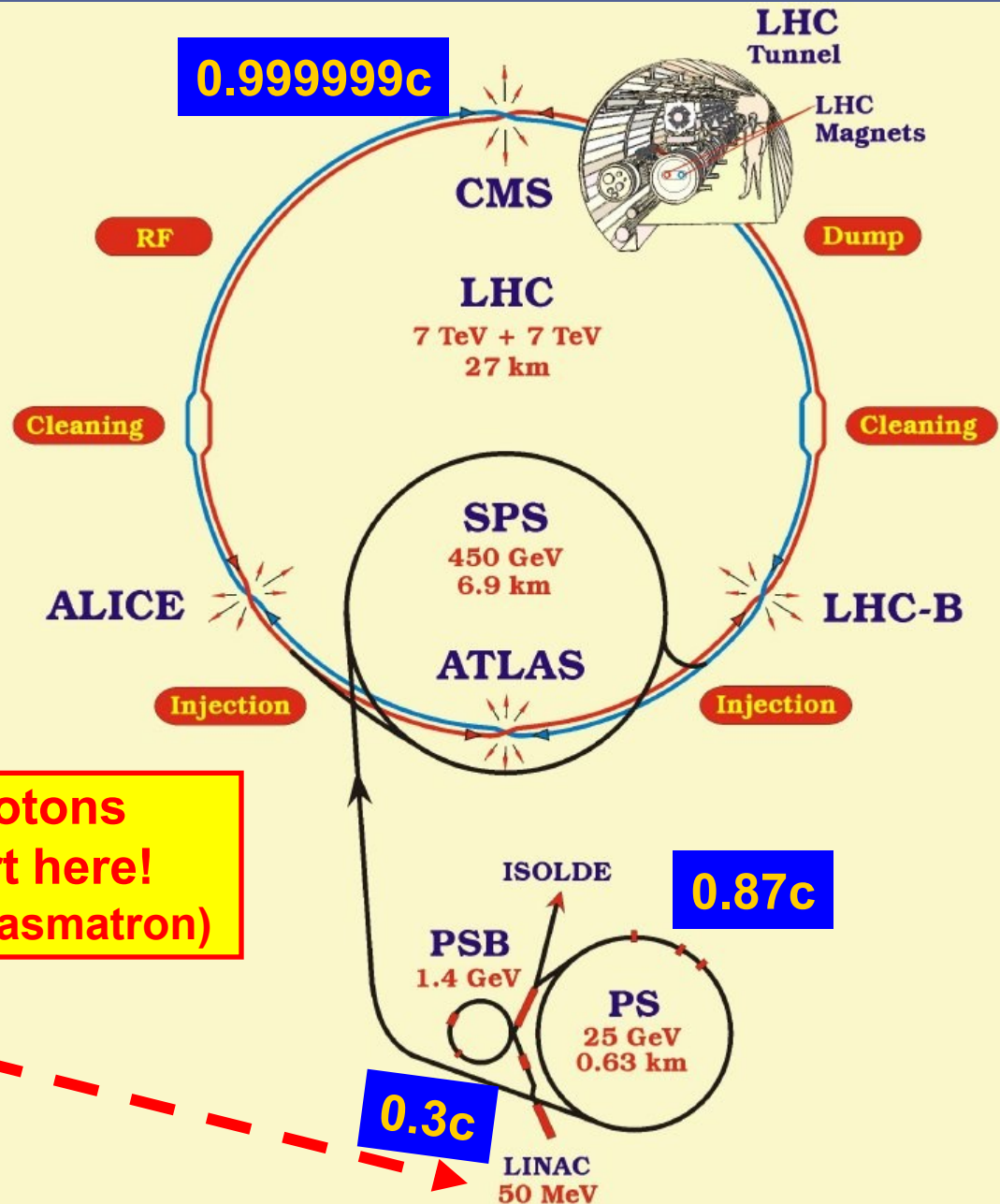


# Not Just One Accelerator

**LINAC 2 – 50 MeV**



**Protons start here! (Duoplasmatron)**

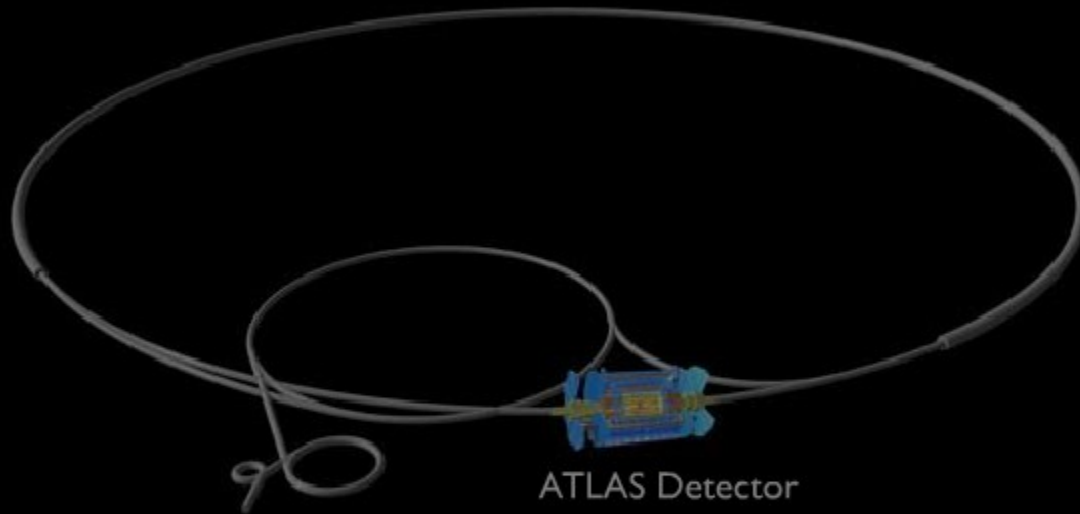




# How it Works

PLAY ▶

Large Hadron Collider



ATLAS Detector

# Bending Magnets



1,232 cryodipoles – 8 Tesla



LHC design magnet current = 11,850A,  
but the machine is 27km long!

$$P = I^2 R$$

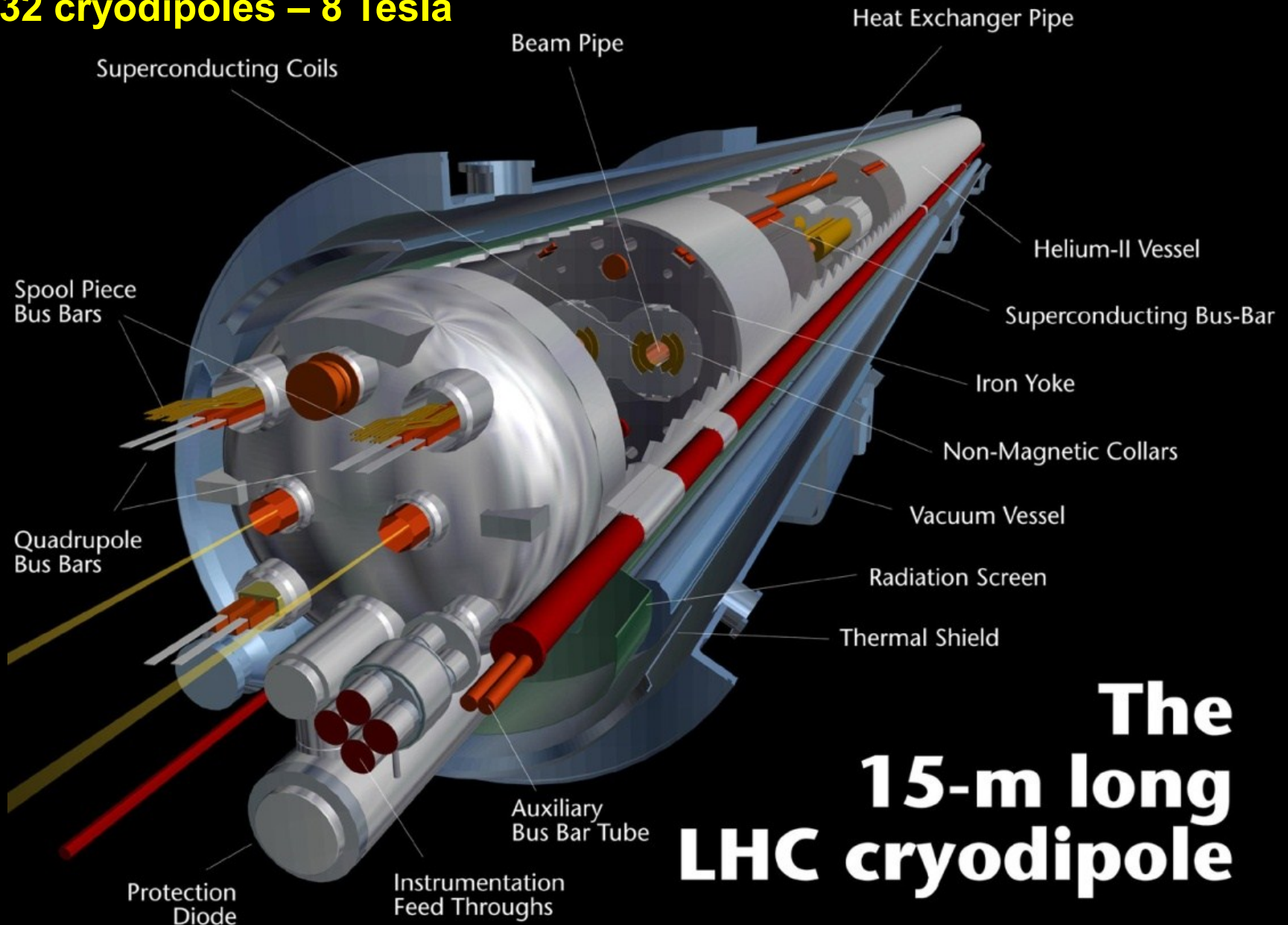
Reduce ohmic losses to a minimum.

Solution: ***Superconductivity***



# Bending Magnets

**1,232 cryodipoles – 8 Tesla**



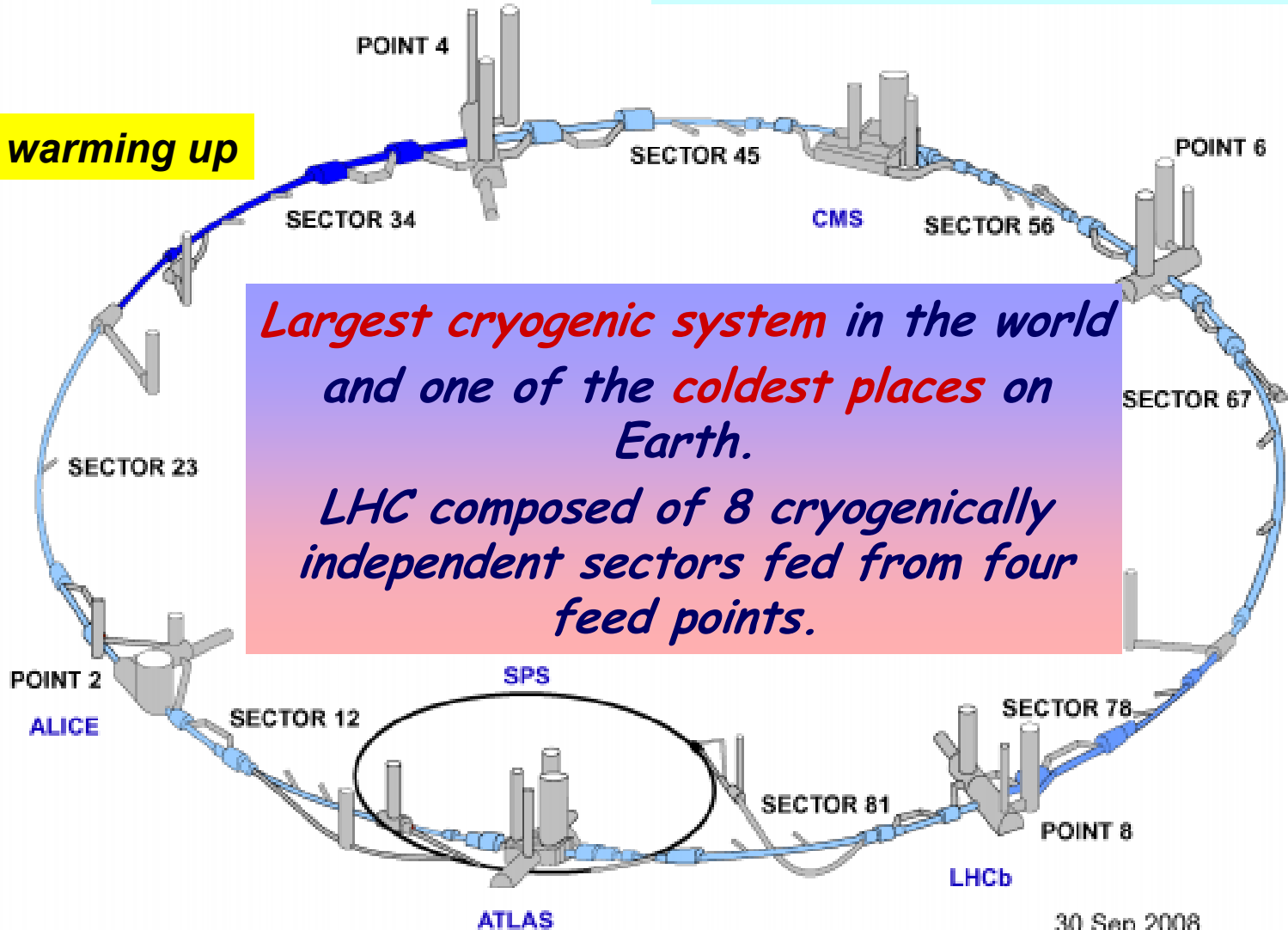
**The  
15-m long  
LHC cryodipole**

# Very Cold Machine



**7 sectors at 1.9K = -271.1°C**

**Sector warming up**



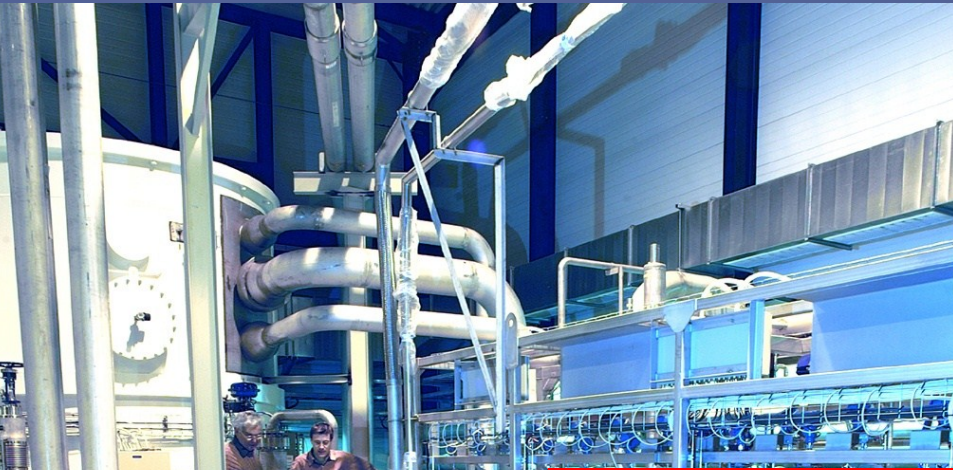
*Largest cryogenic system in the world and one of the coldest places on Earth.*

*LHC composed of 8 cryogenically independent sectors fed from four feed points.*

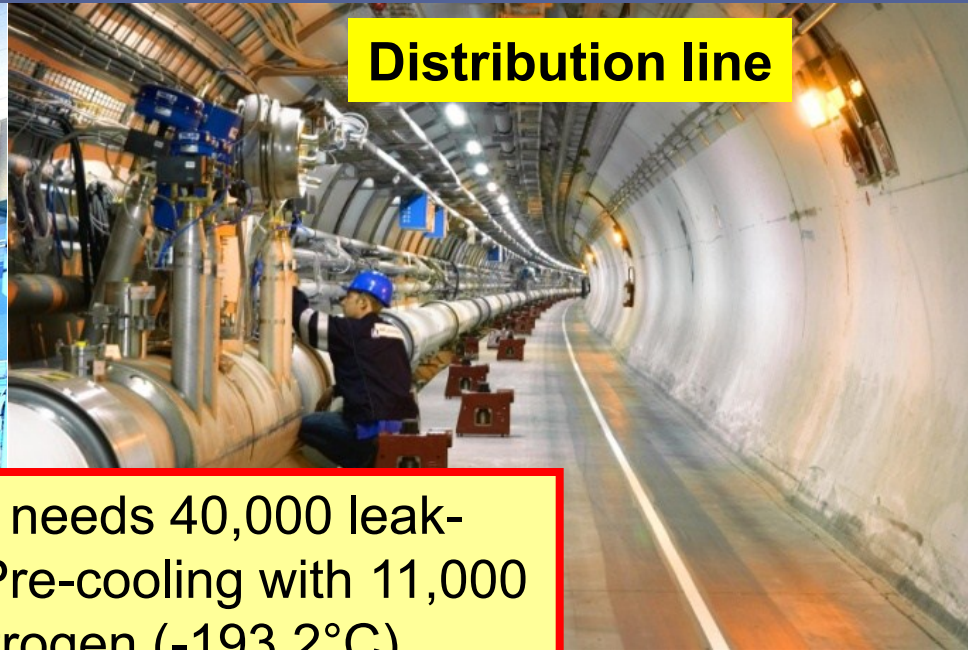
30 Sep 2008



# Superconducting Cryogenics



**4.5K refrigerator**



**Distribution line**

LHC cryogenics needs 40,000 leak-tight junctions. Pre-cooling with 11,000 litres of liquid nitrogen ( $-193.2^{\circ}\text{C}$ ). Total inventory of liquid helium is 700,000 litres (100 tonnes).

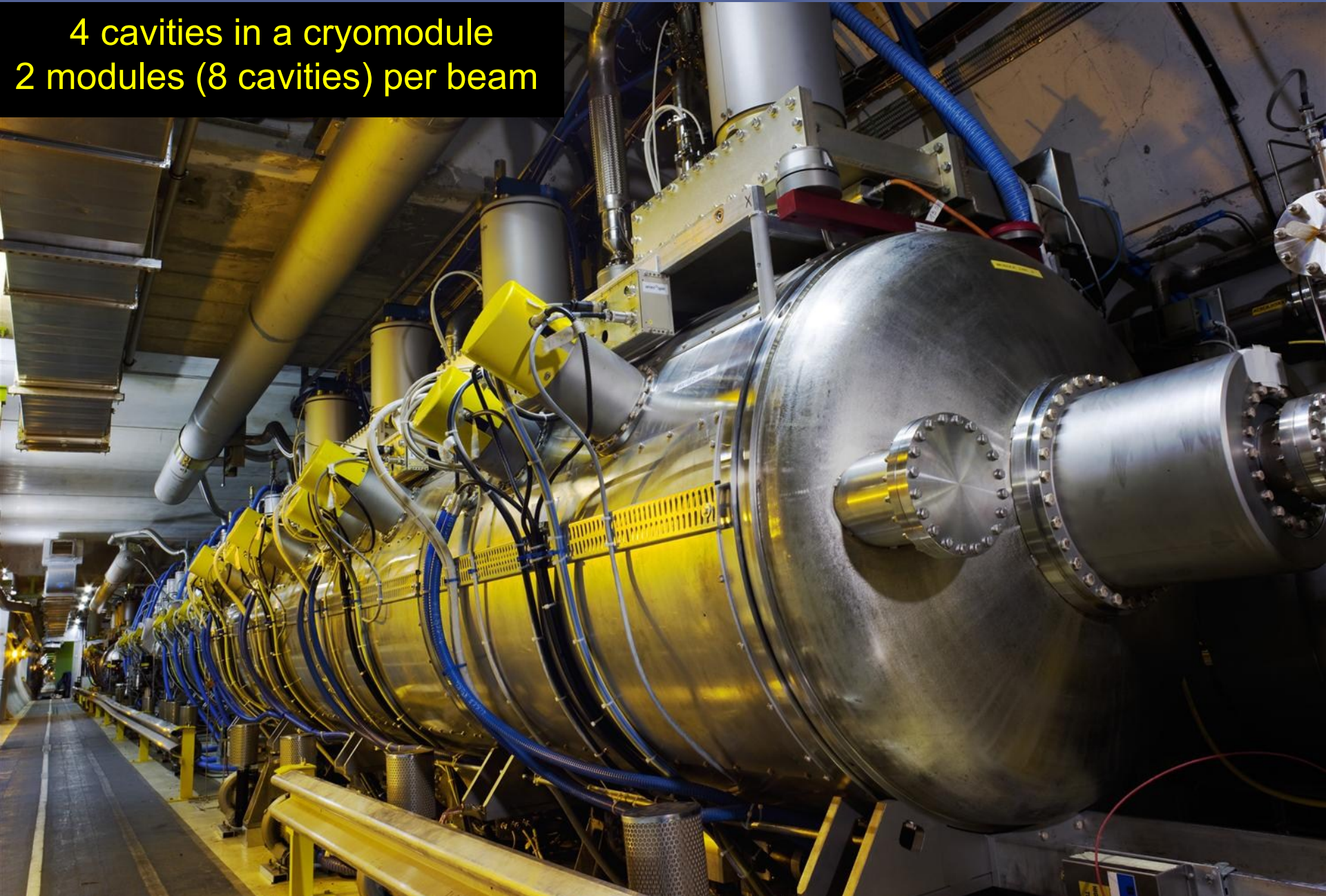


**He Storage**



# Superconducting RF Cavity

4 cavities in a cryomodule  
2 modules (8 cavities) per beam





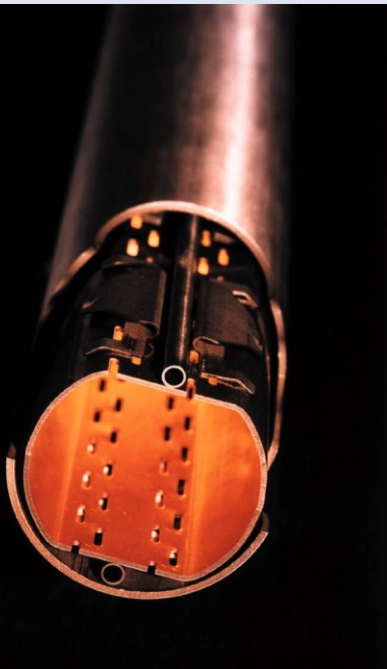
# Proton Beams

Each bunch of 100 billion protons is squeezed to 16 microns in diameter as they approach the experiments.

Peak Luminosity  $\sim 10^{34} \text{ cm}^{-2}\text{s}^{-1}$

**Energy stored** in one beam is 360 MJoule.

- Energy of TGV train at 150 km/hour.
- 77 kg of TNT.
- Enough to melt 0.5 tonne of copper.
- Aircraft carrier travelling at 12 knots.



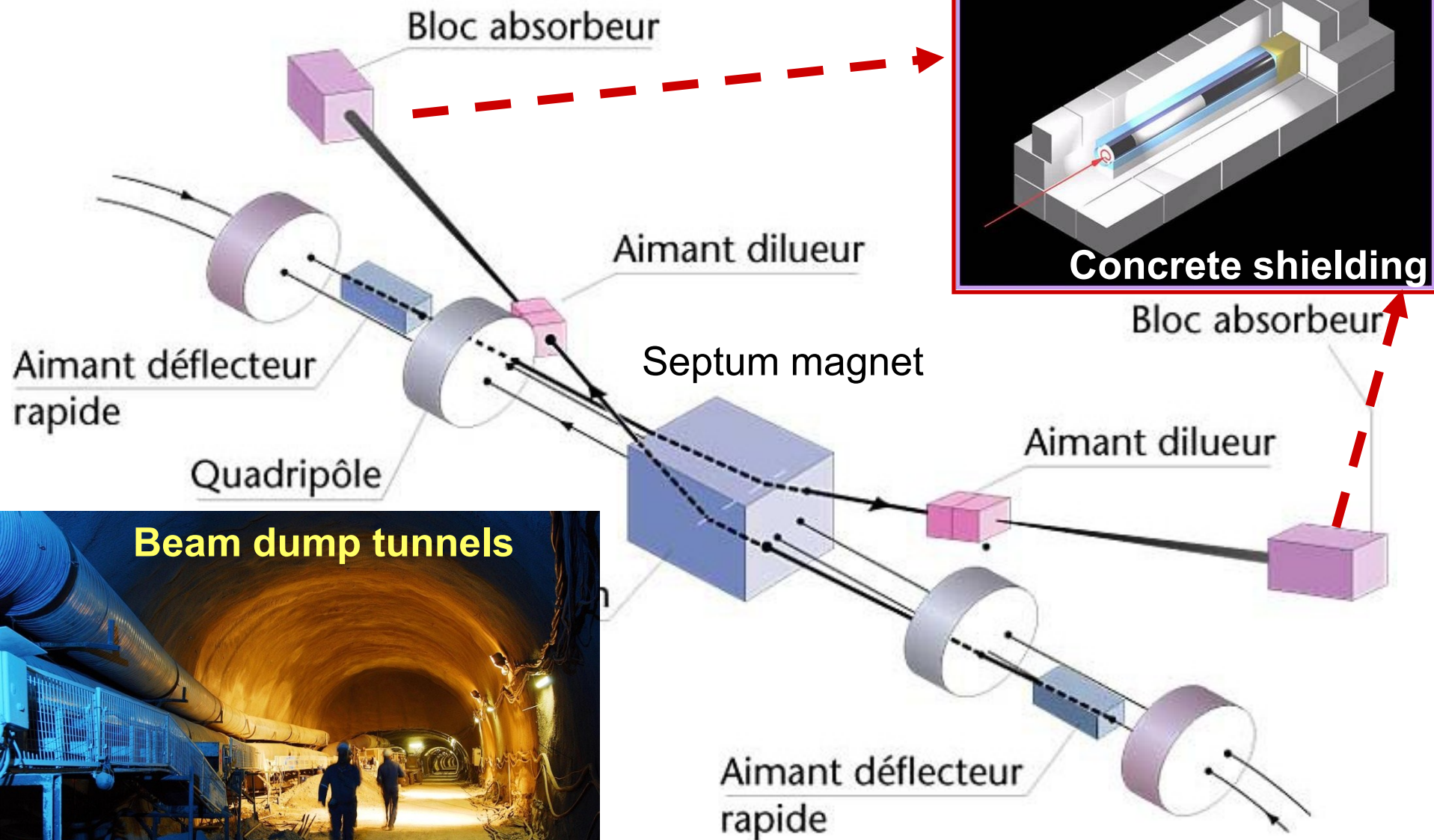
Vacuum  $\sim 10^{-13}$  Torr.

Total pumped volume  
 $\sim 6500 \text{ m}^3$

Size of a cathedral!

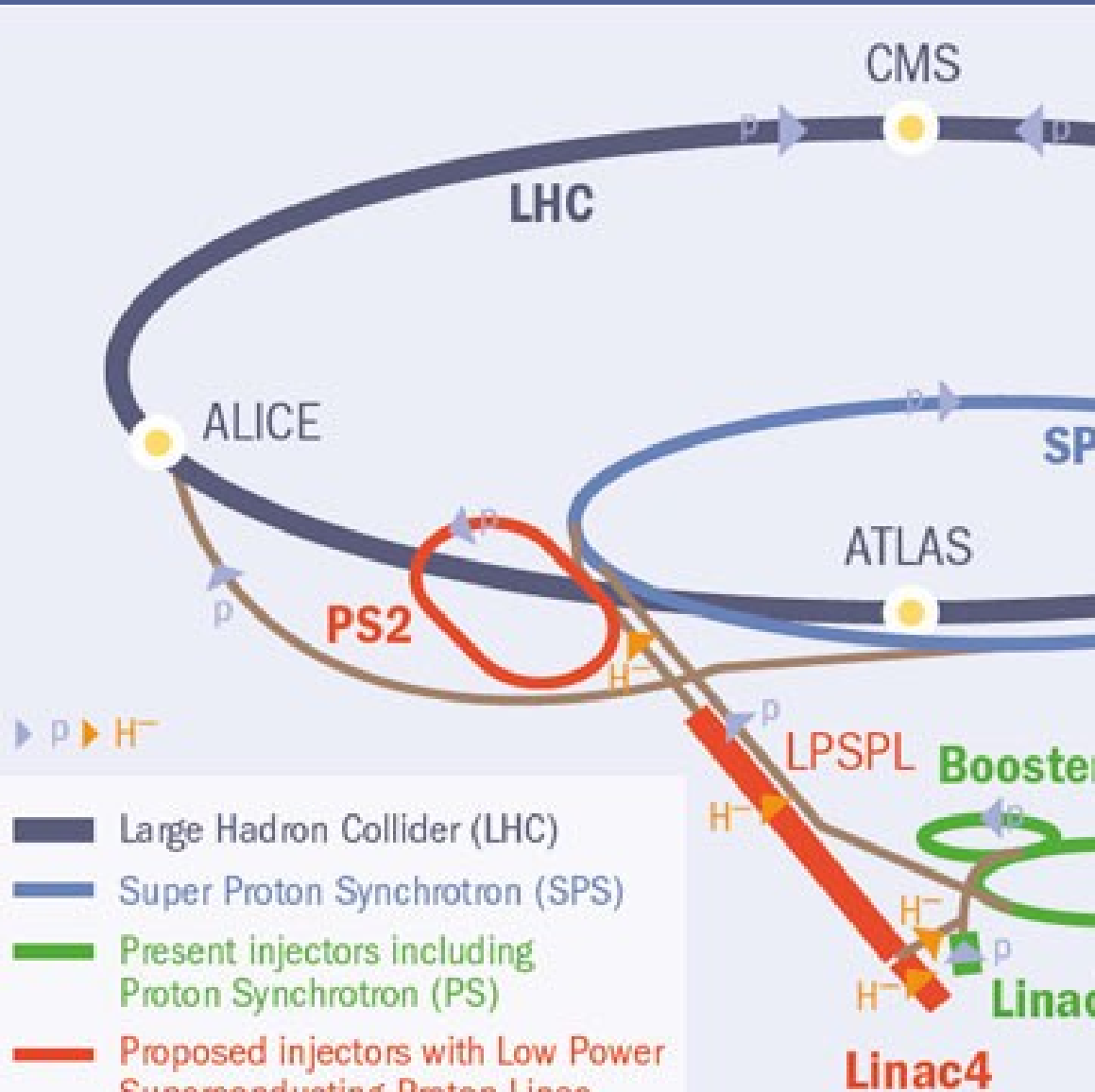


# Beam Dumps





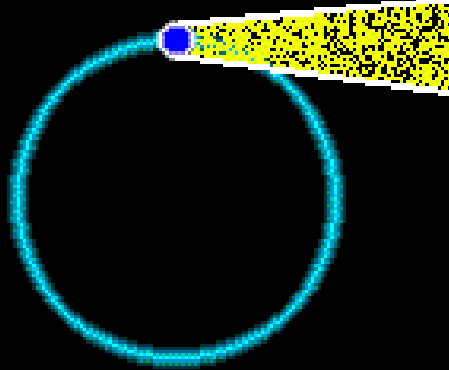
# Intensity Frontier: Super LHC



**LINAC4**  
*In the beginning...*

**New injector accelerators  
Increase luminosity by a factor of 10**

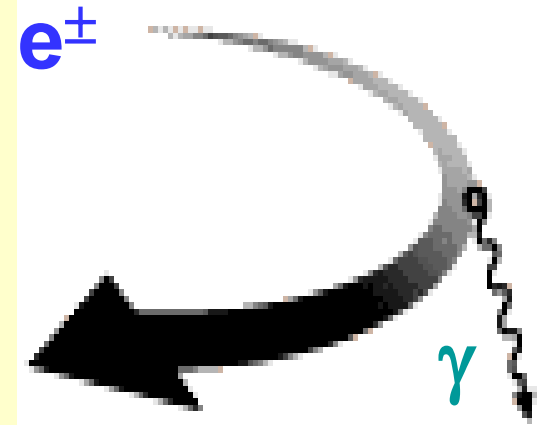
# Synchrotron Radiation



A charge undergoing acceleration will radiate energy.

Radial acceleration gives rise to **synchrotron radiation**.

First observed in a circular accelerator in 1947 (General Electric)



Energy loss per turn:

$$\Delta E = \frac{q^2}{3\epsilon_0 (m_0 c^2)^4} \frac{E^4}{R}$$

For **electrons** only:

$$\Delta E [\text{keV}] = 88.5 \frac{E^4 [\text{GeV}^4]}{R [\text{m}]}$$

	Particle	Energy (GeV)	R(m)	$\Delta E$ (GeV)	
LEP	electrons	104	3096.175	<b>3.3</b>	← <b>~3% of total beam energy!</b>
LHC	protons	7000	2803.95	$6.7 \times 10^{-6}$	



# Diamond Light Source (RAL)



3 GeV electron storage ring. Started operation Feb 2007.

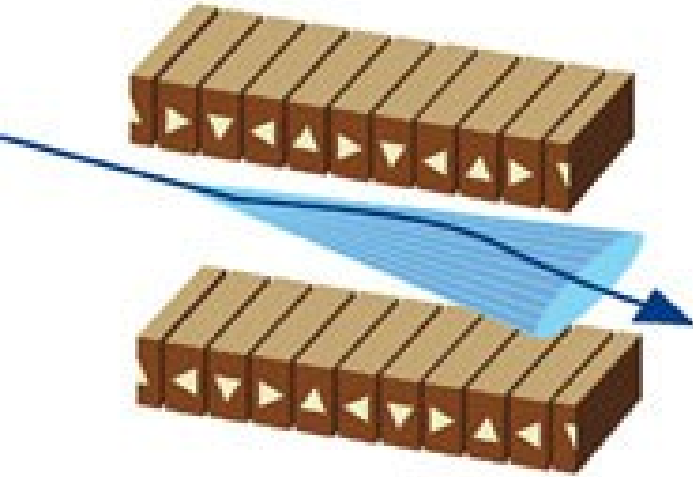
Energy loss = 3.785 MeV/turn

Uses synchrotron radiation for studies at molecular/atomic level.

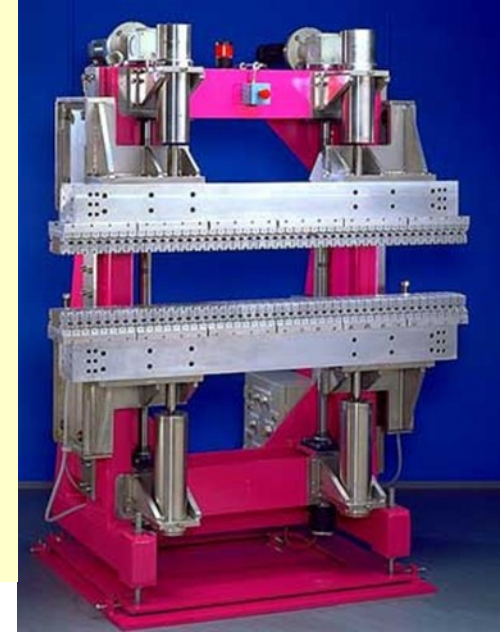
# Insertion Devices

## Wiggler

Wide cone, spread of wavelengths

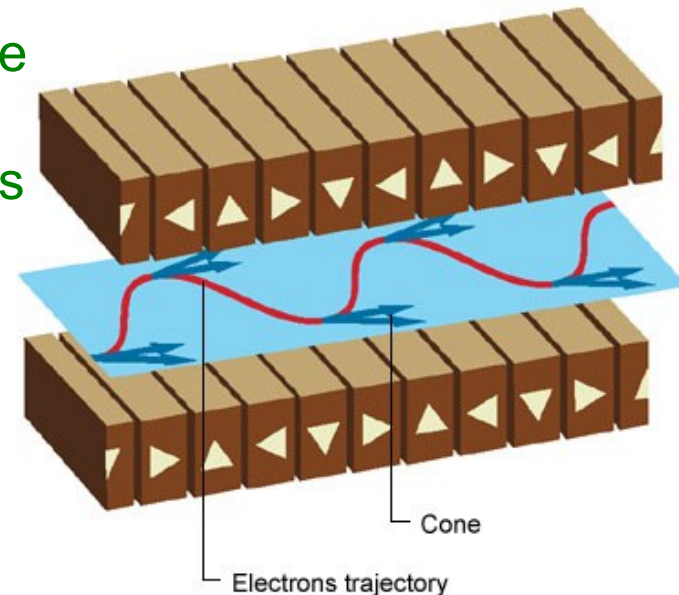


Can increase flux & brightness of light from normal bending magnets many thousands of times by using **insertion devices**.



## Undulator

Narrow cone  
Specific wavelengths



Rows of small magnets which “jiggle” the electron beam causing it to emit more radiation.

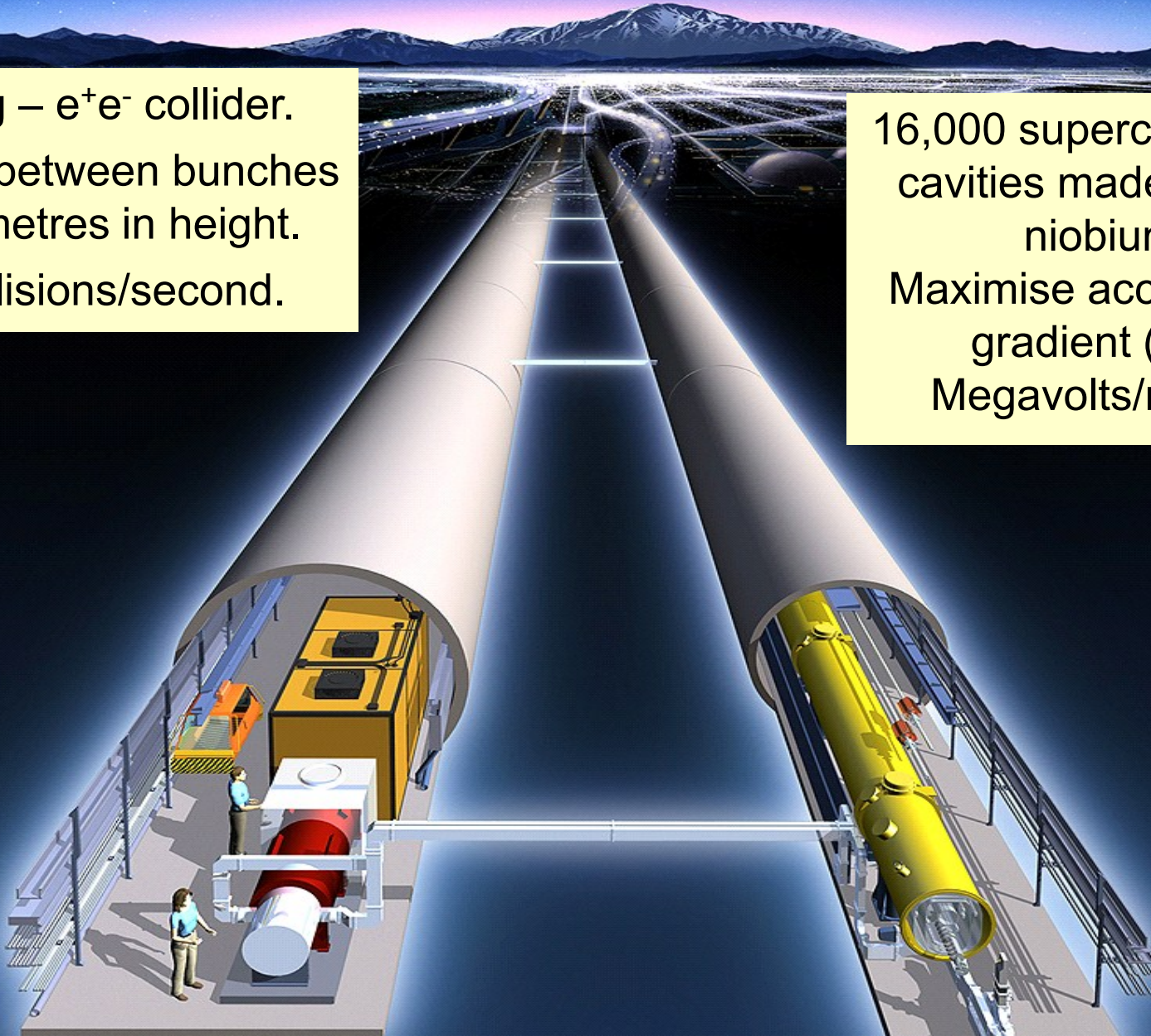
Positioned on straight sections of the storage ring.



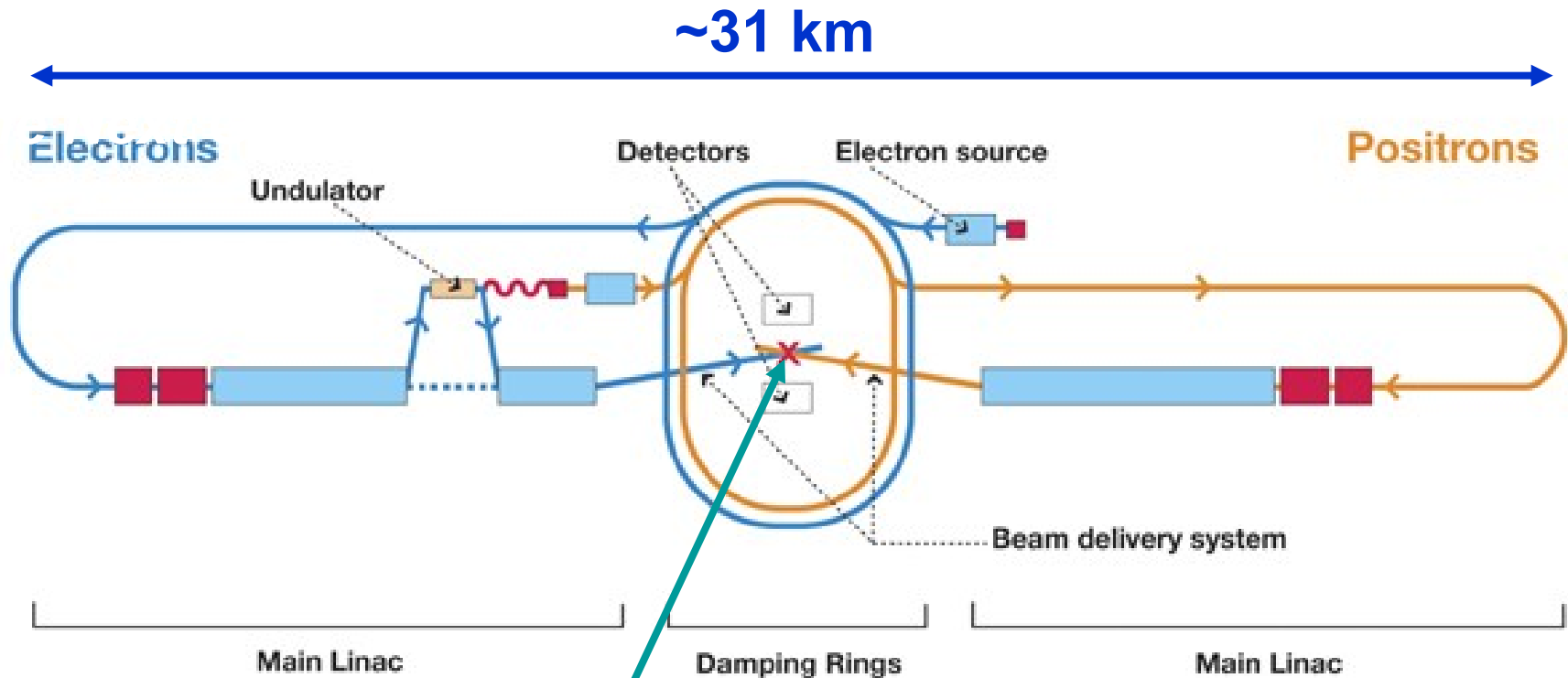
# International Linear Collider

31 km long –  $e^+e^-$  collider.  
Collisions between bunches  
of 5 nanometres in height.  
14,000 collisions/second.

16,000 superconducting  
cavities made of pure  
niobium.  
Maximise accelerating  
gradient (31.5  
Megavolts/metre).



# International Linear Collider



250 GeV electrons colliding with 250 GeV positrons

8 February 2007 2010 – 2012 ?	Reference Design Report Technical Design Phase Construction/Operation
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# Compact Linear Collider (CLIC)

100 MV/m!!

— existing LHC

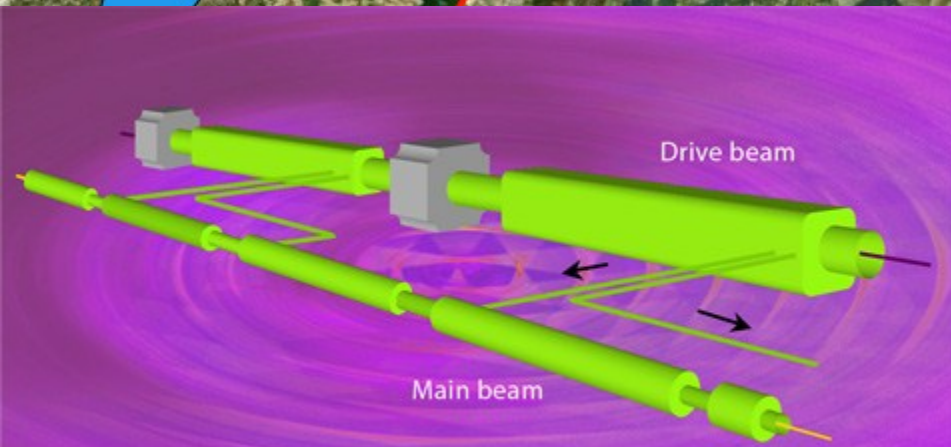
Potential underground siting:

- CLIC 500 GeV
- CLIC 1.5 TeV
- CLIC 3 TeV

Jura Mountains

IP

Lake Geneva





# My Portsmouth Proposal: *Spinnakertron*



Spinnaker Tower - 170m high  
Good linear structure

Good location - close to  
campus

Plenty of cooling water  
nearby.

Highest accelerating gradient  
~100MV/m

**Energy = 17 GeV each pass**

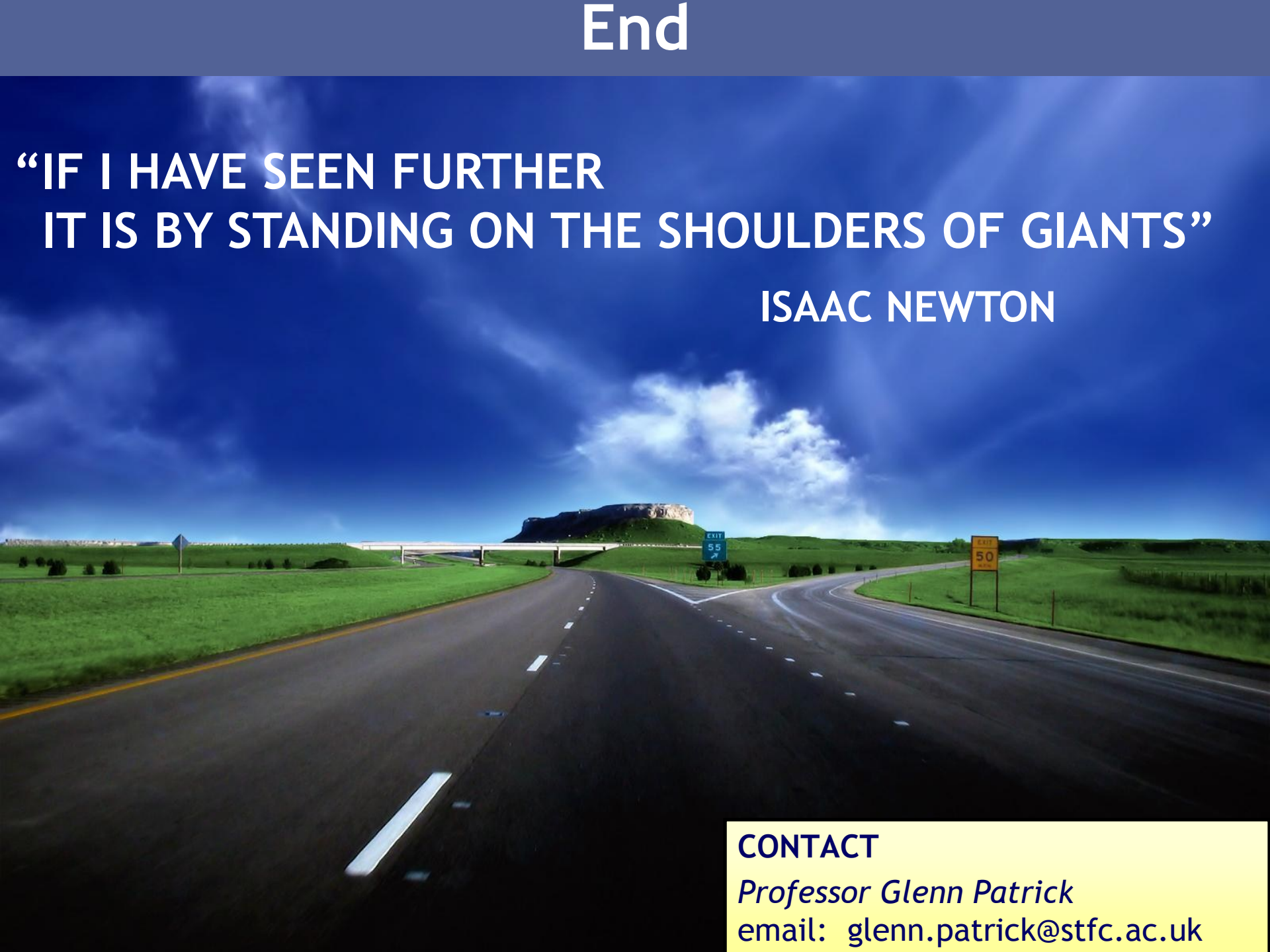
Just need a way to recycle  
the beam many times or build  
the tower higher....



# End

**“IF I HAVE SEEN FURTHER  
IT IS BY STANDING ON THE SHOULDERS OF GIANTS”**

**ISAAC NEWTON**



## **CONTACT**

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# LHC Civil Engineering



Point 1 - UX15 vault demolition of central pillar - September 20, 2000 - CE



# In the beginning...



**Empty tunnel after Large Electron Positron Collider**



# SPS Proton-Antiproton Collider

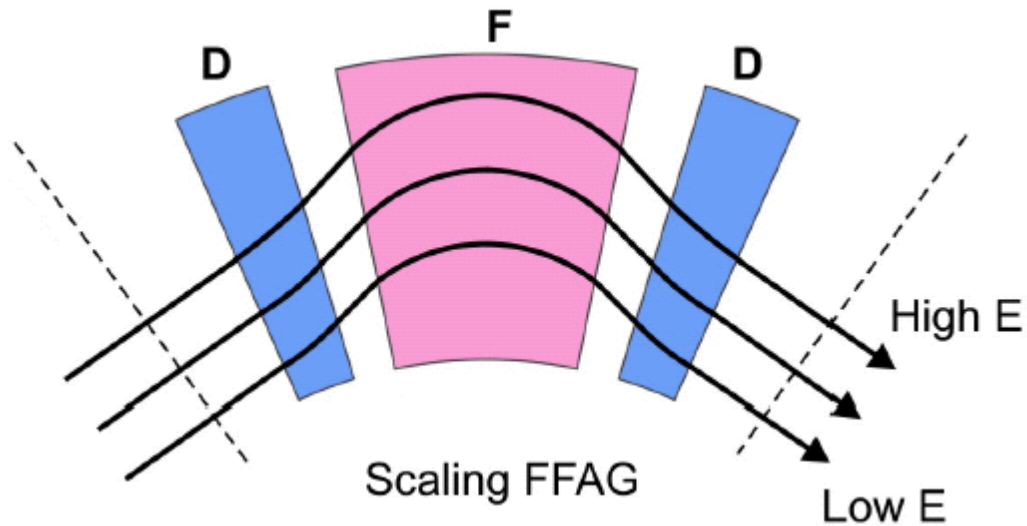


**Super Proton Synchrotron  
CERN, Geneva (6km circ).**

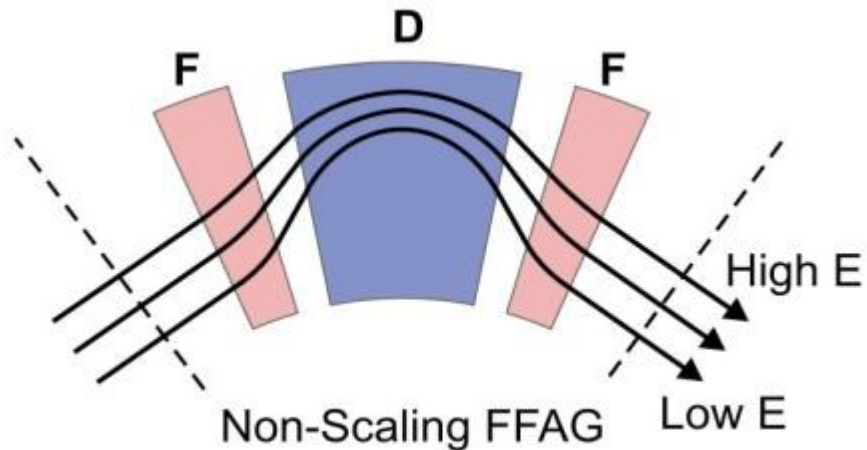
Converted into **proton-antiproton collider**  
(Rubbia & van de Meer)  
Stochastic cooling technique.



# FFAG



Old idea (1950s)  
Use DC magnets with carefully shaped pole profiles.  
Beam orbit scales with energy so apertures are large.



New idea (1990s)  
Use simple DC magnets (e.g. quadrupoles).  
Beam orbit changes shape with energy enabling apertures to be small.