

**A DIGITAL PROGRAM
FOR DESIGNING MINIMUM WEIGHT
FUEL CELL POWER SYSTEMS**

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ALLIS-CHALMERS MANUFACTURING COMPANY

Milwaukee, Wisconsin

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A B S T R A C T

12196

This document presents an IBM-704 FORTRAN program to design minimum weight fuel cell power systems. For a selected power profile, i.e., power versus mission time, and voltage requirements; this program provides the significant parameters of a system. In addition, it permits computing design parameters for a combined fuel cell-battery system, where batteries supply power for peak loads.

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1.0 INTRODUCTION

Determination of a minimum weight fuel cell power system design requires the solution of a complex system of equations. Therefore, a digital computer program has been developed to improve accuracy and conserve time. This document explaining methods of solution, and use of the program, was written to aid in the optimization of a fuel cell power system with respect to weight.

It should be noted that the subsystems are optimized, i.e., for a given problem both the fuel storage and heat sink subsystems are designed for minimum weight. Several methods for designing these subsystems are included in the program.

2.0 DESCRIPTION OF THE PROGRAM

Among devices presently under consideration for supplying auxiliary power to space vehicles, fuel cells are gaining more and more prominence. A system consisting of fuel cells and batteries presents some interesting advantages; fuel cells would supply the normal or base power, and the batteries would supply part of the peak power.

An auxiliary power system for space vehicles is weight limited. This report presents a general method for minimizing the weight of a combined fuel cell and battery system, and describes a digital computer program for performing the necessary calculations. Basically, the method consists of determining the minimum weight when fuel cells are the only source of power and then checking whether the use of storage batteries leads to further weight reduction.

The basic power system shown in Figure 1 contains a fuel cell stack, reactant supply, heat sink, and auxiliaries. The weight of each of the first three items can be expressed in terms of a single independent parameter. The most convenient variable is the individual cell operating voltage.

From the appropriate expressions for subsystem weights, that value of voltage can be found for which the total system weight is a minimum. The minimum system weight is not necessarily coincident with minimum fuel cell, reactant, or heat sink weight. Hence, the weight of a complete power system must be minimized as a whole. Once the minimum weight of a pure fuel cell system is known, one can determine whether the use of batteries would further reduce this weight. In these analyses, the amount of power provided by batteries is gradually increased until the weight of the combined system reaches a minimum.

When power requirements are constant and continuous, and when voltage is a linear function of power density, simple explicit solutions for the optimum

operating voltage can be obtained. Most space vehicles, however, require several levels of auxiliary power during a mission. Typical profiles show a large difference between peak and minimum power levels and in the duration of these levels. Additionally, voltage must be regulated within specified limits throughout the load profile. Finally, the voltage-power density relationship is generally non-linear, further complicating an analytical solution of the minimum weight problem.

In view of these complications, this problem was programmed for a solution by a digital computer. The program can determine:

Area of cells

Number of cells

Operating voltage for each power level

Operating current at each power level

Rate of heat dissipation

Total heat load

Rate of reactant consumption

Total reactant consumption

Optimum cell voltage

Optimum system weight and system weights at different cell voltages

Weights of each subsystem at optimum and other cell voltages

Fuel cell stack weight and reliability.

2.1 Analysis

The analysis is conducted in two stages. First, the minimum weight of a system using only fuel cells is computed. Then, the proportion of load to be assigned to

batteries is determined, and finally the weight of the combined system is calculated.

2. 1. 1 Analysis to Determine the Minimum Weight of a System Using Fuel Cells Only

The system weight is computed for several values of individual cell voltage, V . The optimum system is selected on the basis of minimum weight.

$$W_T = W_C + W_A + W_F + W_R$$

Where W_T , W_C , W_A , W_F , and W_R are the weights of total system, stack, auxiliaries, reactant storage and supply, and radiator, respectively.

The weight of the stack, W_C , is based on the cell area A and cell constant, S_C .

$$W_C \approx AS_C = \frac{PS_C}{V J}$$

The weight of the reactant storage and supply subsystem, W_F , is based on the energy supplied by fuel cells. It is computed for three different methods of fuel storage:

- (1) Supercritical Method of Storage ¹

$$W_F = 30.29 + \left[\frac{11.3 (1+a)}{F} \sum_{i=1}^S \frac{P_i t_i}{V_i} \right]^{2/3}$$

$$+ (0.00345 T) \left[\frac{(1+a)}{F} \sum_{i=1}^S \frac{P_i t_i}{V_i} \right]$$

(2) Subcritical Method of Storage¹

$$W_F = 30.29 + \left[\frac{9.7 (1+a)}{F} \sum_{i=1}^S \frac{P_i t_i}{V_i} \right]$$

$$+ (0.00345 T) \left[\frac{(1+a)}{F} \sum_{i=1}^S \frac{P_i t_i}{V_i} \right]^{2/3}$$

(3) Empirical Method²

$$W_F = \frac{A_H + 7.95 A_o (1+a)}{F} \sum_{i=1}^S \frac{P_i t_i}{V_i}$$

Where P_i , t_i , and V_i , are power, time and voltage, respectively, corresponding to the i th period of the power profile. S is the total power profile and F is Faraday's constant.

The weight of the heat sink subsystem, W_R , is based on the heat generated by the fuel cell. It is computed for four different kinds of radiators.

(1) Flat Radiator With No Environmental Heat Input³

$$W_R = \frac{55.6 (P_{PR})^{1.533} (T_T)^{0.5}}{(1 - R_{PS})^{0.5} (T_C - 220)^{3.57}}$$

(2) Cylindrical Radiator With No Environmental Heat Input⁴

$$W_R = \left[(0.0001138 P_{PR})^{W_1} \right] (W_2) + (W_3) (W_4) (W_6)$$

Where:

$$W_1 = (0.906) (0.0833 T_T)^{W_5}$$

$$W_5 = 0.015 (0.0001138 P_{PR})^{0.1974}$$

$$W_2 = \left[27.3 + (0.0833 T_T)^{0.3065} \right] \left[(0.04166 T_T)^{0.0314} \right]$$

$$W_3 = \left[\frac{0.4343 (\ln R_{PS} - \ln 0.99)}{2.82} \right]^{1.07} = 34.6$$

$$W_4 = (0.0001141 T_T)^{0.2467}$$

$$W_6 = (0.00003412 P_{PR})^{1.227}$$

(3) Empirical Method⁵

$$W_R = \frac{(1.975 \times 10^9) (P_{PR}) (K_R)}{e (T_C^4 - T_S^4)}$$

(4) Flat Radiator with Provision for Environmental Heat Input^{6, 7}

$$W_R = C_1 (0.0043 P_{PR})^{C_2} \left(\frac{T_T}{24} \right)^{C_3} \left(\frac{0.01}{1 - R_{PS}} \right)^{C_4} \left(\frac{559.8}{T_C} \right)^{C_5}$$

Where:

$$C_1 = 0.70935$$

$$C_2 = 1.56 + (2.15 \times 10^{-6}) P_{PR} + \frac{2 \times 10^{-6}}{1 - R_{PS}}$$

$$+ (1.667 \times 10^{-5}) T_T$$

$$C_3 = 0.208 \left(\frac{0.01}{1 - R_{PS}} \right)^{C_6} + (2.0833 \times 10^{-5}) T_T$$

$$C_4 = 0.2088 + 0.000521 \left(\frac{0.01}{1 - R_{PS}} \right)^{1.04}$$

$$C_5 = -31.6 + \frac{8.6 \times 10^{-5}}{1 - R_{PS}} + (2.917 \times 10^{-5}) T_T$$

$$+ \frac{29389.5}{T_C} + (1.29 \times 10^{-4}) P_{PR}$$

$$C_6 = 0.20808 - \frac{4.08 \times 10^{-6}}{1 - R_{PS}}$$

In all the equations for W_R , P_{PR} can be expressed as below:

$$P_{PR} = (1 - 0.67 V) (P_{max}) + \frac{P_p}{0.67} - \frac{0.0002165 P_{max} Q_W}{V}$$

Where P_{max} is the maximum power supplied by the fuel cells, T_T is the mission duration, and P_p is the total parasitic power.

The weight of auxiliaries, W_A , is based on the maximum power supplied by the fuel cells.

$$W_A = K + P_{max} S'_A$$

The values of individual cell voltage and number of cells in a fuel cell stack are so selected that the stack voltage is always within specified limits. Hence, a particular cell voltage that yields minimum system weight will not be accepted if a corresponding value for number of cells cannot be found to meet the stack voltage regulation limits. For example, let the cell voltage for minimum weight be 0.8 volt, corresponding to a maximum power level of 2,000 watts. Also, let the value of minimum power be 200 watts and the regulation requirement be 28 ± 2 volts. Cell voltage corresponding to minimum power will be 1.021 volts. At minimum voltage, 33 cells are required; at maximum voltage, 29 cells. This indicates that voltage regulation is not possible for a cell voltage of 0.8, and $V = 0.8$ is not acceptable. For P_{max} , V should be at least 0.929 for these requirements. The fuel cell system is thus at minimum weight and within voltage regulation limits.

2.1.2 Analysis to Size a Fuel Cell-Battery Combination for Minimum Weight

This minimization is obtained by an iterative procedure. At each step, a slightly larger fraction of the peak power is allocated to the battery. A check is then made to determine whether the secondary battery can be recharged during normal power demand periods. The process continues until the weight of the combined system reaches a minimum.

A summary of the procedure for a simple profile with two power levels, shown in Figure 2, is given below:

Step 1 Divide $(P_{max} - P_{min})$ into N equal intervals with

$$dP = \frac{P_{max} - P_{min}}{N}$$

where, P_{min} is the minimum power supplied by fuel cells, and P_{max} is the maximum power supplied by fuel cells.

Step 2 Calculate the optimum weight W_o of the system when $P_{fc\ max}$, maximum power supplied by fuel cells, is equal to P_{max} by using the analysis given in 2.1.1.

Step 3 Set $i = 1$

Step 4 Reduce P_{max} by $i dP$. Go to Step 5 in the case of a rechargeable battery. Go directly to Step 28 in the case of a primary battery.

Step 5 Determine first profile segment where battery power will be needed; segment number two in this case.

Step 6 Determine next load segment where battery power will be needed; segment number four in this case.

Step 7 Determine available charging time, T_A , between above two peaks.

Step 8 Calculate the discharging current, I_{BD} .

$$I_{BD} = \frac{i (dP)}{(V_{BMIN}) (E_{RD})}$$

Step 9

Set the depth of battery discharge, α , equal to its maximum allowable value, α_{\max} , which is an input quantity. This is done in an attempt to use a battery of as low a capacity as possible.

Step 10

Calculate C , capacity of the battery.

$$C = \frac{I_{BD} t_d}{\alpha}$$

Also, obtain the corresponding energy density, R_D , by referring to the table of C versus R_D .

Step 11

$$\text{Set } \left(\frac{I_{BC}}{C} \right) = \left(\frac{I_{BC}}{C} \right)_{\text{MIN}}$$

This is done to increase the charging efficiency of battery.

Step 12

Calculate the charging current, I_{BC} .

$$I_{BC} = C \left(\frac{I_{BC}}{C} \right)$$

Step 13

Calculate the current corresponding to the power for load segment three. (The segment during which battery charging will take place.)

$$I_{\text{LOAD}} = \frac{P_{\text{LOAD}}}{V_{\text{P LOAD}}}$$

Step 14 Since fuel cells will have to supply both charging and load currents, total current supplied by fuel cells, I_{FC} , will be the sum of these.

$$I_{FC} = I_{BC} + I_{LOAD}$$

Step 15 Calculate J_{FC} , the current density corresponding to Step 14.

$$J_{FC} = \frac{I_{FC}}{\text{Cell Area}}$$

Calculate corresponding power density, VJ_{FC} , by referring to the V-J table, and then calculate power, P_{charge} (P_{ch})

$$P_{ch} = VJ_{FC} (\text{cell area}) (\text{Number of cells})$$

Step 16 Compare P_{ch} with P_{FCMX} . If P_{FCMX} is less than P_{ch} , combine load profile segment two and four. Then go back to Step 5 to determine whether the total time for recharging (now the combined segments three and five) can recharge the battery. Continue this process until P_{FCMX} is equal to or greater than P_{ch} . Then continue with Step 17.

Step 17 Calculate required charging time, T_c

$$T_c = \frac{\alpha}{(E_{RC}) (E_C) \left[\frac{I_{BC}}{C} \right]}$$

This formula is valid if the battery can be recharged at constant current. However, if the maximum allowable charging voltage V_{MAXB} is reached during charge, it is necessary to reduce the charging current so that V_{MAXB} is not exceeded. Should this occur the charge time T_c will be computed by subroutines SUBA and SUBA1.

- Step 18 Compare T_c with the available charging time, T_A . If T_c is greater than T_A , increase $\left(\frac{I_{BC}}{C}\right)$ by $\Delta\left(\frac{I_{BC}}{C}\right)$ and repeat steps 12 through 17. Again compare T_c with T_A and if T_c is greater than T_A , continue increasing $\left(\frac{I_{BC}}{C}\right)$ until it has reached the value $\left(\frac{I_{BC}}{C}\right)_{max}$. If T_c is still greater than T_A , start reducing α by $\Delta\alpha$ until α becomes α_{min} . If T_c is still greater than T_A , combine two adjacent power peaks (segment 2 and 4 in this case) and repeat this process until T_c is equal to or less than T_A . (See listing of subroutine SUBP.)
- Step 19 Repeat Steps 2 through 18 for the rest of the power profile. Compare the required capacities of the battery for each peak, and thus determine the maximum capacity of the battery. Recalculate the depth of discharge for each peak.

Step 20 Modify the original power profile by using the calculated charging power, P_{charge} .

Step 21 Calculate the optimum weight, W_{fc_1} , for the modified power profile by using the method given in 2.1.1.

Step 22 Corresponding to the recalculated values of α and $\left(\frac{I_{BD}}{C}\right)$, determine V_{min} by referring to the discharge table for the battery.

Step 23 Calculate, n the number of cells required in the battery.

$$n = \frac{V_{BMIN}}{V_{min}}$$

If n is not an integer, then use the next integer as the value for n .

Step 24 Calculate the maximum voltage for the battery consisting of n cells.

$$V_{BMAX} = nV_{maxB}$$

Step 25 Calculate W_{Ri} , the weight of voltage regulator

$$W_{Ri} = (V_{BMAX}) (I_{BD}) (0.005)$$

Step 26 Calculate the weight of rechargeable battery, W_{RBi} .

$$W_{RBi} = \frac{(dP)(t_d)}{\propto R_D}$$

Step 27 Calculate W_{TRBi} , total weight of a system using both fuel cells and a rechargeable battery.

$$W_{TRBi} = W_{fci} + W_{RBi} + W_{Ri}$$

Go to Step 29.

Step 28 Calculate W_{TPBi} , total weight of a system using both fuel cells and a primary battery.

$$W_{TPBi} = (dP)(t_d)(B) + (W_{fci})$$

Step 29 Repeat Steps 4 through 28 for $i = 2, 3, 4$, and so on up to $i = n$. The optimum combination is the one that weighs the least.

This method has been extended in the computer program to a multi-step power profile with a maximum of fifty steps.

3.0 EXPLANATION OF THE TERMS USED IN THE PROGRAM

The following is an explanation of the terms and symbols used in the program. Typical values of some of the terms are provided as an aid to the use of the program.

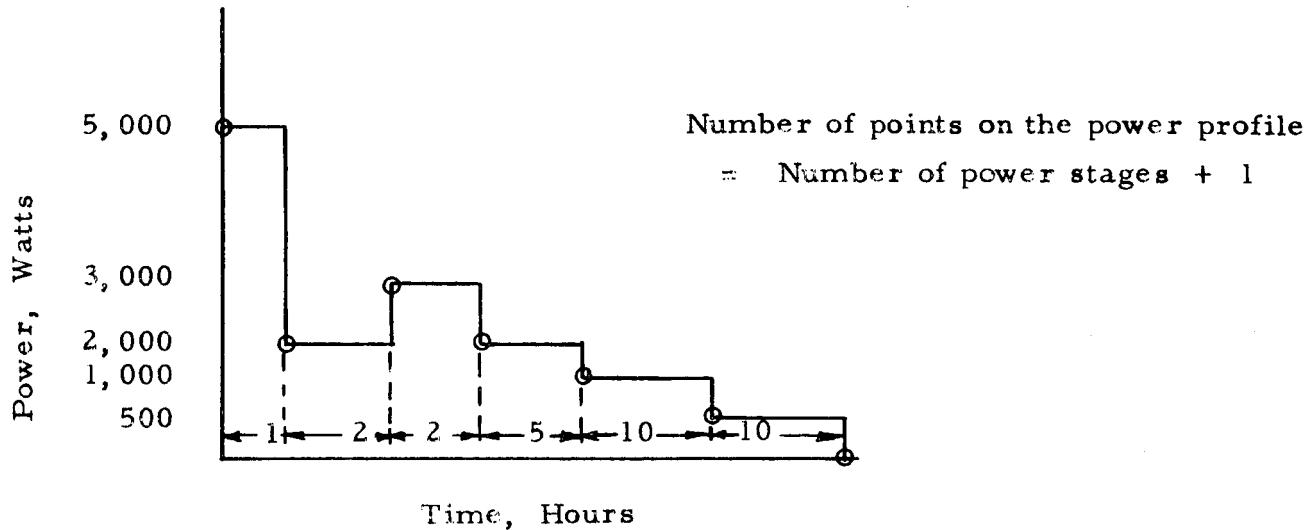
3.1 Terms Used in the Input

Except for the power profile, all terms used in preparing the input are printed on Page one of the output. Input power profile is printed on output Page two.

3.1.1 Power Profile

NOPROF = Number of points on power profile.

Time and power values for the profile. This can best be explained by the following example.



In the above power profile, there are six power stages and hence seven points. Each point to be considered in the preparation of input is circled. The card input should be prepared as follows

T	P	T	P	T	P
0	5,000	1	2,000	3	3,000
5	2,000	10	1,000	20	500
30	0				

Where P is power in watts and T is time in hours. Thus, the points at which both the power and time change should be listed in the input. Note that number of points on the power profile should not be greater than fifty.

3.1.2 Voltage-Current Density Curve of the Fuel Cell

NXP is the number of values selected to represent the V-J curve, where V is the individual cell voltage in volts and J is the current density of the cell in amperes per square foot. Note that a product of V and J, power density of the cell, is tabulated on page one of the output. Also note that the maximum allowable value of NXP is thirty.

3.1.3 Explanation of Constants and Nomenclature

The following pages contain the explanation of constants and nomenclature.

Equations	Computer Program	Definition	Units	Used For	Typical Value
S_C	SC	Cell constant	lbs/sq. ft.	Weight of cell	7.0
S_A	SAP	Auxiliary constant	lb/watt	Variable part of weight of auxiliaries	0.00548 to 0.00748
K	CON	Auxiliary constant	lbs	Constant part of weight of auxiliaries	14.5 to 16.5
-	VOC	Open-circuit cell voltage	volt	Upper cell voltage limits	1.10
-	VAB	Minimum cell voltage	volt	Lower cell voltage limits	0.7
-	PPC	Constant parasitic power	watts	Parasitic power	60
-	PPV	Variable parasitic power	watts/watt	Variable part of parasitic power	0.005 to 0.01
a	ADD	Additional reactants for residual and safety factor	-	Weight of reactants and reactant storage packages	0.12
B	BATT	Battery constant for primary batteries	lb/watt-hr	Weight of primary batteries	0.02
I_{BD}	FIBD	Battery discharge current	Amperes	Capacity of rechargeable batteries	0.1 to 200

Equations	Computer Program	Definition	Units	Used For	Typical Value
T_C		Average radiator coolant temperature	° R	Weight of radiator	560° R to 640° R
Q_W	Q_W	Heat content of one pound of evaporated water	BTU/lb	Weight of Radiator	1100
-	SP2	Spare Location	-	Future Use	-
α_{\max}	ALFMX	Maximum depth of battery discharge	-	Depth of discharge	0.75
α_{\min}	ALFMN	Minimum depth of battery discharge	-	Depth of discharge	0.01
$\left(\frac{I_{BC}}{C}\right)_{\min}$	BCMIN	Minimum ratio of charging current to the capacity of the battery	hr ⁻¹	Charging current	0.01 to 0.1
$\Delta \left(\frac{I_{BC}}{C}\right)$	DBC	Arbitrarily selected increment in the value of the ratio of charging current to the capacity of the battery	hr ⁻¹	Charging current	0.01 to 0.1
$\left(\frac{I_{BC}}{C}\right)_{\max}$	BCMAX	Maximum ratio of charging current to the capacity of the battery	hr ⁻¹	Charging current	0.50 to 0.75
E_C	E_C	Charging efficiency of the battery	-	Charging current and charging time	0.90

Equations	Computer Program	Definition	Units	Used For	Typical Value
E_{RC}	ERC	Charging efficiency of the regulator	-	Charging current and charging time	0.90
E_{RD}	ERD	Discharging efficiency of the regulator	-	Discharge current of the battery	0.90
-	SP3	Spare location	-	Future Use	-
-	XNAM	Number of operating fuel cell stacks	-	Reliability and weight of fuel cell subsystems	1 to 4
-	FR	Failure rate of fuel cell stack	Failure/hr	Reliability of fuel cell subsystem	0.000025 to 0.000040
R_{PS}	RPS	Radiator probability of survival	-	Weight of radiator	0.99 to 0.9999
-	XNRM	Number of redundant fuel cell stacks	-	Reliability and weight of fuel cell subsystem	0 to 2
N	FN	Total number of increments into which the difference between the maximum and minimum positive power is divided	-	Portion of load assigned to batteries	2 to 25
$\Delta \alpha$	DALFA	Increment in the value of the depth of discharge	-	Depth of discharge	0.01 to 0.25

Equations	Computer Program	Definition	Units	Used For	Typical Value
-	SP4	Spare location	-	Future use	-
-	VMAXC	Maximum fuel cell stack voltage	volts	Operating characteristics of fuel cell subsystem	30
-	VMINC	Minimum fuel cell stack voltage	volts	Operating characteristics of fuel cell subsystem	26
VMAXB	VMAXB	Maximum rechargeable battery voltage per cell	volts	Weight of voltage regulator	1.55 for Ag-Cd batteries
V _{BMIN}	V _{BMIN}	Minimum battery voltage for all cells	volts	Discharge current, no. of battery cells, and weight of voltage regulator	20 to 28
-	SP5	Spare location	-	Future use	-
-	SP6	Spare location	-	Future use	-
-	SP7	Spare location	-	Future use	-
A _H	TKH	<u>Weight of hydrogen + tankage</u> <u>Weight of hydrogen</u>	lbs/lb	Weight of reactant supply and storage package	2.5
A _O	TKO	<u>Weight of oxygen + tankage</u> <u>Weight of oxygen</u>	lbs/lb	Weight of reactant supply and storage package	1.5

Equations	Computer Program	Definition	Units	Used For	Typical Value
ϵ	EMISS	Emissivity of radiator material	-	Weight of radiator	0.9
T_S		Radiator sink temperature	° R	Weight of radiator	430
K_R	CONKR	<u>Weight of radiator</u> sq. ft. of fin area	lbs / sq. ft.	Weight of radiator	0.5

3.1.4 List of Control Characters

- NPP- 0- All the output pages will be printed.
 1- Output page five and six will not be printed.
- LBT- 0- Only consider fuel cells.
 1- Consider fuel cell-rechargeable battery combination.
 2- Consider fuel cell-primary battery combination.
 3- Consider both fuel cell-rechargeable battery and
 fuel cell-primary battery combinations.
- LFL- 0- Calculate weight of reactants only.
 1- Calculate weight of reactants together with the
 weight of supercritical storage and supply system.
 2- Calculate weight of reactants together with the
 weight of subcritical storage and supply system.
 3- Calculate weight of reactants and tankage using an
 empirical method.
- LRD- 0- Do not consider a heat sink subsystem in the optimization.
 1- Calculate the weight of heat sink subsystem using a flat
 radiator and not considering heat input from the
 environment.
 2- Calculate the weight of heat sink subsystem using a
 cylindrical radiator, and not considering heat input
 from the environment.
 3- Calculate the weight of heat sink subsystem using an
 empirical relationship.
 4- Calculate the weight of heat sink subsystem using a
 flat radiator and considering heat input from the
 environment.
- IBAT- 1- Consider Ni-Cd rechargeable batteries
 2- Consider Ag-Cd rechargeable batteries
 3- Consider Ag-Zn rechargeable batteries

- LV 1- Effect of very small change in cell voltage due to modification of power profile is considered. Total system weight might change by less than 0.5 percent.
 0- Effect of very small change in cell is not considered. This reduces the computer time by approximately 50 percent.

LSPI- Spare location

- QW- 1100- System weight when water is not collected.
 0- System weight when entire amount of generated water is collected.
 110- System weight when ninety percent of the generated water is collected.

3.2 Terms Used on Output Page TWO

This page presents the input power profile,

3.3 Terms Used on Output Page THREE

Stage: The number of increments of power supplied by batteries.

- 0- All the power supplied by fuel cells.
1- Portion of power equal to ΔP is supplied by the batteries.
2- Portion of power equal to $2 \Delta P$ is supplied by the batteries.
N- Portion of power equal to $N (\Delta P)$ is supplied by the batteries.
VOPT- Optimum cell voltage for the fuel cell system corresponding to the maximum power supplied by fuel cells, volt.

WT TOTAL Total system weight, pounds.
WT CELL Weight of fuel cell subsystem, pounds.
WT AUX Weight of auxiliaries, pounds.
WT FUEL Weight of reactants together with the weight of reactant storage and supply package, pounds.

WT RAD	Weight of heat sink subsystem, pounds
WT BAT	Weight of batteries, pounds
NO CELL	Number of individual cells in a fuel cell stack
CELL AREA (A)	Area of one cell, square feet
WT REG	Weight of voltage regulator, pounds.

3.4

Terms Used on Output Page FOUR

All the values presented on this page are for the optimum combination of rechargeable batteries and fuel cells. Explanation of some of the terms is given in input and output page Three. Rest of the terms are described below.

DISRAT-	Ratio of discharge current to the capacity of the battery, hr^{-1}
TX, PX-	These represent the modified power profile that is supplied by fuel cells. Power profile had to be modified to include the effect of recharging the batteries, TX is time in hours and PX is power in watts.
C-	Capacity of the batteries, ampere-hours
RD-	Energy density of the batteries, $\frac{\text{watt-hours}}{\text{pound}}$
BAT-	Number of individual batteries required.
VBMAX-	Maximum value of the total battery voltage.

3.5

Terms Used on Output Page FIVE

This page presents the system weight tabulation for twenty-five different values of individual fuel cell voltage between VAB and VOC when NPP is zero. No output will be presented on this page if NPP is one.

VIN- Individual cell voltage corresponding to the maximum power supplied by the fuel cells, volts
V2N- Individual cell voltage corresponding to the minimum positive power supplied by the fuel cells, volts.

WT, WTC, WTAUX, WTF, WTR, WTRB, and WTREG have the same meaning as WT TOTAL, WT CELL, WT AUX, WT FUEL, WT RAD, WT BAT, and WT REG respectively of output page THREE.

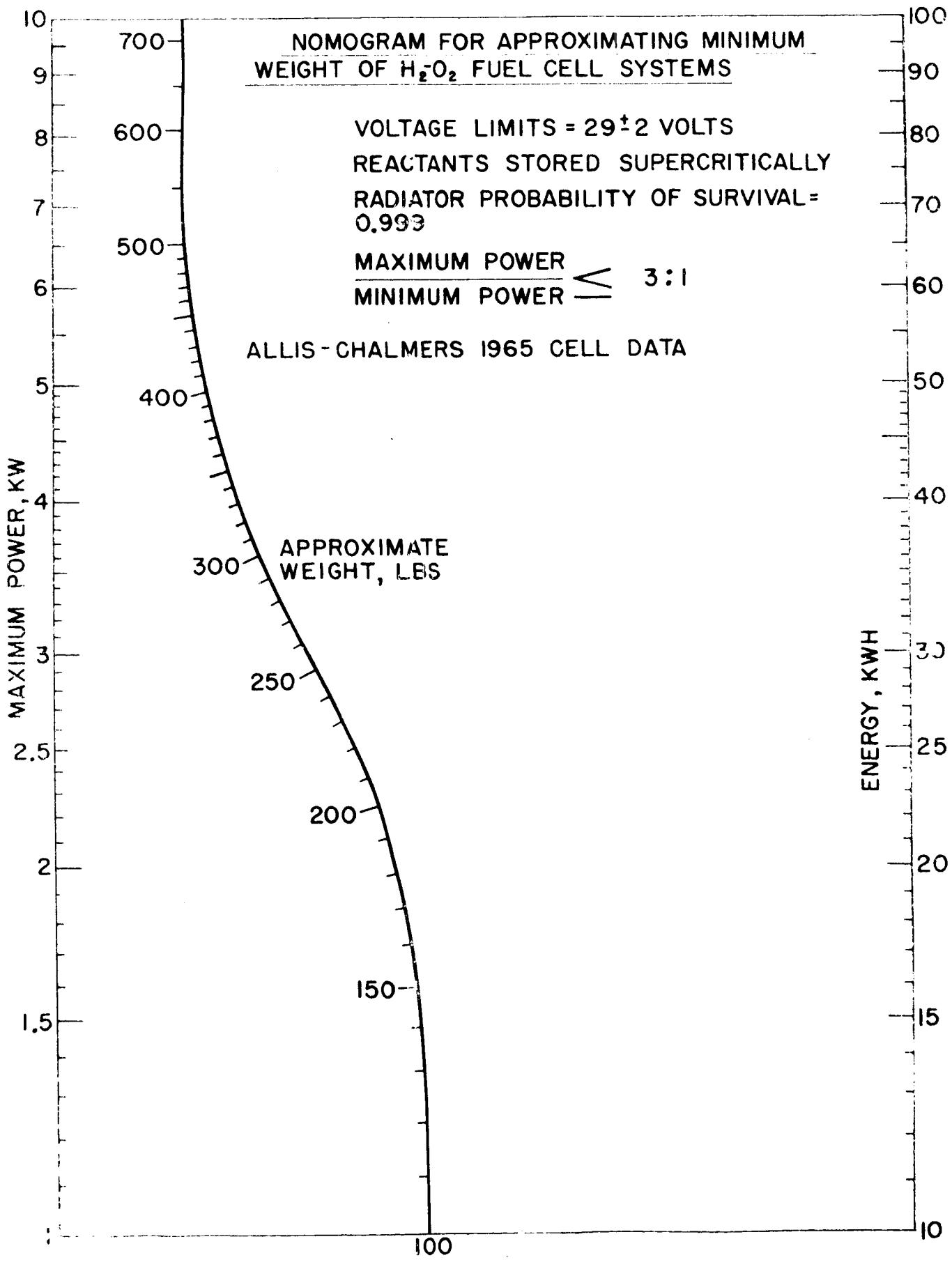
3.6

Terms Used on Output Page SIX

This page will be printed only if NPP = 0

$$\text{Module weight} = \frac{\text{Weight of a single fuel cell module}}{\text{total number of modules}} = \frac{\text{weight of cells} + \text{weight of auxiliaries}}{\text{total number of modules}}$$

T	= Duration of power stage, hours
PFC	= Power supplied by the fuel cell system, watts
V MOD	= Stack voltage, volts
I/A	= J = current density, amperes per square foot
I	= Stack current, amperes
PW	= Waste heat to be removed from a stack, watts
WH ₂	= Stoichiometric rate of hydrogen consumption for a stack, pounds per hour
WO ₂	= Stoichiometric rate of oxygen consumption for a stack, pounds per hour
SUMT	= Total mission duration, hours
SUM PEC*T	= Energy supplied by the fuel cells, watt-hours
SUM PW*T	= Total waste heat removed from a stack, watt hours
SUM WH*T	= Total hydrogen consumed by a stack, pounds
SUM WO*T	= Total oxygen consumed by a stack, pounds.



CONCLUSIONS

This program will calculate the minimum weight of fuel cell systems supplying power within set voltage limits. Nomograms on the following pages approximate the minimum system weight for various energy and power levels. The weights are determined on the basis of present Allis-Chalmers capabilities, a supercritical reactant storage, a radiator with a 0.999 probability of survival, and a voltage regulation requirement of 29 ± 2 volts.

Minimum system weight can be further reduced by using either primary or rechargeable batteries to supply a portion of peak power. The reduction in weight can be fifty percent or more if the peak power is four to five times the base load. Rechargeable batteries should be used if the peaks occur repeatedly. Percentage weight savings¹² that can be obtained under an ideal set of conditions by using rechargeable batteries are presented in Figures 7, 8, and 9. These ideal conditions are:

- (1) A sufficient charging time is available during low level portions of the load profile.
- (2) The power supplied by the fuel cells during any interval of time plus the power required to recharge batteries is always less than or equal to the maximum power supplied by fuel cells.
- (3) Battery weight is 0.04 pounds per watt hour.
- (4) Required charging current is less than maximum specified charging current.
- (5) Charging and discharging efficiencies are equal to one.
- (6) Weight of the voltage regulator is zero.
- (7) The system will always stay within the voltage regulation limits regardless of the depth of discharge.
- (8) Fuel cells must be capable of recharging batteries.

NOMOGRAM FOR APPROXIMATING MINIMUM WEIGHT
OF H₂-O₂ FUEL CELL SYSTEMS

VOLTAGE LIMITS = 29 ± 2 VOLTS

REACTANTS STORED SUPERCRITCALLY

RADIATOR PROBABILITY OF
SURVIVAL = 0.999

MAXIMUM POWER 3:1
MINIMUM POWER

ALLIS - CHALMERS 1965 CELL DATA

MAXIMUM POWER · KW

10
9
8
7
6
5
4
3
2
1.5
1
0.5
0

10,000
5,000
4,000
3,000
2,000
1,500
1,000
700
600
500
400
300
250
200
150
100

APPROXIMATE
WEIGHT , LBS

1,000
900
800
700
600
500
400
300
200

ENERGY, KWH

220

5.0 REFERENCES

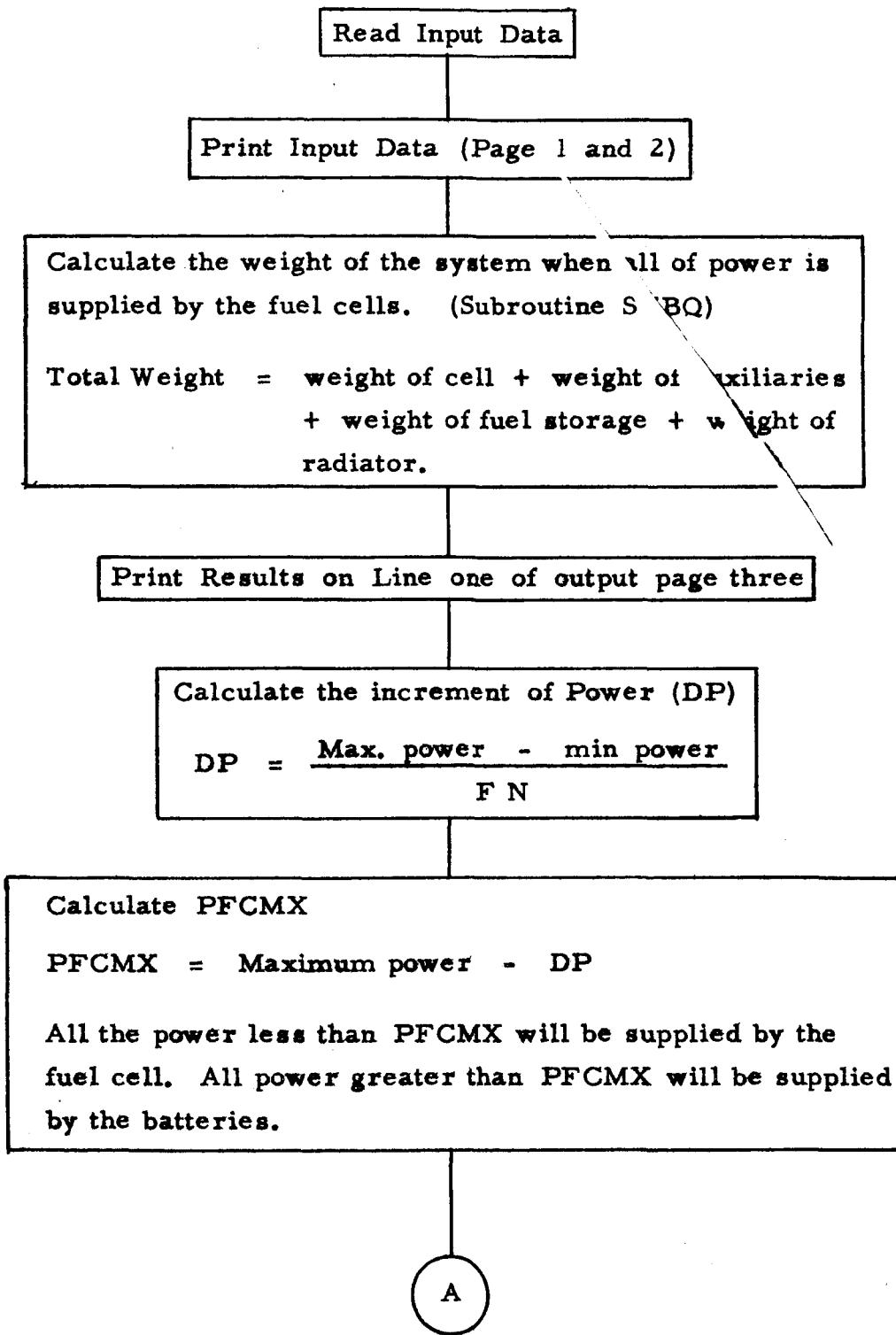
1. The Cryhocycle, Sundstrand Aviation - Denver, A Division of Sundstrand Corporation.
2. Private Communication
3. Investigation of a 3 KW Stirling Cycle Solar Power System, Volume VII, WADD-TR-61-122, Flight Accessories Laboratory, Wright-Patterson Air Force Base, Ohio, March 1962.
4. Optimization of a Non-Condensing Cylindrical Radiator (With Modified Penetration Criteria). Report H-81. Prepared by Harrell Stovall of Allison Division of General Motors Corporation, Indianapolis, Indiana, February 20, 1963.
5. Private Communication
6. Digital Programs for Establishing Steady-State Space Radiator Performance, AST-TDR-63-722, Flight Dynamics Laboratory, Wright-Patterson Air Force Base, Ohio, October 1963.
7. Research and Development of Open Cycle Fuel Cells, NAS 8-5392-QPR-003, Third Quarterly Report, Research Division, Allis-Chalmers Manufacturing Company, June 15, 1965.
8. Eagle-Picher Company, Chemical and Metal Division, Personal Communication, November 18, 1964.

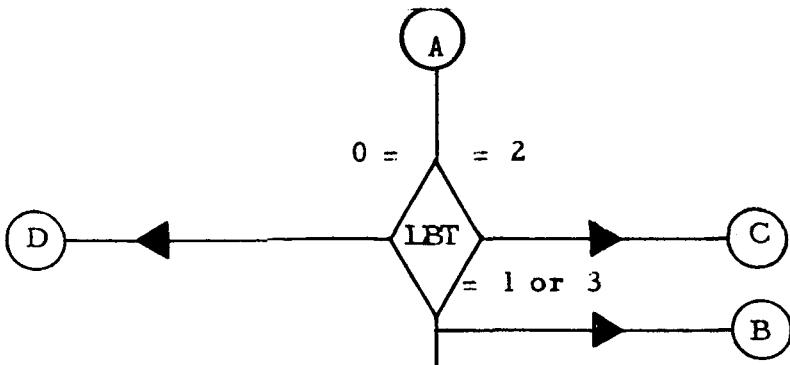
9. Direct Energy Conversion Operation, 63 DE 16, Quarterly Report Number Five of Contract NO_W 62-0984-D, General Electric Company, August 30, 1962.
10. Gulton Industries Incorporated, Alkaline Battery Division, personal communication, September 10, 1964.
11. Yardney Electric Corporation, personal communication, November 19, 1964.
12. Research and Development of Open Cycle Fuel Cells, NAS 8-5392-QPR-002, Second Quarterly Report, Research Division, Allis-Chalmers Manufacturing Company, March 15, 1965.

6.0 APPENDIX A

Included in this appendix are a flow diagram, a listing of the main program, sub-routines, and a table identifying error messages for the program.

6.1 Flow Diagram

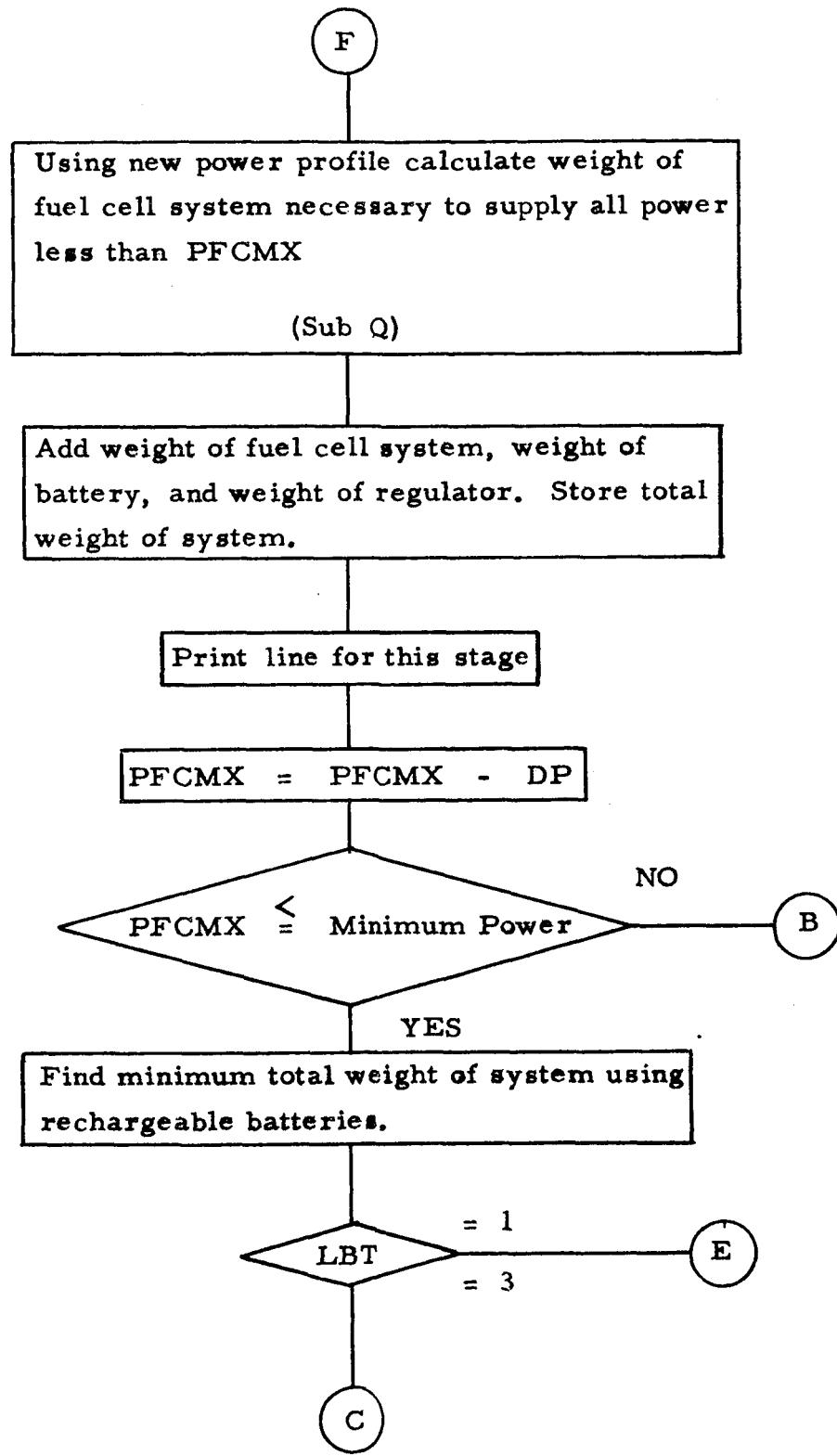


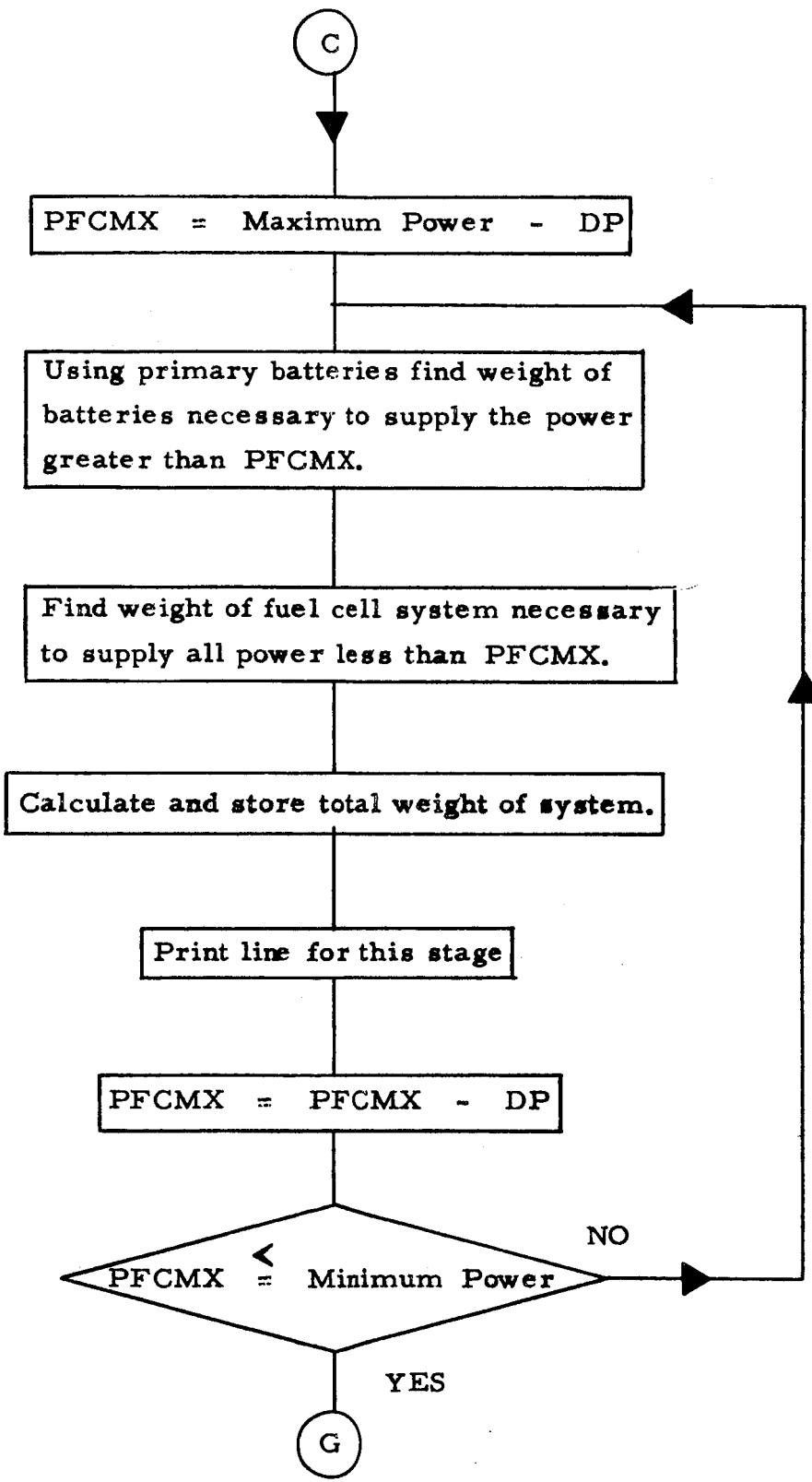


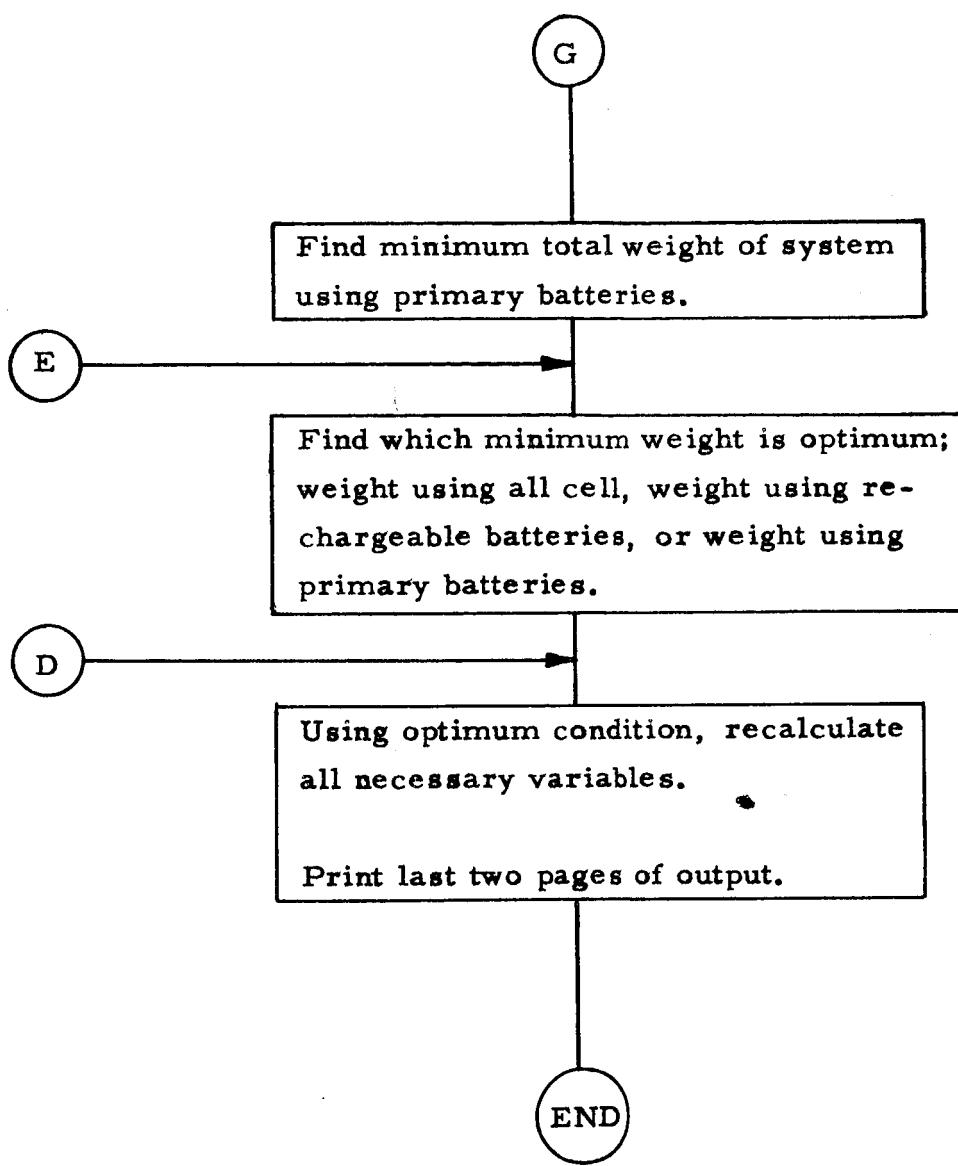
Using PFCMX calculate weight of battery, weight of regulator, and new power profile.

1. Determine first peak where battery power will be needed. (Subroutine SUBB)
2. Determine next peak where battery power will be needed. (Subroutine SUBB)
3. Determine charging time available for the section of the power profile being considered. (Subroutine SUBC)
4. Determine capacity of battery, Ratio 1 and Ratio 2 for the section of the power profile being considered. (Subroutine SUBA)
5. Is charging time sufficient to recharge battery? If not, combine peaks and go back to Step 2; otherwise continue.
6. Store the capacity of the battery needed for this section of the power profile.
7. Have all peaks been considered? If not, go back to Step 2; otherwise continue.
8. Find maximum capacity.
9. Using maximum capacity find corresponding VMINB; also find new power profile which includes charging power for battery. (Subroutines SUBA1, SUBE, and SUBD)
10. Find weight of battery and regulator.

F







6.2 Listing and Subroutines Of The Program

PAUL CALLEN DEPT. 3258 PROGRAM NO. 3258-734 MAIN

IBM 704 PROGRAM WRITTEN IN FORTRAN II
CARGE NO.....02-4800-00008
FOR DEPT NO....3341
JOB NO.....3258-734

THIS PROGRAM DETERMINES THE COMBINATION OF FUEL CELL AND
BATTERY FOR WHICH TOTAL SYSTEM WEIGHT IS MINIMUM.
THE POWER PROFILE AND TYPE OF BATTERY TO BE USED ARE SPECIFIED

MAIN PROGRAM

```
DIMENSION PABT(55),TABT(55)
DIMENSION TRD(4,4),TCD1(11,2),TCD2(9,2),TIBD(7),TALPHA(10),
1TVMINB(10,7),P(55),T(55),TA(75),PA(75),TX(75),PX(75),V(30),
2AMP(30),VJ(30),TR(75),PR(75),WTF(2),WTC(2),WTR(2),WT(2)
DIMENSION WTCCELL(25),AREA(25)
EQUIVALENCE (NXP,NVJ),(VMAX,VMAXC),(VMIN,VMINC)
COMMON NVJ ,TCD1 ,TCD2 ,TIBD ,TALPHA,TVMINB,P ,T
1TA , PA ,TX ,PX ,V ,AMP ,VJ ,NOPROF,NPROFA,
2NPROFX, TRD ,NIP ,REJECT,WTC ,HTA ,WTF ,WTR ,WREG ,
3WRB , WTOPT ,WTOLD ,WTNEW ,DP ,PFCMX ,SC ,SAP ,CON ,
4VOC , VAB ,PPC ,PPV ,ADD ,BATT ,TC ,QW ,SP2 ,
5ALFMX , ALFMN ,BCMIN ,DBC ,BCMAX ,EC ,ERD ,ERC ,EK2 ,
6XNAM , XNRM ,FR ,RPS ,FN ,DALFA ,EX3 ,VMAXC ,VMINC ,
7VMAXB , VBMIN ,EX4 ,EX5 ,EX6 ,NPP ,LBT ,LFL ,LRD ,
8IBAT , ICOMB ,LSP1 ,TKH ,TKO ,EMISS ,TS ,CONKR ,NPFL ,
9NPF2 , IPX ,IP ,C ,RATIO1,RATIO2,T1 ,T2 ,AREA
COMMON TT ,NN ,VCOR ,NWT ,PARA ,TR ,PR ,VJCOR ,
1SWH , SWO ,WT ,DPCH1 ,ZZ ,VCORI ,VOP1 ,VJOP1 ,TCH ,
2M1 ,M2 ,CODE ,ALPHA ,TD ,COMB ,FIBD ,FJBC1 ,FIBC1 ,
3CRIT ,ALFAC ,VJBC1 ,TCC ,DISRAT,VMINB
```

CALL EFM

READ FIXED TABLES OF DATA

```
DO 15 K=1,4
15 READ 5,(TRD(K,I),I=1,4)
DO 16 K=1,11
16 READ 5,(TCD1(K,I),I=1,2)
DO 17 K=1,9
17 READ 5,(TCD2(K,I),I=1,2)
READ 5,(TIBD(I),I=1,7)
READ 5,(TALPHA(I),I=1,5)
READ 5,(TALPHA(I),I=6,10)
DO 18 K=1,7
18 READ 6,(TVMINB(I,K),I=1,10)
6 FORMAT (10F7.0)
5 FORMAT(7F10.0)
NIP=3
20 TRY=0.
```

```

VOPOLD=0.0
REJECT=0.
CALL INPUT
C      READ INPUT DATA AND PRINT IT.
CALL ARANGE (T,P,NOPROF,TA,PA,NPROFA,PMAX,PMIN)
C      ARRANGE THE POWER PROFILE IN DESCENDING ORDER OF POWER AND TO
C      DETERMINE THE MAXIMUM AND MINIMUM POWER VALUES.
WRITE OUTPUT TAPE 2,201
201 FORMAT (1H1POWER PROFILE)
WRITE OUTPUT TAPE 2,203
203 FORMAT(1H0,7X,1HT,11X,1HP)
DO 205 I=1,NOPROF
205 WRITE OUTPUT TAPE 2,207,T(I),P(I)
207 FORMAT (1H 2F12.3)
PMAXXX=PMAX
PMINX=PMIN
CALL SUBQ
C      COMPUTE THE WEIGHT OF CELL,AUXILIARY,FUEL AND RADIATOR FOR
C      ALL CELL OPERATION OF THE SYSTEM.
WTOLD=WTC(1)+WTA+WTF(1)+WTR(1)
C
WTAC=WTOLD
I STAGE=0
IZ=ZZ
WRITE OUTPUT TAPE 2,105
105 FORMAT (1H1)
WRB=0.0
WREG=0.0
IF (LBT-2)1500,1510,1500
1500 WRITE OUTPUT TAPE 2,1501
1501 FORMAT (1H 5X,21HRECHARGEABLE BATTERIES)
GO TO 1550
1510 WRITE OUTPUT TAPE 2,1301
1550 WRITE OUTPUT TAPE 2,101
101 FORMAT (1H 7X,11HSTAGE VOPT,4X,7HWTTOTAL,4X,6HWTCCELL,4X,5HWTAUX,
14X,6HWTFUEL,4X,4HWRAD,5X,5HWTBAT,4X,7HNO CELL,3X,9HCELL AREA,5X,
25HWTREG)
WRITE OUTPUT TAPE 2,102,I STAGE,VOP1,WTOLD,WTC(1),WTA,WTF(1),WTR(1)
1,WRB,IZ,AREA,WREG
WRITE OUTPUT TAPE 2,103
103 FORMAT (1H+,10HALL CELL =)
IF (FN-1.0)300,300,40
40 DP=(PMAX-PMIN)/FN
IF (LBT-1)300,45,44
44 IF (LBT-2)45,1100,45
45 PFCMX=PMAX-DP
COUNT=0.0
I=0
IF (NOPROF-1)300,300,80
80 CALL SUBP
IF (CODE-1.0)82,800,20
C      COMPUTE THE WEIGHT OF RECHARGEABLE BATTERY AND REGULATOR FOR
C      THE SPECIFIED TYPE OF BATTERY AND THE MAXIMUM LEVEL OF
C      POWER SUPPLIED BY FUEL CELL.

```

```

82 CALL ARANGE(TX,PX,NPROFX,TA,PA,NPROFA,PMAX,PMIN)
C           ARRANGE THE POWER PROFILE AFTER RECHARGING THE BATTERIES IN
C           ORDER TO DETERMINE NEW WEIGHT OF THE SYSTEM
CALL SUBQ
IF (ICOMB)83,83,599
599 IF (COUNT-10.0)600,700,700
600 IF (ABSF(VOP1-VOPOLD)-.0005)83,83,650
650 VOPOLD=VOP1
COUNT=COUNT+1.0
GO TO 80
700 WRITE OUTPUT TAPE 2,501
501 FORMAT (34H0OPTIMUM VOLTAGE WILL NOT CONVERGE)
83 I=I+1
WTCELL(I)=WTC(1)+WTA+WTF(1)+WTR(1)+WRB+WREG
VOPOLD=0.0
IZ=ZZ
ISTAGE=ISTAGE+1
WRITE OUTPUT TAPE 2,102,ISTAGE,VOP1,WTCELL(I),WTC(1),WTA,WTF(1),
1WTR(1),WRB,IZ,AREA,WREG
102 FORMAT (10X,I2,F7.3,6F10.3,I7,3X,2F10.3)
COUNT=0.0
AAREA(I)=AREA
PFCMX=PFCMX-DP
IF(PMINX-PFCMX+.01)84,800,800
84 TRY=1.0
AREA=(PFCMX+PARA)/VJOP1/ZZ/XNAM
GO TO 80
800 WTEMP=WTCELL(1)
TAREA=AAREA(1)
JSAVE=1
805 DO 840 J=1,I
IF (WTEMP-WTCELL(J))840,840,810
810 WTEMP=WTCELL(J)
TAREA=AAREA(J)
JSAVE=J
840 CONTINUE
IF (LBT-2)910,1100,1100
1100 PFCMX=PMAXXX
IF (LBT-2)1302,1303,1302
1302 WRITE OUTPUT TAPE 2,1301
WRITE OUTPUT TAPE 2,101
1301 FORMAT (1H0,5X,17HPRIM BATTERIES)
1303 IWT=0
1110 IWT=IWT+1
PFCMX=PFCMX-DP
CALL ARANGE (T,P,NPROF,TA,PA,NPROFA,PMAX,PMIN)
IYY=0
DO 1130 I=1,NPROFA
PABT(I)=PA(I)-PFCMX
TABT(I)=TA(I)
IF (PABT(I))1150,1150,1120
1120 IYY=IYY+1
1130 CONTINUE
1150 PTSUM=0.0

```

```

DO 1160 I=1,IYY
1160 PTSUM=PTSUM+PART(I)*TABF(I)
WTPRB=PTSUM*BATT
DO 1190 I=1,NPROFA
IF (PA(I)-PFCMX)1170,1170,1180
1170 PX(I)=PA(I)
TX(I)=TA(I)
GO TO 1190
1180 PX(I)=PFCMX
TX(I)=TA(I)
1190 CONTINUE
CALL ARANGE (TX,PX,NPROFA,TA,PA,NPROFA,PMAX,PMIN)
CALL SUBQ
AAREA(IWT)=WTPRB
WTCELL(IWT)=WTC(1)+WTA+WTF(1)+WTR(1)+WTPRB
IZ=ZZ
WRITE OUTPUT TAPE 2,102,IWT,VOP1,WTCELL(IWT),WTC(1),WTA,WTF(1),
IWTR(1),WTPRB,IZ,AREA
IF (PMINX-PFCMX+DP+.01)1110,1200,1200
1200 IPSTG=1
WTPRB=AAREA(1)
WPRIM=WTCELL(1)
DO 1260 I=1,IWT
IF (WPRIM-WTCELL(I))1260,1260,1210
1210 IPSTG=I
WTPRB=AAREA(I)
WPRIM=WTCELL(I)
1260 CONTINUE
XTEM=IPSTG
IF (LBT-2)20,1270,1400
1270 IF (WPRIM-WTAC)1280,300,300
1280 PFCMX=PMAXXX-XTEM*DP
DO 1350 I=1,NOPROF
IF (P(I)-PFCMX)1300,1300,1310
1300 PX(I)=P(I)
TX(I)=T(I)
GO TO 1350
1310 PX(I)=PFCMX
TX(I)=T(I)
1350 CONTINUE
CALL ARANGE (TX,PX,NOPROF,TA,PA,NPROFA,PMAX,PMIN)
WRITE OUTPUT TAPE 2,1351,IPSTG
1351 FORMAT (1H0,5X,26HTHE OPTIMUM CASE IS STAGE ,12,25H USING PRIMARY
1 BATTERIES)
CALL SUBQ
WREG=0.0
WRB=WTPRB
GO TO 500
1400 IF (WTAC-WPRIM)1410,1410,1420
1410 IF (WTAC-WTEMP)300,300,400
1420 IF (WPRIM-WTEMP)1280,1280,400
910 IF (WTEMP-WTAC)400,300,300
300 CALL ARANGE(T,P,NOPROF,TA,PA,NPROFA,PMAX,PMIN)
CALL SUBQ

```

```

WTOPT=WTC(1)+WTA+WTF(1)+WTR(1)
WREG=0.0
WRB=0.0
WRITE OUTPUT TAPE 2,104
104 FORMAT (1H0,10X,28HTHE OPTIMUM CASE IS ALL CELL)
GO TO 500
400 XTEM=JSAVE
PFCMX=PMAXXX-DP*XTEM
AREA=TAREA
CALL SUBP
IF (CODE-2.0)410,20,20
410 CALL ARANGE (TX,PX,NPROFX,TA,PA,NPROFA,PMAX,PMIN)
CALL SUBQ
WTOPT=WTC(1)+WTA+WTF(1)+WTR(1)+WREG+WRB
WRITE OUTPUT TAPE 2,106
106 FORMAT (1H1,5X,40HOPTIMUM CASE USING RECHARGEABLE BATTERIES)
WRITE OUTPUT TAPE 2,107
107 FORMAT (1H0)
WRITE OUTPUT TAPE 2,101
J=JSAVE
I STAGE=JSAVE
WRITE OUTPUT TAPE 2,102,I STAGE,VOP1,WTOPT      ,WTC(1),WTA,WTF(1),
1WTR(1),WRB,I Z,AREA,WREG
WRITE OUTPUT TAPE 2,107
WRITE OUTPUT TAPE 2,108,VMINB,ALPHA,IBAT,DISRAT
108 FORMAT (1H0,10X,7HVMINB =,F7.3,3X,7HALPHA =,F7.3,3X,6HIBAT =,I3,
15X,8HDISRAT =,F7.3)
WRITE OUTPUT TAPE 2,111
111 FORMAT (1H0,15X,2HTX,11X,2HPX)
DO 113 I=1,NPROFX
113 WRITE OUTPUT TAPE 2,112,TX(I),PX(I)
112 FORMAT (1H ,11X,F8.3,5X,F8.3)
EX3=C*VBMIN*ERD/WRB
WRITE OUTPUT TAPE 2,114,C,EX3
114 FORMAT (1H0,15X,3HC =,F8.3,6X,4HRD =,F8.3)
WRITE OUTPUT TAPE 2,115,EX2,REJECT
115 FORMAT (1H0,13X,5HBAT =,F8.3,3X,7HVBMAX =,F8.3)
845 DO 900 J=1,25
WTCELL(J)=0.0
900 AAREA(J)=0.0
IF (NPP-1)500,20,500
500 CALL SUBR
GO TO 20
END(0,1,0,1,0)

```

C JAYISH DALAL D-3258 3258-734M INPUT

C SUBROUTINE INPUT
C READ CONTROL CARD
C

```
DIMENSION TRD(4,4),TCD1(11,2),TCD2(9,2),TIBD(7),TALPHA(10),
1TVMINB(10,7),P(55),T(55),TA(75),PA(75),TX(75),PX(75),V(30),
2AMP(30),VJ(30),TR(75),PR(75),WTF(2),WTC(2),WTR(2),WT(2)
COMMON NVJ ,TCD1 ,TCD2 ,TIBD ,TALPHA,TVMINB,P ,T ,
1TA , PA ,TX ,PX ,V ,AMP ,VJ ,NOPROF,NPROFA,
2NPROFX , TRD ,NIP ,REJECT,WTC ,WTA ,WTF ,WTR ,WREG ,
3WRB , WTOPT ,WTOLD ,WTNEW ,DP ,PFCMX ,SC ,SAP ,CON ,
4VUC , VAB ,PPC ,PPV ,ADD ,BATT ,TC ,QW ,SP2 ,
5ALFMX , ALFMN ,BCMIN ,DBC ,BCMAX ,EC ,ERD ,ERC ,EX2 ,
6XNAM , XNRM ,FR ,RPS ,FN ,DALFA ,EX3 ,VMAXC ,VMINC ,
7VMAXB , VBMIN ,EX4 ,EX5 ,EX6 ,NPP ,LBT ,LFL ,LRD ,
8IBAT , ICOMB ,LSP1 ,TKH ,TKO ,EMISS ,TS ,CONKR ,NPFI ,
9NPFI , IPX ,IP ,C ,RATIO1,RATIO2,T1 ,T2 ,AREA
COMMON TT ,NN ,VCOR ,NWT ,PARA ,TR ,PR ,VJCOR ,
1SWH , SWO ,WT ,DPCH1 ,ZZ ,VCORI ,VOP1 ,VJOP1 ,TCH ,
2M1 ,M2 ,CODE ,ALPHA ,TD ,COMB ,FIBD ,FJBC1 ,FIBC1 ,
3CRIT ,ALFAC ,VJBC1 ,TCC ,DISRAT,VMINB
EQUIVALENCE (NXP,NVJ),(VMAX,VMAXC),(VMIN,VMINC)
DIMENSION TITLE(10)
425 READ 12,I1,I2,I3,I4,I5,I6,I7,I8,I9,I10,(TITLE(I),I=1,10)
IF(I1-1) 600,475,415
475 READ 20,NOPROF
READ 25,(T(I),P(I),I=1,NOPROF)
N=NOPROF-1
TT=T(NOPROF)
DO 595 I=1,N
595 T(I)=T(I+1)-T(I)
NOPROF=NOPROF-1
600 IF(I2) 800,800,625
625 READ 20,NXP
READ 25,(V(I),AMP(I),I=1,NXP)
DO 700 I=1,NXP
700 VJ(I)=V(I)*AMP(I)
800 IF(I3) 900,900,825
825 READ 5,SC ,SAP ,CON ,VOC ,VAB ,PPC ,PPV
900 IF(I4) 1000,1000,925
925 READ 5,ADD ,BATT ,TC ,QW ,SP2 ,ALFMX ,ALFMN
1000 IF(I5) 1100,1100,1025
1025 READ 5,BCMIN ,DBC ,BCMAX ,EC ,ERD ,ERC ,SP3
1100 IF(I6) 1200,1200,1125
1125 READ 5,XNAM ,XNRM ,FR ,RPS ,FN ,DALFA ,SP4
1200 IF(I7) 1300,1300,1225
1225 READ 5,VMAXC ,VMINC ,VMAXB ,VBMIN ,SP5 ,SP6 ,SP7
1300 IF(I8) 1350,1350,1325
1325 READ 5,TKH ,TKO ,EMISS ,TS ,CONKR
1350 IF(I9) 1400,1400,1375
1375 READ 30,NPP ,LBT ,LFL ,LRD ,IBAT ,ICOMB ,LSP1
C
C PRINT OUT INPUT DATA
```

```

C
1400 PRINT 55,(TITLE(I),I=1,10)
PRINT 60,NXP
PRINT 65,(V(I),AMP(I),VJ(I),I=1,NXP)
PRINT 70
PRINT 68,SC,SAP,CON,VOC,VAB,PPC,PPV
PRINT 80
PRINT 68,ADD,BATT,TC,QW,SP2,ALFMX,ALFMN
PRINT 90
PRINT 68,BCMIN,DBC,BCMAX,EC,ERD,ERC,SP3
PRINT 100
PRINT 68,XNAM,XNRM,FR,RPS,FN,DALFA,SP4
PRINT 110
PRINT 68,VMAXC,VMINC,VMAXB,VBMIN,SP5,SP6,SP7
PRINT 130
PRINT 68,TKH,TKO,EMISS,TS,CONKR
PRINT 120
PRINT 128,NPP,LBT,LFL,LRD,IBAT,ICOMB,LSP1
RETURN
5 FORMAT(7F10.0)
12 FORMAT(10I1,10A6)
20 FORMAT(I2)
25 FORMAT(6F10.0)
30 FORMAT(7I1)
55 FORMAT(1H120X,10A6//1X)
60 FORMAT(28H NO OF POINTS ON V-J CURVE =I3//6X,1HV10X,1HJ12X,2HVJ//)
68 FORMAT(1XF10.5,6(2XF10.5))
65 FORMAT(1XF10.5,2XF10.5,2XF10.5)
70 FORMAT(1H0,4X2HSC10X3HSAP9X3HCON9X3HVOC9X3HVAB9X3HPPC9X3HPPV)
80 FORMAT(1H0,3X3HADD8X4HBATT9X,2HTC10X2HQW10X3HSP27X5HALFMX9X,
15HALFMN)
90 FORMAT(1H0,1X5HBCMI N9X3HDBC6X5HBCMAX10X2HEC10X3HERD9X 3HERC9X3HSP3)
100 FORMAT(1H0,2X,4HXNAM8X4HXNRM9X2HFR9X3HRPS10X2HFN8X5HDAL FA9X3HSP4)
110 FORMAT(1H0,1X5HVMAXC7X5HVMINC6X5HVMAXB7X5HVBMIN9X3HSP510X3HSP6,
19X3HSP7)
120 FORMAT(1H0,3X3HNPP9X3HLBT8X3HLFL9X3HLRD8X4HIBAT8X5HLV 8X4HLS P1)
128 FORMAT(1H0,3X,7(I1,11X))
130 FORMAT(1H0,3X,3HTKH,9X,3HTKO,7X,5HEMISS,9X,2HTS,8X,5HCONKR)
415 PAUSE 111
GO TO 425
END (0,1,0,1,0)

```

```

C      JAYESH G. DALAL      DEPT-3258 X-3362
C      SUBROUTINE TO REARRANGE THE POWER PROFILE IN DESCENDING ORDER
SUBROUTINE ARANGE(T,P,NOPROF,TA,PA,NPROFA,PMAX,PMIN)
DIMENSION T(1),P(1),TA(1),PA(1)
DO 10 I=1,NOPROF
    TA(I)=T(I)
10 PA(I)=P(I)
C      PA AND TA CONTAIN POWER PROFILE ARRANGED IN DESCENDING
C      ORDER OF POWER
C
IF (NOPROF-1)100,100,20
20 K1=NOPROF
M= NOPROF
K2=K1+1
DO 77 K=1,K1
DO 76 I=2,M
IF (PA(I-1)-PA(I))75,76,76
75 TEM1=PA(I-1)
TEM2=TA(I-1)
PA(I-1)=PA(I)
TA(I-1)=TA(I)
PA(I)=TEM1
TA(I)=TEM2
76 CONTINUE
M=M-1
77 CONTINUE
PMAX=PA(1)
PMIN=PA(NOPROF)
C      COMBINE EQUAL POWER VALUES
C
79 I=2
81 IF (PA(I))300,300,80
80 IF (ABSF(PA(I)-PA(I-1))-0.01)200,200,90
90 I=I+1
GO TO 81
100 PMAX=PA(1)
PMIN=PA(1)
NPROFA=1
GO TO 320
200 TA(I-1)=TA(I-1)+TA(I)
K2=K2-1
DO 210 J=I,K2
PA(J)=PA(J+1)
210 TA(J)=TA(J+1)
GO TO 79
300 NPROFA=K2-1
320 IF (SENSE SWITCH 4)350,500
350 PRINT 400,PMAX,PMIN,NPROFA,(PA(I),TA(I),I=1,NPROFA)
400 FORMAT( 8HOARRANGE/5X,5HPMAX=,F10.4,5HPMIN=,F10.4,7HNPROFA=,
1   I3/1H ,10X,2HPA,10X,2HTA/{1H ,2F12.4})
500 RETURN
END(0,1,0,1,0)

```

C PAUL CALLEN DEPT. 3258
 SUBROUTINE WTFUEL
 EQUIVALENCE (NXP,NVJ), (VMAX,VMAXC), (VMIN,VMINC)
 DIMENSION TRD(4,4), TCD1(11,2), TCD2(9,2), TIBD(7), TALPHA(10),
 TVMINB(10,7), P(55), T(55), TA(75), PA(75), TX(75), PX(75), V(30),
 ZAMP(30), VJ(30), TR(75), PR(75), WTF(2), WTC(2), WTR(2), WT(2)
 COMMON NVJ , TCD1 , TCD2 , TIBD , TALPHA, TVMINB, P , T ,
 1TA , PA , TX , PX , V , AMP , VJ , NOPROF, NPROFA,
 2NPROFX, TRD , NIP , REJECT, WTC , WTA , WTF , WTR , WREG ,
 3WRB , WTOPT , WTOLD , WTNEW , DP , PFCMX , SC , SAP , CON ,
 4VOC , VAB , PPC , PPV , ADD , BATT , TC , QW , SP2 ,
 5ALFMX , ALFMN , BCMIN , DBC , BCMAX , EC , ERD , ERC , EX2 ,
 6XNAM , XNRM , FR , RPS , FN , DALFA , EX3 , VMAXC , VMINC ,
 7VMAXXB , VBMIN , EX4 , EX5 , EX6 , NPP , LBT , LFL , LRD ,
 8IRAT , ICOMB , LSP1 , TKH , TKO , EMISS , TS , CONKR , NPFI ,
 9NPF2 , IPX , IP , C , RATIO1, RATIO2, TI , T2 , AREA
 COMMON TT , NN , VCOR , NWT , PARA , TR , PR , VJCOR ,
 1SWH , SWO , WT , DPCH1 , ZZ , VCORI , VOP1 , VJOP1 , TCH ,
 2M1 , M2 , CODE , ALPHA , TD , COMB , FIBD , FJBC1 , FIIBC1 ,
 3CRIT , ALFAC , VJBC1 , TCC , DISRAT, VMINB
 CALL ACFLAG (VCOR, VJCOR, NXP, NIP, V, VJ)
 SUM=TR(1)/VCOR
 N1=NPROFA-NN
 IF (N1-1)205,205,100
 100 DO 200 I=2,N1
 VJCORI=PR(I)*VJCOR
 CALL ACFLAG (VJCORI, VCORI, NXP, NIP, VJ, V)
 200 SUM=SUM+PR(I)*TR(I)/VCORI
 205 AH=SUM*(PA(NN+1)+PARA)*TT
 SWH=(AH/12100.0)*(1.0+ADD)
 SWO=7.95*SWH
 IF (LFL-1)201,202,210
 210 IF (LFL-2)203,203,212
 212 FSS=TKH*SWH+TKO*SWO
 GO TO 204
 201 FSS=SWH+SWO
 GO TO 204
 202 FSS=30.29+11.3*SWH+(.00345*TT)*SWH**.666667
 GO TO 204
 203 FSS=30.29+9.7*SWH+(.00345*TT)*SWH**.666667
 204 WTF(NWT)=FSS
 TEMP=((PA(NN+1)+PARA)/VJCOR)*SC*((XNAM+XNRM)/XNAM)
 WTC(NWT)=TEMP
 RETURN
 END (0,1,0,1,0)

C

SUBROUTINE TO CALCULATE RADIATOR

```

SUBROUTINE RADWT
EQUIVALENCE (NXP,NVJ),(VMAX,VMAXC),(VMIN,VMINC)
DIMENSION TRD(4,4),TCD1(11,2),TCD2(9,2),TIBD(7),TALPHA(10),
1TVMINB(10,7),P(55),T(55),TA(75),PA(75),TX(75),PX(75),V(30),
2AMP(30),VJ(30),TR(75),PR(75),WTF(2),WTC(2),WTR(2),WT(2)
EQUIVALENCE (NXP,NVJ),(VMAX,VMAXC),(VMIN,VMINC)
COMMON NVJ ,TCD1 ,TCD2 ,TIBD ,TALPHA,TVMINB,P ,T ,
1TA , PA ,TX ,PX ,V ,AMP ,VJ ,NOPROF,NPROFA,
2NPROFX, TRD ,NIP ,REJECT,WTC ,WTA ,WTF ,WTR ,WREG ,
3WRB , WTOPT ,WTOLD ,WTNEW ,DP ,PFCMX ,SC ,SAP ,CON ,
4VOC , VAB ,PPC ,PPV ,ADD ,BATT ,TC ,QW ,SP2 ,
5ALFMX , ALFMN ,BCMIN ,DBC ,BCMAX ,EC ,ERD ,ERC ,EX2 ,
6XNAM , XNRM ,FR ,RPS ,FN ,DALFA ,EX3 ,VMAXC ,VMINC ,
7VMAXB , VBMIN ,EX4 ,EX5 ,EX6 ,NPP ,LBT ,LFL ,LRD ,
8IBAT , ICOMB ,LSP1 ,TKH ,TKO ,EMISS ,TS ,CONKR ,NPFI ,
9NPFI , IPX ,IP ,C ,RATIO1,RATIO2,T1 ,T2 ,AREA
COMMON TT ,NN ,VCOR ,NWT ,PARA ,TR ,PR ,VJCOR ,
1SWH , SWO ,WT ,DPCH1 ,ZZ ,VCORI ,VOP1 ,VJOP1 ,TCH ,
2M1 ,M2 ,CODE ,ALPHA ,TD ,COMB ,FIBD ,FJBC1 ,FIBC1 ,
3CRIT ,ALFAC ,VJBC1 ,TCC ,DISRAT,VMINB
PPR=0.0
IF (NPROFA-NN)15,15,10
10 PPR1=((1.0-.67*VCOR)*PA(NN+1)+PARA)/(1.67*VCOR)
PPR=PPR1-(.0002165*PA(NN+1)*QW/VCOR)
PPR=PPR+.175*(PA(1)-PA(NN+1))
30 IF (LRD-1)21,22,24
24 IF (LRD-3)23,40,50
50 RPS1=1.0-RPS
C1=0.70935
C2=1.56+PPR*2.15E-6+2.0E-6/RPS1+TT*1.667E-5
C3=0.208*(0.01/RPS1)**(.20808-4.08E-6/RPS1)+TT*2.083E-5
C4=0.2088+0.000521*(0.01/RPS1)**1.04
C5=-31.6+8.6E-5/RPS1+TT*2.917E-5+29389.5/TC+PPR*1.29E-4
WTRAD=C1*((.0043*PPR)**C2)*(TT/24.0)**C3*((.01/RPS1)**C4)*
1((559.8/TC)**C5)
GO TO 25
40 WTRAD=PPR*3.415*CONKR/(EMISS*0.173((TC/100.)**4-(TS/100.1)**4))
GO TO 25
21 WTRAD=0.0
GO TO 25
15 PPR=.175*PA(1)
GO TO 30
22 WTRAD1=55.6*PPR**1.533*TT**0.5
WTRAD=WTRAD1/(1.0-RPS)**0.5/(TC-220.0)**3.57
GO TO 25
23 W1=0.906*(.0833333*TT)**(0.015*(0.0001138*PPR)**0.1974)
WT1=(0.0001138*PPR)**W1
WT2=(27.3+(0.0833333*TT)**0.3065)*(0.04166666*TT)**0.0314)
W3=(0.434294*(LOGF(RPS)-LOGF(.99))/2.82)**1.07-34.6
WT3=W3*(0.0001141*TT)**.2467*(0.00003412*PPR)**1.227
WTRAD=WT1*WT2+WT3
25 WTR(NWT)=WTRAD
RETURN

```

END(0,1,0,1,0)

```

C      JAYESH DALAL D-3258 JOB-734M ACFLAG
C      3324-493 (DP-303) DUFRESNE
C      X=INDEPENDENT VARIABLE
C      NXP=NO OF X POINTS
C      NIP=NO OF INTERPOLATION POINTS
C      XP=X POINTS IN TABLE
C      YP=Y POINTS IN TABLE
C
C
C      SUBROUTINE ACFLAG(X,Y,NXP,NIP,XP,YP)
C      DIMENSION XP(1),YP(1)
C
C
TEST=0.
IF(XP(1)-XP(NXP)) 4,1,1
1 TEST=1.
N=NXP/2
M=NXP
DO 3 I=1,N
HOLD=XP(I)
XP(I)=XP(M)
XP(M)=HOLD
HOLD=YP(I)
YP(I)=YP(M)
YP(M)=HOLD
M=M-1
3 CONTINUE
4 NIPA=NIP
VAR=X
IF(VAR-XP(1)) 5,15,15
5 ANS=-1.
GO TO 100
15 DO 20 I=1,NXP
IF(XP(I)-VAR)20,25,30
20 CONTINUE
ANS=-1.
GO TO 100
25 ANS=YP(I)
GO TO 100
C      TEST IF NO OF INTERPOLATION POINTS IS EVEN
30 IF(NIPA-(NIPA/2)*2)44,40,44
40 NQ=NIPA/2
GO TO 55
44 IF (ABSF(XP(I)-VAR)-ABSF(VAR-XP(I-1))) 45,45,50
45 NQ=(NIPA-1)/2
GO TO 55
50 NQ=(NIPA+1)/2
55 IF(I-NQ) 60,60,65
60 JJ=1
GO TO 76
C      I-NQ IS THE POINT TO START INTERPOLATING WITH
C      NXP , THE NO OF POINTS MUST NOT EXCEED THE STARTING INTERPOLATION
C      POINT PLUS THE NO OF POINTS TO INTERPOLATE WITH
65 IF (NXP-(I-NQ+NIPA)) 70,75,75

```

```
70    JJ=NXP+1-NIPA
      GO TO 76
75    JJ=I-NQ
76    ANS=0.
      J=JJ
      DO 90 L=1,NIPA
          SAVE=YP(J)
          K=JJ
          DO 88 M=1,NIPA
              HOLD=XP(J)-XP(K)
              IF(HOLD) 80,85,80
80      SAVE=(VAR-XP(K))/HOLD*SAVE
85      K=JJ+M
88      CONTINUE
          ANS=ANS+SAVE
          J=JJ+L
90      CONTINUE
100     Y=ANS
          IF(TEST) 101,110,101
101     M=NXP
          DO 103 I=1,N
              HOLD=XP(I)
              XP(I)=XP(M)
              XP(M)=HOLD
              HOLD=YP(I)
              YP(I)=YP(M)
              YP(M)=HOLD
              M=M-1
103     CONTINUE
110     RETURN
      END(0,1,0,1,1)
```

C PAUL CALLEN DEPT. 3258

SUBROUTINE SUBQ

EQUIVALENCE (NXP,NVJ), (VMAX,VMAXC), (VMIN,VMINC)

DIMENSION TRD(4,4), TCD1(11,2), TCD2(9,2), TIBD(7), TALPHA(10),
 1TVMINB(10,7), P(55), T(55), TA(75), PA(75), TX(75), PX(75), V(30),
 2AMP(30), VJ(30), TR(75), PR(75), WTF(2), WTC(2), WTR(2), WT(2)

COMMON NVJ , TCD1 , TCD2 , TIBD , TALPHA, TVMINB, P , T ,
 1TA , PA , TX , PX , V , AMP , VJ , NOPROF, NPROFA ,
 2NPROFX , TRD , NIP , REJECT, WTC , WTA , WTF , WTR , WREG ,
 3WRB , WTOPT , WTOLD , WTNEW , DP , PFCMX , SC , SAP , CON ,
 4VOC , VAB , PPC , PPV , ADD , BATT , TC , QW , SP2 ,
 5ALFMX , ALFMN , BCMIN , DBC , BCMAX , EC , ERD , ERC , EX2 ,
 6XNAM , XNRM , FR , RPS , FN , DALFA , EX3 , VMAXC , VMINC ,
 7VMAXB , VBMIN , EX4 , EX5 , EX6 , NPP , LBT , LFL , LRD ,
 8IBAT , ICOMB , LSP1 , TKH , TKD , EMISS , TS , CONKR , NPFI ,
 9NPFI , IPX , IP , C , RATIO1, RATIO2, T1 , T2 , AREA
 COMMON TT , NN , VCOR , NWT , PARA , TR , PR , VJCOR ,
 1SWH , SWO , WT , DPCH1 , ZZ , VCORI , VOP1 , VJOP1 , TCH ,
 2M1 , M2 , CODE , ALPHA , TD , COMB , FIBD , FJBC1 , FIBC1 ,
 3CRIT , ALFAC , VJBC1 , TCC , DISRAT, VMINB

NN=0
 NIP=3
 DELTAV=(VOC-VAB)/50.0

222 VCOR=VAB
 AMKR=0.0
 NJUMP=200
 NPG3=0
 NWT=1
 N5=0
 NCNT2=0
 NCNT3=0

20 PARA=PPC*XNAM+PPV*PA(NN+1)
 KAT=NPROFA-NN
 DO 21 I=1,KAT
 I1=I+NN

21 PR(I)=(PA(I1)+PARA)/(PA(NN+1)+PARA)
 TSUM=0.0
 K=NN+1
 DO 22 I=1,K
 22 TSUM=TSUM+TA(I)
 TR(1)=TSUM/TT
 DO 23 I=2,KAT
 I1=I+NN

23 TR(I)=TA(I1)/TT
 IF (NPG3)62,24,62

24 WTA={(PA(NN+1)+PARA)*SAP/XNAM+CON)*(XNAM+XNRM)}

333 CALL WTFUEL
 CALL RADWT
 WT(NWT)=WTC(NWT)+WTA+WTF(NWT)+WTR(NWT)
 IF(N5)30,31,30

30 VOP1=VCOR
 GO TO 32

31 IF(NCNT2-1)34,35,36

34 VCOR=VCOR+DELTAV

```

NWT=2
NCNT2=1
GO TO 333
35 IF(WT(1)-WT(2))37,37,136
136 NWT=1
VCOR=VAB
36 CALL TERP (AMKR,22,DELTAV,VCOR,WT(1))
IF(AMKR)38,39,38
38 NCNT2=2
GO TO 333
39 VOP1=VCOR
GO TO 33
37 VOP1=VAB
NWT=1
VCOR=VAB
33 CALL WTFUEL
CALL RADWT
WTT =WTC(NWT)+WTA+WTF(NWT)+WTR(NWT)
32 IF(INJUMP-250)40,41,42
40 CALL ACFLAG (VOP1,VJOP1,NXP,NIP,V,VJ)
VJOP2=VJOP1*PR(KAT)
CALL ACFLAG (VJOP2,VOP2,NXP,NIP,VJ,V)
IF(VMIN)43,44,43
43 ZZ=INTF(VMIN/VOP1+.999999)
GO TO 45
44 ZZ=INTF(VMAX/VOP2)
45 IF(VMAX-ZZ*VOP2)47,46,46
46 ZZ=MAX1F(ZZ,INTF(VMAX/VOP2))
GO TO 555
47 VNOP2=VMAX/ZZ
ZZMOP=ZZ
NWT=1
CALL ACFLAG (VNOP2,VJNOP2,NXP,NIP,V,VJ)
VJNOP1=VJNOP2*PR(KAT)
CALL ACFLAG (VJNOP1,VNOP1,NXP,NIP,VJ,V)
IF(VNOP1)57,57,58
57 VNOP1=VAB
GO TO 49
58 IF(VMIN-ZZ*VNOP1)50,50,49
41 NWT=2
49 ZZ=ZZ-1.
VNOP1=VMIN/ZZ
CALL ACFLAG (VNOP1,VJNOP1,NXP,NIP,V,VJ)
VJNOP2=VJNOP1*PR(KAT)
CALL ACFLAG (VJNOP2,VNOP2,NXP,NIP,VJ,V)
IF(VMAX-VNOP2*ZZ)49,51,51
51 VCOR=VNOP1
NJUMP=300
52 N5=1
GO TO 333
50 VCOR=VNOP1
VTEMP=VNOP1
NJUMP=250
GO TO 52

```

```
42 IF (NWT-1)53,56,53
53 IF(WT(2)-WT(1))54,54,55
54 WT(1)=WT(2)
    WTR(1)=WTR(2)
    WTC(1)=WTC(2)
    WTF(1)=WTF(2)
    GO TO 56
55 VOP1=VTEMP
    ZZ=ZZMOP
56 WTT=WT(1)
555 WTMOD=(WTC(1)+WTA)/(XNAM+XNRM)
    CALL ACFLAG (VOP1,VJOP1,NXP,NIP,V,VJ)
    AREA=(PA(NN+1)+PARA)/VJOP1/ZZ/XNAM
    IF (SENSE SWITCH 4)600,62
600 PRINT 110,NN,VOP1,WTT,WTC(1),WTA,WTF(1),WTR(1),ZZ,AREA
110 FORMAT(5HOSUBQ/9H      NN= I3,7X,8H  VOP1= F10.5,8H  WTT= F10.3,
        18H  WTC= F10.3,8H  WTA= F10.3/9H  WTF= F10.3,8H  WTR= F10.3,
        28H  ZZ= F10.3,8H  AREA= F10.5)
62 RETURN
END(0,1,0,1,0)
```

JAYESH DALAL D-3258 3258-734M SUBP.

THIS SUBROUTINE DETERMINES WT OF REGULATOR AND RECHARGEABLE BATTERY FOR A SPECIFIED POWER LEVEL OF FUEL CELL OPERATION. IT ALSO DETERMINES CAPACITY OF BATTERY, ALPHA AND MODIFIED POWER PROFILE AFTER CHARGING BATTERY.

SUBROUTINE SUBP

```
DIMENSION TRD(4,4),TCD1(11,2),TCD2(9,2),TIBD(7),TALPHA(10),
1 TVMINB(10,7),P(55),T(55),TA(75),PA(75),TX(75),PX(75),V(30),
2AMP(30),VJ(30),TR(75),PR(75),WTF(2),WTC(2),WTR(2),WT(2)
EQUIVALENCE (NXP,NVJ),(VMAX,VMAXC),(VMIN,VMINC)
COMMON NVJ ,TCD1 ,TCD2 ,TIBD ,TALPHA,VMINB,P ,T
1TA , PA ,TX ,PX ,V ,AMP ,VJ ,NOPROF,NPROFA,
2NPROFX, TRD ,NIP ,REJECT,WTC ,HTA ,WTF ,WTR ,WREG ,
3WRB , WTOPT ,WTOLD ,WTNEW ,DP ,PFCMX ,SC ,SAP ,CON ,
4VOC , VAB ,PPC ,PPV ,ADD ,BATT ,TC ,QW ,SP2 ,
5ALFMX , ALFMN ,BCMIN ,DBC ,BCMAX ,EC ,ERD ,ERC ,EX2 ,
6XNAM , XNRM ,FR ,RPS ,FN ,DALFA ,EX3 ,VMAXC ,VMINC ,
7VMAXB , VBMIN ,EX4 ,EX5 ,EX6 ,NPP ,LBT ,LFL ,LRD ,
8IBAT , ICOMB ,LSP1 ,TKH ,TKO ,EMISS ,TS ,CONKR ,NPFI ,
9NPFI , IP ,C ,RATIO1,RATIO2,T1 ,T2 ,AREA
COMMON TT ,NN ,VCOR ,NWT ,PARA ,TR ,PR ,VJCOR ,
1SWH , SWO ,WT ,DPCH1 ,ZZ ,VCORI ,VOP1 ,VJOP1 ,TCH ,
2M1 ,M2 ,CODE ,ALPHA ,TD ,COMB ,FIBD ,FJBC1 ,FIBC1 ,
3CRIT ,ALFAC ,VJBC1 ,TCC ,DISRAT,VMINB
```

DIMENSION ST01(30),ST02(30), ST04(30),ST05(30),ST06(30)

IXX=0

NPK=1

NP=0

ALPHA=ALFMX

RATIO1=BCMIN

RATIO2=0.

COMB=0.

CODE=0.

CALL SUBB(P,NOPROF,PFCMX,NP,NP1)

SCAN THE INPUT POWER PROFILE TO DETERMINE A POINT WHERE THE POWER REQUIREMENT EXCEEDS THE MAXIMUM LIMIT FOR FUEL CELL.

NPF1=NP1

NP=NP1

TD=T(NPF1)

DPBAT=P(NPF1)-PFCMX

ED=TD+DPBAT

EX5=ED

FIBD=DPBAT/(VBMIN*ERD)

C=FIBD*TD/ALPHA

CALL SUBB(P,NOPROF,PFCMX,NP,NP1)

IF(NP1)100,100,300

100... THERE IS ONLY ONE PEAK IN THE POWER PROFILE HIGHER THAN PFCMX.HENCE RECHARGING OF BATTERY IS NOT NECESSARY.

300... THERE IS ONE MORE HIGHER POINT ON THE PROFILE SO

```

C           RECHARGING IS REQUIRED.
100 DO 110 I=1,NOPROF
      PX(I)=P(I)
110 TX(I)=T(I)
      PX(NPF1)=PFCMX
      NOPROFX=NOPROF
      DISRAT=FIBD/C
      CALL SUBH(TRD,IBAT,C,RD)
      CALL SUBE
C           DETERMINE MINIMUM BATTERY VOLTAGE.
      BAT=INTF(VBMIN/VMINB+0.99)
      EX2=BAT
      VMAXBT=BAT-VMAXB
      REJECT=VMAXBT
      WREG=FIBC1*(VMAXBT-VBMIN)/200.
      WRB=ED/(ALPHA*RD)
      IF (SENSE SWITCH 4)149,160
149 PRINT 150,WREG,WRB,BAT,C,ALPHA,RATIO1,WTOLD
150 FORMAT( SHOSUBP/9H    WREG=F10.5,8H    WRB= F10.5,8H    BAT= F10.5,
18H      C= F10.5,8H ALPHA= F10.5/9H RATIO1= F10.5,8H WTOLD= F10.5)
160 RETURN
300 NPF2=NPF1
      CODE=0.0
      M1=NPF1+1
      M2=NPF2-1
      FIBC1=C*RATIO1
      FJBC1=FIBC1/AREA
      CALL SUBC
C           DETERMINE CHARGING TIME AVAILABLE
      CALL SUBG (IBAT,RATIO1,CRIT,ALFAC,ALFMX,BCMAX)
C           DETERMINE THE CRITICAL VALUES OF RATIO1 AND ALPHA
      CALL SUBA
C           DETERMINE THE CAPACITY OF BATTERY AND RATIO1,RATIO2 FOR THE
C           SECTION OF POWER PROFILE BETWEEN NPF1 AND NPF2
      IF(CODE)310,310,500
C           500...CHARGING TIME IS NOT ENOUGH BETWEEN NPF1 AND NPF2.
C           COMBINE MORE PEAKS AND TRY AGAIN.
      310 STO1(NPK)=NPF1
      STO2(NPK)=C
      STO5(NPK)=NPF2
      IF (IXX)311,311,312
      312 STO4(NPK)=-ED
      STO6(NPK)=FIBD
      GO TO 313
      311 STO6(NPK)=DPBAT
      STO4(NPK)=TD
      313 NPK=NPK+1
      IXX=0
      NPF1=NPF2
      NP=NPF2
      ALPHA=ALFMX
      RATIO1=BCMIN
      RATIO2=0.
      TD=T(NPF1)

```

```

DPBAT=P(NPF1)-PFCMX
ED=TD*DPBAT
EX5=ED
FIBD=DPBAT/(VBMIN*ERD)
C=FIBD*TD/ALPHA
320 CALL SUBB(P,NOPROF,PFCMX,NP,NP1)
IF(NP1)400,400,300
C      400... THERE IS NO HIGHER PEAK IN THE POWER PROFILE BEYOND
C      NPF2. COMPUTE THE CAPACITY OF BATTERY REQUIRED FOR PEAK
C      AT NPF1.
400 STO1(NPK)=NPF1
IF (CODE)1400,1400,1000
1400 STO2(NPK)=C
STO4(NPK)=TD
STO5(NPK)=NPF2
STO6(NPK)=DPBAT
GO TO 600
C      600... BATTERY CAPACITIES ARE DETERMINED FOR EACH PEAK GREATER
C      THAN PFCMX. DETERMINE THE MAXIMUM CAPACITY OF BATTERY
C      REQUIRED AND HENCE THE WTS. OF BATTERY AND REGULATOR
500 NP=NPF2
ALPHA=ALFMX
RATIO1=BCMIN
RATIO2=0.
IXX=1
ED=ED+(P(NPF2)-PFCMX)*T(NPF2)
EX5=ED
C=ED/(VBMIN*ERD*ALPHA)
PNPF1=P(NPF1)
DO 520 JJ=NPF1,NPF2
IF(PNPF1-P(JJ))510,520,520
510 PNPF1=P(JJ)
520 CONTINUE
FIBD=(PNPF1-PFCMX)/(VBMIN*ERD)
GO TO 320
600 CMAX=0.
DO 620 I=1,NPK
IF(CMAX-STO2(I))610,620,620
610 CMAX=STO2(I)
620 CONTINUE
C      DETERMINE THE WEIGHTS OF REGULATOR AND BATTERY FOR THE MAXIMUM
C      VALUE OF C.
C
C=CMAX
650 IP=0
IPX=0
I=1
660 NPF1=STO1(I)
NPF2=STO5(I)
IF (STO4(I))670,680,680
670 ED=-STO4(I)
FIBD=STO6(I)
GO TO 690
680 TD=STO4(I)

```

```

DPBAT=ST06(I)
ED=T0*DPBAT
FIBD=DPBAT/(VBMIN*ERD)
690 ALPHA=ED/(C*VBMIN*FRD)
RATIO1=BCTMIN
RATIO2=0.
DISRAT=FIBD/C
M1=NPF1+1
M2=NPF2-1
FIBC1=C*RATIO1
FJBC1=FIBC1/AREA
CALL SUBC
CALL SUBE
STO2(I)=VMINB
IF(I-NPK)700,800,800
700 CALL SUBG(IBAT,RATIO1,CRIT,ALFAC,ALFMX,BCMAX)
CALL SUBA1
IF (CODE-2.0)720,1000,720
720 CALL SUBD
I=I+1
GO TO 660
800 IP=-1
CALL SUBD
VMINB=STO2(1)
DO 900 I=2,NPK
IF(VMINB-STO2(I))900,900,810
810 VMINB=STO2(I)
900 CONTINUE
CALL SUBH(TRD,IBAT,CMAX,RD)
BAT=INTF(VBMIN/VMINB+0.99)
EX2=BAT
VMAXBT=BAT*VMAXB
REJECT=VMAXBT
WREG=FIBC1*(VMAXBT-VBMIN)/200.
WRB=C*VBMIN*ERD/RD
IF (SENSE SWITCH 4)950,1000
950 PRINT 150,WREG,WRB,BAT,C,ALPHA,RATIO1,WTOLD
C
1000 RETURN
END(0,1,0,1,0)

```

C JAYESH DALAL D-3258 3258-734M SUBA.

C THIS SUBROUTINE COMPUTES THE VALUE OF RATIO1 AND RATIO2 AND
C AT THE SAME TIME CHECKS IF THERE IS SUFFICIENT CHARGING TIME.
C TIME

C SUBROUTINE SUBA

DIMENSION TRD(4,4),TCD1(11,2),TCD2(9,2),TIBD(7),TALPHA(10),
1TVMINB(10,7),P(55),T(55),TA(75),PA(75),TX(75),PX(75),V(30),
2AMP(30),VJ(30),TR(75),PR(75),WTF(2),HTC(2),WTR(2),WT(2)
EQUIVALENCE (NXP,NVJ),(VMAX,VMAXC),(VMIN,VMINC)
COMMON NVJ ,TCD1 ,TCD2 ,TIBD ,TALPHA,TVMINB,P ,T
1TA , PA ,TX ,PX ,V ,AMP ,VJ ,NOPROF,NPROFA,
2NPROFX , TRD ,NIP ,REJECT,WTC ,WTA ,WTF ,WTR ,WREG
3WRB , WTOPT ,WTOLD ,WTNEW ,DP ,PFCHMX ,SC ,SAP ,CON
4VOC , VAB ,PPC ,PPV ,ADD ,BATT ,TC ,QW ,SP2
5ALFMX , ALFMN ,BCMIN ,DBC ,BCMAX ,EC ,ERD ,ERC ,EX2
6XNAM , XNRM ,FR ,RPS ,FN ,DALFA ,EX3 ,VMAXC ,VMINC
7VMAXB , VBMIN ,EX4 ,EX5 ,EX6 ,NPP ,LBT ,LFL ,LRD
8IBAT , ICOMB ,LSP1 ,TKH ,TKO ,EMISS ,TS ,CONKR ,NPFI
9NPFI , IPX ,IP ,C ,RATIO1,RATIO2,T1 ,T2 ,AREA
COMMON TT ,NN ,VCOR ,NWT ,PARA ,TR ,PR ,VJCOR
1SWH , SWO ,WT ,DPCH1 ,ZZ ,VCORI ,VOP1 ,VJOP1 ,TCH
2M1 ,M2 ,CODE ,ALPHA ,TD ,COMB ,FIBD ,FJBC1 ,FIBC1
3CRIT ,ALFAC ,VJBC1 ,TCC ,DISRAT,VMINB

C CODE=0.

C COMPARE THE REQUIRED CHARGING TIME WITH THE AVAILABLE TIME-TCH.
IF (TCH)400,400,10

10 IF(RATIO1-CRIT)20,20,100

20 TCC=ALPHA/(ERC*EC*RATIO1)

C CHECK FOR CRITICAL VALUE OF CHARGING TIME-TCH

IF(TCC-TCH)30,30,200

30 IF (SENSE SWITCH 4)35,50

35 PRINT 40,TCC,ALPHA,RATIO1,RATIO2,C,TCH,NPFI,NPFI,CODE

40 FORMAT(5HOSUBA/ 9H TCC= F10.5,8H ALPHA= F10.5,8HRATIO1= F10.5,
18HRATIO2= F10.5,8H C= F10.5/9H TCH= F10.5,8H NPFI= I2,8X ,
28H NPFI= I2,8X,8H CODE= F10.5)

50 RETURN

C CHECK FOR CRITICAL VALUE OF ALPHA

100 TCC=TCH

IF(ALPHA-ALFAC)150,150,110

110 TEMP=EC*RATIO1*TCH*ERC-ALPHA

RATIO2=RATIO1*(ALFAC-TEMP)/(TEMP+ALFAC)

111 IF(RATIO2)200,200,120

120 IF(RATIO2-RATIO1)30,30,200

150 RATIO2=2.*ALPHA/(TCH*EC*ERC)-RATIO1

GO TO 111

200 RATIO1=RATIO1+DBC

IF(RATIO1-BCMAX)210,210,300

210 FIBC1=C*RATIO1

FJBC1=FIBC1/AREA

```
CALL SUBC
CALL SUBG (IBAT,RATIO1,CRIT,ALFAC,ALFMX,BCMAX)
GO TO 10
300 RATIO1=BCMAX
ALPHA=ALPHA-DALFA
IF(ALPHA-ALFMN)400,310,310
310 C=EX5/(VBMIN*ERD*ALPHA)
GO TO 210
400 CODE=1.0
PRINT 410,NPF1,NPF2
410 FORMAT (10X,6HPEAKS ,I2,6H THRU ,I2,19H HAVE BEEN COMBINED)
GO TO 30
END(0,1,0,1,0)
```

JAYESH DALAL D-3258 3258-734M SUBA1

THIS SUBROUTINE COMPUTES THE VALUE OF RATIO1 AND RATIO2
CORRESPONDING TO CMAX.

SUBROUTINE SUBA1

```
DIMENSION TRD(4,4),TCD1(11,2),TCD2(9,2),TIBD(7),TALPHA(10),  
1TVMINB(10,7),P(55),T(55),TA(75),PA(75),TX(75),PX(75),V(30),  
2AMP(30),VJ(30),TR(75),PR(75),WTF(2),WTC(2),WTR(2),WT(2)  
EQUIVALENCE (NXP,NVJ),(VMAX,VMAXC),(VMIN,VMINC)  
COMMON NVJ ,TCD1 ,TCD2 ,TIBD ,TALPHA,TVMINB,P ,T ,  
1TA , PA , TX , PX , V ,AMP ,VJ ,NOPROF,NPROFA,  
2NPROFX , TRD ,NIP ,REJECT,WTC ,WTA ,WTF ,WTR ,WREG ,  
3WRB , WTOPT ,WTOLD ,WTNEW ,DP ,PFCMX ,SC ,SAP ,CON ,  
4VOC , VAB ,PPC ,PPV ,ADD ,BATT ,TC ,QW ,SP2 ,  
5ALFMX , ALFMN ,BCMIN ,DBC ,BCMAX ,EC ,ERD ,ERC ,EX2 ,  
6XNAM , XNRM ,FR ,RPS ,FN ,DALFA ,EX3 ,VMAXC ,VMINC ,  
7VMAXB , VBMIN ,EX4 ,EX5 ,EX6 ,NPP ,LBT ,LFL ,LRD ,  
8IBAT , ICOMB ,LSP1 ,TKH ,TKO ,EMISS ,TS ,CONKR ,NPFI ,  
9NPFI , IPX ,IP ,C ,RATIO1,RATIO2,T1 ,T2 ,AREA  
COMMON TT ,NN ,VCOR ,NWT ,PARA ,TR ,PR ,VJCOR ,  
1SWH , SWO ,WT ,DPCH1 ,ZZ ,VCORI ,VOP1 ,VJOP1 ,TCH ,  
2M1 ,M2 ,CODE ,ALPHA ,TD ,COMB ,FIBD ,FJBC1 ,FIBC1 ,  
3CRIT ,ALFAC ,VJBC1 ,TCC ,DISRAT,VMINB
```

```
10 IF(RATIO1-CRIT)20,20,100  
20 TCC=ALPHA/(ERC*EC*RATIO1)  
    IF(TCC-TCH)30,30,200  
30 T1=TCH  
    T2=0.  
31 IF (SENSE SWITCH 4)35,50  
35 PRINT 40,TCC,ALPHA,RATIO1,RATIO2,C,TCH,NPFI,NPFI,CODE  
40 FORMAT(6HOSUBA1/ 9H      TCC= F10.5,8H ALPHA= F10.5,8HRATIO1= F10.5,  
     18HRATIO2= F10.5,8H      C= F10.5/9H      TCH= F10.5,8H NPFI= I2,8X ,  
     28H NPFI= I2,8X,8H CODE= F10.5)  
50 RETURN  
100 TCC=TCH  
    IF(ALPHA-ALFAC)150,150,110  
110 TEMP=EC*RATIO1*TCH*ERC-ALPHA  
    RATIO2=RATIO1*(ALFAC-TEMP)/(TEMP+ALFAC)  
    T1=(ALPHA-ALFAC)/(EC*ERC*RATIO1)  
    T2=TCH-T1  
111 IF(RATIO2)200,200,120  
120 IF(RATIO2-RATIO1)31,31,200  
150 RATIO2=2.*ALPHA/(TCH*EC*ERC)-RATIO1  
    T1=0.  
    T2=TCH  
    GO TO 111  
200 RATIO1=RATIO1+DBC  
    IF(RATIO1-BCMAX)210,210,300  
210 FIBC1=C*RATIO1  
    FJBC1=FIBC1/AREA
```

```
CALL SUBC
CALL SUBG (IBAT,RATIO1,CRIT,ALFAC,ALFMX,RCMAX)
GO TO 10
300 PRINT 310
310 FORMAT(6HOSUBA1/105H ERROR IN COMPUTING CMAX.FURTHER COMPUTATIONS
I TERMINATED.PRESS START TO PROCEED WITH THE NEXT SET OF DATA)
ERROR=1.0
PAUSE 22222
CODE=2.0
RETURN
END(0,1,0,1,0)
```

C RETURN TO CARPENTER DEPT 3258
C
C SUBROUTINE SUBB(P,NOPROF,PFCMX,NP,NP1)
C
C
DIMENSION P(1)
K=N^P+1
J=NOPROF
C IS THE PROFILE POINT GREATER THAN PFCMX(MAXIMUM POWER LEVEL AT
C WHICH FUEL CELL OPERATES)
50 IF(P(K)-PFCMX)60,60,100
C PROFILE POINT LESS THAN PFCMX
60 K=K+1
IF(K-J)50,50,70
C NO PROFILE POINT GREATER THAN PFCMX
70 NP1=0
GO TO 110
C PROFILE POINT GREATER THAN PFCMX
100 NP1=K
110 IF (SENSE SWITCH 4)150,300
150 PRINT 200,NP1,PFCMX
200 FORMAT(1H0,22HSUBROUTINE SUBB NP1=,I3, 6HPFCMX=,F10.4)
300 RETURN
END(0,1,0,1,~~03~~

```

C      PAUL CALLEN DEPT. 3258          X-2507
C DETERMINES THE AVAILABLE CHARGING TIME FOR A SECTION OF POWER
C PROFILE
SUBROUTINE SUBC
DIMENSION TRD(4,4),TCD1(11,2),TCD2(9,2),TIBD(7),TALPHA(10),
1TVMINB(10,7),P(55),T(55),TA(75),PA(75),TX(75),PX(75),V(30),
2AMP(30),VJ(30),TR(75),PR(75),WTF(2),WTC(2),WTR(2),WT(2)
EQUIVALENCE (NXP,NVJ),(VMAX,VMAXC),(VMIN,VMINC)
COMMON NVJ ,TCD1 ,TCD2 ,TIBD ,TALPHA,TVMINB,P ,T ,
1TA , PA ,TX ,PX ,V ,AMP ,VJ ,NOPROF,NPROFA,
2NPROFX, TRD ,NIP ,REJECT,WTC ,WTA ,WTE ,WTR ,WREG ,
3WRB , WTOPT ,WTOLD ,WTNEW ,DP ,PFCMX ,SC ,SAP ,CON ,
4VDC , VAB ,PPC ,PPV ,ADD ,BATT ,TC ,QW ,SP2 ,
5ALFMX , ALFMN ,BCMIN ,DBC ,BCMAX ,EC ,ERD ,ERC ,EX2 ,
6XNAM , XNRM ,FR ,RPS ,FN ,DALFA ,EX3 ,VMAXC ,VMINC ,
7VMAXB , VBMIN ,EX4 ,EX5 ,EX6 ,NPP ,LBT ,LFL ,LRD ,
8IRAT , ICOMB ,LSP1 ,TKH ,TKU ,EMISS ,TS ,CONKR ,NPFI ,
9NPFI , IPX ,IP ,C ,RATIO1,RATIO2,T1 ,T2 ,AREA
COMMON TT ,NN ,VCOR ,NWT ,PARA ,TR ,PR ,VJCOR ,
1SWH , SWO ,WT ,DPCH1 ,ZZ ,VCORI ,VOP1 ,VJOP1 ,TCH ,
2M1 ,M2 ,CODE ,ALPHA ,TD ,COMB ,FIBD ,FJBC1 ,FIBC1 ,
3CRIT ,ALFAC ,VJRC1 ,TCC ,DISRAT,VMINB
TCH=0
I=M1
10 PXXX=P(I)/AREA/ZZ
CALL ACFLAG (PXXX,FXXX,NVJ,NIP,VJ,AMP)
IF (FXXX)60,15,15
15 FTOT1=FXXX+FJBC1
CALL ACFLAG (FTOT1,PXX1,NVJ,NIP,AMP,VJ)
IF (PXX1)60,20,20
20 PI=PXX1*AREA*ZZ
C IS POWER VALUE ON POWER PROFILE PLUS CHARGING POWER FOR BATTERY
C LESS THAN PFCMX
IF(PI-PFCMX) 40,40,60
40 TCH=TCH+T(I)
60 I=I+1
C IS THIS THE END POINT ON THE PROFILE
IF(I-M2)10,10,70
70 IF(SENSE SWITCH 2)80,90
80 PRINT 200,TCH,M1,M2,PFCMX
200 FORMAT(1H0,2HSUBROUTINE SUBC TCH=,F10.4,5X,3HM1=I3,5X,
13HM2=I3, 5X,6HPFCMX=,F10.4)
90 RETURN
END(0,1,0,1,0)

```

PAUL CALLEN DEPT. 3258 SUBROUTINE SUBD

THIS SUBROUTINE MODIFIES THE POWER PROFILE TO COMPENSATE FOR
THE POWER REQUIRED TO RECHARGE THE BATTERIES
SUBROUTINE SUBD

```
DIMENSION TRD(4,4),TCD1(11,2),TCD2(9,2),TIBD(7),TALPHA(10),
1TVMINB(10,7),P(55),T(55),TA(75),PA(75),TX(75),PX(75),V(30),
2AMP(30),VJ(30),TR(75),PR(75),WTF(2),WTC(2),WTR(2),WT(2)
EQUIVALENCE (NXP,NVJ),(VMAX,VMAXC),(VMIN,VMINC)
COMMON NVJ ,TCD1 ,TCD2 ,TIBD ,TALPHA,TVMINB,P ,T ,
1TA , PA , TX ,PX ,V ,AMP ,VJ ,NOPROF,NPROFA,
2NPROFX, TRD ,NIP ,REJECT,WTC ,WTA ,WTF ,WTR ,WREG ,
3WRB , WTOPT ,WTOLD ,WTNEW ,DP ,PFCMX ,SC ,SAP ,CON ,
4VOC , VAB ,PPC ,PPV ,ADD ,BATT ,TC ,QW ,SP2 ,
5ALFMX , ALFMN ,BCMIN ,DBC ,BCMAX ,EC ,ERD ,ERC ,EK2 ,
6XNAM , XNRM ,FR ,RPS ,FN ,DALFA ,EX3 ,VMAXC ,VMINC ,
7VMAXB , VBMIN ,EX4 ,EX5 ,EX6 ,NPP ,LBT ,LFL ,LRD ,
8IBAT , ICOMB ,LSP1 ,TKH ,TKO ,EMISS ,TS ,CONKR ,NPFI ,
9NPFI , IPX ,IP ,C ,RATIO1,RATIO2,T1 ,T2 ,AREA ,
COMMON TT ,NN ,VCOR ,NWT ,PARA ,TR ,PR ,VJCOR ,
1SWH , SWO ,WT ,DPCH1 ,ZZ ,VCORI ,VOP1 ,VJOP1 ,TCH ,
2M1 ,M2 ,CODE ,ALPHA ,TD ,COMB ,FIBD ,FJBC1 ,FIBC1 ,
3CRIT ,ALFAC ,VJBC1 ,TCC ,DISRAT,VMINB

C IP IS A CODE USED TO INDICATE WHICH PART OF THE POWER PROFILE IS
C BEING MODIFIED
M1=NPFI+1
IF (IP)10,30,50
10 IF (NPFI-NOPROF)11,210,210
11 DO 20 I=M1,NOPROF
  IPX=IPX+1
  TX(IPX)=T(I)
20 PX(IPX)=P(I)
  GO TO 210
30 DO 40 I=1,NPFI
  PX(I)=P(I)
40 TX(I)=T(I)
  IP=1
  PX(NPFI)=PFCMX
  IPX=NPFI
50 FIBC1=RATIO1*C
  FIBC2=RATIO2*C
  FJBC1=FIBC1/AREA
  FJBC2=FIBC2/AREA
  TSUM1=0.0
  DO 200 I=M1,NPFI2
  IPX=IPX+1
  IF (P(I)-PFCMX)60,140,140
60 PXXX=P(I)/AREA/ZZ
  CALL ACFLAG (PXXX,FXXX,NVJ,NIP,VJ,AMP)
  FTOT1=FXXX+FJBC1
  FTOT2=FXXX+FJBC2
  CALL ACFLAG (FTOT1,PXX1,NVJ,NIP,AMP,VJ)
  CALL ACFLAG (FTOT2,PXX2,NVJ,NIP,AMP,VJ)
```

```

DPCH1=PXX1*AREA*ZZ-P(I)
DELP2=PXX2*AREA*ZZ-P(I)
DELP2=(DELP2+DPCH1)/2.0
IF (T1-TSUM1)120,120,70
70 PTEM=P(I)+DPCH1
IF (PTEM-PFCMX)80,80,150
80 TSUM1=TSUM1+T(I)
IF (T1-TSUM1)100,90,90
90 TX(IPX)=T(I)
PX(IPX)=P(I)+DPCH1
GO TO 200
100 TX(IPX)=T1-TSUM1+T(I)
PX(IPX)=P(I)+DPCH1
IPX=IPX+1
PX(IPX)=P(I)+DELP2
TX(IPX)=T(I)-TX(IPX-1)
GO TO 200
120 PTEM=P(I)+DELP2
IF (PTEM-PFCMX)130,130,150
130 TX(IPX)=T(I)
PX(IPX)=P(I)+DELP2
GO TO 200
140 PX(IPX)=PFCMX
TX(IPX)=T(I)
GO TO 200
150 PX(IPX)=P(I)
TX(IPX)=T(I)
200 CONTINUE
210 NPROFX=IPX
IF (SENSE SWITCH 4)300,600
300 WRITE OUTPUT TAPE 2,500
WRITE OUTPUT TAPE 2,510
WRITE OUTPUT TAPE 2,520,NPROFX,FIBC1,FIBC2
WRITE OUTPUT TAPE 2,530
WRITE OUTPUT TAPE 2,540,(TX(I),PX(I),I=1,IPX)
500 FORMAT(1H0,15X,15HSUBROUTINE SUBD)
510 FORMAT(1H0,3X,6HNPROFX,4X,5HFIBC1,4X,5HFIBC2)
520 FORMAT (1H I7,2F11.3)
530 FORMAT(1H0,4X,2HTX,10X,2HPX)
540 FORMAT(1H ,2F10.3)
600 RETURN
END(0,1,0,1,0)

```

C PAUL CALLEN DEPT. 3258
 SUBROUTINE SUBE
 DIMENSION TRD(4,4),TCD1(11,2),TCD2(9,2),TIBD(7),TALPHA(10),
 1TVMINB(10,7),P(55),T(55),TA(75),PA(75),TX(75),PX(75),V(30),
 2AMP(30),VJ(30),TR(75),PR(75),HTF(2),HTC(2),WTR(2),WT(2)
 COMMON NVJ , TCD1 , TCD2 , TIBD , TALPHA, TVMINB,P , T
 1TA , PA , TX , PX , V , AMP , VJ , NOPROF,NPROFA,
 2NPROFX , TRD , NIP , REJECT,HTC , WTA , WTF , WTR , WREG ,
 3WRB , WTOPT , WTOLD , WTNEW , DP , PFCMX , SC , SAP , CON ,
 4VOC , VAB , PPC , PPV , ADD , BATT , TC , QW , SP2 ,
 5ALFMX , ALFMN , BCMIN , DBC , BCMAX , EC , ERD , ERC , EX2 ,
 6XNAM , XNRM , FR , RPS , FN , DALFA , EX3 , VMAXC , VMINC ,
 7VMAXB , VBMIN , EX4 , EX5 , EX6 , NPP , LBT , LFL , LRD ,
 8IBAT , ICOMB , LSP1 , TKH , TKO , EMISS , TS , CONKR , NPFI ,
 9NPFI , IPX , IP , C , RATIO1,RATIO2,T1 , T2 , AREA
 COMMON TT , NN , VCOR , NWT , PARA , TR , PR , VJCOR ,
 1SWH , SWO , WT , DPCH1 , ZZ , VCORI , VOP1 , VJOP1 , TCH ,
 2M1 , M2 , CODE , ALPHA , TD , COMB , FIBD , FJBC1 , FIBC1 ,
 3CRIT , ALFAC , VJBC1 , TCC , DISRAT,VMINB
 EQUIVALENCE (NXP,NVJ),{VMAX,VMAXC},{VMIN,VMINC})
 NSAVE=NXP
 NIP=2
 C IF IBAT=1 - NICKEL CADMIUM BATTERY IBAT=2 - SILVER CADMIUM
 C IBAT=3 - SILVER-ZINC
 IF(IBAT-2) 50,100,300
 C NICKEL CADMIUM BATTERY
 50 NXP=11
 CALL ACFLAG(ALPHA,VMINB,NXP,NIP,TCD1(1,2),TCD1(1,1))
 IF(DISRAT-1.)600,600,75
 75 VMINB=VMINB-0.0225*(DISRAT-1.)
 GO TO 600
 C SILVER CADMIUM BATTERY
 100 NXP=9
 CALL ACFLAG(ALPHA,VMINB,NXP,NIP,TCD2(1,2),TCD2(1,1))
 IF(ALPHA-0.1) 110,110, 150
 110 VMINB=VMINB-0.0032*(0.2-ALPHA)*(DISRAT-1.)
 GO TO 165
 150 VMINB=VMINB-0.032*(DISRAT-1.)
 165 IF(DISRAT-5.55) 600,600,180
 180 IF(ALPHA-0.5) 200,200, 275
 200 VMINB=VMINB-0.03*(DISRAT-5.55)
 GO TO 600
 275 VMINB=VMINB-0.03*((ALPHA/0.5)**1.75)*(DISRAT-5.55)
 GO TO 600
 C SILVER ZINC BATTERY
 300 NXP=10
 I=1
 IF(DISRAT-TIBD(I)) 350,350,310
 310 DO 380 I=2,7
 IF(DISRAT-TIBD(I)) 375,350,380
 350 J=I
 GO TO 390
 375 J1=I
 J2=I-1

GO TO 500
380 CONTINUE
J=7
390 CALL ACFLAG(ALPHA,VMINB,NXP,NIP,TALPHA,TVMINB(1,J))
GO TO 600
500 CALL ACFLAG(ALPHA,VMINB1,NXP,NIP,TALPHA,TVMINB(1,J1))
CALL ACFLAG(ALPHA,VMINB2,NXP,NIP,TALPHA,TVMINB(1,J2))
VMINB=VMINB1+(VMINB2-VMINB1)*(TIBD(J1)-DISRAT)/(TIBD(J1)-TIBD(J2))
600 IF (SENSE SWITCH 4)650,800
650 PRINT 700,VMINB,ALPHA,IBAT,DISRAT
700 FORMAT(1H0, 4HSUBE/1H ,6HVMINB=,F10.4, 6HALPHA=,F10.4, 5HIBAT=,
1I3,7HDISRAT=,F10.4)
800 NXP=NSAVE
NIP=3
RETURN
END(0,1,0,1,0)

C JAYESH DALAL D-3258 JOB-734M SUBG.
C SUBROUTINE TO DETERMINE ALFAC AND CRIT FROM THE CHARGE TABLES
C FOR A SPECIFIC TYPE OF RECHARGEABLE BATTERY.
C
C SUBROUTINE SUBG (IBAT,RATIO1,CRIT,ALFAC,ALFMX,BCMAX)
C
ALFAC=ALFMX
CRIT=BCMAX
IF(IBAT-2)30,20,10
10 CRIT=0.12
GO TO 21
20 CRIT=0.25
21 ALFAC=RATIO1-CRIT
30 IF(SENSE SWITCH 2)80,90
80 PRINT 100,IBAT,RATIO1,CRIT,ALFAC
100 FORMAT(5H0SUBG/7H0IBAT= I2,4X,BHRATIO1= F8.4,4X,6HCRIT= F8.4,4X,
17HALFAC= F8.4)
90 RETURN ***
END(0,1,0,1,0)

C PAUL CALLEN DEPT. 3258 X-3362
C SUBROUTINE TO DETERMINE RD USING TABLE TRD FOR THE
C SPECIFIED CAPACITY AND TYPE OF BATTERY

C SUBROUTINE SUBH(TRD,IBAT,C,RD)

C DIMENSION TRD(4,4)

I=IBAT+1
IF(TRD(1,1)-C)20,10,10

10 K=1
GO TO 200

20 IF(TRD(4,1)-C)30,30,40
30 K=4

GO TO 200

40 DO 100 J=2,4
IF(C-TRD(J,1))60,50,100

50 K=J
GO TO 200

60 K2=J
K1=J-1
GO TO 110

100 CONTINUE

110 C1=TRD(K1,1)
C2=TRD(K2,1)
RD1=TRD(K1,I)
RD2=TRD(K2,I)

C RD=RD1+(RD2-RD1)*(C-C1)/(C2-C1)
GO TO 300

C 200 RD=TRD(K,I)

C 300 IF (SENSE SWITCH 4)500,600

500 PRINT 400,IBAT,C,RD

400 FORMAT(1HO,28H\$UBROUTINE SUBH ...IBAT= 12,5X,3HC= ,F6.2,5X,
14HRD= ,F6.2)

600 RETURN

END(0,1,0,1,0)

C PAUL CALLEN DEPT. 3258

SUBROUTINE SUBR

EQUIVALENCE (NXP,NVJ),(VMAX,VMAXC),(VMIN,VMINC)

DIMENSION TRD(4,4),TCD1(11,2),TCD2(9,2),TIBD(7),TALPHA(10),
 1TVMINB(10,7),P(55),T(55),TA(75),PA(75),TX(75),PX(75),V(30),
 2AMP(30),VJ(30),TR(75),PR(75),WTF(2),WTC(2),WTR(2),WT(2)

COMMON NVJ ,TCD1 ,TCD2 ,TIBD ,TALPHA,TVMINB,P ,T ,
 1TA ,PA ,TX ,PX ,V ,AMP ,VJ ,NOPROF,NPROFA ,
 2NPROFX, TRD ,NIP ,REJECT,WTC ,WTA ,WTF ,WTR ,WREG ,
 3WRB , WTOPT ,WTOLD ,WTNEW ,DP ,PFCMX ,SC ,SAP ,CON ,
 4VOC , VAB ,PPC ,PPV ,ADD ,BATT ,TC ,QW ,SP2 ,
 5ALFMX , ALFMN ,BCMIN ,DBC ,BCMAX ,EC ,ERD ,ERC ,EX2 ,
 6XNAM , XNRM ,FR ,RPS ,FN ,DALFA ,EX3 ,VMAXC ,VMINC ,
 7VMAXB , VBMIN ,EX4 ,EX5 ,EX6 ,NPP ,LBT ,LFL ,LRD ,
 8IBAT , ICOMB ,LSP1 ,TKH ,TKO ,EMISS ,TS ,CONKR ,NPFI ,
 9NPFI2 , IPX ,IP ,C ,RATIO1,RATIO2,T1 ,T2 ,AREA
 COMMON TT ,NN ,VCOR ,NWT ,PARA ,TR ,PR ,VJCOR ,
 1SWH , SWO ,WT ,DPCH1 ,ZZ ,VCORI ,VOP1 ,VJOP1 ,TCH ,
 2M1 ,M2 ,CODE ,ALPHA ,TD ,COMB ,FIBD ,FJBC1 ,FIBC1 ,
 3CRIT ,ALFAC ,VJBC1 ,TCC ,DISRAT,VMINB

WRITE OUTPUT TAPE 2,108

108 FORMAT (1H120X36HTABULATION OF TOTAL WT OVER USABLE V,/1H0,6X,
 13HVIN 6X,3HV2N 7X, 2HWT 8X, 3HWTC 6X, 5HWTAUX 6X, 3HWTF 8X,
 23HWTR 5X,4HWTRB,6X,5HWTRREG)

ICODE=0

WTMOD1=(WTC(1)+WTA)/(XNAM+XNRM)

VCOR=VAB

DELTAB=(VOC-VAB)/25.0

DO 81 I=1,25

CALL WTFUEL

CALL RADWT

WTPG4=WTC(1)+WTA+WTF(1)+WTR(1)+WRB+WREG

WRITE OUTPUT TAPE 2,109,VCOR,VCORI,WTPG4,WTC(1),WTA,WTF(1),WTR(1),
 1WRB,WREG

109 FORMAT (1H ,9F10.3)

81 VCOR=VCOR+DELTAB

80 NTM=XNAM+XNRM

ROM=EXP(-FR*TT)

IF (XNRM)82,82,83

82 REST=ROM**NTM

GO TO 85

83 REST=ROM**NTM

NRM=XNRM

TERM=ROM**NTM

DO 84 I=1,NRM

Y=(NTM-I+1)/I

TERM=TERM*Y*(1.0-ROM)/ROM

84 REST=REST+TERM

85 PARM=PARA/XNAM

WRITE OUTPUT TAPE 2,150,XNAM,XNRM,REST,WTMOD1,PARM

150 FORMAT (1H17X, 35HFUEL CELL SUBSYSTEM DESIGN BASED ON F5.0, 21H A
 1CTIVE MODULES AND ,F5.0, 20H REDUNDANT MODULES./1H07X, 42HFUEL CE
 2LL SUB SYSTEM RELIABILITY ESTIMATE = ,F8.5/1H07X, 15HMODULE WEIGHT
 3= ,F10.3,/1H07X, 24HMODULE PARASITIC POWER = ,F10.3/1H0)

```

      WRITE OUTPUT TAPE 2,151
151 FORMAT (1H038X, 32HMODULE OPERATING CHARACTERISTICS)
      WRITE OUTPUT TAPE 2,152
152 FORMAT (1H07X,1HT10X,1HP10X,3HPFC9X,4HVMOD10X,3HI/A8X,1HI10X,
12HPW9X,3HWH28X,3HW026X,4HPMOD)
      NN=NN+1
      VX=VOP1
      SUM1=0.0
      SUM2=0.0
      SUM3=0.0
      SUM4=0.0
      SUM5=0.0
      SUM6=0.0
      VJX=VJOP1
      J=1
      DO 95 I=1,NPROFA
      IF (I-NN)90,90,91
90 PFC=PA(NN)
      VMOD=ZZ*VOP1
      GO TO 96
91 ITT=I+1-NN
      VJX=VJOP1*PR(ITT)
      CALL ACFLAG (VJX,VX,NXP,NIP,VJ,V)
      VMOD=ZZ*VX
      PFC=PA(I)
96 PMOD=PFC/XNAM
      CUR=PMOD/VMOD
      CURD=VJX/VX
      PW=((1.0-.67*VX)*PMOD+PARM)/(.67*VX)-.0002165*QW*(PMOD+PARM)/VX
      WH2=((PMOD+PARM)/VMOD)*ZZ/12100.0
      W02=7.95*WH2
      SUM1=SUM1+TA(I)
      SUM3=SUM3+PFC*TA(I)
      SUM4=SUM4+PW*TA(I)
      SUM5=SUM5+WH2*TA(I)
      SUM6=SUM6+W02*TA(I)
      WRITE OUTPUT TAPE 2,160,TA(I),          PFC,VMOD,CURD,CUR,PW,WH2,W02,
1PMOD
95 CONTINUE
      WRITE OUTPUT TAPE 2,161
160 FORMAT (F12.3,12X,3F12.3,5F11.3)
161 FORMAT (1H06X,5HSUM T6X,          10X,9HSUM PFC*T36X,8HSUM PW*T4X,
18HSUM WH*T5X,8HSUM W0*T)
      WRITE OUTPUT TAPE 2,162,SUM1,          SUM3,SUM4,SUM5,SUM6
162 FORMAT (F12.3,12X,F12.3,35X,3F11.3)
      RETURN
      END(0,1,0,1,0)

```

REM INPL3 MODIFIED FOR FORTRAN
 TERP REM THIS ROUTINE WORKS ONLY IN THOSE PROGRAMS WHICH
 ITERATE ON ONE VARIABLE AT A TIME.
 FUL
 MZE 0,0,4
 PZE
 PZE END,0,1
 PZE
 BCD 1TERP
 PZE TERP
 REL
 F.F.F. EQU 18
 ORG 0
 SQR T BCD 1SQRT
 TERP SXD COMMON+7,4
 SXD TE30,2
 LXA TE30,2
 CLA 1,4
 STA TE15 TO RESTORE MKR
 CLA 4,4
 STA TE20 TO RESTORE X
 TE3 CLA 1,4
 STA *+1
 CLA **
 TNX TE5,2,1
 STO TE10+4,2
 TXI TE3,4,-1
 TE5 TSX INPL3,4
 TE10 BSS 10
 TNZ *+2
 STZ TE10 ACCURACY OK
 LDQ TE10
 TE15 STQ ** MKR
 LDQ TE10+3
 TE20 STQ ** X
 LXD TE30,2
 LXD COMMON+7,4
 TRA 6,4
 TE30 PZE 5,0,*
 COMMON EQU 8150
 REM 3 POINT INTERPOLATION, USING ABSOLUTE VALUES OF Y AND
 REM SEARCHING FOR MINIMUM, OR USING SIGNED VALUES OF Y AND
 REM SEARCHING FOR ZERO
 REM TSX INPL3,4
 REM +1 MKR MAKE ZERO WHEN STARTING ON NEW ROOT
 REM +2 NUMBER OF BITS ACCURACY DESIRED, MAKE FX PT 0 TO 27
 REM +3 DELTA
 REM +4 X
 REM +5 TO +10 RESERVE FOR ROUTINE TO USE FOR
 REM SAVING X(RIGHT),Y(R),X(M1D),Y(M),X(LEFT),Y(L)
 REM +11 EXIT, IF AC=0 ACCURACY OK, IF AC=NZ MORE ITERATIONS NEEDED
 INPL3 TZE IN97
 ARS 2 MAKE ROOM FOR COUNT
 ALS 2

	SXD IN14,1	
	SXD IN31,2	
	SXD IN19,4	
	STO COMMON	Y(I)
	CLA 1,4	MKR
	TNZ IN15	
	LXA IN26,2	6
IN5	STZ 10,4	
	TXI IN7,4,1	
IN7	TIX IN5,2,1	
	LXD IN19,4	RESTORE
	TSX INA,1	
	CLA FL1	
IN8	STO 1,4	
IN9	LDQ 1,4	MKR
	FMP 3,4	X DELTA
	FAD 4,4	X(I-1)
	STO 4,4	X(I)
IN14	TXL IN90,0,**	TO EXIT
IN15	TMI IN40	TR IF COMING DOWN
	TSX INA,1	
	LDQ 8,4	
	MPY 6,4	
	TMI IN20	CROSSED AXIS
	CLA 8,4	
	SSP	
	SBM 6,4	
	TPL IN20	GETTING CLOSER TO AXIS
	LDQ INB2	GETTING FARTHER AWAY
	FMP 1,4	
IN19	TXL IN8,0,*	
IN20	CLS .25	
	STO 1,4	
	CLA 10,4	
	TNZ IN70	
IN25	CLA 8,4	USE 2 PT
IN26	FSB 6,4	
	STO COMMON	Y
	CLA 5,4	
	FSB 7,4	
	FDH COMMON	
	FMP 8,4	
	FAD 7,4	
IN28	STO COMMON	X FROM 2 PT
	LDQ FL3	
	FMP 3,4	
	FAD 4,4	X+3DELTA
	LDQ COMMON	
	STQ 4,4	
	TLQ IN90	TO EXIT
	STO 4,4	NEW X
IN31	TXL IN90,0,**	TO EXIT
IN40	ADD FL1	
	TZE IN48	

	CLA 9,4	
	TNZ IN41	THIRD PT FOUND
	LDQ 6,4	NO THIRD PT
	MPY 8,4	
	TPL IN41	
	CLS FL1	
	STO 1,4	BOUNDED
	TXL IN49,0	
IN41	CLA 4,4	NEW X
	SUB 5,4	OLD X
	TMI IN44	X BACKED UP
	TSX INA,1	
	LDQ 6,4	Y(I)
	MPY 10,4	Y(I-2)
	TMI IN42	CROSSED
	CLA 8,4	Y(I-1)
	SSP	
	SBM COMMON	
	TPL IN70	X NOT YET BOUNDED
IN42	CLS FL1	
	STO 1,4	
	TXL IN70,,	
IN44	CLS FL1	
	STO 1,4	
IN48	CLA COMMON	
	SSP	
	SBM 8,4	
	TPL IN50	NEW PR FARTHER AWAY THAN MIDDLE PT
IN49	CLA 7,4	
	STO COMMON+1	
	LDQ 8,4	
	CLA 4,4	
	STO 7,4	
	CLA COMMON	
	STO 8,4	
	CLA COMMON+1	
	TXL IN53,0	
IN50	CLA 4,4	
	LDQ COMMON	
IN53	CAS 7,4	
	TXI IN55,4,4	
	HTR	
IN55	STO 9,4	
	STQ 10,4	
	LXD IN19,4	
	LXD IN63,1	
IN60	CAL 6,4	Y
	ACL FX1	
	SLW 6,4	
	ANA FX3	
	TZE IN62	FORCE THIS PT OUT
	TNX IN64,1,1	
	TXI IN60,4,-4	
IN62	CLA 5,4	

LXD IN19,4
 FSB 7,4
 FDH IN83
 STQ COMMON
 CLA 7,4
 FAD COMMON
 STO 4,4
 IN63 TXL IN90,0,2
 IN64 LXD IN19,4
 REM THREE POINT INTERPOLATION
 IN70 CLA 5,4 X SUB 1
 FSB 9,4
 STO COMMON X(1)-X(3)
 CLA 5,4
 FSB 7,4
 STO COMMON+1 X(1)-X(2)
 TZE IN96
 CLA 6,4
 FSB 8,4
 FDH COMMON+1
 STQ COMMON+2 FRAC 2
 CLA 7,4
 FSB 9,4
 STO COMMON+3 X(2)-X(3)
 TZE IN96
 CLA 10,4
 FSB 8,4
 FDH COMMON+3
 STQ COMMON+3
 CLA COMMON+3
 FAD COMMON+2
 FDH COMMON
 STQ COMMON+5 A
 FMP COMMON+1
 FSB COMMON+2
 LDQ COMMON+5
 TQP **2
 CHS CHANGE SIGNS OF A,B,C
 STO COMMON+6 -B
 CLA COMMON+5
 SLW COMMON+5 SSP
 FDH .25 X4
 FMP 8,4
 STO COMMON
 LDQ COMMON+6
 FMP COMMON+6
 FSB COMMON
 TMI IN80 FIND MIN
 TSX SQRT,4
 NOP PROVIDE FOR RETURN FROM SAP OR FORTRAN
 STO COMMON+1 DISCRIM
 SSM
 IN77 FAD COMMON+6 -B
 IN78 FDH COMMON+5

FMP	FL.5	
LXD	IN19,4	
FAD	7,4	
STO	COMMON	
SUB	9,4	
TPL	IN79	
CLA	COMMON+1	DISCRIM
TXL	IN77,0	
IN79	CLA 1,4	
	ADD .25	
	TNZ IN28+1	
	LDQ FL.5	
	FMP 3,4	
	FAD 4,4	
	LDQ COMMON	
	TLQ IN28	
	TXL IN28+1	
IN80	CLA COMMON+6	
	TXL IN78,0	
IN90	LXA FX3,2	
	LXD IN19,1	
	CLA 2,4	
	ARS F.F.F.	F=18 FOR FORTRAN, F=0 FOR SAP
	STA IN95	
IN91	CLA 4,4	
	UFS 5,1	
	LRS 27	
	CLM	
IN95	LLS •	
	TZE IN96	
	TXI *+1,1,-2	
	TIX IN91,2,1	
IN96	LXD IN14,1	
	LXD IN31,2	
	LXD IN19,4	
	TNZ 11,4	NOT FINAL EXIT
IN97	STZ 1,4	RESET MKR
	TRA 11,4	FINAL EXIT
	REM MOVE ALL POINTS BACK	
INA	LXA INA10,2	
INA2	LDQ 8,4	
	STQ 10,4	
	TXI INA5,4,1	
INA5	TIX INA2,2,1	
	LXD IN19,4	
INA10	CLA 4,4	
	STO 5,4	
	CLA COMMON	
	STO 6,4	
	TRA 1,1	
INB2	DEC 1.25	TO MODIFY DELTA
INB3	DEC 6.	CONSTANT TO FORCE OUT PERSISTENT POINT
FX1	DEC 1	
FX3	DEC 3	

.25 DEC .25
FL.5 DEC .5
FL1 DEC 1.
FL3 DEC 3.
END BSS 0
END

6.2.1 Explanation of Subroutine TERP - A 3-Point Interpolation Routine

Purpose

Many problems can be represented by the equation $f(X) = Y$. Often it is desired to find the value of X to make $Y = 0$, and this X is found by repeated evaluation of $f(X)$. The purpose of this routine is to aid in estimating new values of X by saving the three best values and interpolating between them. The routine will attempt to find the X such that $f(X) = 0$ if the curve actually crosses the X axis, or it will find the X such that $\frac{df(X)}{dX} = 0$ if the curve does not cross the axis.

Use

- (1) In SAP programs, the routine is entered with the accumulator containing the value of X which is associated with the current value of X . The calling sequence is:

TSX	INPL3, 3
PZE	AMKR
PZE	ACC
PZE	DELTA
PZE	X
PZE	X(R)
PZE	Y(R)
PZE	X(M)
PZE	Y(M)
PZE	X(L)
PZE	Y(L)
NORMAL RETURN	

These quantities are defined to be:

AMKR - A marker which must be set to zero for each new function which will be evaluated.

ACC - The number of bits of accuracy desired for an acceptable solution--it must be a fixed point number between 0 and 27.

DELTA - The increment to be added to the initial X to get the second X.

X - The current value of X.

These four quantities need to be set before the first entry to the subroutine. The routine will modify them after that, and the new value of X will always be left in X. The next six locations contain the points which are being saved and are probably of no value to the programmer. On exiting from the routine, the accumulator and AMKR will be zero if the desired accuracy has been reached, and they will be non-zero if the desired accuracy has not been reached.

(2) In FORTRAN programs, the call statement is:

CALL TERP (AMKR, ACC, DELTA, X,Y)

6.2.2 EFM

EFM puts the program in a floating trap mode. Under this condition, a message is printed for each underflow or overflow. An adjustment is then made for this condition.

Table of Error Messages

(1) Computer halt

Computer halts displaying 22222; this means that RATIO 1 has exceeded BCMAX, and therefore CMAX cannot be calculated.
Press start to proceed with the next set of data.

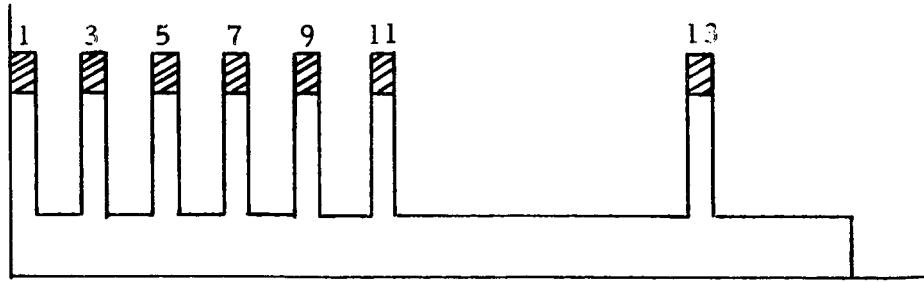
(2) Error Messages

A. "OPTIMUM VOLTAGE WILL NOT CONVERGE"

This message will be printed out only if LV is 1 and the optimum voltage does not converge after 10 iterations.

B. "PEAKS 1 THROUGH 3 HAVE BEEN COMBINED
PEAKS 1 THROUGH 5 HAVE BEEN COMBINED
PEAKS 1 THROUGH 7 HAVE BEEN COMBINED
PEAKS 1 THROUGH 9 HAVE BEEN COMBINED
PEAKS 1 THROUGH 11 HAVE BEEN COMBINED
PEAKS 13 THROUGH 15 HAVE BEEN COMBINED
PEAKS 13 THROUGH 17 HAVE BEEN COMBINED"

This message can be explained by the Figure given below.



Batteries after discharging at peak 1 could not be recharged during the period between peaks 1 and 3. An attempt was then made to see if the batteries could be recharged by combining the charging periods between peaks 1 and 3 and peaks 3 and 5. Batteries could not be recharged during this period. They could be charged, however, when all the charging times up to peak 13 were combined.

NOTE: Subroutine ACFLAG uses Lagrange method to interpolate between values in a table. If the independent variable exceeds the limits of the table being considered, the dependent variable is assigned the value of -1.0; e.g., if $V = 0.6$, then J will be -1.0.

7.0 APPENDIX B

A sample program is presented to demonstrate the capabilities and limitations of the program. It also explains the steps necessary in the program, shows a sample of input-output-data, and illustrates how the output data might be used.

7.1 Given

A combined fuel cell battery system is proposed as a power supply.

The power profile for the mission is shown in Figure 3. Sixteen points on the voltage-current density graph, see Figure 4, were selected. These are tabulated on page 93. Water generated in the fuel cell is collected. Reactants are stored supercritically. A flat radiator is used, with environmental heat input. Consideration should be given to both primary and rechargeable batteries.

PPC	=	Constant parasitic power	=	0
PPV	=	Variable parasitic power	=	0
ADD	=	Additional fuel for safety	=	0.12 pound/pound
BATT	=	Weight constant of primary batteries	=	0.02 pound/watt hour
TC	=	Temperature of coolant used in radiator	=	625° R
ALFMX	=	Maximum depth of discharge	=	0.75
ALFMN	=	Minimum depth of discharge	=	0.01

BCMIN	=	Minimum ratio of charging current to the capacity of the batteries	=	0.06/hr
BCMAX	=	Maximum ratio of charging current to the capacity of the batteries	=	0.50/hr
DBC	=	Increment in the above ratio	=	0.04/hr
EC	=	Charging efficiency	=	0.90
ERD	=	Regulator efficiency during discharge	=	0.90
ERC	=	Regulator efficiency during charge	=	0.90
XNAM	=	Number of operating fuel cell stacks	=	1
XNRM	=	Number of redundant fuel cell stacks	=	0
FR	=	Failure rate of fuel cells	=	0
RPS	=	Radiator probability of survival	=	0.999
FN	=	Number of increments between the maximum and minimum power	=	4
DALFA	=	Increment in the value of depth of discharge	=	0.10
VMAXC	=	Maximum fuel cell stack voltage	=	30 volts

VMINC	=	Minimum fuel cell stack voltage	=	26 volts
VMAXB	=	Maximum voltage per cell of the rechargeable battery	=	1.55 volts
VBMIN	=	Minimum total voltage for all cells of the battery	=	26

7.2 Required

Using the optimizing program establish the following parameters;

- (1) Minimum weight
- (2) Optimum voltage
- (3) Weights of subsystems
- (4) Cell area
- (5) Number of cells
- (6) Current and voltage for each power level
- (7) Proportion of load assigned to primary or rechargeable batteries
- (8) Rate of reactant consumption
- (9) Total reactants consumed
- (10) Total heat generated
- (11) Table of subsystem and total weight for several individual cell voltages.

Additional Data Used

The following constants and tables were used in designing the system

SC	Cell Constant	=	2.95 pounds/square feet
SAP	Auxiliary Constant	=	0.00548 pounds/watts
K	Auxiliary Constant	=	14.49 pounds
VAB	Minimum limit of cell voltage	=	0.75 volts
TKH *	<u>Weight of hydrogen + tankage</u> Weight of hydrogen	=	2.5 pounds/pound
TKO *	<u>Weight of oxygen + tankage</u> Weight of oxygen	=	1.5 pounds/pound
EMISS *	Emissivity	=	0.85
TS *	Radiator sink temperature	=	430° R
CONKR *	<u>Weight of radiator</u> Square feet of fin area	=	0.5

The table presented in Figure 5 was also used in designing the system.

* Values not used in the sample problem.

7.4 Sample Input Data Sheets

Data sheets for the problem are presented in Figure 5.

7.5 Output Data

The program solves the problem and prints data as shown in Figure 6. A reproduction of input data is printed out along with the calculated results.

7.6 Comments

From output page three, it is evident that a fuel cell-rechargeable battery combination would result in the lightest system. For such a system, maximum power supplied by fuel cells equals 1,625 watts. More refined results could be obtained by increasing the number of increments (FN), and by reducing DALFA and DBC. The refinement in the results would, of course, be obtained at the cost of longer machine time.

FUEL CELL POWER SYSTEM

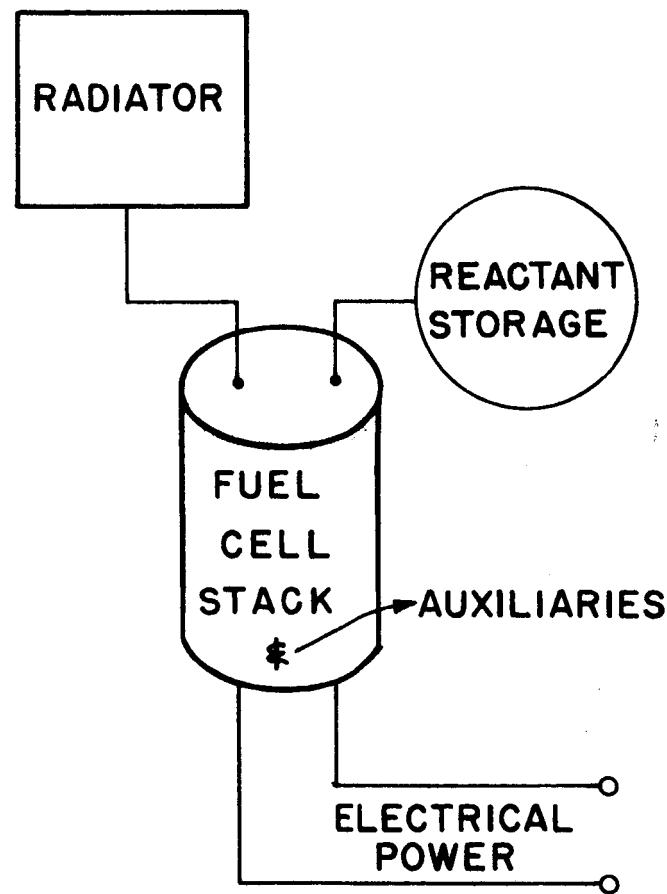
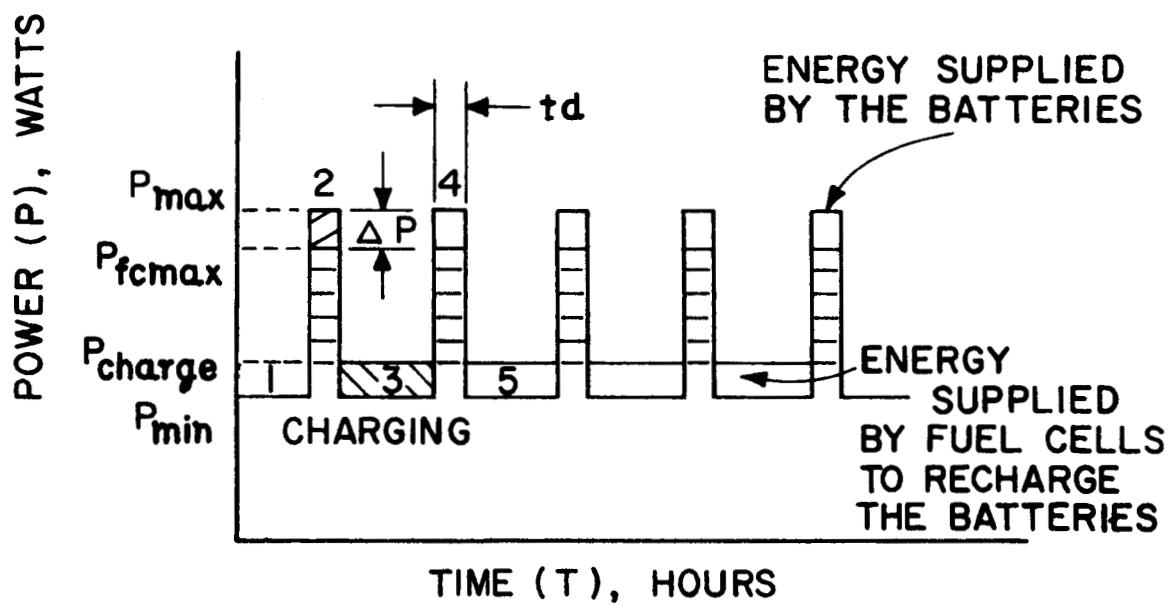


FIGURE I

TWO STEP POWER PROFILE



NOMENCLATURE

P_{\max} = MAXIMUM POWER LEVEL

P_{fcmax} = MAXIMUM POWER SUPPLIED BY THE FUEL CELLS

P_{charge} = POWER LEVEL AT WHICH THE BATTERIES ARE RECHARGED

P_{min} = MINIMUM POSITIVE POWER

FIGURE 2

POWER PROFILE FOR THE SAMPLE PROBLEM

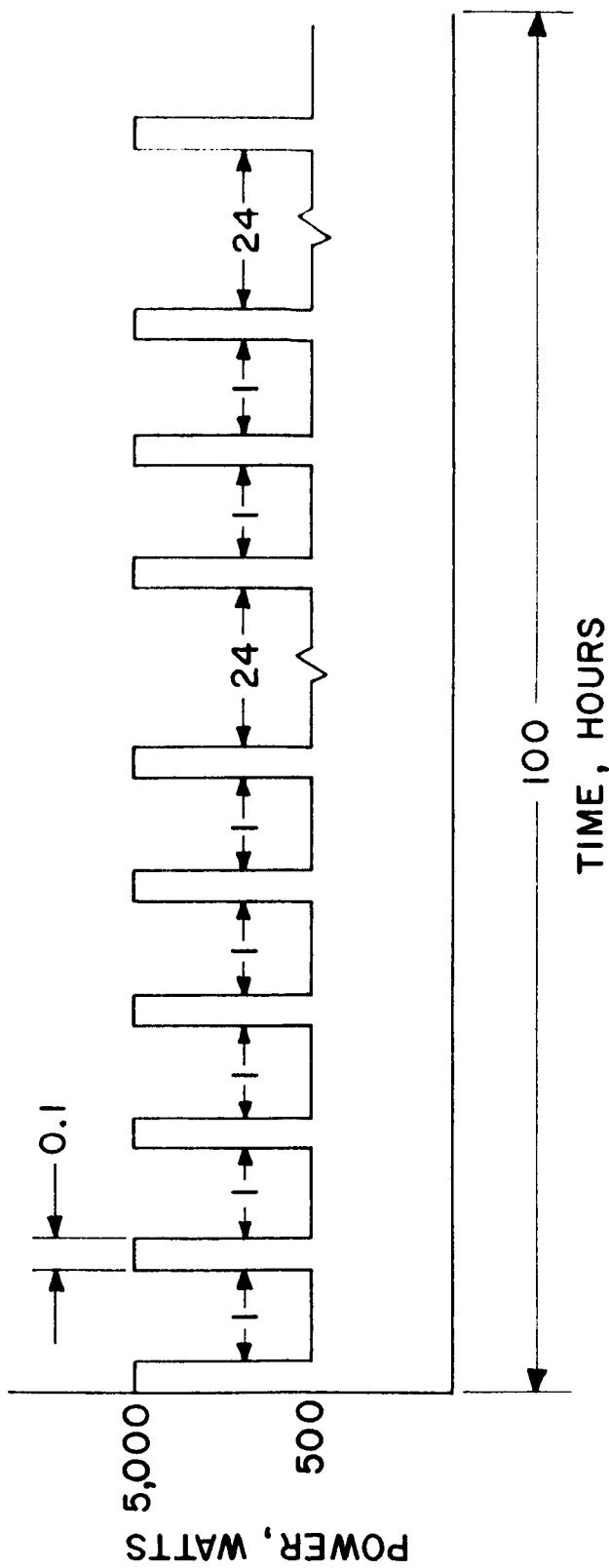


FIGURE 3

V-J CURVE OF A FUEL CELL

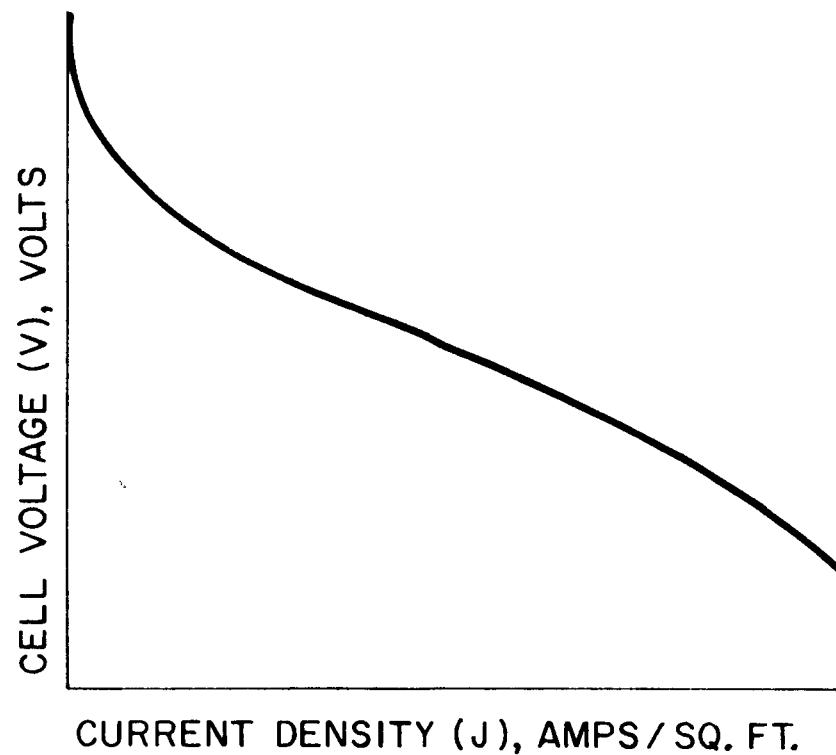


FIGURE 4

FUEL CELL OPTIMIZATION

TYPICAL INPUT DATA

Control Card:

	I1	I2	I3	I4	I5	I6	I7	I8	I9	I10	Title
COLS	1	2	3	4	5	6	7	8	9	10	70
	1	1	1	1	1	1	1	1	1	1	$P_{max} = 5,000; T=100 \text{ hrs}; \text{Ag-Cd}$

I1 = 0 - Do not read set #1

= 1 - Read Set #1

= 2 - End of Job

I2-I10 = 0 - Set i absent

= 1 - Set i present

Title - Data Identification (60 characters maximum)

FIGURE 5

1. Set #1: Power Profile

(a) NOPROF - (I2): No. of values on power profile
card columns 1-2

cols	1	2
	2	1

(b) TIME AND POWER VALUES FOR THE POWER PROFILE

	T	P	T	P	T	P	T	P
CARD#1	1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48 49 50 51 52 53 54 55 56 57 58 59 60							
#2	1 . 2	5 0 0 0 .	1 .	5 0 0 .	1 . 1	5 0 0 0 .		
#3	3 . 3	5 0 0 0 .	3 . 4	5 0 0 .	4 . 4	5 0 0 0 .		
#4	4 . 5	5 0 0 .	5 . 5	5 0 0 .	5 . 6	5 0 0 .		
#5	2 9 . 6	5 0 0 0 .	2 9 . 7	5 0 0 .	3 0 . 7	5 0 0 0 .		
#6	3 0 . 8	5 0 0 .	3 1 . 8	5 0 0 0 .	3 1 . 9	5 0 0 0 .		
#7	5 5 . 9	5 0 0 0 .	5 6 .	5 0 0 .	1 0 0 .	0 .		
#8								
#9								
#10								
#11								
#12								
#13								
#14								
#15								
#16								
#17								

FIGURE 5

2. Set #2: V-J Curve for fuel-cell

(a) NXP-(I2): Number of values on V-J curve
card columns 1-2

cols	1	2
	1	6

(b) VOLTAGE AND CURRENT VALUES FOR V-J CURVE

CARD #	V	AMP / Sq.Ft.	V	AMP		V	AMP
				1	2		
1	1.1	0.1	1.0				1.06
#2	1.01	2.11	1.02	1.1		1.00	7.0
#3	.975	1.10	.95	1.15	6.0	.925	2.09
#4	.900	2.69	.875	3.34		.850	1.04
#5	.825	1.75	.800	5.50		.775	6.28
#6	.750	7.12					
#7							
#8							
#9							
#10							

FIGURE 5

3. Set #3

VARIABLE	SC	SAP	CON	VOC	VAB	PPC	PPV
CARD COL	1-10	11-20	21-30	31-40	41-50	51-60	61-70
	2.95	.00548	14.49	1.10	.75	0	0

4. Set #4

VARIABLE	ADD	BATT	TC	QW	SP2	ALFMX	ALFMN
CARD COL	1-10	11-20	21-30	31-40	41-50	51-60	61-70
	.12	.02	625.	0.	0.	0.75	0.01

5. Set #5

VARIABLE	BCMIN	DBC	BCMAX	EC	ERD	ERC	SP3
CARD COL	1-10	11-20	21-30	31-40	41-50	51-60	61-70
	.0625	0.04	0.50	.9	.9	.9	0.

6. Set #6

VARIABLE	XNAM	XNRM	FR	RPS	FN	DALFA	SP4
CARD COL	1-10	11-20	21-30	31-40	41-50	51-60	61-70
	1.	0.	0.	.999	4.	0.1	0.

7. Set #7

VARIABLE	VMAXC	VMINC	VMAXB	VBMIN	SP5	SP6	SP7
CARD COL	1-10	11-20	21-30	31-40	41-50	51-60	61-70
	30	26	1.55	26.	0.	0.	0.

8. Set #8

VARIABLE	TKH	TKO	EMISS	TS	CONKR
CARD COL	1-10	11-20	21-30	31-40	41-50
	2.5	1.5	0.85	430.0	0.5

9. Set #9

VARIABLE	NPP	LBT	LFL	LRD	IBAT	LV	LSP1
CARD COL	1-10	11-20	21-30	31-40	41-50	51-60	61-70
	0	3	1	4	2	0	0

FIGURE 5

FORMAT FOR TABLES

1. Table of d: TRD

The values are read in row at a time with four values per card.
FORMAT (4F10.0)

2. Nickel-Cadmium Cell Discharge Model: TCD1

The values are read in row at a time with two values per card.
FORMAT (2F10.0)

3. Silver-Cadmium Cell Discharge Model: TCD2

The values are read in row at a time with two values per card.
FORMAT (2F10.0)

4. Silver-Zinc Cell Discharge Model

TIBD:

All the values of TIBD are read in on one card. FORMAT (7F10.0)

TALPHA:

The values of TALPHA are read in on two cards with five values per card. FORMAT (5F10.0)

TVMINB:

The values of TVMINB are read in column at a time on seven cards with 10 values per card. FORMAT (10F7.0)

FIGURE 5

FUEL CELL OPTIMIZATION

TABLES

1. Table of ζ_d : PRD

(Reference 6)

Capacity Amp-hr	ζ_d -	Watt-hr / lb	
		Ni-Cd	Ag-Cd
1.	8.	12.	30.
25.	12.	21.	50.
100.	17.	32.	70.
300.	22.	41.	90.

$$IBD/C = 1$$

2. Nickel-Cadmium Cell Discharge Model: TCDI

(References 7 and 8)

No.	V_{minb}	α
1	1.290	0.00
2	1.250	0.10
3	1.225	0.20
4	1.220	0.30
5	1.215	0.40
6	1.210	0.50
7	1.205	0.60
8	1.200	0.70
9	1.195	0.80
10	1.170	0.90
11	1.100	1.00

$$IBD/C = 1$$

FIGURE 5

3. Silver-Cadmium Cell Discharge Model: TCD2 (References 7 and 8)

No.	Vminb	α
1	1.35	0.0000
2	1.14	0.0555
3	1.06	0.11
4	1.06	0.7200
5	1.04	0.7770
6	1.00	0.8330
7	0.95	0.8880
8	0.84	0.9420
9	0.60	1.0000

4. Silver-Zinc Cell Discharge Model (References 7 and 9)

a. Table of Values for IBD/C: TIBD

No.	IBD/C
1	0.0208
2	0.1000
3	0.3333
4	1.0000
5	2.0000
6	3.0000
7	6.0000

b. Table of Values for: TALPHA

No.	α	No.	α
1	0.000	6	0.175
2	0.050	7	0.250
3	0.100	8	0.300
4	0.1250	9	0.750
5	0.150	10	1.000

FIGURE 5

c. Table of Values for Vminb: TVMINB (Reference 7 and 8)

IBD/C	0.0208	0.1	0.333	1.0	2.0	3.0	6.0
0.000	1.85	1.8	1.73	1.7	1.66	1.62	1.49
0.050	1.8475	1.79	1.715	1.69	1.62	1.5	1.37
0.100	1.845	1.78	1.7	1.68	1.58	1.42	1.30
0.125	1.845	1.765	1.68	1.64	1.54	1.41	1.295
0.150	1.83	1.751	1.66	1.60	1.50	1.4	1.29
0.175	1.80	1.72	1.64	1.575	1.48	1.4	1.31
0.250	1.60	1.60	1.58	1.50	1.45	1.4	1.33
0.300	1.58	1.54	1.52	1.50	1.45	1.4	1.33
0.750	1.58	1.54	1.52	1.50	1.45	1.4	1.33
1.000	1.58	1.54	1.52	1.50	1.45	1.33	1.2

FIGURE 5

NO. OF POINTS ON V-J CURVE .. 16

V	J	VJ				
1.10000	0.	0.				
1.08000	4.00000	4.32000				
1.06000	11.00000	11.66000				
1.04000	24.00000	24.96000				
1.02000	44.00000	44.88000				
1.00000	70.00000	70.00000				
0.97500	110.00000	107.25000				
0.95000	156.00000	148.20000				
0.92500	209.00000	193.32500				
0.90000	269.00000	242.10000				
0.87500	334.00000	292.25000				
0.85000	404.00000	343.39999				
0.82500	475.00000	391.87500				
0.80000	550.00000	440.00000				
0.77500	628.00000	486.70000				
0.75000	712.00000	534.00000				
SC	SAP	CON	VOC	VAB	PPC	PPV
2.95000	0.00548	14.49000	1.10000	0.75000	0.	0.
ADD	BATT	TC	QW	SP2	ALFMX	ALFMN
0.12000	0.02000	625.00000	0.	0.	0.75000	0.01000
BCMIN	DBC	BCMAX	EC	ERD	ERC	SP3
0.06000	0.04000	0.50000	0.90000	0.90000	0.90000	0.
XNAM	XNRM	FR	RPS	FN	DALFA	SP4
1.00000	0.	0.	0.99900	4.00000	0.10000	0.
VMAXC	VMINC	VMAXB	VBMIN	SP5	SP6	SP7
30.00000	26.00000	1.55000	26.00000	0.	0.	0.
TKH	TKO	EMISS	TS	CONKR		
2.50000	1.50000	0.85000	430.00000	0.50000		
NPP	LBT	LFL	LRD	IBAT	LV	LSP1
0	3	1	4	2	0	0

FIGURE 6

POWER PROFILE

T	P
0.100	5000.000
1.000	500.000
0.100	5000.000
1.000	500.000
0.100	5000.000
1.000	500.000
0.100	5000.000
1.000	500.000
0.100	5000.000
1.000	500.000
0.100	5000.000
1.000	500.000
0.100	5000.000
1.000	500.000
24.000	500.000
0.100	5000.000
1.000	500.000
0.100	5000.000
1.000	500.000
0.100	5000.000
24.000	500.000
0.100	5000.000
44.000	500.000

FIGURE 6

RECHARGEABLE BATTERIES

STAGE	V _{OPT}	WT _{TOTAL}	WT _{CELL}	WT _{AUX}	WT _{FUEL}
ALL CELL 0	0.929	225.559	79.023	41.890	86.278
1	0.897	203.570	45.921	35.725	88.455
2	0.897	190.989	32.589	29.560	90.239
3	0.867	178.141	15.504	23.395	93.586

WRAD	WTBAT	NO CELL	CELL AREA	WTREG
18.368	0.	28	0.957	0.
14.244	19.160	29	0.537	0.065
8.377	30.093	29	0.381	0.131
4.211	41.249	30	0.175	0.196

PRIMARY BATTERIES

STAGE	V _{OPT}	WT _{TOTAL}	WT _{CELL}	WT _{AUX}	WT _{FUEL}
1	0.897	204.385	45.921	35.725	85.995
2	0.897	200.780	32.589	29.560	85.253
3	0.867	196.523	15.504	23.395	85.913

WRAD	WTBAT	NO CELL	CELL AREA	WTREG
14.244	22.500	29	0.537	
8.377	45.000	29	0.381	
4.211	67.500	30	0.175	

FIGURE 6

OPTIMUM CASE USING RECHARGEABLE BATTERIES

STAGE	V _{OPT}	WT _{TOTAL}	WT _{CELL}	WT _{AUX}	WT _{FUEL}	WRAD	WT _{BAT}	NO CELL	CELL AREA	WT _{REG}
3	0.867	178.194	15.504	23.395	93.639	4.211	41.249	30	0.175	0.196

V _{MINB} = 0.980	ALPHA = 0.350	I _{BAT} = 2	DISRAT = 3.500
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TX	PX
0.100	1625.000
0.376	998.512
0.624	951.918
0.100	1625.000
0.376	998.512
0.624	951.918
0.100	1625.000
0.376	998.512
0.624	951.918
0.100	1625.000
0.376	998.512
0.624	951.918
0.100	1625.000
0.376	998.512
0.624	951.918
0.100	1625.000
24.000	568.039
0.100	1625.000
0.376	998.512
0.624	951.918
0.100	1625.000
0.376	998.512
0.624	951.919
0.100	1625.000
24.000	568.039
0.100	1625.000
44.000	500.000

C = 41.209 RD = 23.377
 BAT = 27.000 VBMAX = 41.850

FIGURE 6

TABULATION OF TOTAL WT OVER USABLE V

VIN	V2N	WT	WTC	WTAUX	WTF	WTR	WTRB	WTREG
0.750	0.941	177.766	8.977	23.395	97.077	6.872	41.249	0.196
0.764	0.945	177.442	9.447	23.395	96.672	6.483	41.249	0.196
0.778	0.950	177.194	9.965	23.395	96.273	6.116	41.249	0.196
0.792	0.955	177.018	10.533	23.395	95.875	5.770	41.249	0.196
0.806	0.960	176.937	11.185	23.395	95.470	5.442	41.249	0.196
0.820	0.965	176.967	11.939	23.395	95.058	5.131	41.249	0.196
0.834	0.970	177.121	12.802	23.395	94.643	4.837	41.249	0.196
0.848	0.975	177.428	13.800	23.395	94.229	4.559	41.249	0.196
0.862	0.981	177.948	15.019	23.295	93.794	4.296	41.249	0.196
0.876	0.987	178.748	16.517	23.395	93.345	4.046	41.249	0.196
0.890	0.992	179.857	18.297	23.395	92.911	3.809	41.249	0.196
0.904	0.998	181.370	20.468	23.395	92.477	3.584	41.249	0.196
0.918	1.005	183.433	23.201	23.395	92.021	3.371	41.249	0.196
0.932	1.011	186.174	26.584	23.395	91.581	3.169	41.249	0.196
0.946	1.017	189.860	30.900	23.395	91.144	2.977	41.249	0.196
0.960	1.024	194.836	36.505	23.395	90.697	2.794	41.249	0.196
0.974	1.030	201.783	44.053	23.395	90.268	2.621	41.249	0.196
0.988	1.038	212.173	55.057	23.395	89.819	2.457	41.249	0.196
1.002	1.046	227.685	71.229	23.395	89.316	2.301	41.249	0.196
1.016	1.053	252.755	96.867	23.395	88.896	2.152	41.249	0.196
1.030	1.063	295.050	139.882	23.395	88.317	2.011	41.249	0.196
1.044	1.072	374.710	220.196	23.395	87.797	1.878	41.249	0.196
1.058	1.082	530.635	376.814	23.395	87.232	1.750	41.249	0.196
1.072	1.089	848.631	695.390	23.395	86.771	1.630	41.249	0.196
1.086	1.096	1923.679	1770.932	23.395	86.392	1.515	41.249	0.196

NOTE: Even though a value of cell voltage equal to 0.806 volt gives the minimum system weight, it cannot be used because of its failure to meet the voltage regulation limits of 28 ± 2 volts. Cell voltage equal to 0.867 volt will meet the voltage regulation limits. The purpose of the output on this page is to indicate the possibility of weight reduction by relaxing the voltage regulation limits.

FIGURE 6

FUEL CELL SUBSYSTEM DESIGN BASED ON 1. ACTIVE MODULES AND 0. REDUNDANT MODULES.

FUEL CELL SUBSYSTEM RELIABILITY ESTIMATE = 1.00000

MODULE WEIGHT = 38.899

MODULE PARASITIC POWER = 0.

MODULE OPERATING CHARACTERISTICS

T	P	PFC	VMOD	I//	I	PW	WH2	WO2	PMOD
1.000		1625.000	26.000	356.756	62.500	1173.508	0.155	1.232	1625.000
2.630		998.512	27.804	204.995	35.913	609.533	0.089	0.708	998.512
4.370		951.919	27.948	194.424	34.061	573.199	0.084	0.671	951.919
48.000		568.039	29.234	110.913	19.431	301.995	0.048	0.383	568.039
44.000		500.000	29.487	96.791	16.957	259.256	0.042	0.334	500.000
SUM T		SUM PFC*T				SUM PW*T	SUM WH*T	SUM WO*T	
100.000		57676.876				31184.508	4.920	39.117	

FIGURE 6

PERCENTAGE WEIGHT SAVING VERSUS DISCHARGE TIME

For Ideal Set of Conditions

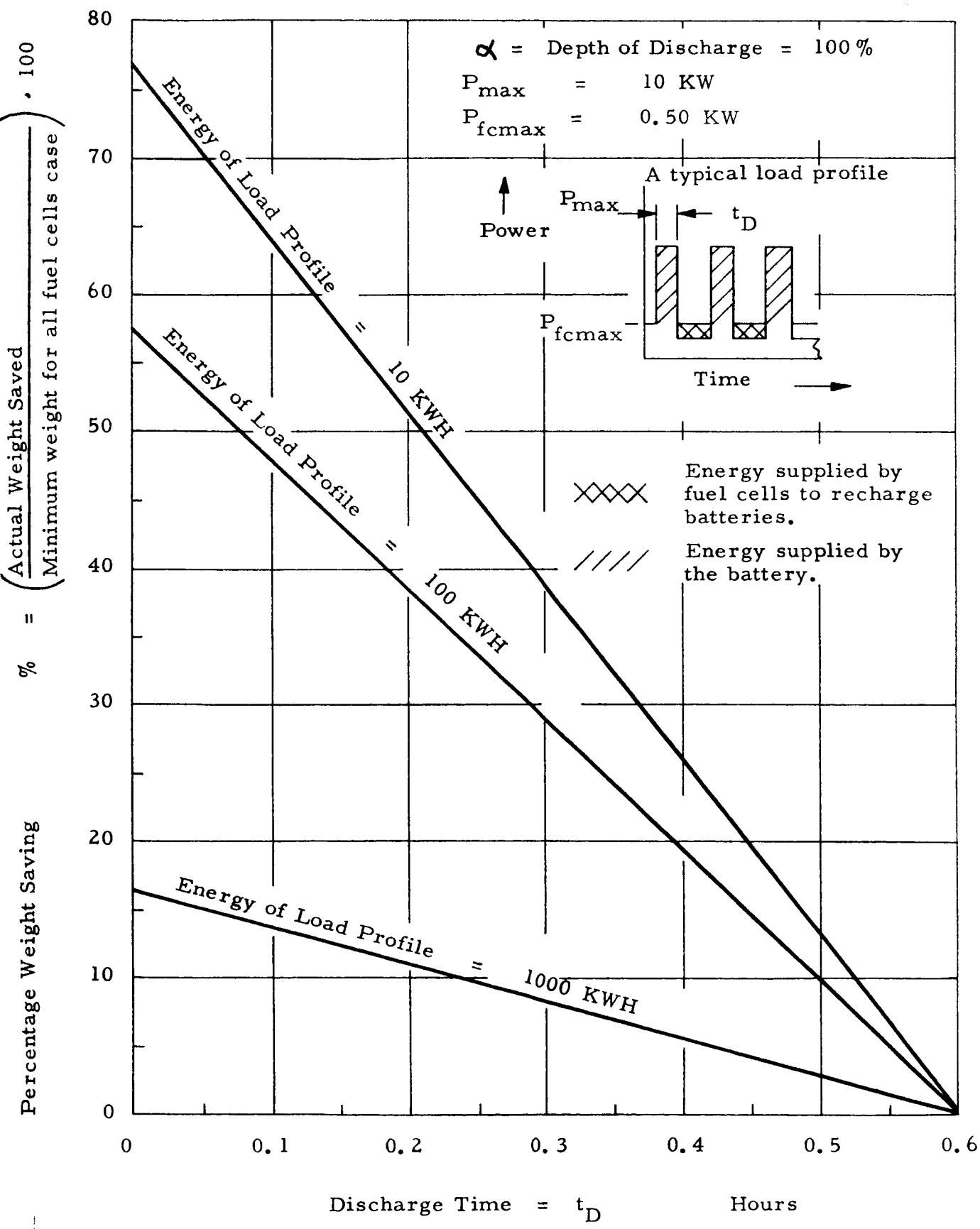


FIGURE 7

PERCENTAGE WEIGHT SAVING VERSUS DISCHARGE TIME

Percentage Weight Saving = { Minimum weight for all fuel cells case /

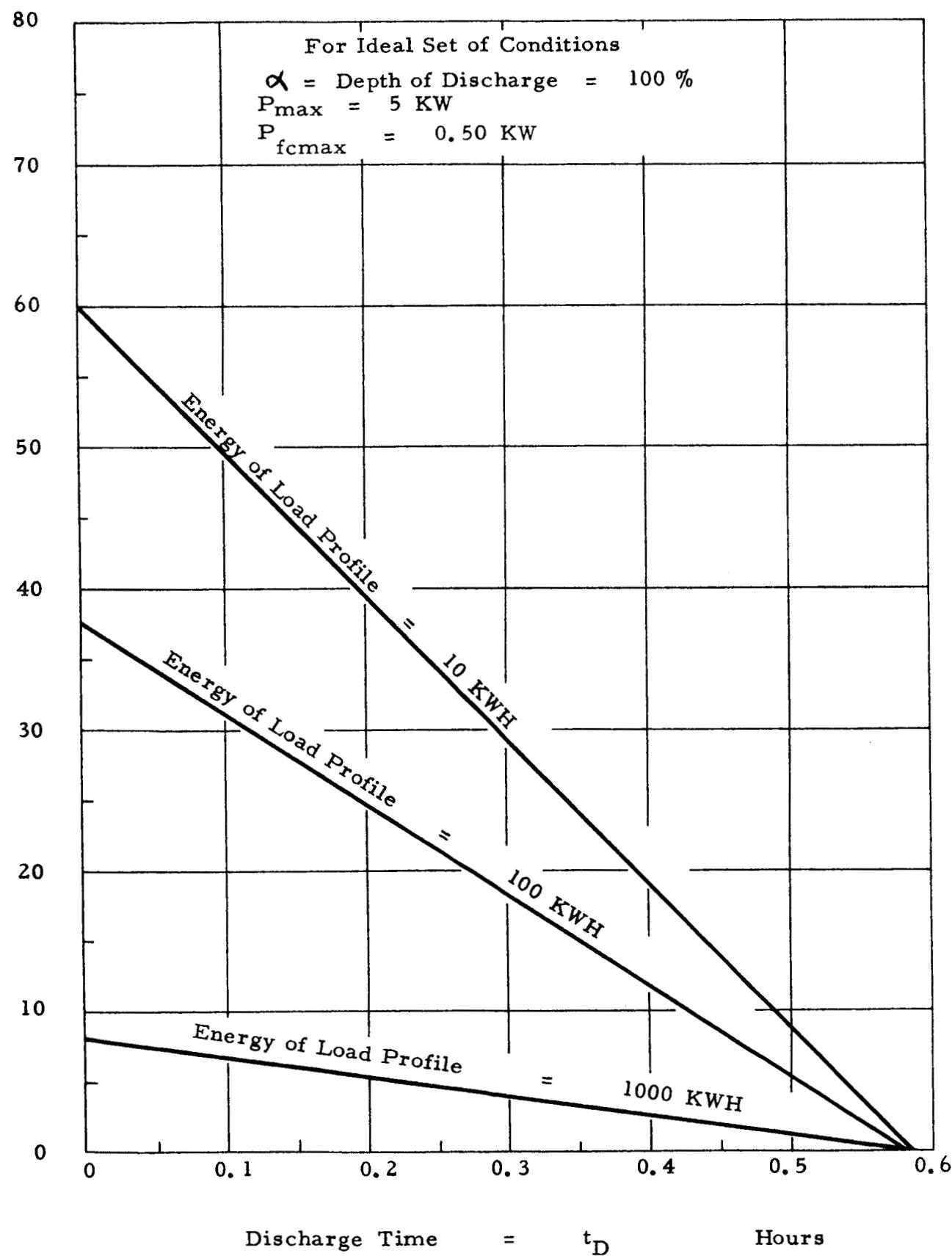


FIGURE 8

PERCENTAGE WEIGHT SAVING VERSUS DISCHARGE TIME

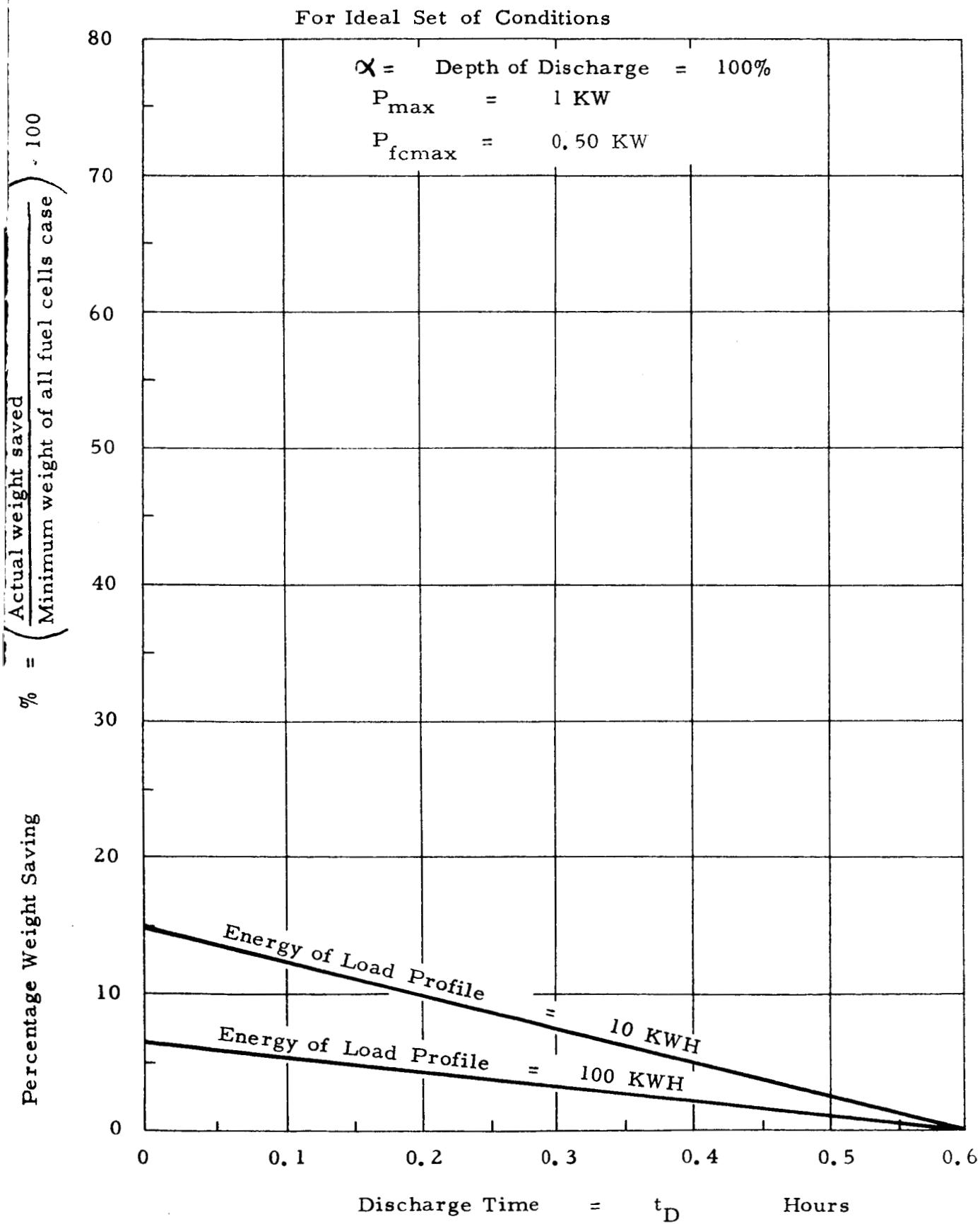


FIGURE 9