

**2016 Fall**

# **“Phase Transformation *in* Materials”**

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Contents for previous class

## Chapter 3 Crystal Interfaces and Microstructure

### 1) Interfacial Free Energy ( $\gamma$ : J/m<sup>2</sup>)

→ The Gibbs free energy of a system containing an interface of area A

→  $G_{\text{bulk}} + G_{\text{interface}}$  vapor  
solid  $G = G_0 + \gamma A$  →  $F = \gamma + A d\gamma/dA$  (liq. :  $d\gamma/dA = 0$ )

\* Origin of the **surface free energy ( $E_{sv}$ )**? → **Broken Bonds**

### 2) Solid/Vapor Interfaces

$high T_m \rightarrow high L_s \rightarrow high \gamma_{sv}$

\*  $\gamma$  interfacial energy = free energy (J/m<sup>2</sup>)      $\gamma$ - $\theta$  plot

→  $\gamma = G = H - TS$

$= E + PV - TS$  (: PV is ignored)

→  $\gamma = E_{sv} - TS_{sv}$  ( $S_{sv}$  thermal entropy, configurational entropy)

→  $\partial\gamma/\partial T = -S$  : **surface energy decreases with increasing T**

Equilibrium shape: Wulff surface

$\sum_{i=1}^n A_i \gamma_j = \text{Minimum}$

$E_{sv} = 3 \epsilon/2 = 0.25 L_s / N_a$       $\Rightarrow$       $\gamma_{sv} = 0.15 L_s / N_a$      J / surface atom     2

(∵ surface free Es averaged over many surface plane, S effect at high T)

## Contents for previous class

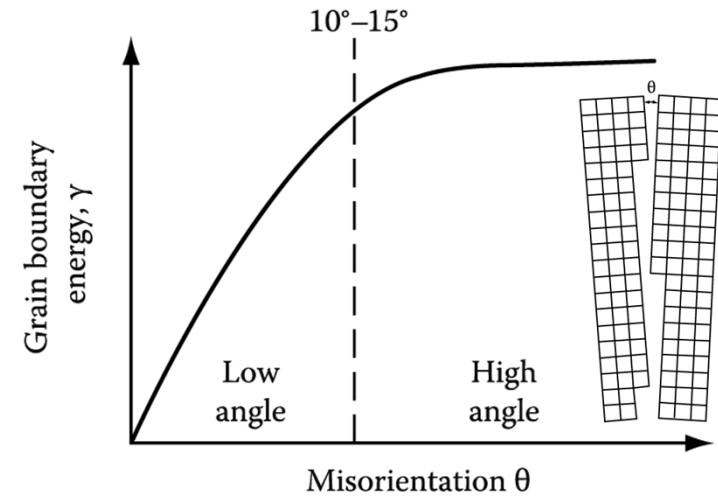
### 3) Boundaries in Single-Phase Solids

#### (a) Low-Angle and High-Angle Boundaries

$\Theta < 15^\circ$  : total energy of the dislocations within unit area of boundary

$\Theta > 15^\circ$  : impossible to physically identify the individual dislocations  $\rightarrow$  strain field overlap  $\rightarrow$  cancel out

Broken Bonds  $\rightarrow$  high angle  $\gamma_{g.b.} \approx 1/3 \gamma_{S/V}$ .



# **Q: Grain boundary ( $\alpha/ \alpha$ interfaces)**

**= Boundaries in Single-Phase Solids**

**(a) Low-Angle and High-Angle Boundaries**

**(b) Special High-Angle Grain Boundaries**

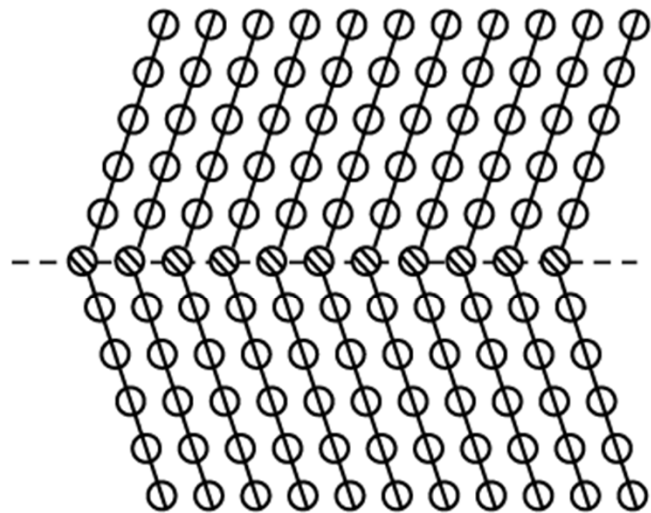
**(c) Equilibrium in Polycrystalline Materials**

# Boundaries in Single-Phase Solids

## (a) Low-Angle and High-Angle Boundaries

### (b) Special High-Angle Grain Boundaries I

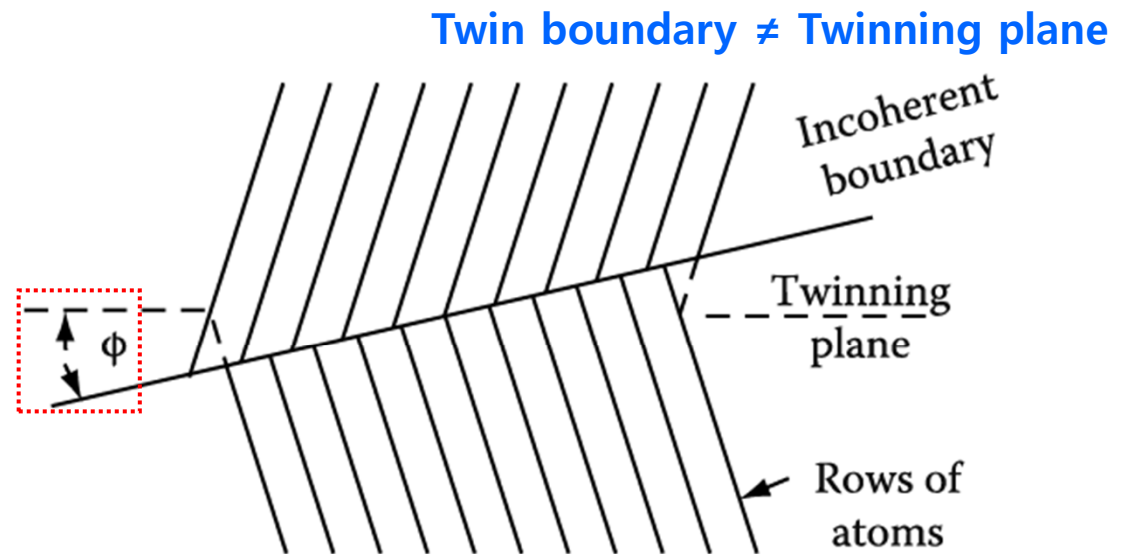
: high angle boundary but with low  $\gamma_{g.b.}$



a) **Coherent twin boundary**  
symmetric twin boundary

→ low  $\gamma_{g.b.}$

Atoms in the boundary  
are essentially in  
undistorted positions



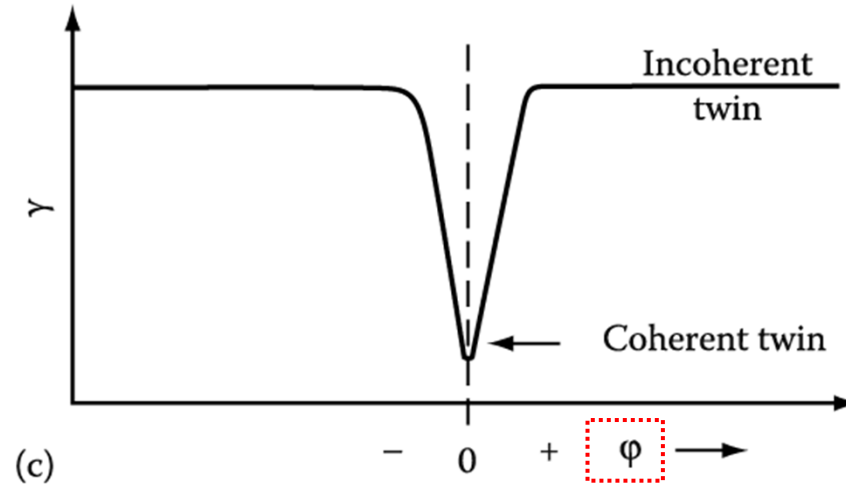
b) **Incoherent twin boundary**  
asymmetric twin boundary

→ low  $\gamma_{g.b.}$

Energy of twin boundary~  
very sensitive to the orienta-  
tion  $\phi$  of the boundary plane

## (b) Special High-Angle Grain Boundaries I

c) Twin boundary energy as a function of the grain boundary orientation



**Table 3.3 Measured Boundary Free Energies for Crystals in Twin Relationships**  
(Units  $\text{mJ/m}^2$ )

Crystal	Coherent Twin-Boundary Energy	Incoherent Twin-Boundary Energy	Grain-Boundary Energy
Cu	21	498	623
Ag	8	<<	377
Fe-Cr-Ni (stainless steel type 304)	19	209	835

## (b) Special High-Angle Grain Boundaries II

Two grains ~ a rotation about a (100) axis < a rotation about a (110) axis

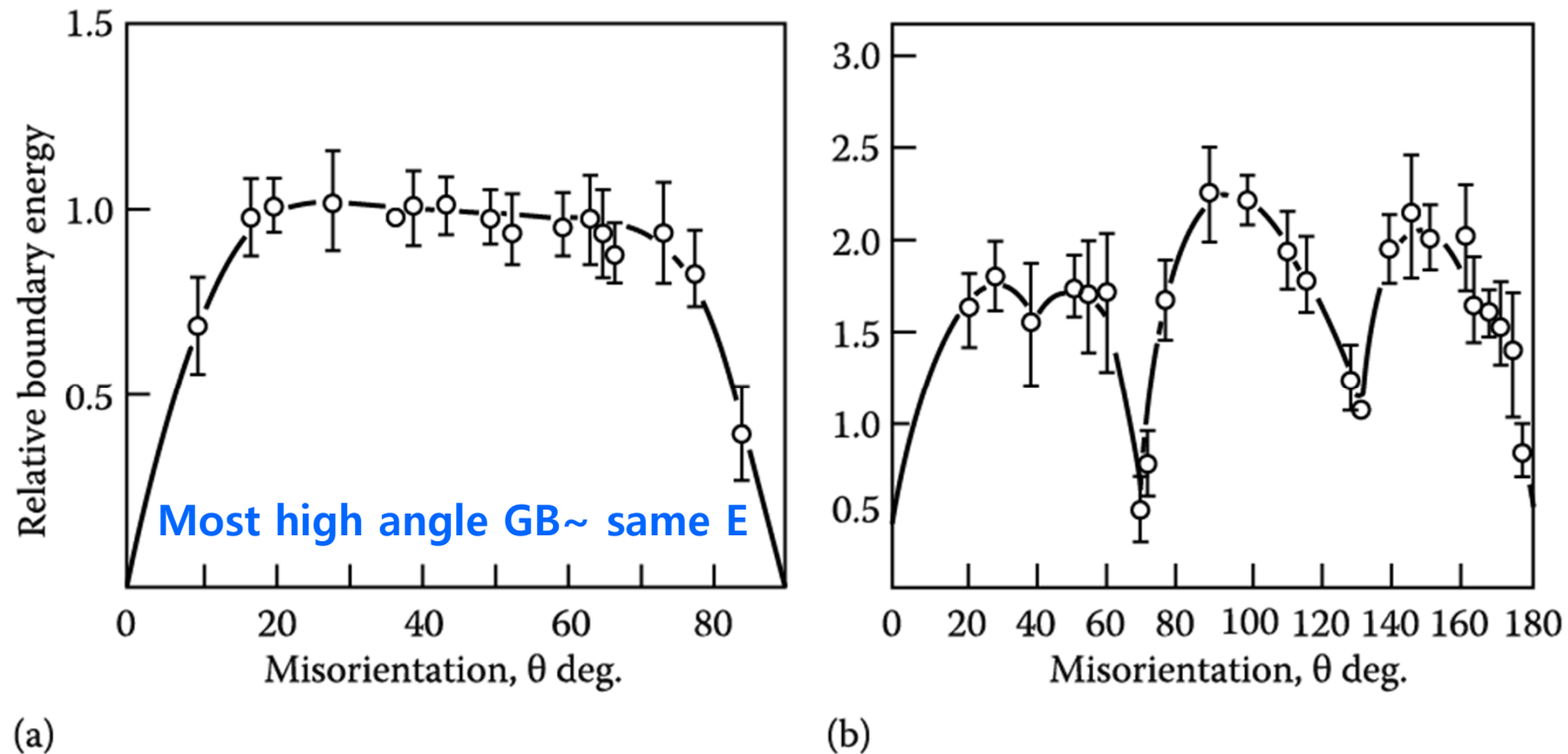


Fig. 3.13 Measured grain boundary energies for symmetric tilt boundaries in Al (a) When the rotation axis is parallel to (100), (b) when the rotation axis is parallel to (110).

### Why are there cusps in Fig. 3.13 (b)?

In FCC metal, several large-angle orientations with significantly lower energies than the random boundaries.

$\phi = 70.5^\circ$  ~ coherent twin boundary (next page), others ~ not well understood

- symmetrical tilt boundary  
~38.2 °
- a small group of atoms are repeated regular intervals along the boundary.  
~relatively little free volume

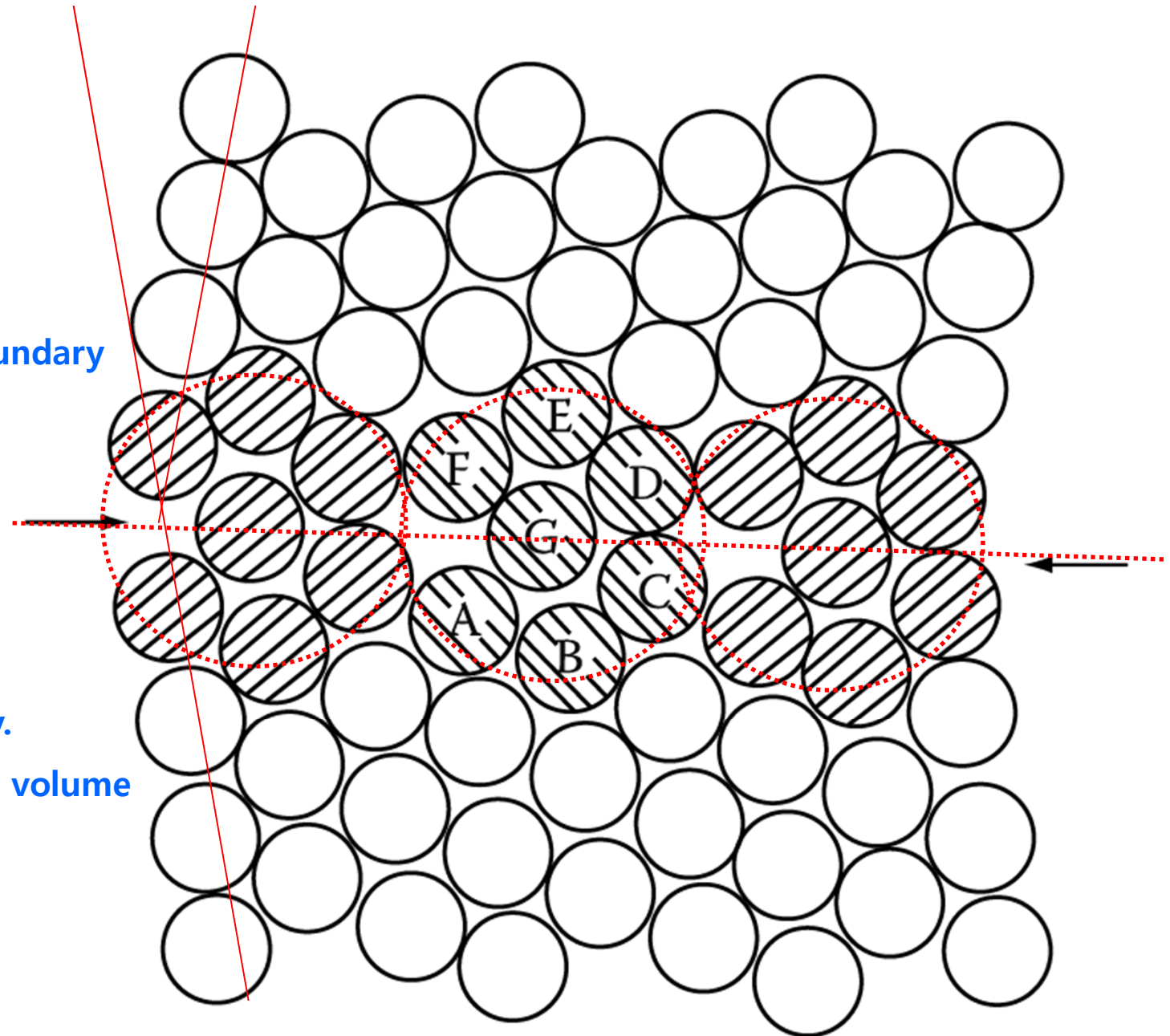


Fig. 3. 14 Special grain boundary: two dimensional example.

입계의 원자구조가 주위의 격자와 폭넓게 잘 일치 됨



# Contents for previous class

## 3) Boundaries in Single-Phase Solids

### (a) Low-Angle and High-Angle Boundaries

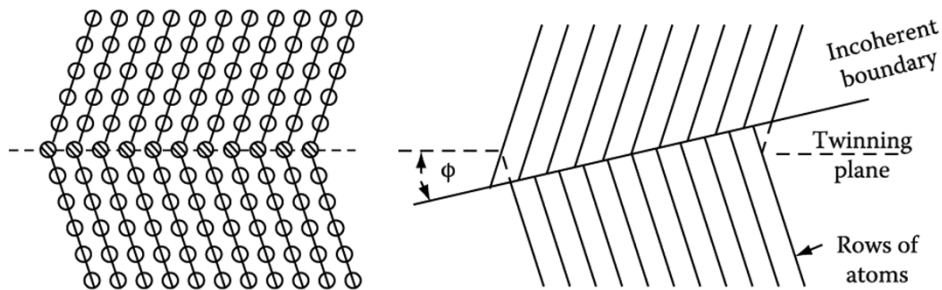
$\Theta < 15^\circ$  : total energy of the dislocations within unit area of boundary

$\Theta > 15^\circ$  : impossible to physically identify the individual dislocations  $\rightarrow$  strain field overlap  $\rightarrow$  cancel out

Broken Bonds  $\rightarrow$  high angle  $\gamma_{g.b.} \approx 1/3 \gamma_{S/V}$ .

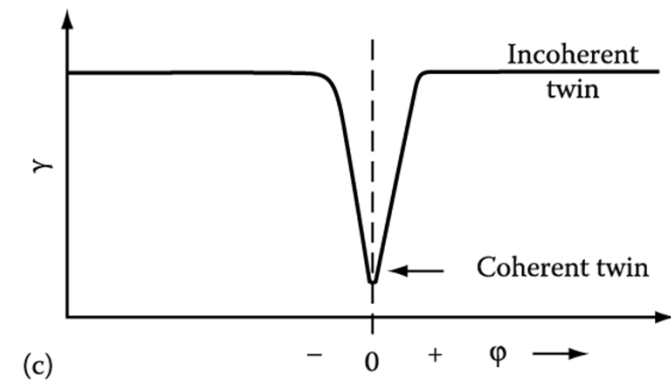
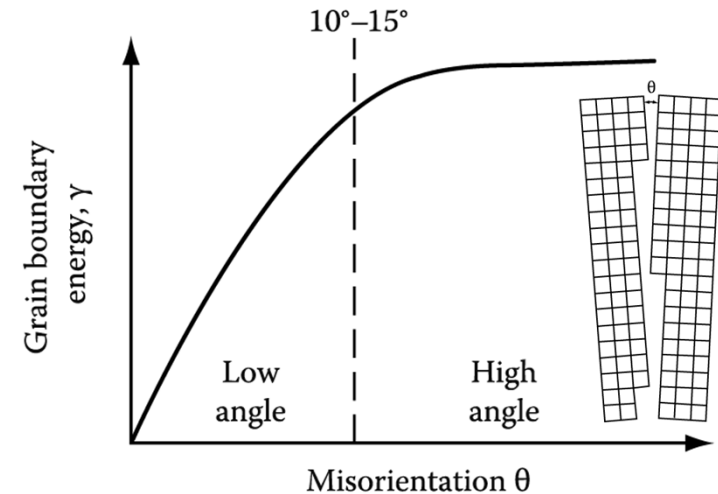
### (b) Special High-Angle Grain Boundaries

: high angle boundary but with low  $\gamma_{g.b.}$



$\rightarrow$  twin boundary

Atoms in the boundary are essentially in undistorted positions  $\sim$ relatively little free volume



# Contents for today's class

< Boundaries in Single-Phase Solids >

## (c) Equilibrium in Polycrystalline Materials

### 1) GB intersection: Balance of 1) boundary E & 2) surface tension

GBs in a polycrystal can adjust themselves during annealing to produce a metastable equilibrium at the GB intersections.

### 2) Thermally Activated Migration of Grain Boundaries

- Grain coarsening at high T, annealing due to metastable equilibrium of GB

### 3) Kinetics of Grain Growth

- Grain boundary migration by thermally activated atomic jump

- Mobility of GB ~ GB structures and GB segregations

i.e Normal grain growth  $\longleftrightarrow$  Abnormal grain growth

### 4) Effect of second-phase particle on GB migration: Zener Pinning

$$\bar{D}_{\max} = \frac{4r}{3f_v}$$

# Q: Grain boundary ( $\alpha/\alpha$ interfaces)

= Boundaries in Single-Phase Solids

(a) Low-Angle and High-Angle Boundaries

(b) Special High-Angle Grain Boundaries

(c) Equilibrium in Polycrystalline Materials

**1) GB intersection: Balance of 1) boundary E & 2) surface tension**

**GBs in a polycrystal can adjust themselves during annealing to produce a metastable equilibrium at the GB intersections.**

### (c) Equilibrium in Polycrystalline Materials

Microstructure → determined by how the different GBs join together in space

⇒ Examine how the possibility of different GB energies affects the microstructure of a poly crystalline material

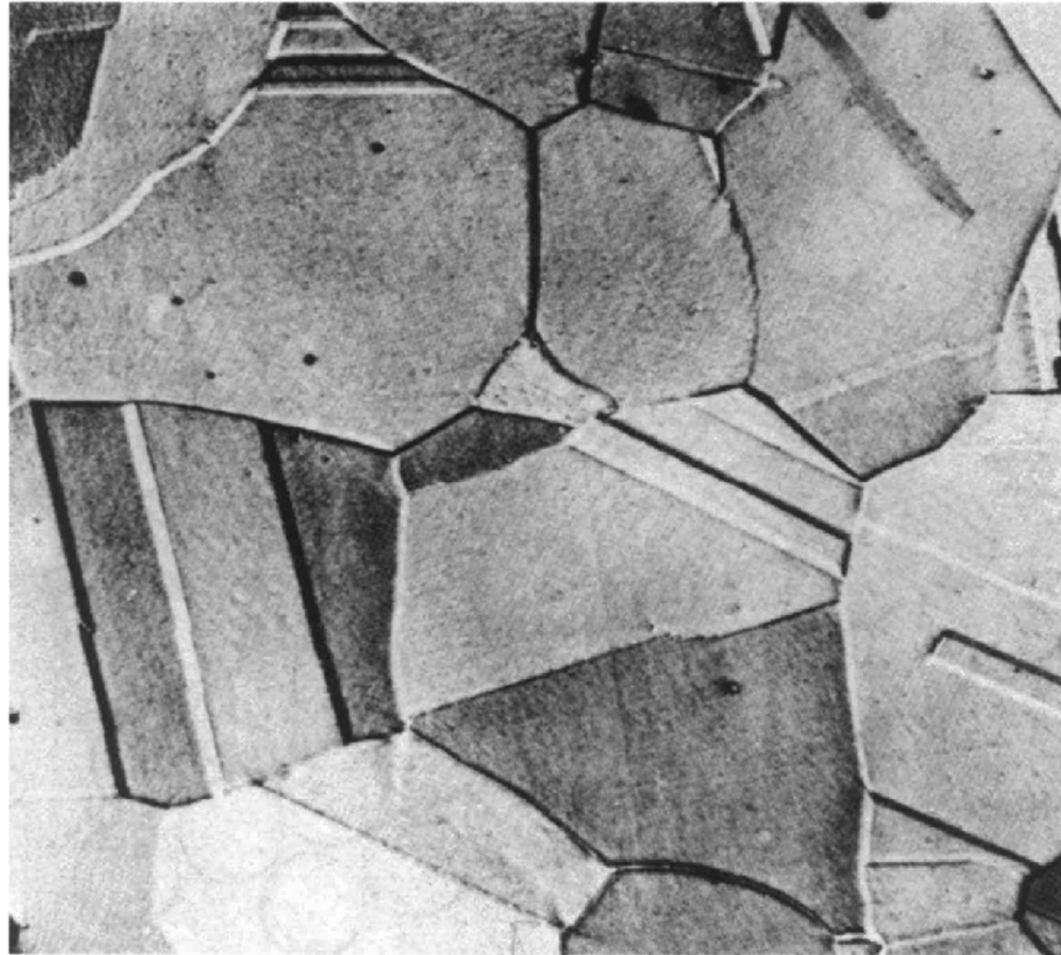
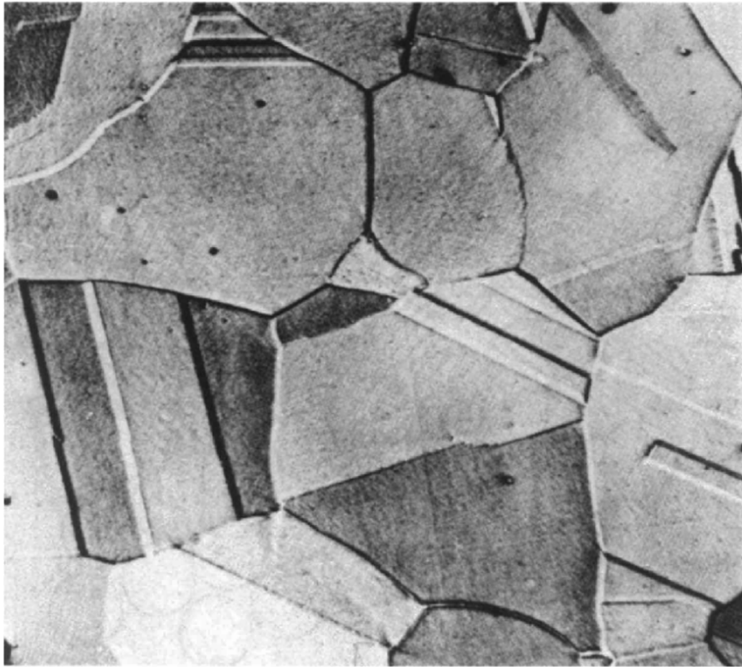


Fig. 3.15 Microstructure of an annealed crystal of austenitic stainless steel. 12  
: contains high-/low-angle GBs as well as (in-)coherent twin Bs with different GB energies

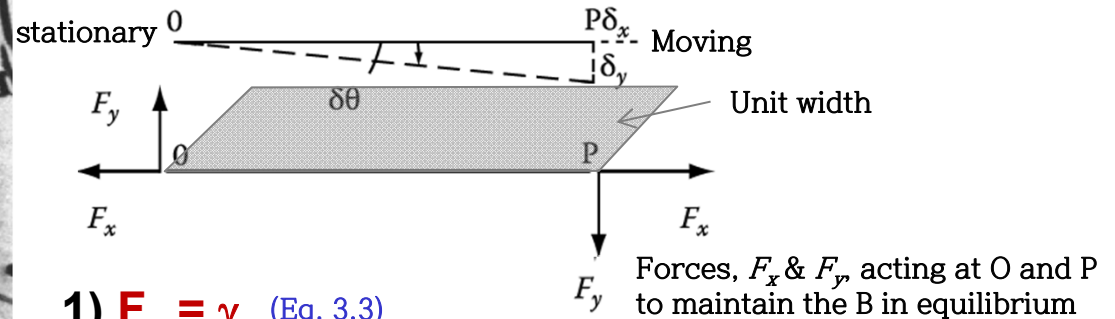
# Poly grain material: consider the factors that control the grain shapes!

Two grains: a plane (GB), three grains: a line (grain edge), four grains: at a point (grain corner)



## 2) Conditions for equilibrium at a GB junction

by considering the forces that each B exerts on the junction



1)  $F_x = \gamma$  (Eq. 3.3)

2)  $F_y$  ?

**P is moved at a small distance ( $\delta_y$ )**

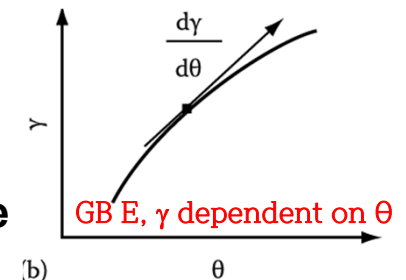
A. work done by :  $F_y \delta_y$

B. increase boundary energy caused

by the change in orientation  $\delta\theta \sim l (d\gamma/d\theta) \delta\theta$

$F_y \delta_y = l (d\gamma/d\theta) \delta\theta (\because \delta_y \sim l d\theta)$

$\rightarrow$   $F_y = d\gamma/d\theta$  torque force



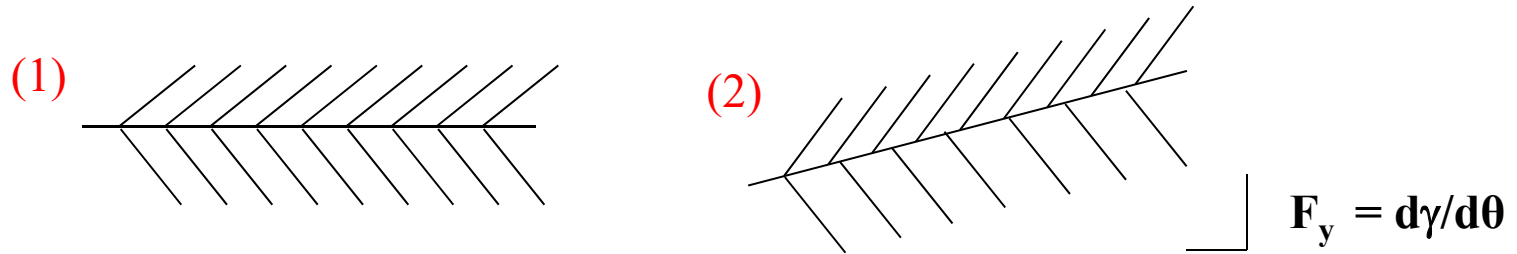
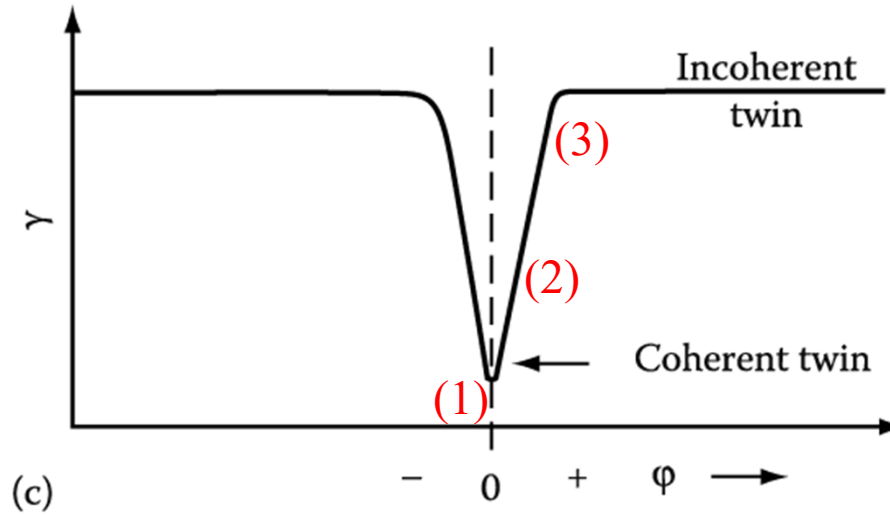
1) Why GBs exist at all in annealed materials?

Equilibrium ~ Mater. with no GB

$\because$  G.B.=high-E regions  $\rightarrow G \uparrow$

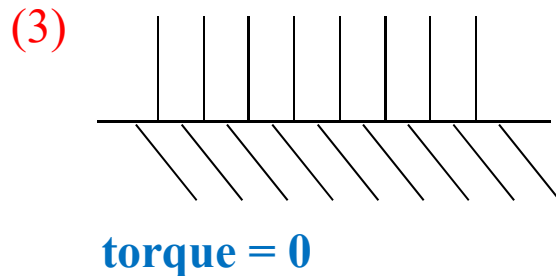
: never a true equilibrium structure

$\rightarrow$  GBs in a polycrystal can adjust themselves during annealing to produce a metastable equilibrium at the GB intersections.



Minimum  $\gamma \sim \text{torque} = 0$  No rotation!

If Pulling force,  $F_y > (d\gamma/d\theta)_{\text{cusp}} \rightarrow \text{Rotating}$



$\rightarrow$  There is little effect of orientation

$F_y = d\gamma/d\theta \sim \text{torque} > 0$

If the GB E is dependent on the orientation of the B, a force  $d\gamma/d\theta (>0)$  must be applied to the ends of the boundary to prevent it rotating into a lower energy orientation.

입계 E가 입계 방위에 의존한다면, 회전하지 않고 유지하기 위해 입계에 cusp까지 끌어당기는 힘에 대응하는 힘 작용

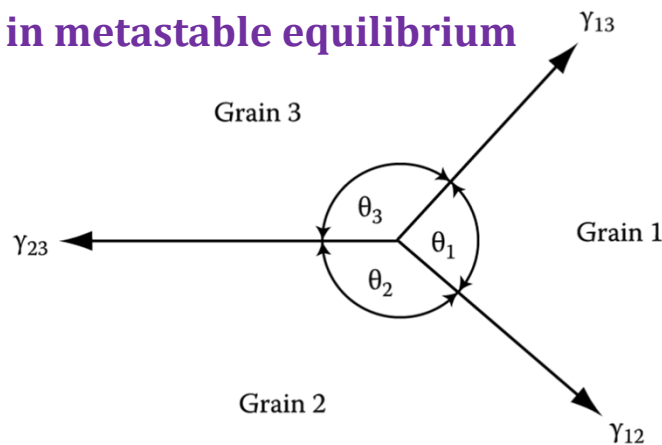
$\Rightarrow$  How metastable equilibrium?  $\rightarrow$  force (torque)

If the boundary E is independent of orientation,

\* **General high angle boundary** :  $d\gamma/d\theta \approx 0$  (GB behaves like a soap film)

→ Under these conditions the requirements for metastable equilibrium at junction between three grains is that the boundary tensions  $\gamma_{13}, \gamma_{23}, \gamma_{12}$  must balance.

**3) The balance of GB tensions for a GB intersection in metastable equilibrium**



$$\frac{\gamma_{23}}{\sin \theta_1} = \frac{\gamma_{31}}{\sin \theta_2} = \frac{\gamma_{12}}{\sin \theta_3} \quad (\text{Eq. 3.13})$$

if all GBs have same GB energy independent of boundary orientation

$$\rightarrow \theta = 120^\circ$$

Eq. 3.13 applies to any three boundaries i.e. grain 1 ~ different phase to grain 2 & 3.

**Ex) If the solid-vapor energy ( $\gamma_{sv}$ ) is the same for both grains,**

$$2\gamma_{sv} \cos \frac{\theta}{2} = \gamma_b$$

**(Here, presence of any torque terms ~ neglected)**

**One method of measuring GB energy:**

: anneal a specimen at a high temp. and then measure the angle at the intersection of the surface with B.

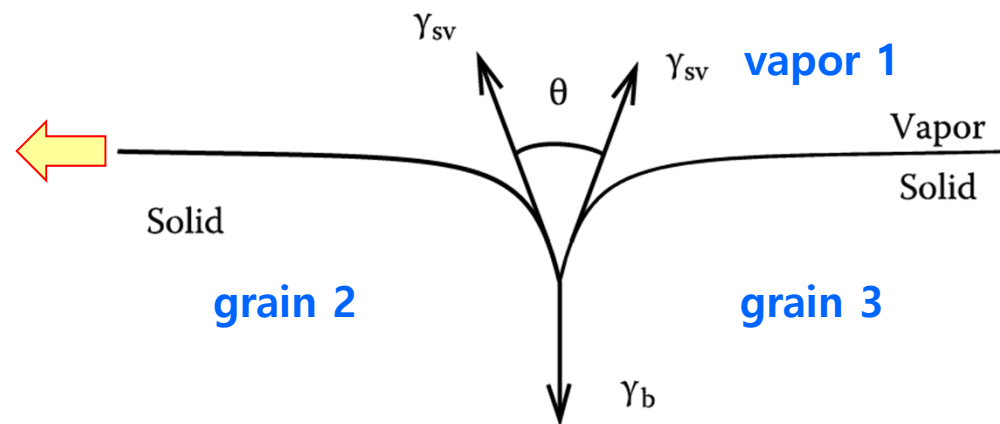


Fig. 3. 18 The balance of surface and grain boundary tensions at the intersection of a grain boundary with a free surface.

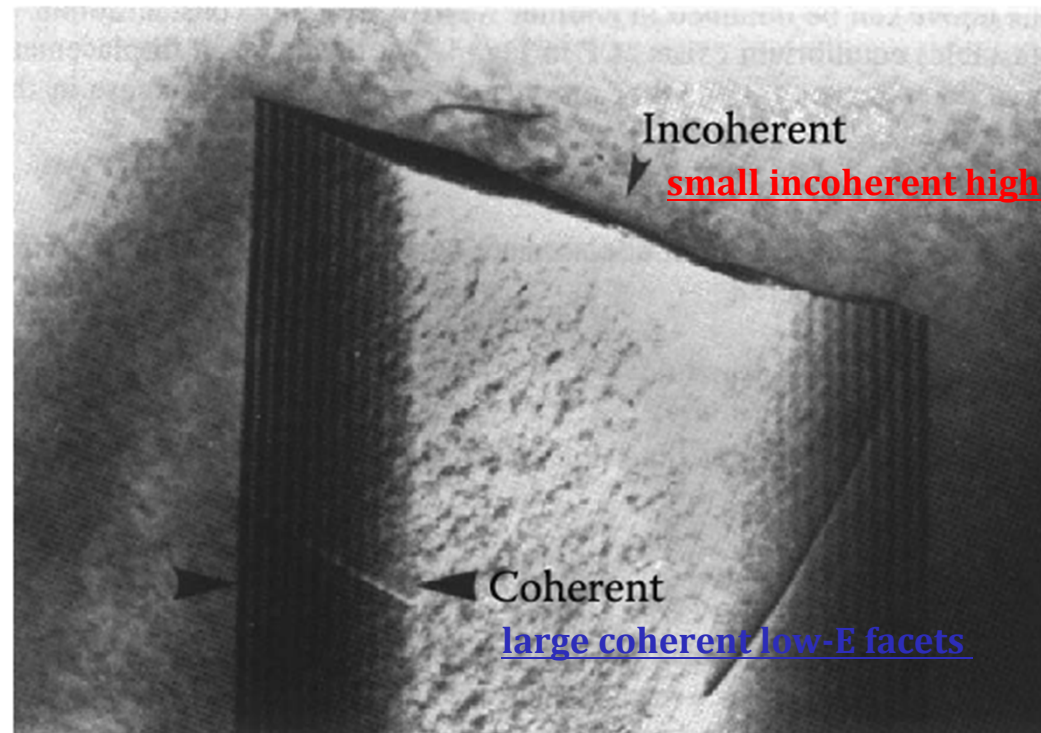
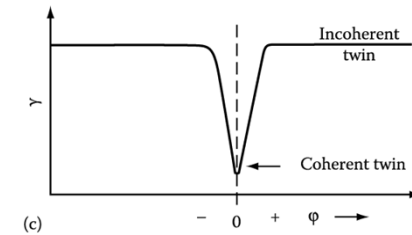
\* **Junction between coherent and incoherent twin boundary segments showing the importance of torque effects**

: the orientation dependence of twin boundary E, Fig. 3.13b

→ It is energetically favorable for twin boundaries to align themselves parallel to the twinning plane.

→ If the boundary is constrained to follow a macroscopic plane that is near but not exactly parallel to the twinning plane the boundary will usually develop a stepped appearance with large coherent low-E facets and small incoherent high-E risers.

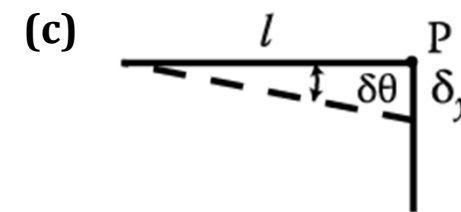
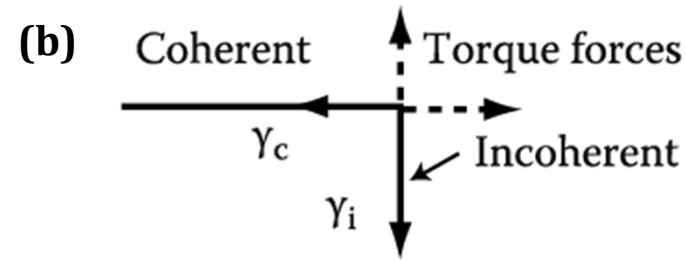
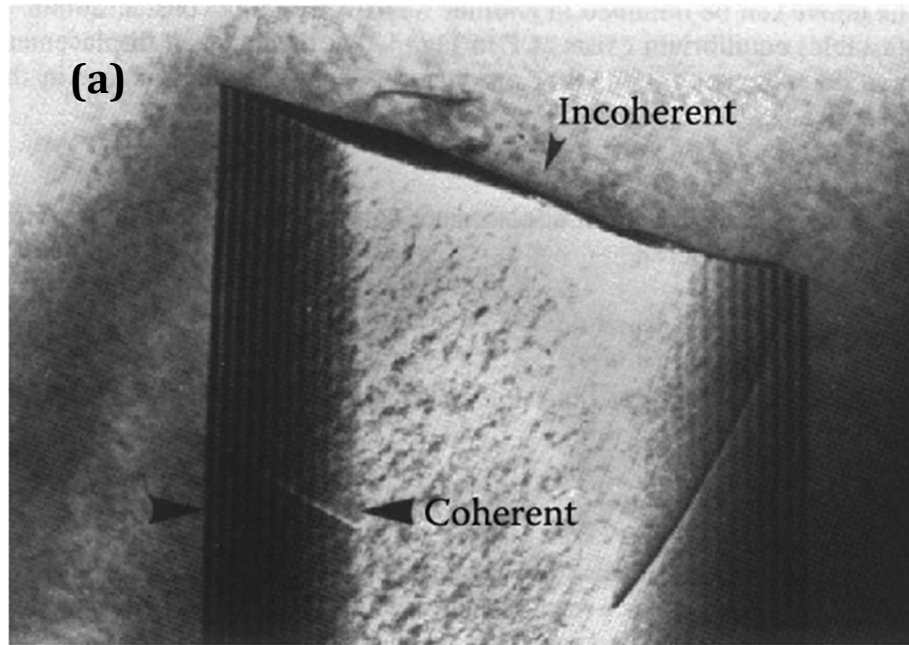
→ does not minimize the total twin boundary E but minimize the total free E



(a) twin boundary in a thin foil specimen as imaged in the TEM



**\* Junction between coherent and incoherent twin boundary segments showing the importance of torque effects**



(a) twin B in a thin foil specimen as imaged in the TEM, (b) & (c), the coherent and incoherent segments of the twin B.

At the coherent/incoherent twin junction as shown in (b),

incoherent twin B tension,  $\gamma_i$  must be balanced by a torque term

$$\gamma_i \leq d\gamma_c/d\theta$$

Likewise, coherent twin B tension,  $\gamma_c$  must be balanced by a torque term

$$\gamma_c \leq d\gamma_i/d\theta$$

However, since  $\gamma_c$  is usually very small, the incoherent interface need only lie in a rather shallow energy cusp.

From energy consideration,

if (metastable) equilibrium exists at P in Fig. (c), then a small displacement such as that shown should either produce no change or an increase in the total free energy of the system, i.e.  $dG > 0$

considering unit depth a small displacement  $\delta y$  at P will increase the total free E by an amount

$$dG = l (d\gamma_c/d\theta) \delta\theta - \gamma_i \delta y > 0 \quad (\because \delta y \sim l d\theta) \quad \Rightarrow \quad \gamma_i \leq d\gamma_c/d\theta$$

# Q: Grain boundary ( $\alpha/\alpha$ interfaces) = Boundaries in Single-Phase Solids

(a) Low-Angle and High-Angle Boundaries

(b) Special High-Angle Grain Boundaries

(c) Equilibrium in Polycrystalline Materials

## 2) Thermally Activated Migration of Grain Boundaries

: Grain coarsening at high T, annealing due to metastable equilibrium of GB

## Considering factors of G.B. growth

**(a) Pinning particle**

**(b) 2<sup>nd</sup> phases**

**(c) Anisotropic  $\sigma$ , M**

**(d) Impurity (solute) drag**

**(e) Strain energy**

**(f) Free surface**

## GB intersection: Balance of 1) boundary E & 2) surface tension

### 3.3.4. Thermally Activated Migration of Grain Boundaries

If the boundary is curved in the shape of cylinder, Fig. 3.20a, it is acted on by a force of magnitude  $\gamma/r$  towards its center of curvature.

Therefore, the only way the boundary tension forces can balance in three dimensions is if the boundary is planar ( $r = \infty$ ) or if it is curved with equal radii in opposite directions, Fig. 3.20b and c.

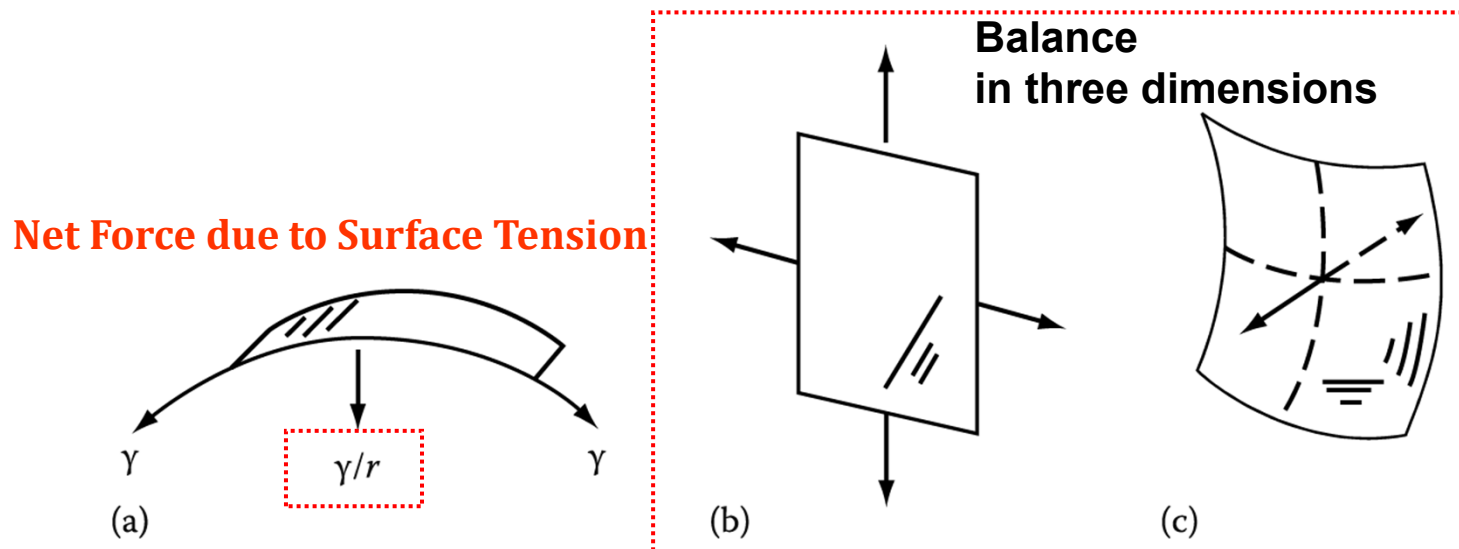


Fig. 3. 20 (a) A cylindrical boundary with a radius of curvature  $r$  is acted on by a force  $\gamma/r$ . (b) A planar boundary with no net force. (c) A doubly curved boundary with no net force.

A random grain structure is inherently unstable and, on annealing at high temperatures, the unbalanced forces will cause the boundaries to migrate towards their centers of curvature.

## a) Direction of Grain Boundary Migration during Grain Growth

For isotropic grain boundary energy in **two dimensions**,

Equilibrium angle at each boundary junction? → **120°** **3 boundaries intersections**

Equilibrium angle at each boundary junction in 3D? → **109°28'** **A corner formed by 4 grains**

**Morphology of metastable equilibrium state** → **Migration during annealing**

Effect of different boundary curvatures in two dimensions

**Boundaries** around Grain  $< 6$   
; **grain shrink, disappear**

**Boundaries** around Grain  $= 6$   
; **equilibrium**

**Boundaries** around Grain  $> 6$   
; **grain growth**

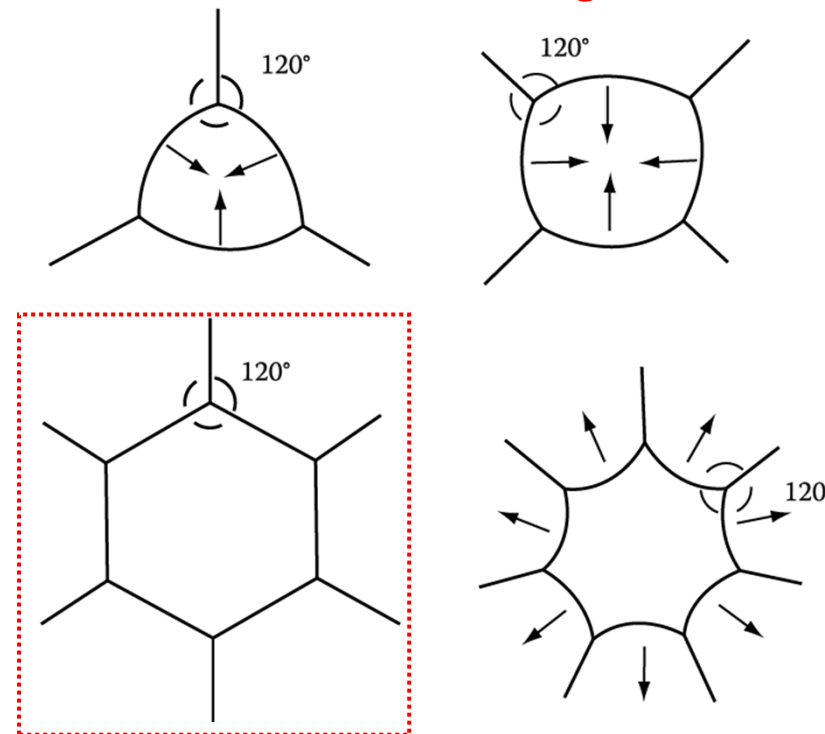


Fig. 3. 21 Two-dimensional GB configurations, The arrows indicate the directions boundaries will migrate during grain growth.

⇒ **Reduce the # of grains, increase the mean grain size, reducing the total G.B. energy called **grain growth (or grain coarsening)**: at high temperature above about  $0.5 T_m$**

## Grain Growth (Soap Bubble Model)

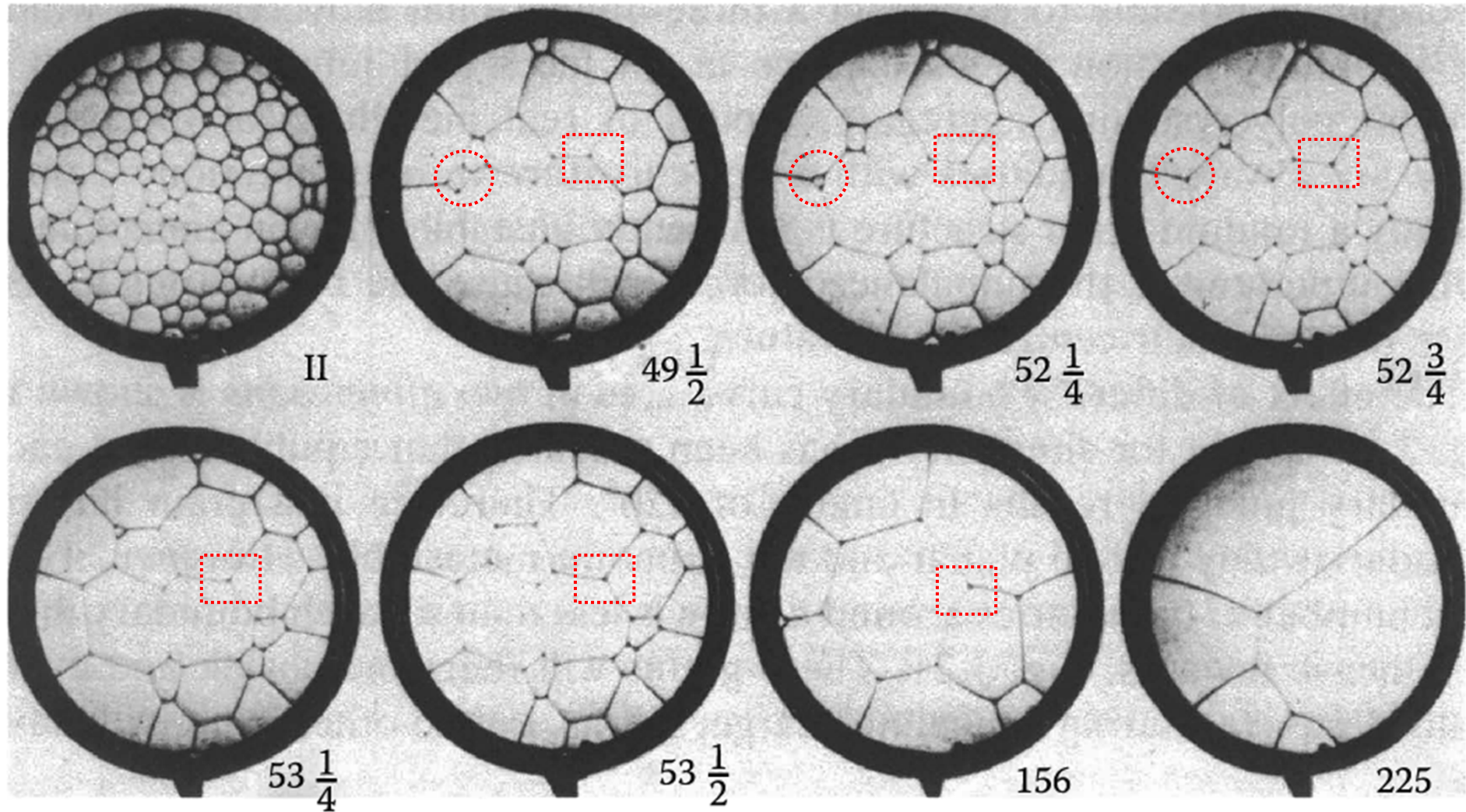
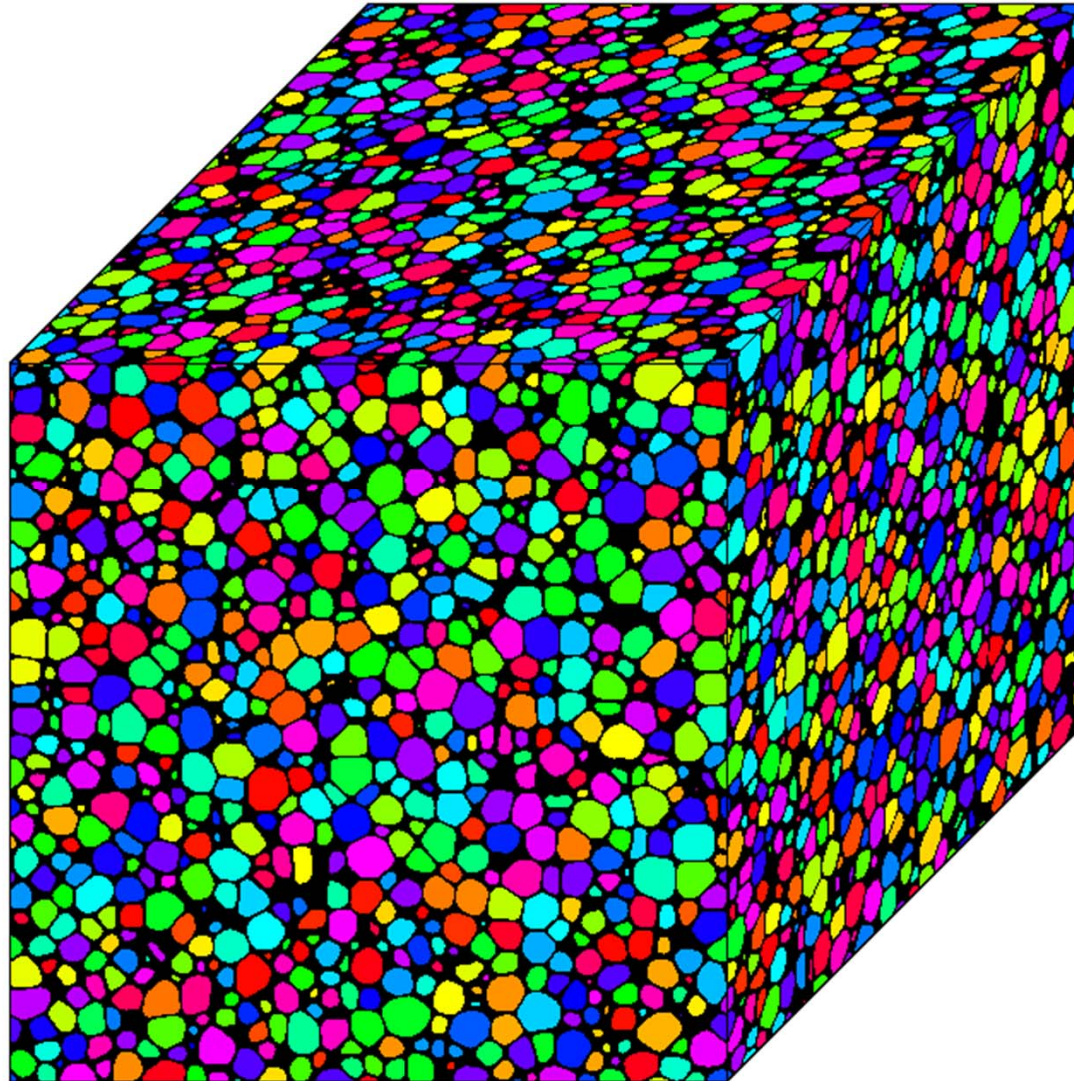


Fig. 3.22 Two-dimensional cells of a soap solution illustration the process of grain growth. Numbers are time in minutes.

## Example of Grain Growth simulation in 3D



**b) Grain Coarsening at High Temp. annealing (above about  $0.5 T_m$ ):**

The atoms in the shrinking grain detach themselves from the lattice on the high pressure side of the boundary and relocate themselves on a lattice site of the growing grain.

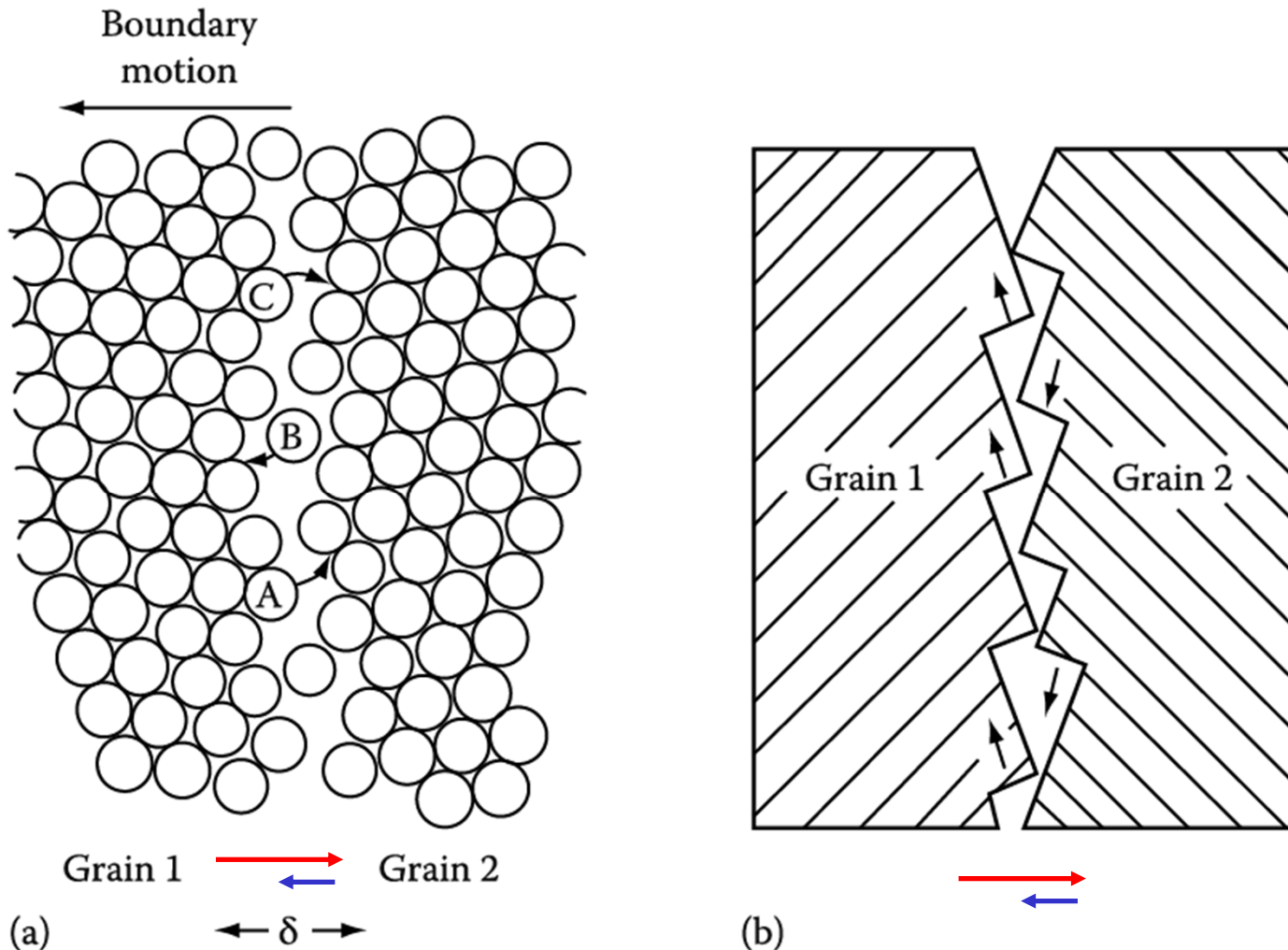


Fig. 3. 23 (a) The atomic mechanism of boundary migration. The boundary migrates to the left if the jump rate from grain 1  $\rightarrow$  2 is greater than 2  $\rightarrow$  1. Note that the free volume within the boundary has been exaggerated for clarity. (b) Step-like structure (돌출맥 구조) where close-packed planes protrude into the boundary.



\* Grain coarsening at high T annealing curvature  $\sim \Delta P \sim \Delta\mu$

→ metastable equilibrium state

: # ↓ , size ↑

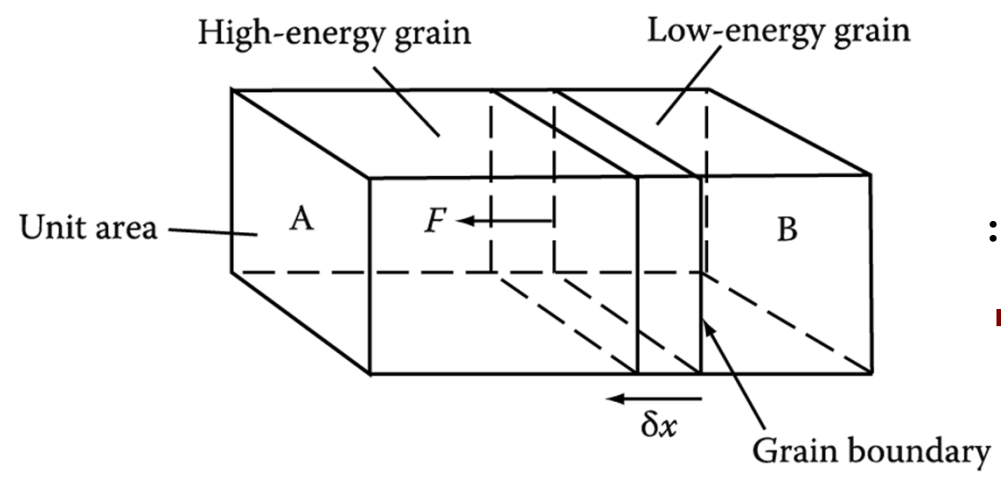
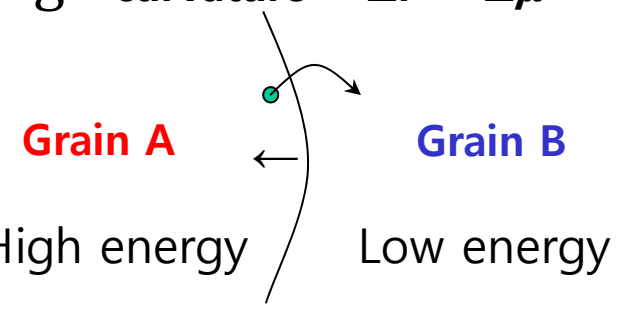


Fig. 3.25 A boundary separating grains with different free energies is subjected to a pulling force  $F$ .



$\Delta G = 2\gamma V_m / r \sim \Delta\mu$  **Gibbs-Thomson Eq.**  
 : effect of pressure difference by curved boundary

➔ **Driving force for grain growth : F**

If unit area of GB advances a distance  $\delta x$ , # of moles of material that enter **grain B**

$$\delta x \cdot (1/V_m)$$

**Work :**  $F dx = (2\gamma V_m / r) (\delta x / V_m)$

→  $F = 2\gamma / r = \Delta G / V_m$  (by curvature)

**1) Pulling force per unit area of boundary :**  $F = \frac{\Delta G}{V_m}$  ( $N m^{-2}$ ) (Eq. 3.18)

Applies equally to any boundary whose migration causes a decrease in free energy, i.e. during recrystallization, the boundaries btw the new strain-free grains and the original deformed grains

Free energy difference per unit volume

# Q: Grain boundary ( $\alpha/\alpha$ interfaces)

(a) Low-Angle and High-Angle Boundaries

(b) Special High-Angle Grain Boundaries

(c) Equilibrium in Polycrystalline Materials

## 3) Kinetics of grain growth

- Grain boundary migration ( $v$ ) by thermally activated atomic jump

Boundary velocity  $v = \frac{A_2 n_1 v_1 V_m^2}{N_a RT} \exp\left(-\frac{\Delta G^a}{RT}\right) \frac{\Delta G}{V_m}$   $v \sim \Delta G/V_m$  driving force  
 $\rightarrow F = \Delta G/V_m$

$M$  : mobility = velocity under unit driving force  $\sim \exp(-1/T)$

rate of grain growth  $dD/dt \sim 1/D$ , exponentially increase with  $T$

$\rightarrow \underline{D} = k't^n$  ( Experimental:  $n \ll 1/2$ ,  $1/2$  at pure metals or high Temp.)

- Mobility of GB  $\sim$  affected by both type of boundaries and GB segregation or 2<sup>nd</sup> phase precipitation

i.e Normal grain growth  $\longleftrightarrow$  Abnormal grain growth

## 2) How fast boundary moves? : Grain Growth Kinetics

Effect of the driving force on the kinetics of boundary migration

### Grain boundary migration by thermally activated atomic jump

\* (1) → (2) : Flux

(1) atoms in probable site :  $n_1$

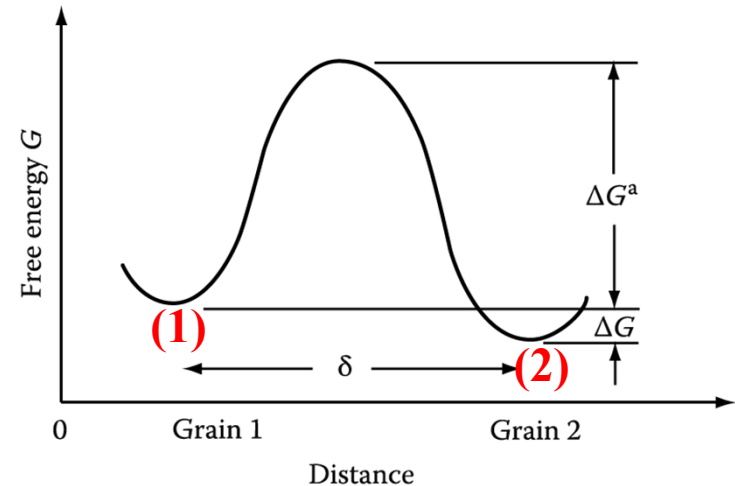
Vibration frequency :  $\nu_1$

$A_2$  : probability of being accommodated in grain (2)

$$\rightarrow A_2 n_1 \nu_1 \exp(-\Delta G^a/RT) \text{ atom/m}^2\text{s} = J_{1 \rightarrow 2}$$

\* (2) → (1) : Flux

$$\rightarrow A_1 n_2 \nu_2 \exp[-(\Delta G^a + \Delta G) /RT] = J_{2 \rightarrow 1}$$



When  $\Delta G = 0$ , there is **no net boundary movement**.

$$A_2 n_1 \nu_1 \approx A_1 n_2 \nu_2 = An\nu$$

When  $\Delta G > 0$ , there will be a **net flux** from grain 1 to 2. (For a high-angle GB,  $A_1 \approx A_2 \approx 1$ )

$$(A_2 n_1 \nu_1 \approx A_1 n_2 \nu_2 = An\nu)$$

$$J_{\text{net}} = J_{1 \rightarrow 2} - J_{2 \rightarrow 1} = An\nu \exp(-\Delta G^a/RT) [1 - \exp(-\Delta G/RT)] \quad 27$$

$$J_{1 \rightarrow 2} - J_{2 \rightarrow 1} = A n v \exp(-\Delta G^a/RT) [1 - \exp(-\Delta G/RT)]$$

- If the boundary is moving with a velocity  $v$ , the above flux must also be equal to 순표류속도

$$J = v \cdot c_B \rightarrow v / (V_m / N_a) \quad (V_m / N_a : \text{atomic volume})$$

Diffusion flux

If  $\Delta G$  is small [ $\Delta G \ll RT$ ]  $\rightarrow$  Apply Taylor expansion to  $\exp(-\Delta G/RT)$  term

$$J_{\text{net}} = A_2 n_1 v_1 \exp(-\Delta G^a/RT) [\Delta G/RT] \text{ (atom/m}^2\text{s)} = v / (V_m / N_a)$$

Boundary velocity  $v = \frac{A_2 n_1 v_1 V_m^2}{N_a R T} \exp\left(-\frac{\Delta G^a}{RT}\right) \frac{\Delta G}{V_m}$   $v \sim \Delta G / V_m$  driving force  $\rightarrow F = \Delta G / V_m$

or  $v = M \cdot \Delta G / V_m$   $M$ : mobility of boundary, i.e., the velocity under unit driving force

$$\text{where } M = \left\{ \frac{A_2 n_1 v_1 V_m^2}{N_a R T} \exp\left(\frac{\Delta S^a}{R}\right) \right\} \exp\left(\frac{-\Delta H^a}{RT}\right)$$

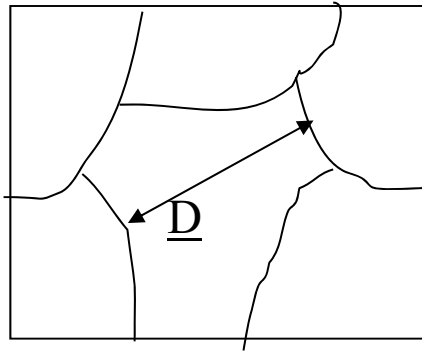
$M$  : mobility = velocity under unit driving force  $\sim \exp(-1/T)$   
exponentially increase with temp

$\rightarrow$  The boundary migration is a thermally activated process.  
(입계 이동은 확산처럼 열활성화 과정)

## \* Kinetic of grain growth

1) driving force  $F = \Delta G/V_m$  →  $v = M (\Delta G/V_m)$  **Boundary velocity**  
**Pulling force** M : exponentially increase with temp.

$v$  : relation to grain coarsening



Mean grain size (diameter) :  $\underline{D}$

Mean radius of curvature of boundary :  $r$

if  $\underline{D} \propto r$ ,

$$\begin{aligned} \text{Mean velocity : } \underline{v} &= \alpha M (\Delta G/V_m) = d\underline{D}/dt \quad (\Delta G = 2\gamma V_m/r) \\ &= \alpha M(2\gamma/\underline{D}) = d\underline{D}/dt \quad (\alpha = \text{proportional constant} \sim 1) \end{aligned}$$

$\underline{v}$  (rate of grain growth)  $\sim 1/\underline{D}$ , exponentially increase with  $T$

Mean velocity :  $\underline{v} = \alpha M (\Delta G/V_m) = d\underline{D}/dt$  ( $\Delta G = 2\gamma V_m/r$ )  
 $= \alpha M(2\gamma/\underline{D}) = d\underline{D}/dt$  ( $\alpha = \text{proportional constant} \sim 1$ )

**Integration of previous eq. from  $D_0$  to  $\underline{D}$  ,**

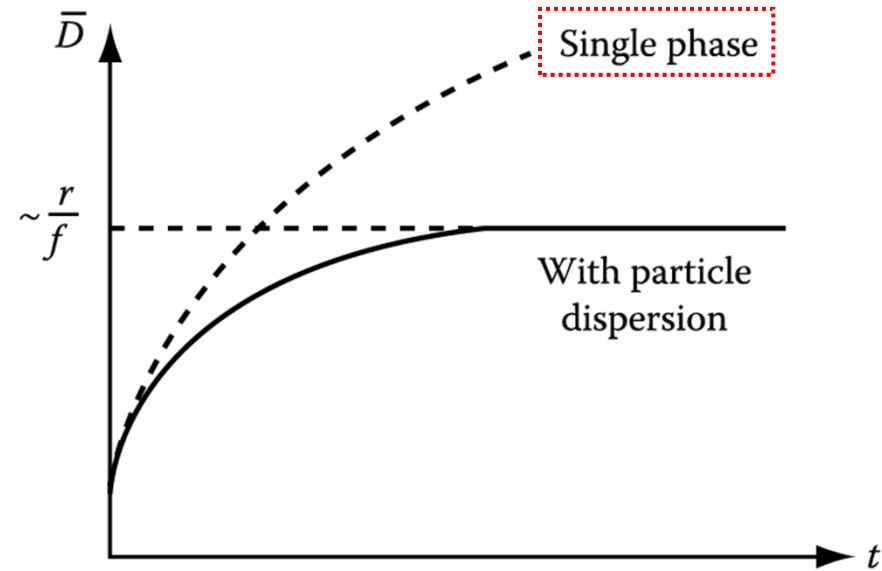
$\rightarrow \int_{D_0}^{\underline{D}} \frac{d\underline{D}}{\underline{D}} = \int 2\alpha M \gamma dt$

$\rightarrow \frac{1}{2} (\underline{D}^2 - D_0^2) = 2\alpha M \gamma t$

$\rightarrow (\underline{D}^2 - D_0^2) = 4\alpha M \gamma t = kt$

$\rightarrow \underline{D}^2 = D_0^2 + kt$

if  $D_0 \approx 0 \rightarrow \underline{D} = k't^{1/2}$



**r = average radius of particles**  
**f<sub>v</sub> = volume fraction of particles**

$\rightarrow \underline{D} = k't^n$  (experimental :  $n \ll 1/2$ ,  $1/2$  in very pure metals or only high temp.)

**Single phase**

- $\because$  the velocity of GB migration,  $v$  is not linear function of  $\Delta G$ .
- $\rightarrow M$  is not a const. but varies with  $\Delta G$  and thus also with  $D$ .
- $\rightarrow$  Variation of  $M$  in alloys could arise from solute drag effects. (M in alloy is relatively slower than that of pure metal)

# Whose mobility would be high between special and random boundaries?

By considering grain boundary structure,

(Mobility depending on GB structures)

High energy G.B. → relatively open G.B. structure → High mobility

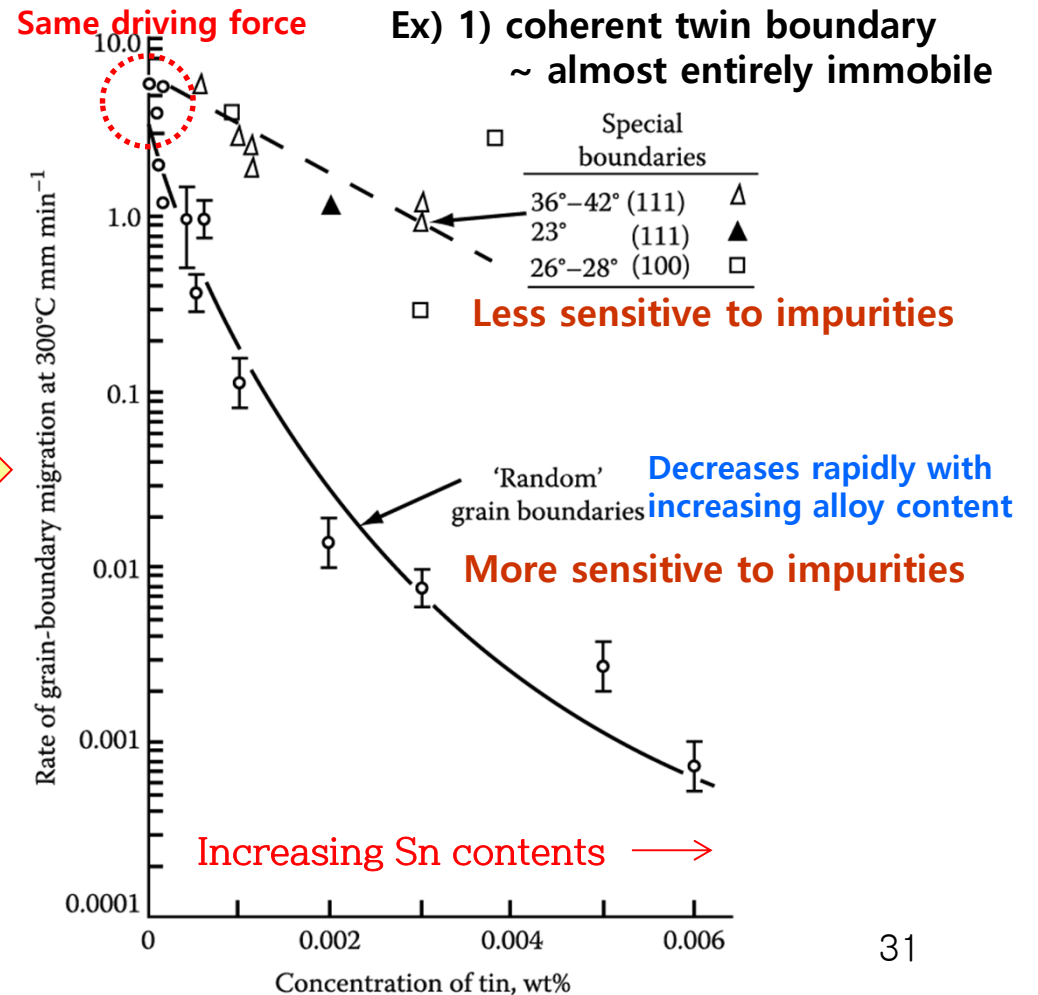
Low energy G.B. → closed (or denser) G.B. structure → Low mobility

But, **Ideal** ↔ **Real**

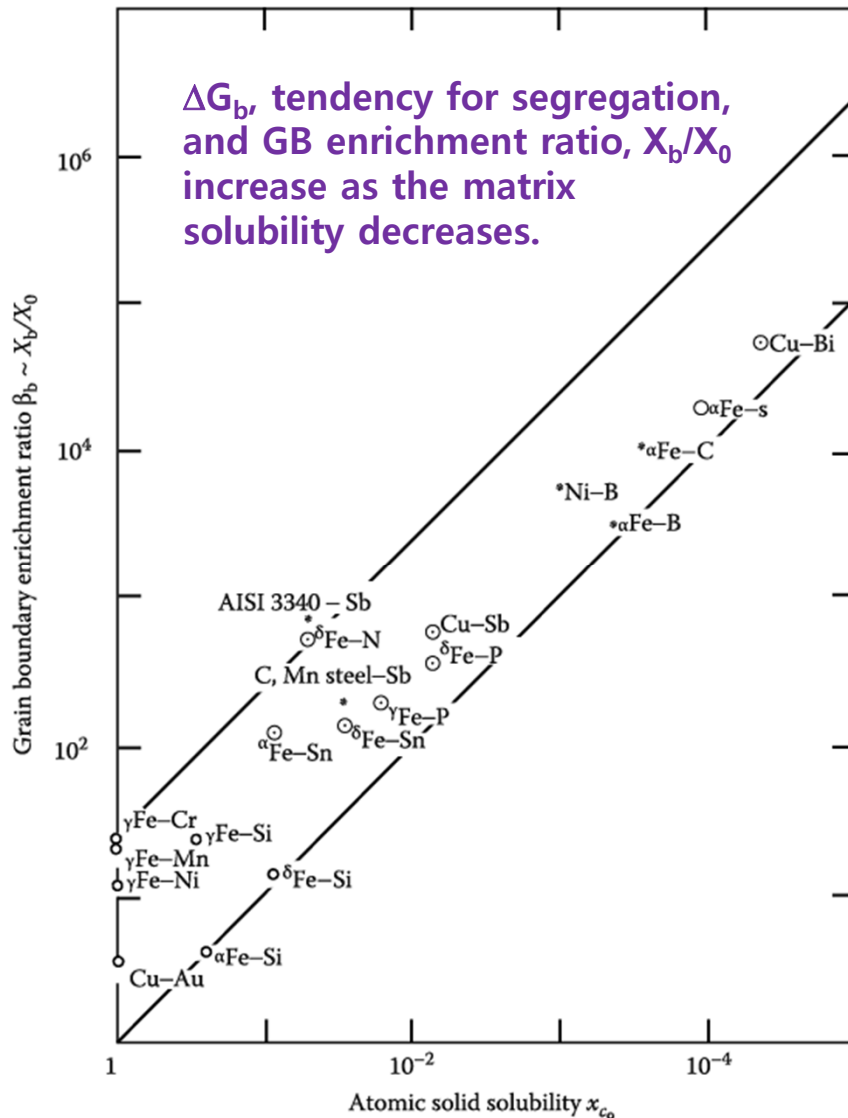
2) The other special boundaries are usually more mobile than random high-angle boundary. Why?

If the metal were “perfectly” pure the random boundaries would have the higher mobility.

⇒ Due to differences in the interactions of alloy elements or impurities with different boundaries



Migration rate of special and random boundaries at 300 °C in zone-refined lead alloyed with tin under equal driving forces



<Increasing GB enrichment with decreasing solid solubility in a range of system>

$X_0$  : matrix solute concentration/  $X_b$  : boundary solute concentration

$\Delta G_b$  : free energy reduced when one mole of solute is moved to GB from matrix.

( $\Delta G_b$ ) → The high mobility of special boundaries can possibly be attributed to a low solute drag on account of the relatively more close-packed structure of the special boundaries.

\* Solute drag effect

In general,  $G_b$  (grain boundary E) and mobility of pure metal decreases on alloying.

~Impurities tend to stay at the GB.

Generally,  $\Delta G_b$ , tendency of segregation, increases as the matrix solubility decreases.

$$X_b = X_0 \exp \frac{\Delta G_b}{RT}$$

$X_b/X_0$ : GB enrichment ratio

- Decreases as temp. increases, i.e., the solute "evaporates" into the matrix

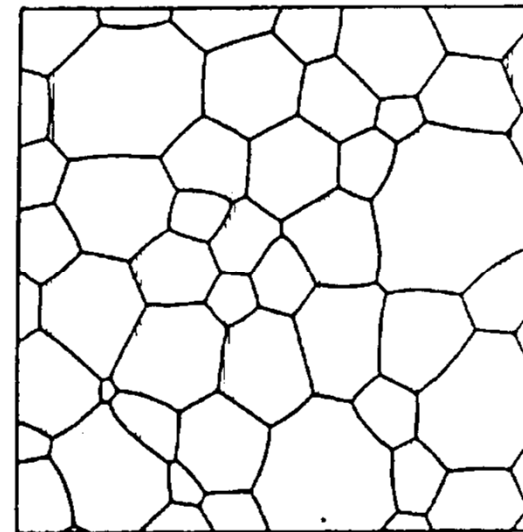
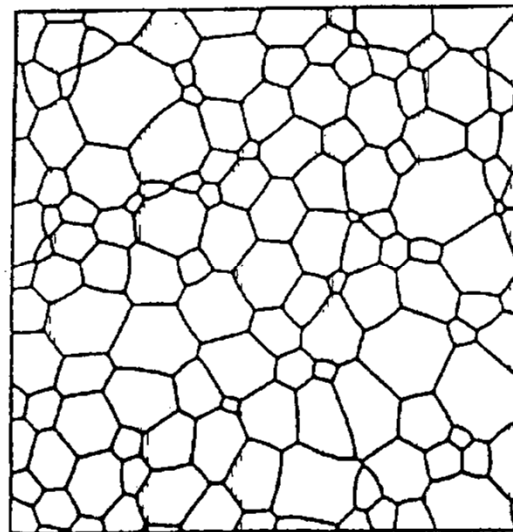
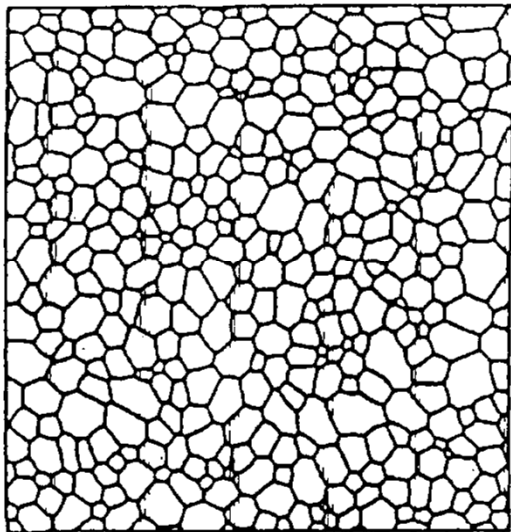
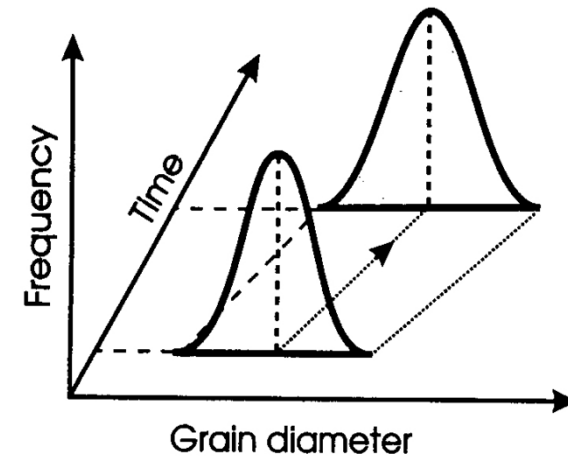
Low T or  $\Delta G_b$  ↑  $X_b$  ↑ Mobility of G.B. ↓

→ Alloying elements affects mobility of G.B.



# Normal Grain Growth

- Grain boundary moves to reduce area and total energy
- Large grain grow, small grains shrink
- Average grain size increases
- Little change of size distribution

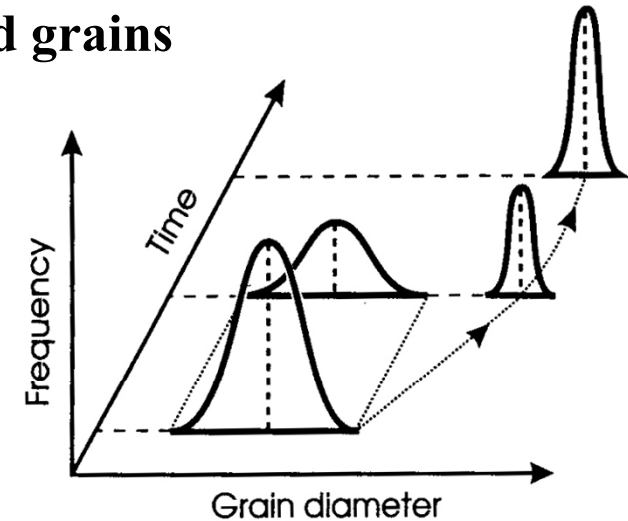


# Abnormal Grain Growth

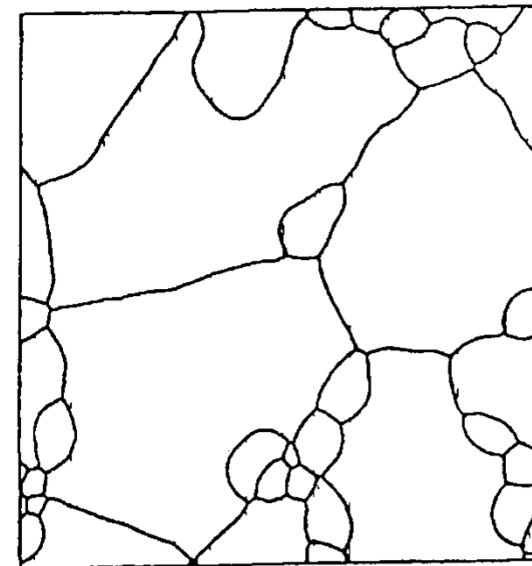
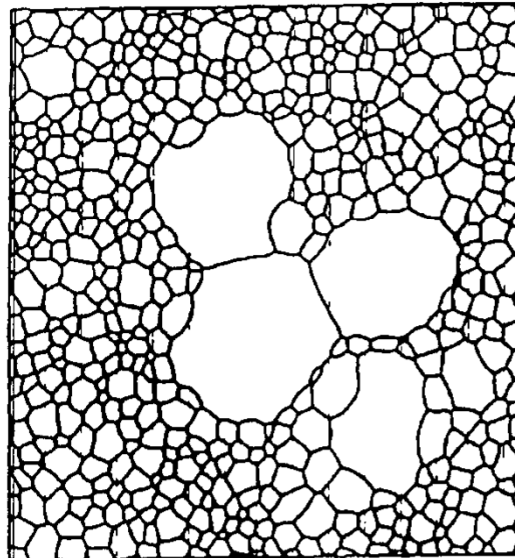
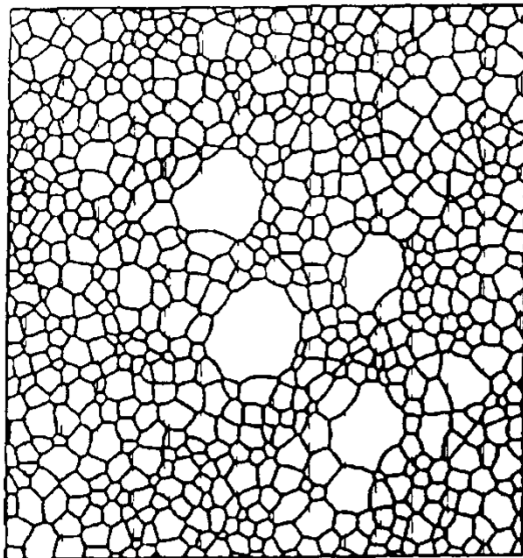
(high mobility of special GBs → development of recrystallization textures)

## ❑ Discontinuous grain growth of a few selected grains

- Local breaking of pinning by precipitates
- Anisotropy of grain boundary mobility
- Anisotropy of surface & grain boundary energy
- Selective segregation of impurity atoms
- Inhomogeneity of strain energy



## ❑ Bimodal Size distribution



# Abnormal Grain Growth

ex) Si steel → improvement of “soft magnetic property”  
= discontinuous grain growth or secondary recrystallization

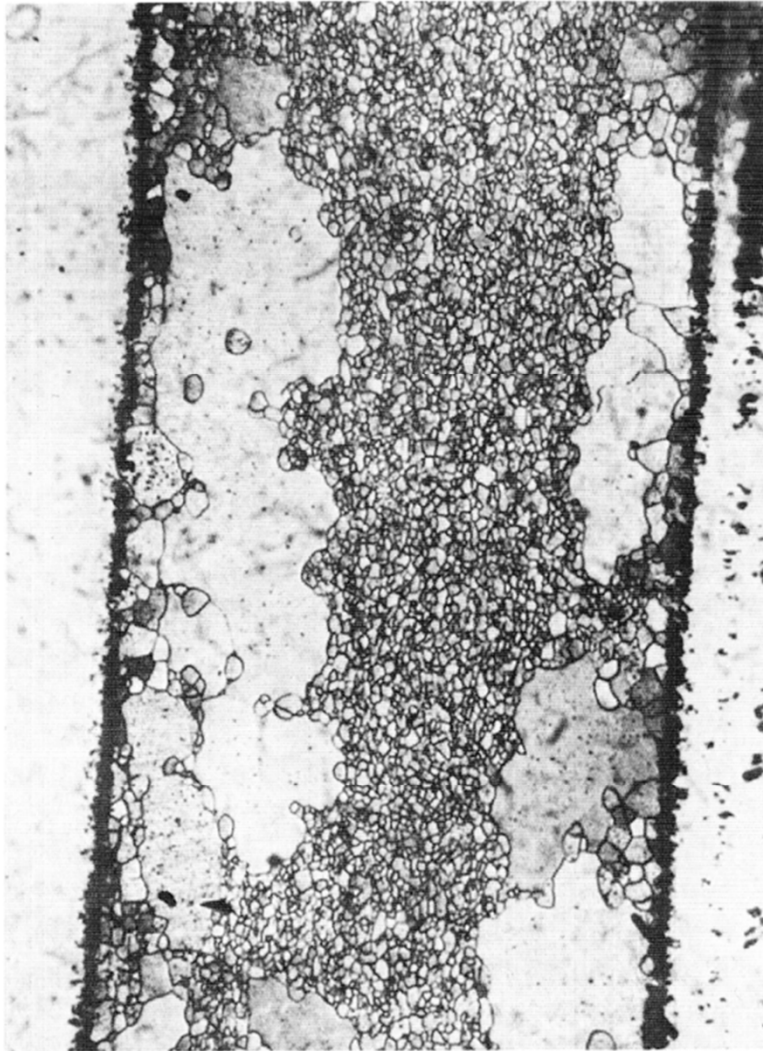


Figure 5.87 Optical micrograph showing abnormal grain growth in a fine grain steel containing 0.4 wt% carbon. The matrix grains are prevented from growing by a fine dispersion of carbide particles that are not revealed. Magnification  $\times 135$ . (After Gawne and Higgins 1971. Courtesy of the Metals Society.)

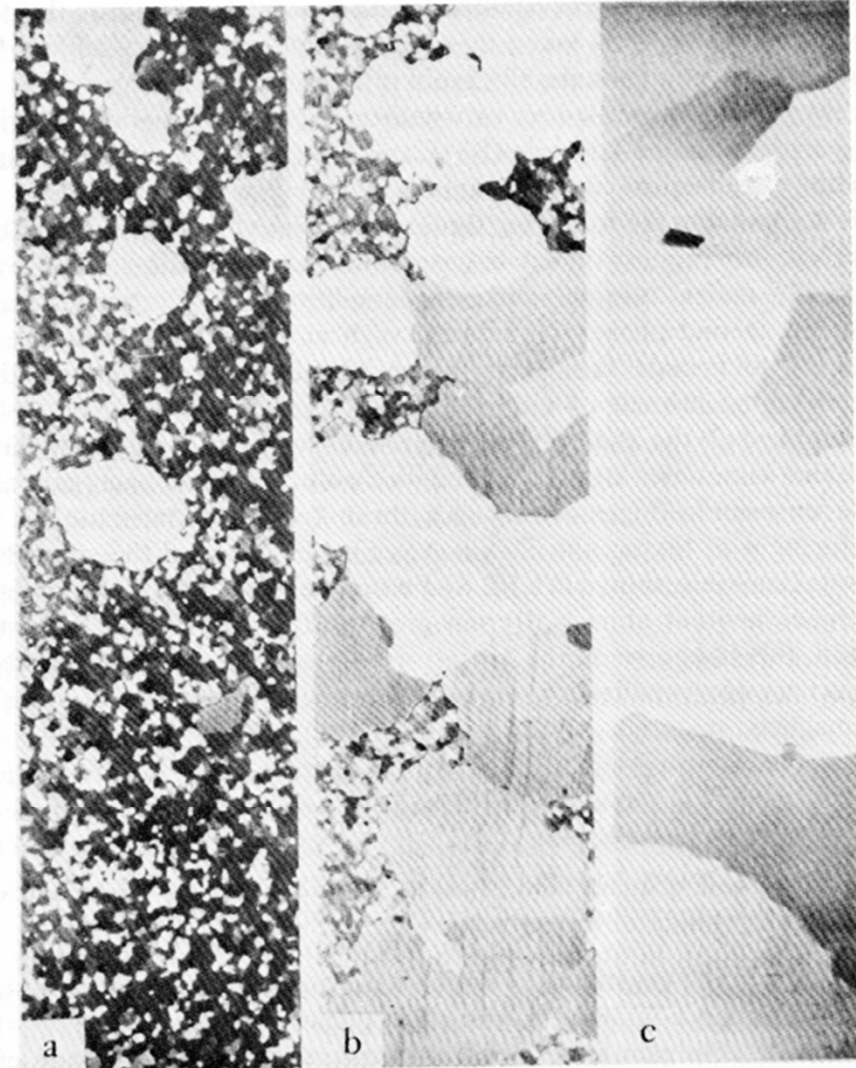


Fig. 5.48. Evidence for the preferential formation of (110)[001]-oriented grains by secondary recrystallization in 5% Si-Fe (Graham [1969]).

# Q: Grain boundary ( $\alpha/\alpha$ interfaces) = Boundaries in Single-Phase Solids

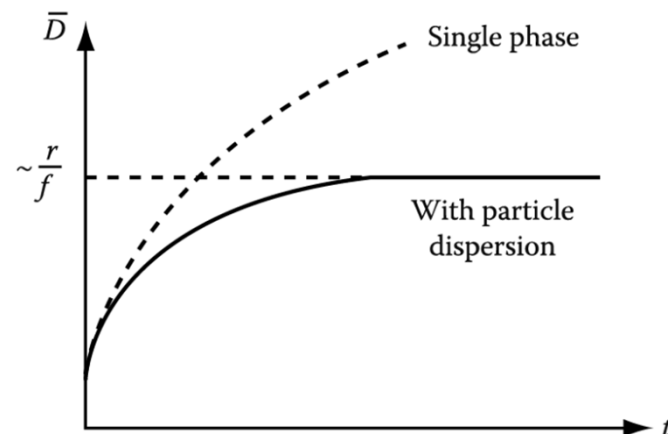
(a) Low-Angle and High-Angle Boundaries

(b) Special High-Angle Grain Boundaries

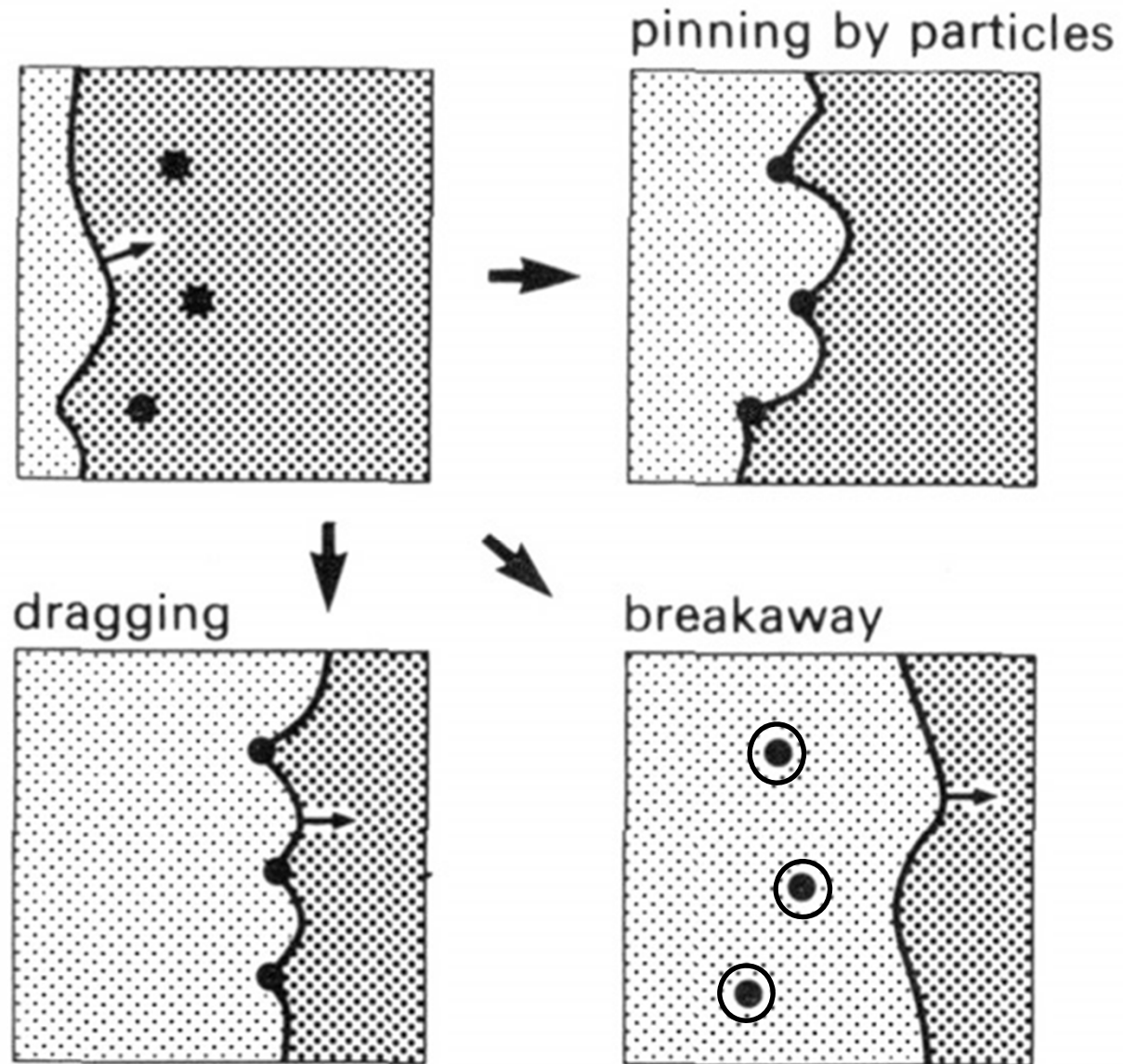
(c) Equilibrium in Polycrystalline Materials

## 4) Effect of second-phase particle on GB migration : Zener Pinning

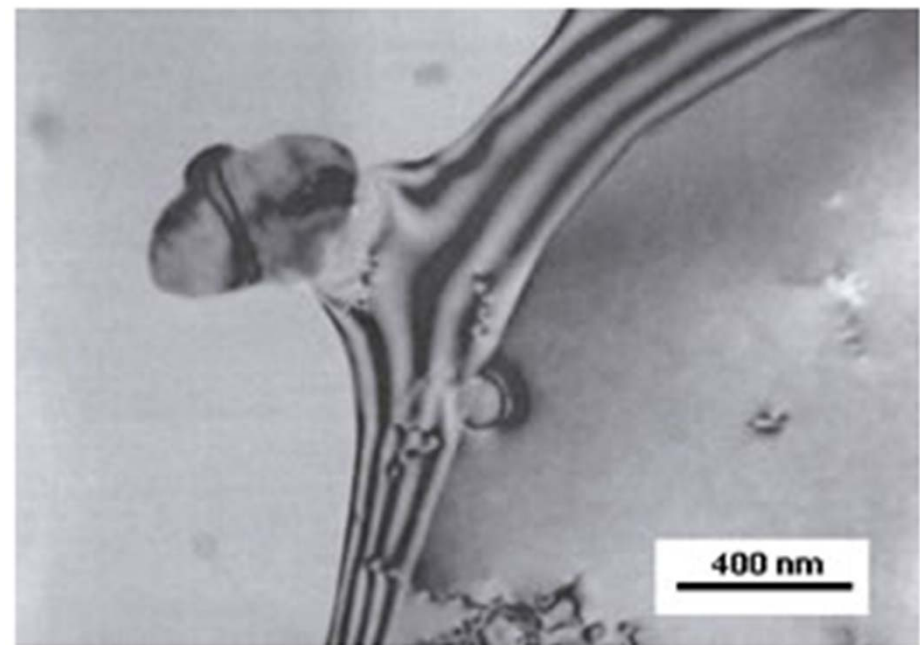
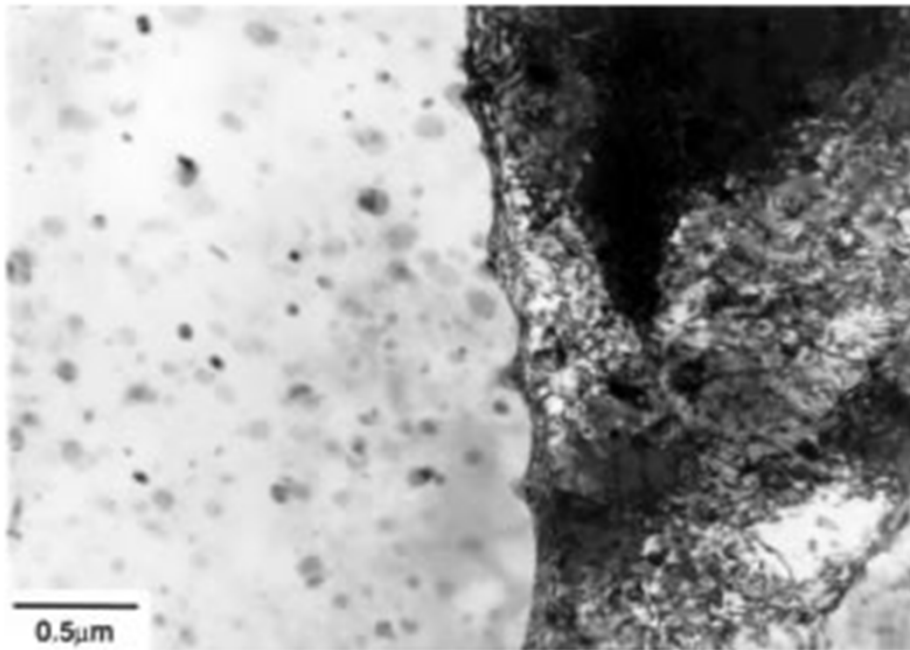
$$\bar{D}_{\max} = \frac{4r}{3f_v}$$



**Schematic diagram illustrating the possible interactions of second phase particles and migrating grain boundaries.**



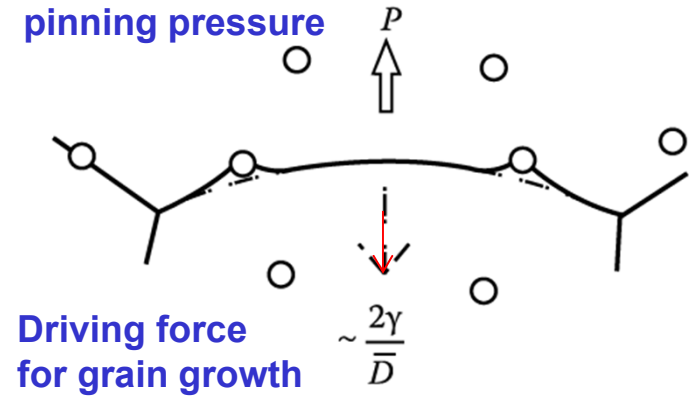
## Pinning by particle



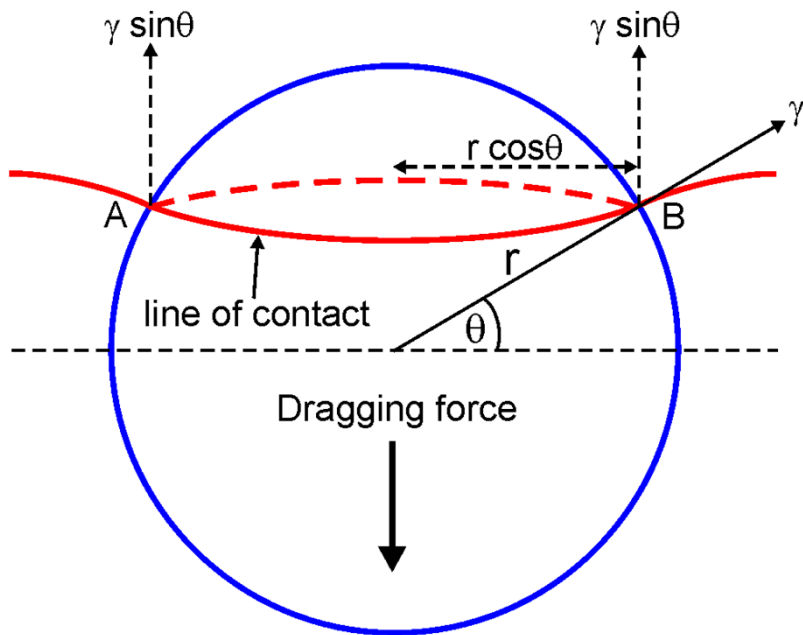
제 2 상이 존재할 때 결정립의 성장

# Effect of Second-Phase Particles on GB migration

Interaction with particles **Zener Pinning**



Derive the expression for the pinning effect of grain boundary migration by precipitates.



since  $\gamma \sin\{\theta\} = \text{force per unit length}$

$$F = \gamma \sin\{\theta\} \times \underbrace{2\pi r \cos\{\theta\}}_{\text{circumference}} = AB$$

so that at  $\theta = 45^\circ$

$$F_{max} = \gamma \pi r$$

Maximum force exerted by a single particle

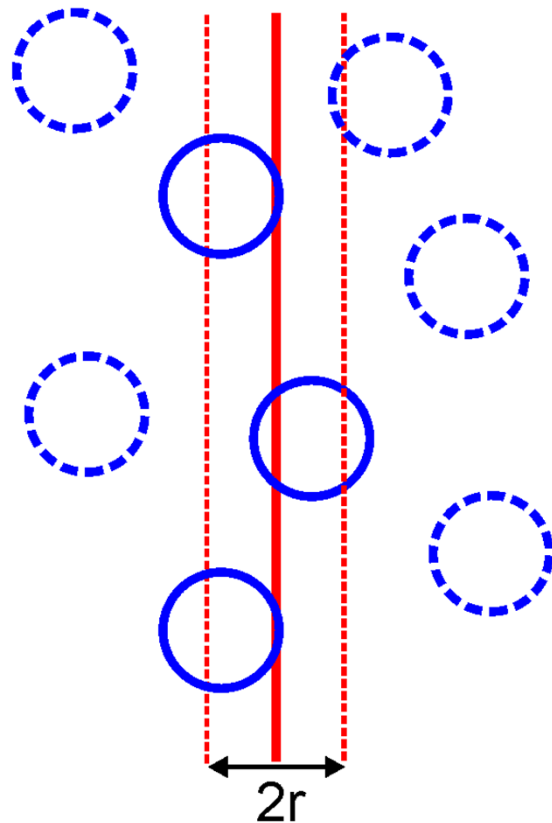
## Interaction with particles

## Zener Pinning

$f_v$  = volume fraction of randomly distributed particles of radius  $r$

$N_{\text{total}}$  = number of particles per unit volume

$$N = \frac{f_v}{\frac{4}{3}\pi r^3}$$



Only particles within one radius (solid circles) can intersect a planar boundary

If the boundary is essentially planar,

$$N_{\text{interact}} = 2rN_{\text{total}} = 3f_v/2\pi r^2$$

Mean # of particles intersecting unit area of a random plane

Given the assumption that

all particles apply the maximum pinning force,

the total pinning pressure

$$P = \frac{3f_v}{2\pi r^2} \cdot \pi r \gamma = \frac{3f_v \gamma}{2r}$$

This force will oppose the driving force for grain growth,  $\frac{2\gamma}{\bar{D}}$ .

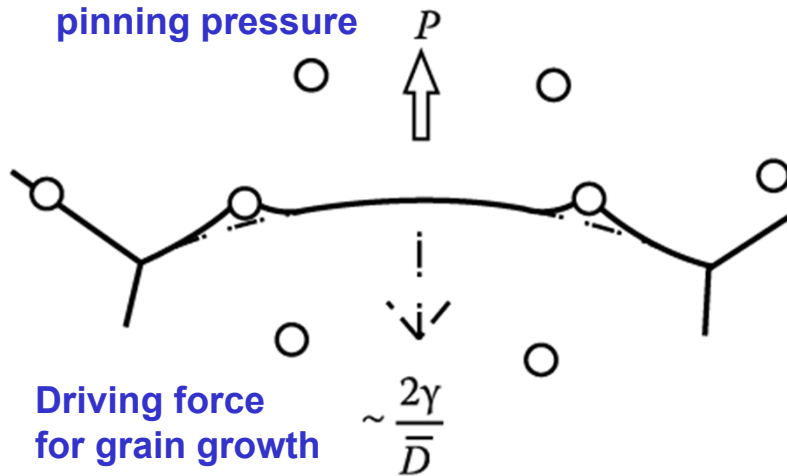


## Interaction with particles

## Zener Pinning

$$P = \frac{3f_v}{2\pi r^2} \cdot \pi r \gamma = \frac{3f_v \gamma}{2r}$$

This force will oppose the driving force for grain growth,  $2\gamma/\bar{D}$ .



$$\frac{2\gamma}{\bar{D}} = \frac{3f_v \gamma}{2r} \rightarrow \bar{D}_{\max} = \frac{4r}{3f_v}$$

Driving force will be insufficient to overcome the drag of the particles and grain growth stagnates.

For fine grain size

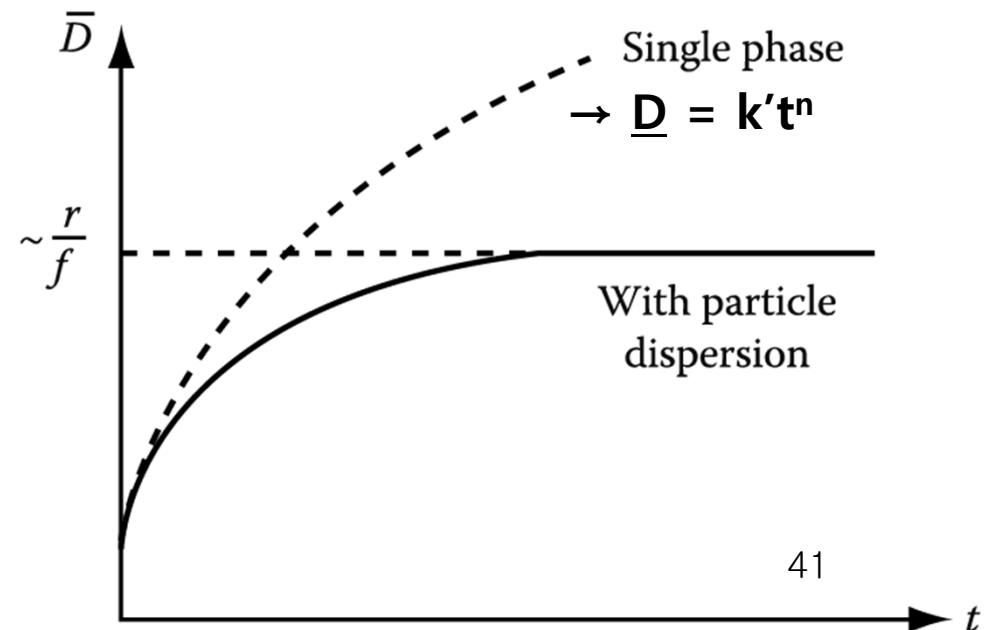
$\rightarrow$  a large volume fraction of very small particles

## \* Effect of second-phase particles on grain growth

$$\bar{D}_{\max} = \frac{4r}{3f_v}$$

: Stabilization of a fine grain size during heating at high temp.  $\rightarrow$  large volume fraction ( $f \uparrow$ ) of very small particles ( $r \downarrow$ ).

$$\bar{D}_{\max} = \frac{4r}{3f_v} \downarrow$$



## Summary for today's class

- **Thermally Activated Migration of Grain Boundaries:**

Metastable equilibrium of grain boundary (Balances of 1) boundary E + 2) surface tension)

→ real curvature ( $\Delta P \rightarrow \Delta G$ : Gibbs Thomson Eq.) →  $F = 2\gamma/r = \Delta G/V_m$  (by curvature)

(Pulling force per unit area of boundary)

→ Grain coarsening at high T annealing

- **Kinetics of Grain Growth**

- Grain boundary migration ( $v$ ) by thermally activated atomic jump

Boundary velocity  $v = \frac{A_2 n_1 v_1 V_m^2}{N_a RT} \exp\left(-\frac{\Delta G^a}{RT}\right) \frac{\Delta G}{V_m}$   $v \sim \Delta G/V_m$  driving force  
 $\rightarrow F = \Delta G/V_m$

$M$  : mobility = velocity under unit driving force  $\sim \exp(-1/T)$

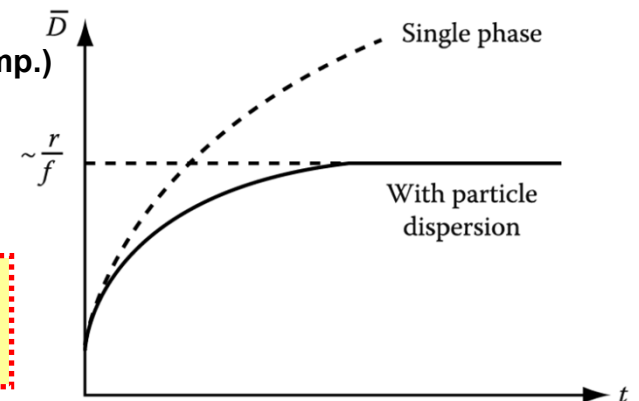
rate of grain growth  $d\bar{D}/dt \sim 1/\bar{D}$ , exponentially increase with T

→  $\bar{D} = k't^n$  (Experimental:  $n \ll 1/2$ ,  $1/2$  at pure metals or high Temp.)

- Mobility of GB ~ affected by both type of boundaries and GB segregation or 2<sup>nd</sup> phase precipitation

Ex) Effect of second-phase particle - Zener Pinning

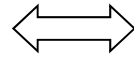
$$\bar{D}_{\max} = \frac{4r}{3f_v}$$



# Summary for today's class

- Grain Growth**

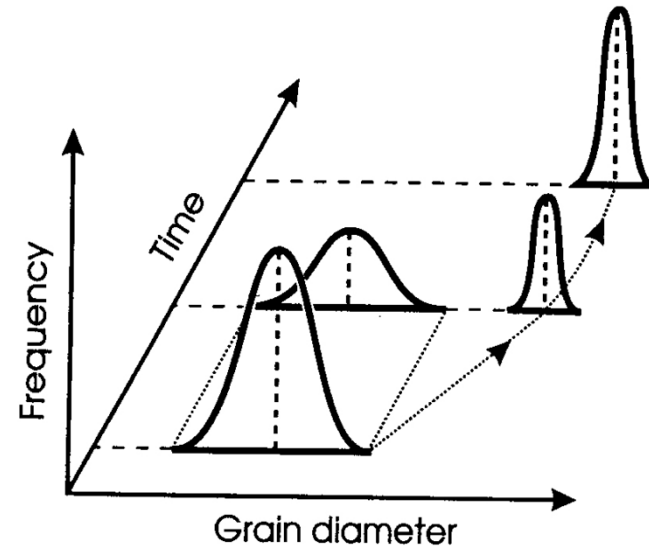
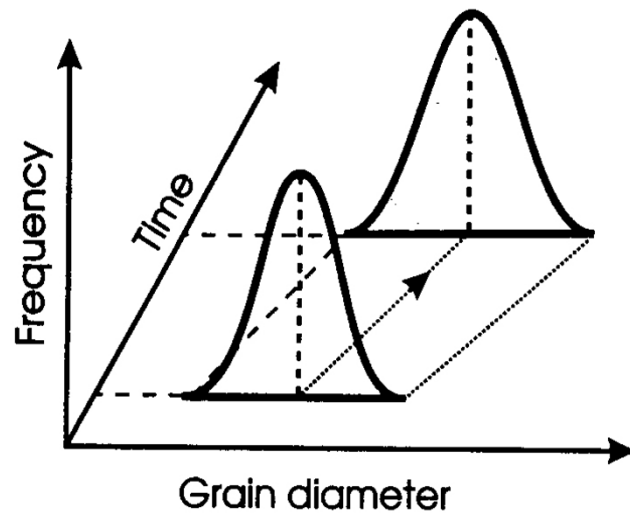
- Normal grain growth



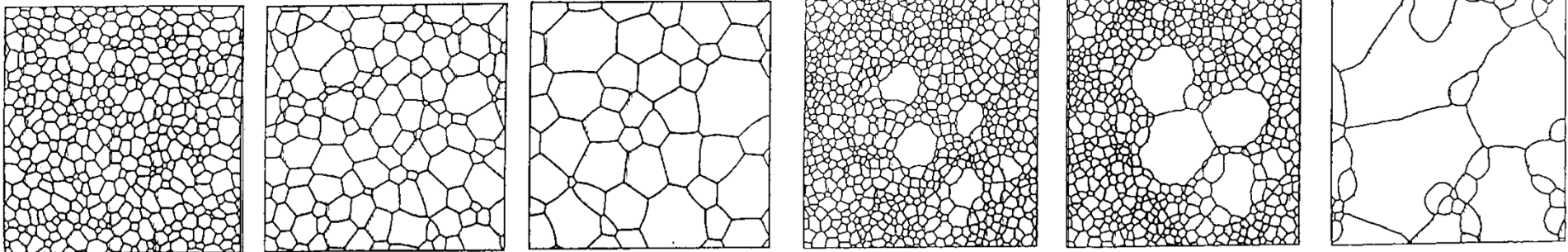
**Abnormal grain growth**

(high mobility of special GBs

→ development of recrystallization textures)



< Bimodal Size distribution >



**MIDTERM (22<sup>nd</sup> October, 9 AM-12 PM)**

**Scopes: Text ~ page 146 (~ chapter 3.3)/**

**Teaching notes: 1~11/**

**and Homeworks**

**Good Luck!!**