

# Radio Interferometry -- II

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# Topics

- Practical Extensions to the Theory:
  - Real Sensors
  - Finite bandwidth
  - Rotating reference frames (source motion)
  - Finite time averaging
  - Local Oscillators and Frequency Downconversion
- Coordinate systems
  - Direction cosines
  - 2-D ('planar') interferometers
  - 3-D ('volume') interferometers
- U-V Coverage, Visibilities, and Simple Structures.



# Review

- In the previous lecture, I set down the principles of Fourier synthesis imaging.

- I showed:

$$V_\nu(\mathbf{b}) = R_C - iR_S = \iint I_\nu(s) e^{-2\pi i \nu \mathbf{b} \cdot \mathbf{s} / c} d\Omega$$

Where the intensity  $I_\nu$  is a real function, and the visibility  $V(\mathbf{b})$  is complex and Hermitian.

- The model used for the derivation was idealistic – not met in practice:
  - Idealized Sensors
  - Monochromatic
  - Stationary reference frame.
  - RF throughout

We now relax, in turn, these restrictions.

# Real Sensors

- I developed the integral relationship presuming idealized sensors – uniform sensitivity in all directions.
- Such a device doesn't exist.
- Real sensors (antennas) have a directional voltage gain pattern  $A(\mathbf{s}, \mathbf{s}_0)$ , where  $\mathbf{s}$  is a general direction, and  $\mathbf{s}_0$  is a pointing direction.
- The gain pattern is (nominally) easily incorporated into the formalism, once we realize that it attenuates the actual sky brightness. We can write:

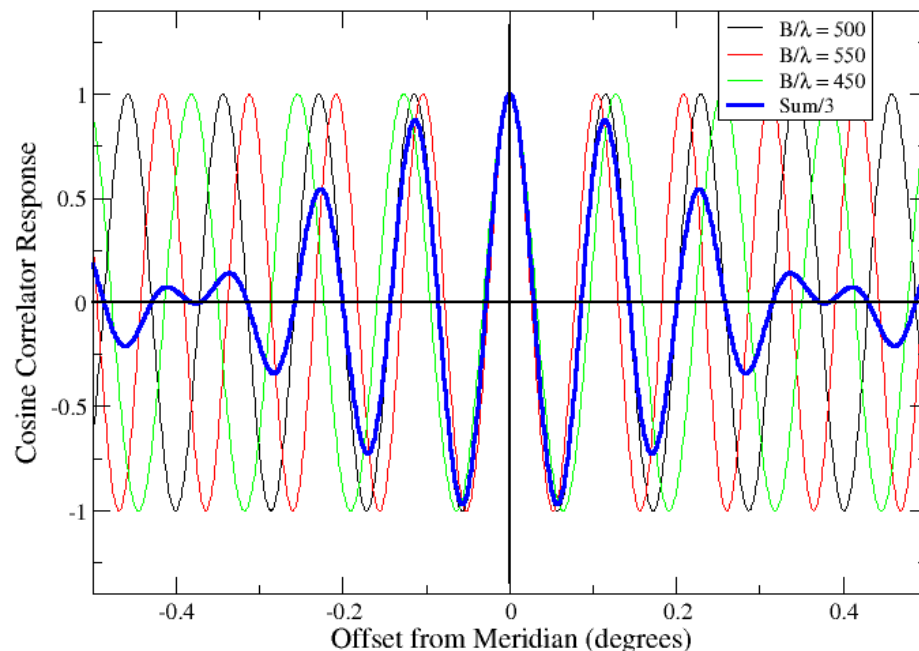
$$V_\nu(\mathbf{s}, \mathbf{b}) = \iint A_1(\mathbf{s}, \mathbf{s}_0) A_2^*(\mathbf{s}, \mathbf{s}_0) I_\nu(s) e^{-2\pi i \nu \mathbf{b} \cdot \mathbf{s} / c} d\Omega$$

- Here,  $A_1$  and  $A_2$  are the normalized complex voltage attenuation functions for the two antennas.
- Note that if the antennas are identical, and pointing in the same direction, then  $A_1 A_2 = P$ , the normalized power response.



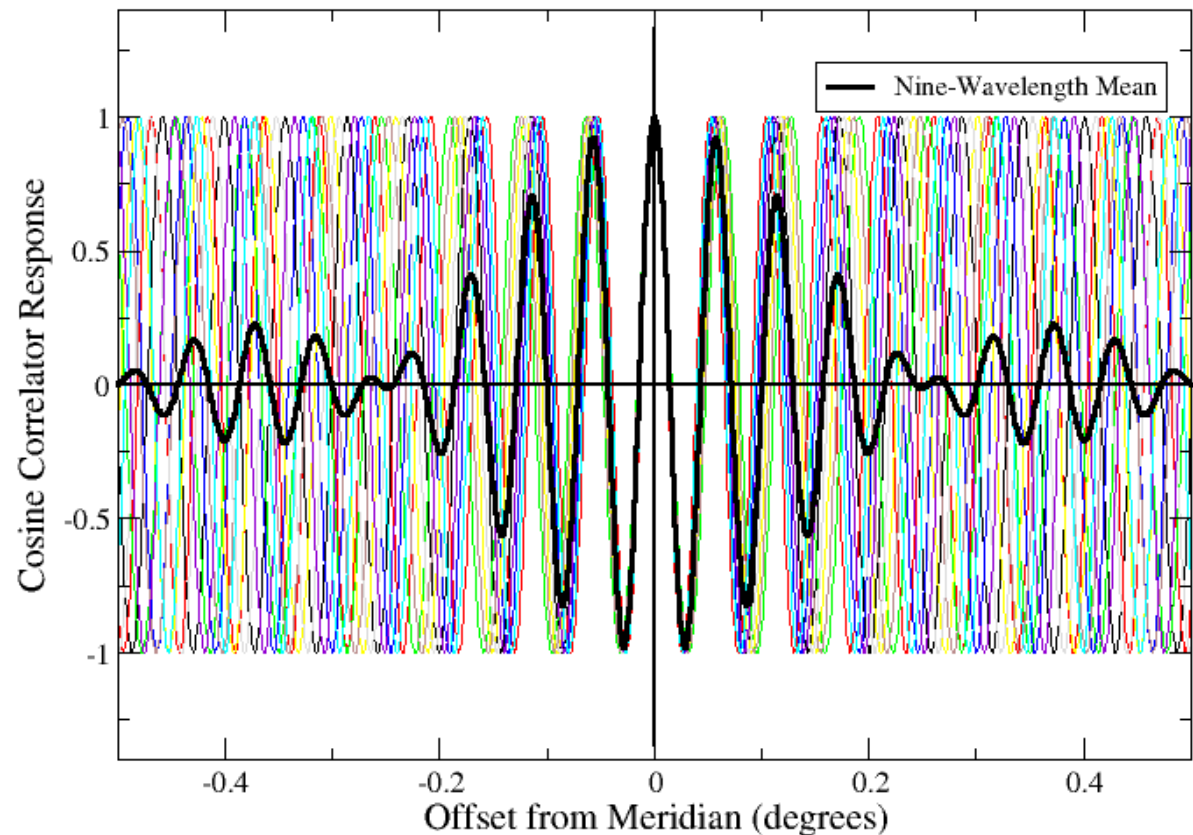
# Effect of Finite Bandwidth

- A baseline has a fixed physical length,  $B$ . But the fringe pattern depends on its length **in wavelengths**.
- Each slice of wavelength has a pattern with angular separation of  $\sim \lambda/B$ .
- Each component has a maximum at the  $n=0$  fringe (meridional plane).
- They get increasingly out of step as  $n$  gets larger.
- A simple illustration – three wavelength components from the same physical baseline.
- The net result is the sum over all components.
- Here, this is shown in the thick blue line.



# Bandwidth Effect (cont.)

- With more components (nine equal ones in this case), the summed response begins to look like a 'wave packet'.



# The Effect of Bandwidth -- Analysis.

- To find the finite-bandwidth response, we integrate our fundamental response over a frequency response  $G(\nu)$ , of width  $\Delta\nu$ , centered at  $\nu_0$ :

$$V = \int \left( \frac{1}{\Delta\nu} \int_{\nu_0 - \Delta\nu/2}^{\nu_0 + \Delta\nu/2} I(\mathbf{s}, \nu) G_1(\nu) G_2^*(\nu) e^{-i2\pi\nu\tau_g} d\nu \right) d\Omega$$

- If the source intensity does not vary over the bandwidth, and the instrumental gain parameters  $G_1$  and  $G_2$  are square and identical, then

$$V = \iint I_\nu(\mathbf{s}) \frac{\sin(\pi\tau_g\Delta\nu)}{\pi\tau_g\Delta\nu} e^{-2i\pi\nu_0\tau_g} d\Omega = \iint I_\nu(\mathbf{s}) \text{sinc}(\tau_g\Delta\nu) e^{-2i\pi\nu_0\tau_g} d\Omega$$

where the **fringe attenuation function**,  $\text{sinc}(x)$ , is defined as:

$$\text{sinc}(x) = \frac{\sin(\pi x)}{\pi x}$$



# Bandwidth Effect Example

- For a square bandpass, the bandwidth attenuation reaches a null when

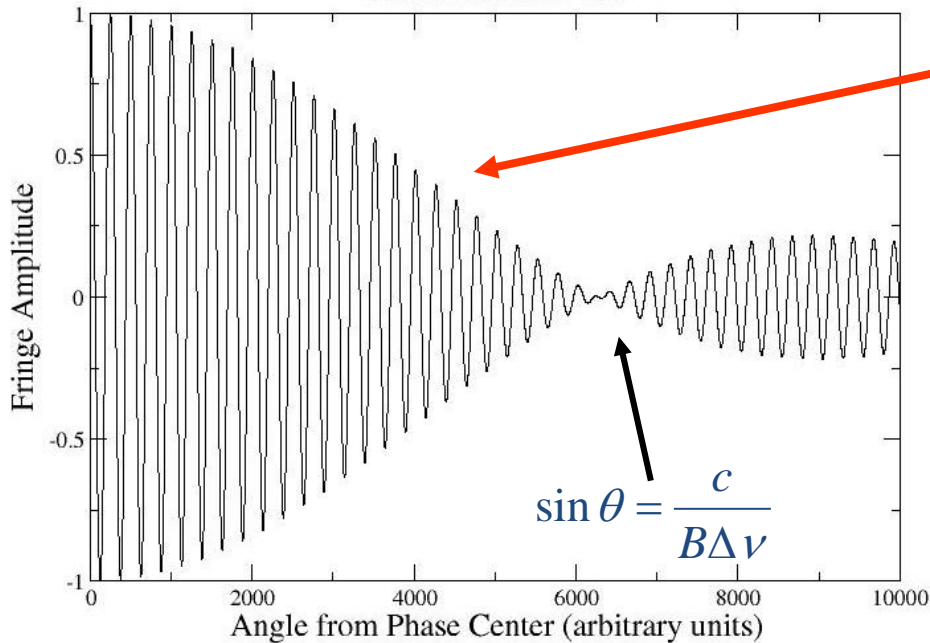
$$\tau_g \Delta \nu = 1, \text{ or}$$

$$\sin \theta = \frac{\lambda / B}{\Delta \nu / \nu_0} = \frac{c}{B \Delta \nu}$$

- For the old VLA, and its 50 MHz bandwidth, and for the 'A' configuration, the null was only  $\sim 35$  arcseconds away.
- For the Jansky VLA,  $\Delta \nu = 1$  MHz, and  $B = 35$  km, then the null occurs at about 30 arcminutes off the meridian.

The Effect of Finite Bandwidth

Fractional Bandwidth = 1/25



Fringe Attenuation function:

$$\text{sinc}\left(\frac{B \Delta \nu}{\lambda \nu} \sin \theta\right) = \text{sinc}\left(\frac{B \Delta \nu}{c} \sin \theta\right)$$

Number of fringes between peak and null:

$$N \sim \frac{c}{B \Delta \nu} \frac{B}{\lambda} \sim \frac{\nu}{\Delta \nu}$$



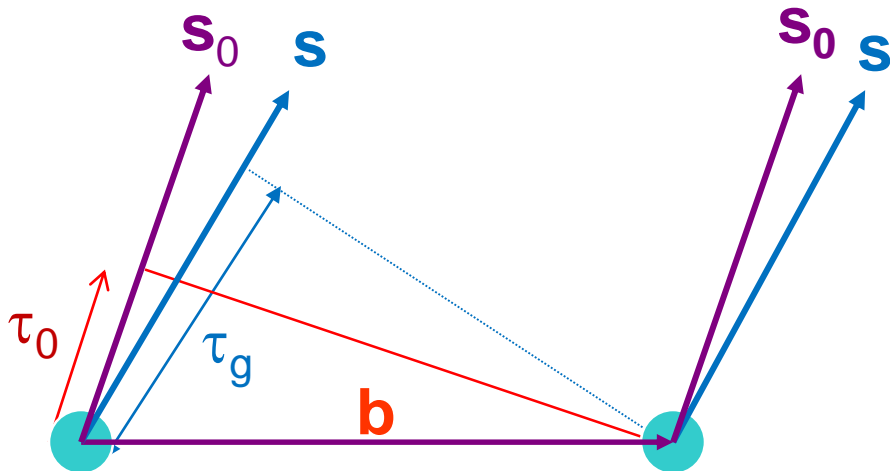
# Observations off the Meridian

- In our basic scenario -- stationary source, stationary interferometer -- the effect of finite bandwidth will strongly attenuate the fringe amplitudes from sources far from the meridional plane.
- Since each baseline has its own plane, the only point on the sky free of attenuation for all baselines is a small angle around the zenith (presuming all baselines are coplanar).
- Suppose we wish to observe an object far from the zenith?
- Best way is to shift the entire 'fringe packet' to the position of interest by adding time delay to the antenna closer to the source.

# Adding Time Delay

$$\tau_g = \mathbf{b} \cdot \mathbf{s} / c$$

$$\tau_0 = \mathbf{b} \cdot \mathbf{s}_0 / c$$



$\mathbf{S}_0$  = reference  
(delay)  
direction  
 $\mathbf{S}$  = general  
direction

$$V_1 = Ee^{-i\omega(t-\tau_g)}$$

$$V_2 = Ee^{-i\omega t}$$

The entire fringe  
pattern has been  
shifted over by  
angle

$$\sin \theta = c\tau_0/b$$

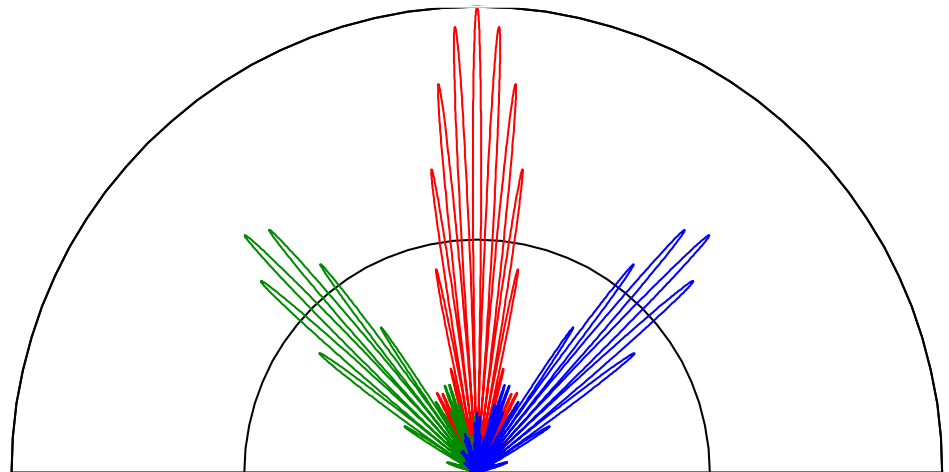
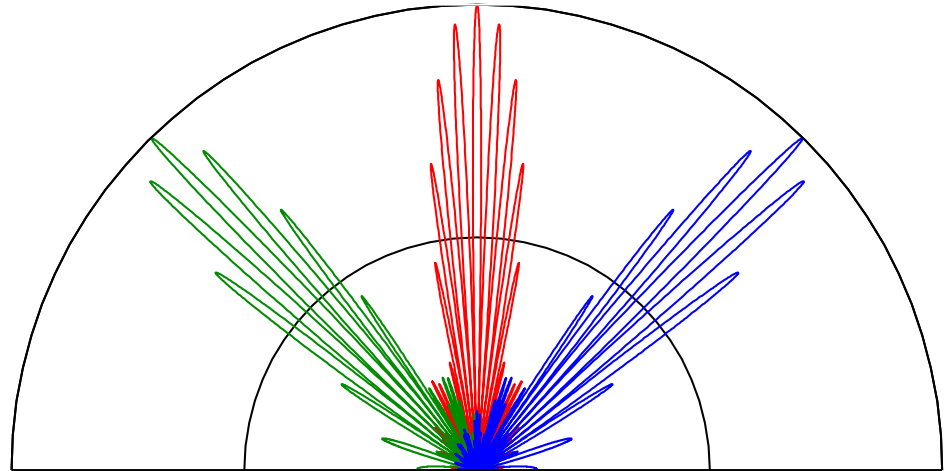
$$V_2 = Ee^{-i\omega(t-\tau_0)}$$

$$V = \langle V_1 V_2^* \rangle = E^2 e^{-i[\omega(\tau_0 - \tau_g)]}$$

$$= E^2 e^{i2\pi[\nu \mathbf{b} \cdot (\mathbf{s} - \mathbf{s}_0) / c]}$$

# Illustrating Delay Tracking

- Top Panel:  
Delay has been added and subtracted to move the delay pattern to the source location.
- Bottom Panel:  
A cosinusoidal sensor pattern is added, to illustrate losses from a fixed sensor.



# Observations from a Rotating Platform

- Real interferometers are built on the surface of the earth – a rotating platform. From the observer's perspective, sources move across the sky.
- Since we know how to adjust the interferometer timing to move its coherence pattern to the direction of interest, it is a simple step to continuously move the pattern to follow a moving source.
- All that is necessary is to continuously add time delay, with an accuracy  $\delta\tau \ll 1/\Delta\nu$  to minimize bandwidth loss.
- But there's one more issue to keep in mind...

# Phase Tracking ...

- Adding time delay will prevent bandwidth losses for observations off the baseline's meridian.
- But between delay settings, the source is moving through the interferometer pattern – a rapidly changing phase.
- How fast?
- The 'natural fringe rate' – due to earth's rotation, is given by

$$\nu_f = u \omega_e \cos \delta \quad \text{Hz}$$

- Where  $u = B/\lambda$ , the (E-W) baseline in wavelengths, and  $\omega_e = 7.3 \times 10^{-5}$  rad/s is the angular rotation rate of the earth.
- For a million-wavelength baseline,  $\nu_f \sim 70$  Hz – that's fast.
- If we leave things this way, we have to sample the output at at least twice this rate. A lot of data!



# Following a Moving Object.

- There is \*no\* useful information in this fringe rate – it's simply a manifestation of the platform rotation.
- Tracking, or 'stopping' the fringes greatly slows down the \*post-correlation\* data processing/archiving needs.
- To 'stop' the fringes, we must adjust the phase in one path.
- How fast:
  - Tracking delay: 
$$\nu_d \gg \Delta \nu \frac{B}{c} \omega_e \cos \delta \sim 1 \text{ Hz}$$
  - Tracking phase: 
$$\nu_f \gg \frac{B}{\lambda} \omega_e \cos \delta \sim 70 \text{ Hz}$$
- The rates given are appropriate for 35 km baselines, 128 MHz bandwidth, and 3 cm wavelength.
- For the 'RF' interferometer, delay insertion does both.



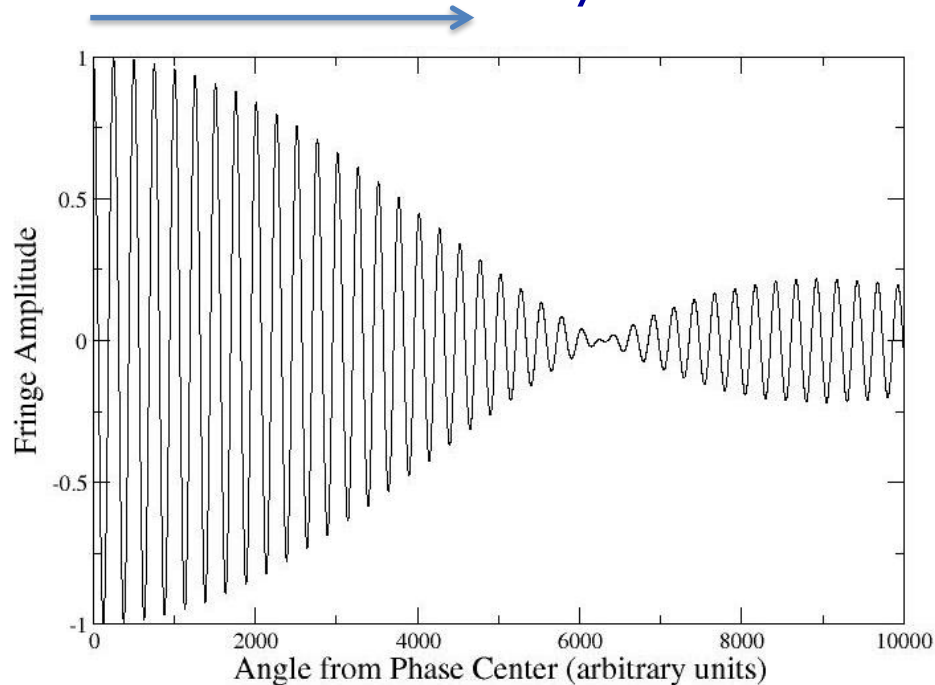
# Emphasis:

Shown again is the fringe pattern of a real wide-band baseline.

To preserve the visibility amplitude, we must re-set delays before source moves too far down the pattern.

To maintain a stable phase, we must reset  $\sim v/\delta v$  times faster.

Source moves this way



# Time Averaging Loss

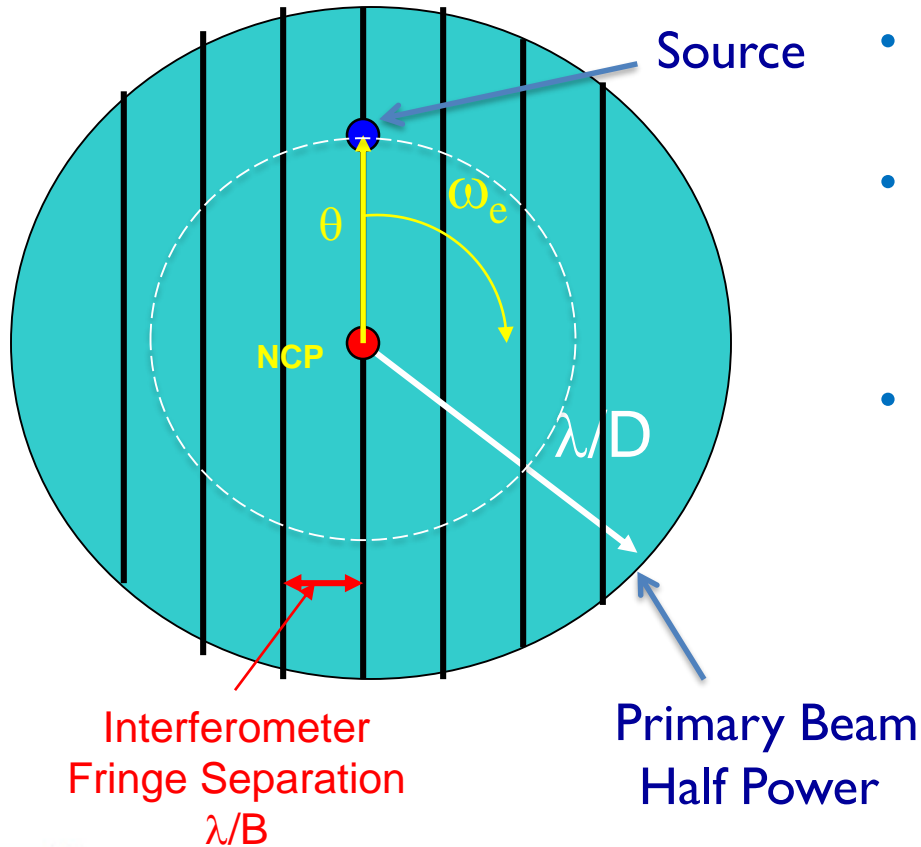
- So – we can track a moving source, continuously adjusting the delay to move the fringe pattern with the source.
- This does two good things:
  - Slows down the data recording needs
  - Prevents bandwidth delay losses.
- From this, you might think that you can increase the time averaging for as long as you please.
- But you can't – because 'stopping the fringes' only works for the object 'in the center' – the point for which the delays and phases have been pre-set.
- All other sources are moving w.r.t. the fringe pattern – and this is where the essential information lies...





# Time-Smearing Loss Timescale

Simple derivation of fringe period, from observation at the NCP.



- Turquoise area is antenna primary beam on the sky – radius =  $\lambda/D$
- Interferometer coherence pattern has spacing =  $\lambda/B$
- Sources in sky rotate about NCP at angular rate:
 
$$\omega_e = 7.3 \times 10^{-5} \text{ rad/sec.}$$
- Minimum time taken for a source to move by  $\lambda/B$  at angular distance  $\theta$  is:

$$t = \frac{\lambda}{B \omega_e \sin \theta}$$

$$\approx \frac{D}{\omega_e B}$$

For sources at the primary beam null

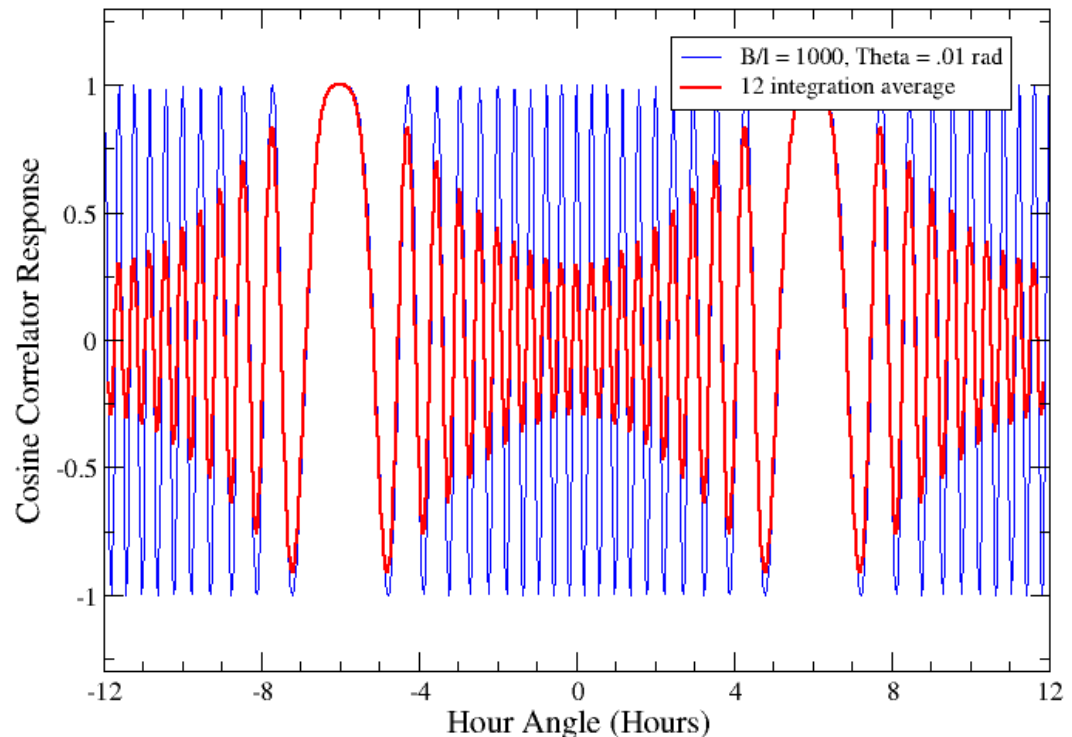
# Illustrating Time Averaging Loss

- An object located away from the fringe tracking center moves through the pattern as the earth rotates.
- It makes one cycle around in 24 hours.
- If we average the correlation products for too long a period, a loss in fringe amplitude will result.

Illustrating time average loss.

Blue trace: the fringe amplitude with no averaging.

Red trace: Amplitude after averaging for 12 'samples'.



# Time-Averaging Loss

- So, what kind of time-scales are we talking about now?
- How long can you integrate before the differential motion destroys the fringe amplitude?
- Case A: A 25-meter paraboloid, and 35-km baseline:
  - $t = D/(B\omega_e) = 10$  seconds. (independent of observing frequency).
- Case B: Whole Hemisphere for a 35-km baseline:
  - $t = \lambda/(B\omega_e)$  sec = 83 msec at 21 cm.
- Averaging for durations longer than these will cause severe attenuation of the visibility amplitudes.
- To prevent ‘delay losses’, your averaging time must be much less than this.
  - Averaging time 1/10 of this value normally sufficient to prevent time loss.

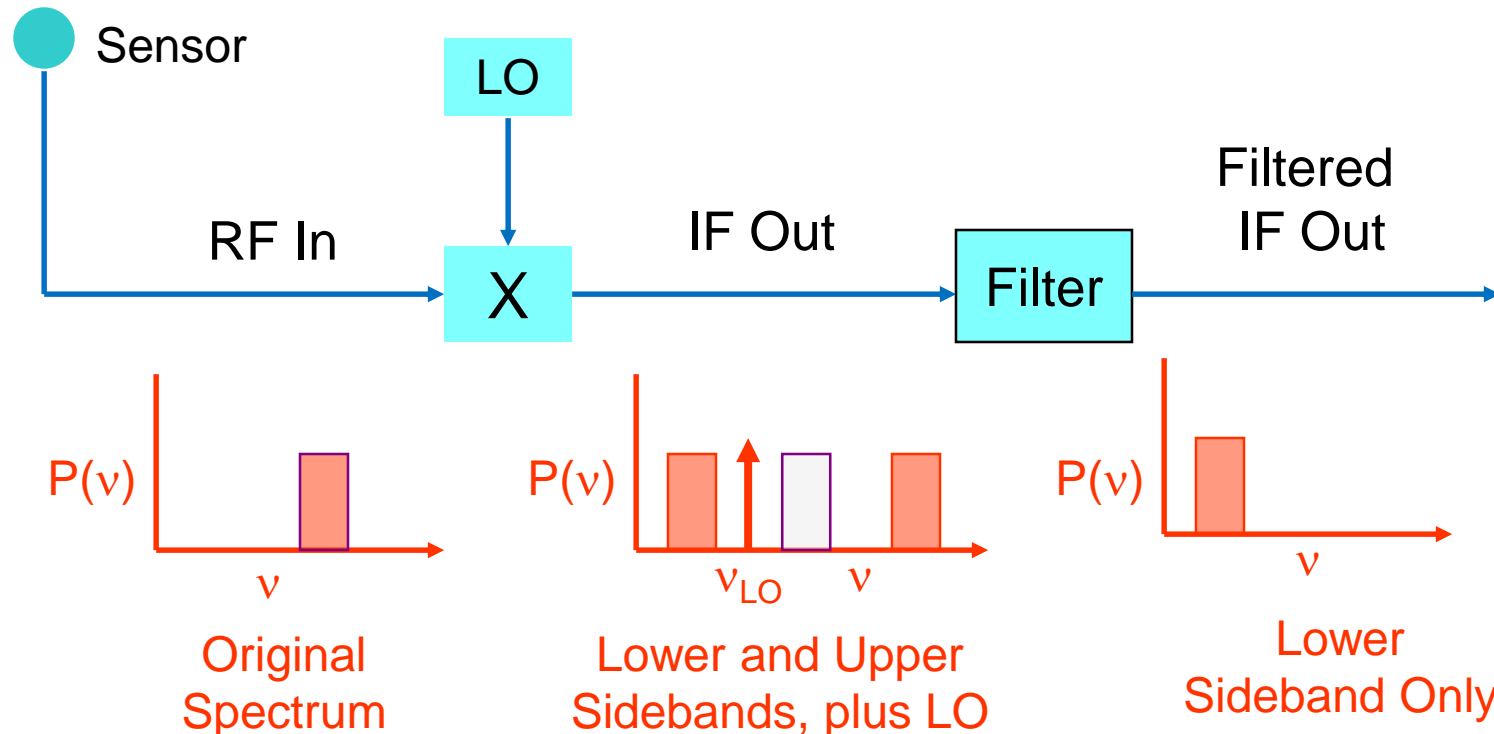


# The Heterodyne Interferometer: LOs, IFs, and Downconversion

- This would be the end of the story (so far as the fundamentals are concerned) if all the internal electronics of an interferometer would work at the observing frequency (often called the 'radio frequency', or RF).
- Unfortunately, this cannot be done in general, as high frequency components are much more expensive, and generally perform more poorly than low frequency components.
- Thus, most radio interferometers use 'down-conversion' to translate the radio frequency information from the 'RF' to a lower frequency band, called the 'IF' in the jargon of our trade.
- For signals in the radio-frequency part of the spectrum, this can be done with almost no loss of information.
- But there is an important side-effect from this operation in interferometry which we now review.

# Downconversion

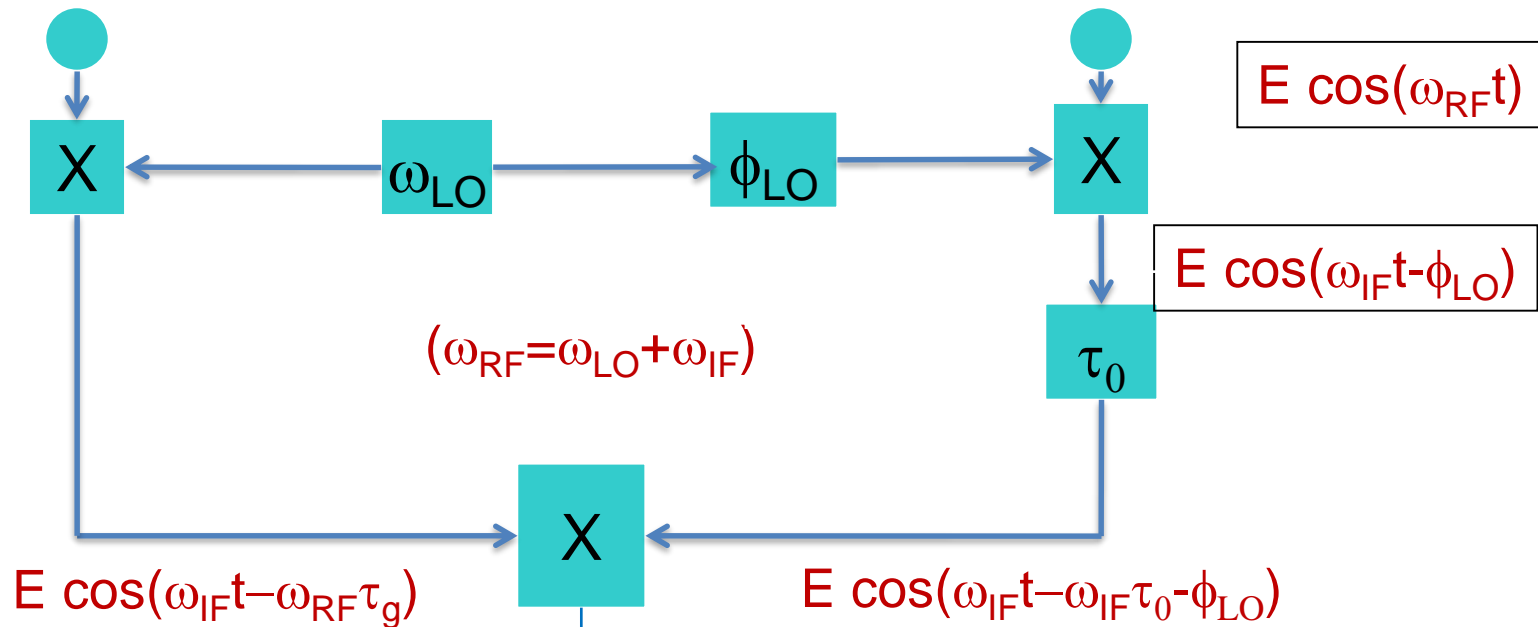
At radio frequencies, the spectral content within a passband can be shifted – with almost no loss in information, to a lower frequency through multiplication by a ‘LO’ signal.



This operation preserves the amplitude and phase relations

# Signal Relations, with LO Downconversion

- The RF signals are multiplied by a pure sinusoid, at frequency  $\nu_{LO}$
- We can add arbitrary phase  $\phi_{LO}$  on one side.



$$V = E^2 e^{-i(\omega_{RF}\tau_g - \omega_{IF}\tau_0 - \phi_{LO})}$$

# Recovering the Correct Visibility Phase

- The correct phase (RF interferometer) is:  $\omega_{RF} (\tau_g - \tau_0)$

- The observed phase (with frequency downconversion) is:

$$\omega_{RF} \tau_g - \omega_{IF} \tau_0 - \phi_{LO}$$

- These will be the same when the LO phase is set to:

$$\phi_{LO} = \omega_{LO} \tau_0$$

- This is necessary because the delay,  $\tau_0$ , has been added in the IF portion of the signal path, rather than at the frequency at which the delay actually occurs.
- The phase adjustment of the LO compensates for the delay having been inserted at the IF, rather than at the RF.

# The Three 'Centers' in Interferometry

- You are forgiven if you're confused by all these 'centers'.
- So let's review:
  1. **Beam Tracking (Pointing) Center:** Where the antennas are pointing to. (Or, for phased arrays, the phased array center position).
  2. **Delay Tracking Center:** The location for which the delays are being set for maximum wide-band coherence.
  3. **Phase Tracking Center:** The location for which the LO phase is slipping in order to track the coherence pattern.
- Note: Generally, we make all three the same. #2 and #3 are the same for an 'RF' interferometer. They are separable in a LO downconversion system.





# Interferometer Geometry

- We have not defined any geometric system for our relations.
- The response functions we defined were generalized in terms of the scalar product between two fundamental vectors:
- The baseline '**B**', defining the direction and separation of the antennas, and
- The unit vector '**s**', specifying the direction of the source.
- At this time, we define the geometric coordinate frame for the interferometer.
- We begin with a special case: An interferometer whose antennas all lie on a single plane.



# The 2-Dimensional Interferometer

To give better understanding, we now specify the geometry.

## Case A: A 2-dimensional measurement plane.

- Let us imagine the measurements of  $V_v(\mathbf{b})$  to be taken entirely on a plane.
- Then a considerable simplification occurs if we arrange the coordinate system so one axis is normal to this plane.
- Let  $(u,v,w)$  be the coordinate axes, with  $w$  normal to this plane. Then:

$$\mathbf{b} = (\lambda u, \lambda v, \lambda w) = (\lambda u, \lambda v, 0)$$

$u, v,$  and  $w$  are always measured in wavelengths.

- The components of the unit direction vector,  $\mathbf{s}$ , are:

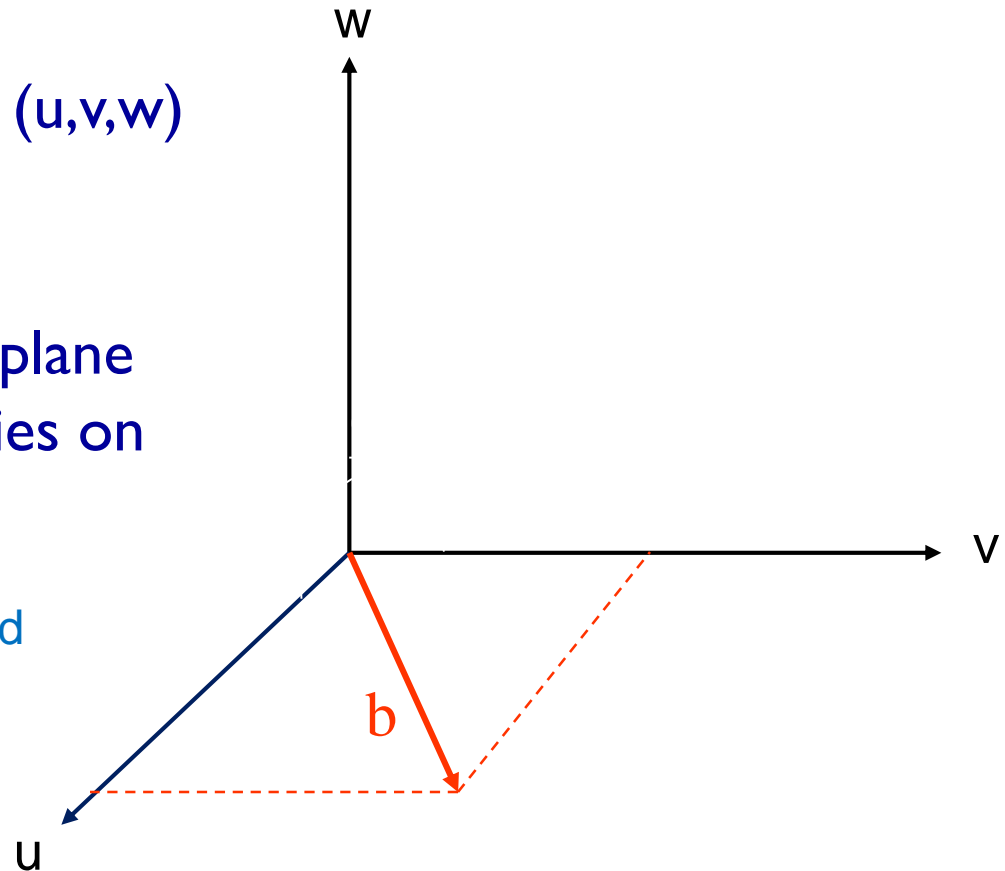
$$\mathbf{s} = (l, m, n) = \left( l, m, \sqrt{1 - l^2 - m^2} \right)$$

# The (u,v,w) Coordinate System.

- Pick a coordinate system (u,v,w) to describe the antenna positions and baselines.
- Orient this frame so the plane containing the antennas lies on  $w = 0$ .

The baseline vector **b** is specified by its coordinates (u,v,w) (measured in wavelengths). In the case shown,  $w = 0$ , and

$$\mathbf{b} = (\lambda u, \lambda v, 0)$$



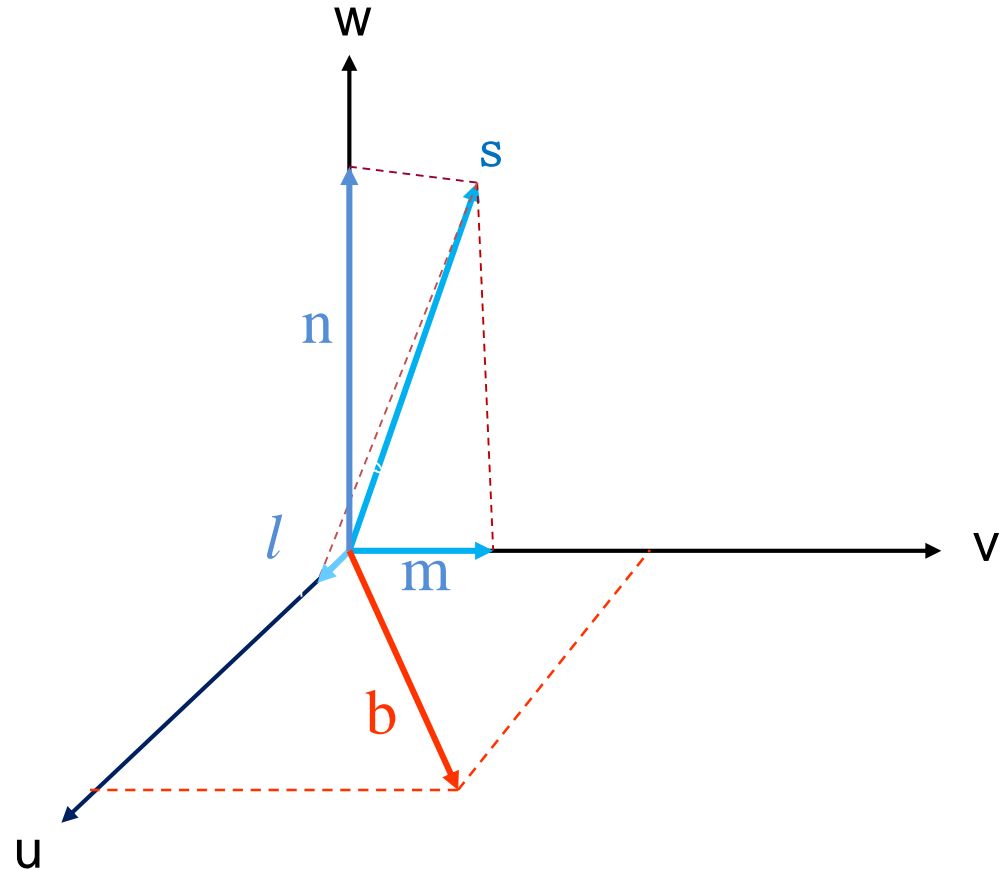
# Direction Cosines – describing the source

The unit direction vector  $\mathbf{s}$  is defined by its projections  $(l, m, n)$  on the  $(u, v, w)$  axes. These components are called the **Direction Cosines**.

$$l = \cos(\alpha)$$

$$m = \cos(\beta)$$

$$n = \cos(\theta) = \sqrt{1 - l^2 - m^2}$$



The angles,  $\alpha$ ,  $\beta$ , and  $\theta$  are between the direction vector and the three axes.

# The 2-d Fourier Transform Relation

Then,  $\mathbf{v} \cdot \mathbf{s}/c = ul + vm + wn = ul + vm$ , from which we find,

$$V_v(u, v) = \iint I(l, m) e^{-i2\pi(ul+vm)} dl dm$$

which is a **2-dimensional Fourier transform** between the brightness and the spatial coherence function (visibility):

$$I_v(l, m) \Leftrightarrow V(u, v)$$

And we can now rely on two centuries of effort by mathematicians on how to invert this equation, and how much information we need to obtain an image of sufficient quality.

Formally,

$$I_v(l, m) = \iint V_v(u, v) e^{i2\pi(ul+vm)} du dv$$

In physical optics, this is known as the ‘Van Cittert-Zernicke Theorem’.

# Interferometers with 2-d Geometry

- **Which interferometers can use this special geometry?**

- a) Those whose baselines, over time, lie on a plane (any plane).

- All E-W interferometers are in this group. For these, the  $w$ -coordinate points to the NCP.

- WSRT (Westerbork Synthesis Radio Telescope)
      - ATCA (Australia Telescope Compact Array) (before the third arm)
      - Cambridge 5km (Ryle) telescope (almost).

- b) Any coplanar 2-dimensional array, at a single instance of time.

- In this case, the ' $w$ ' coordinate points to the zenith.

- VLA or GMRT in snapshot (single short observation) mode.

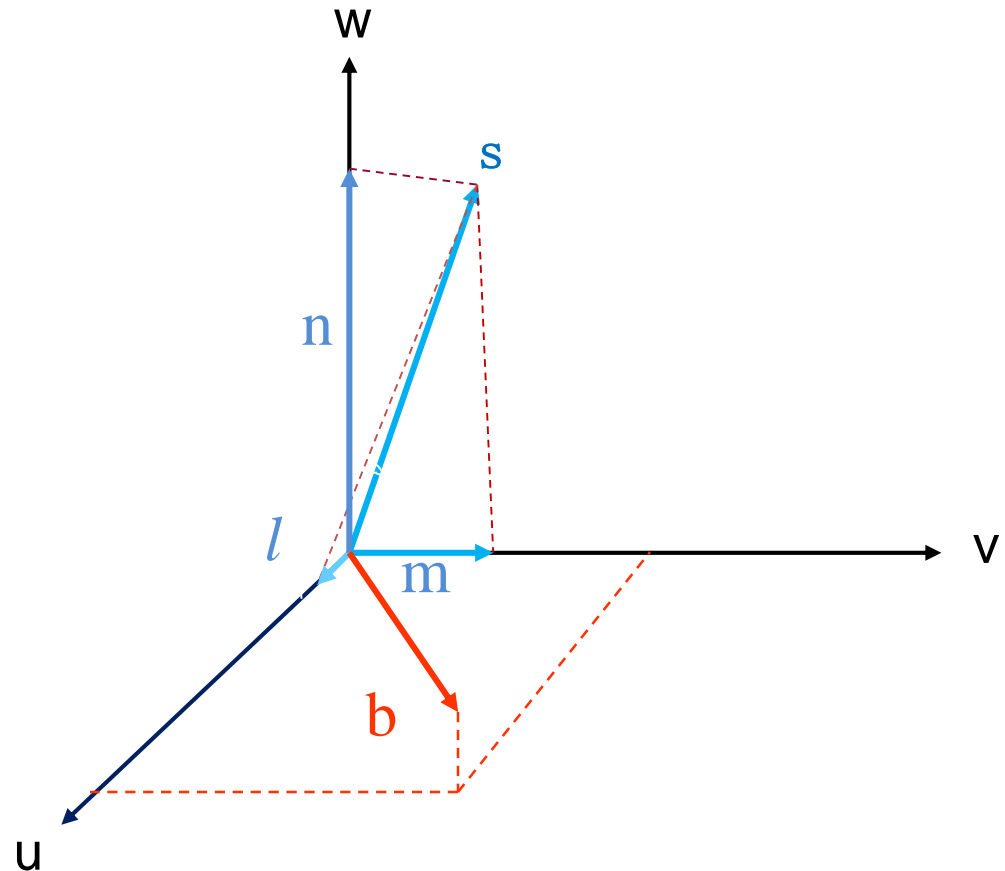
- **What's the 'downside' of 2-d ( $u,v$ ) coverage?**

- Resolution degrades for observations that are not in the  $w$ -direction.

- E-W interferometers have no N-S resolution for observations at the celestial equator.
    - A VLA snapshot of a source will have no 'vertical' resolution for objects on the horizon.

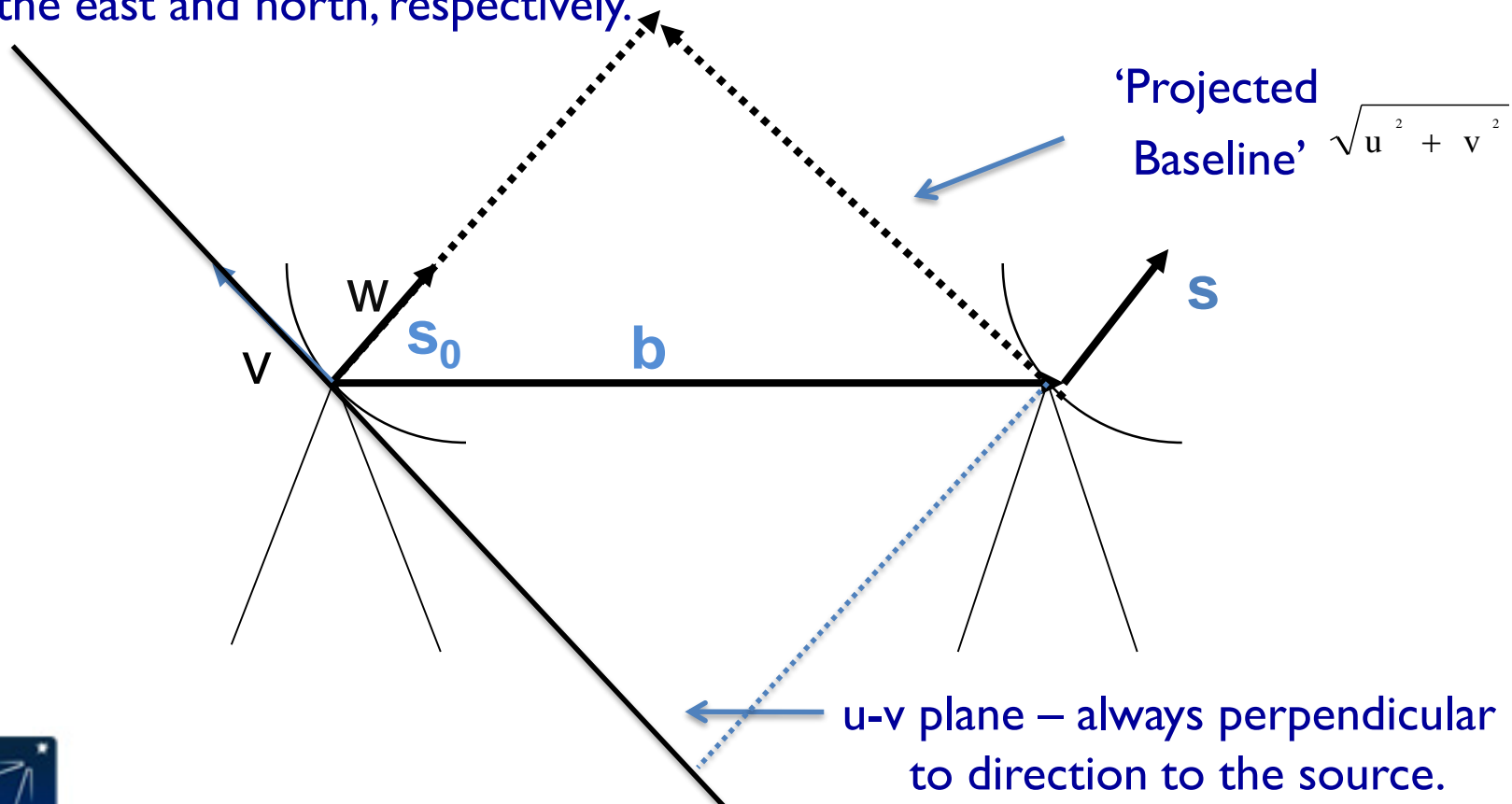
# Generalized Baseline Geometry

- Coplanar arrays (like the VLA) cannot use the 2-d geometry, since the plane of the array is rotating w.r.t. the source.
- In this case, we adopt a more general geometry, where all three baseline components are to be considered.



# General Coordinate System

- This is the coordinate system in most general use for synthesis imaging.
- **w** points to, and follows the source, **u** towards the east, and **v** towards the north celestial pole. The direction cosines  $l$  and  $m$  then increase to the east and north, respectively.





# 3-d Interferometers

## Case B: A 3-dimensional measurement volume:

- What if the interferometer does not measure the coherence function on a plane, but rather does it through a volume? In this case, we adopt a different coordinate system. First we write out the full expression:

$$V_v(u, v, w) = \iint I_v(l, m) e^{-2i\pi(ul+vm+wn)} dl dm$$

(Note that this is not a 3-D Fourier Transform).

- We orient the w-axis of the coordinate system to point to the region of interest. The u-axis point east, and the v-axis to the north celestial pole.
- We introduce phase tracking, so the fringes are 'stopped' for the direction  $l=m=0$ . This means we adjust the phases by  $e^{2i\pi w}$
- Then, remembering that  $n^2 = 1 - l^2 - m^2$  we get:

$$V_v(u, v, w) = \iint I_v(l, m) e^{-2i\pi[ul+vm+w(\sqrt{1-l^2-m^2}-1)]} dl dm$$

## 3-d to 2-d

- The expression is still not a proper Fourier transform.
- We can get a 2-d FT if the third term in the phase factor is sufficient small.

$$w\left(1 - \sqrt{1 - l^2 - m^2}\right) = w(1 - \cos \theta) \sim w\theta^2 / 2 \ll 1$$

- The third term in the phase can be neglected if it is much less than unity:
- This condition holds when:  $\theta_{\max} < \sqrt{\frac{1}{2w}} \sim \sqrt{\frac{\lambda}{B}} \sim \sqrt{\theta_{\text{syn}}}$   
(angles in radians!)
- If this condition is met, then the relation between the Intensity and the Visibility again becomes a 2-dimensional Fourier transform:

$$V'_v(u, v) = \iint I_v(l, m) e^{-2i\pi(ul+vm)} dl dm$$

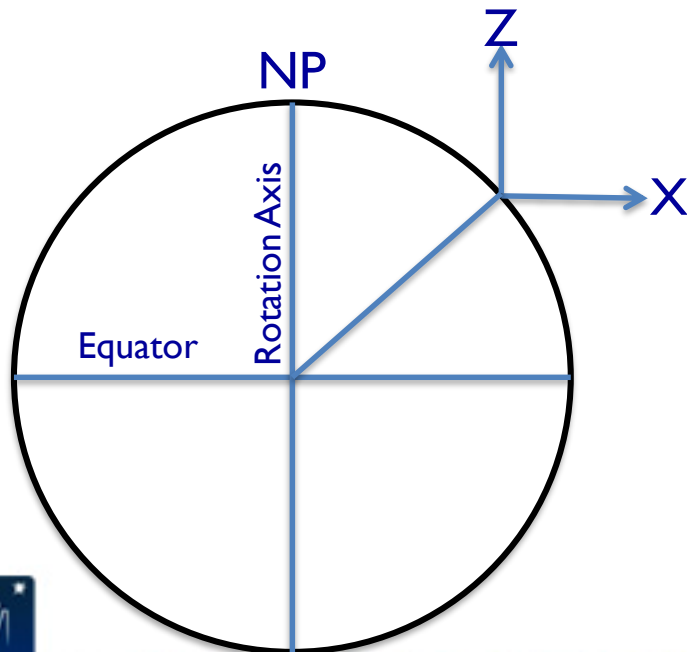
# The Problem with Non-coplanar Baselines

- Use of the 2-D transform for non-coplanar interferometer arrays (like the VLA, when used over time) always results in an error in the images.
- The ‘Clark Condition’ for trouble is:  $\frac{\lambda B}{D^2} > 1$
- Hence, the problem is most acute for small-diameter antennas ( $D$  small) long baselines ( $B$  large), and long wavelengths ( $\lambda$  large)
- The problems are not in the principles, but in the cost of the solutions. Full 3-D imaging works, but isn’t cheap.
- Implemented solutions include faceted imaging, and ‘W-Projection’.



# Coverage of the U-V Plane

- Obtaining a good image of a source requires adequate sampling ('coverage') of the (u,v) plane.
- Adopt an earth-based coordinate grid to describe the antenna positions:
  - X points to  $H=0, \delta=0$  (intersection of meridian and celestial equator)
  - Y points to  $H = -6, \delta = 0$  (to east, on celestial equator)
  - Z points to  $\delta = 90$  (to NCP).



- Thus,  $B_x, B_y$  are the baseline components in the Equatorial plane,
- $B_z$  is the baseline component along the earth's rotation axis.
- All components in wavelengths.
- $\delta_0$  and  $H_0$  are the declination and right ascension of the phase center.

# (u,v,w) Coordinates

- Then, it can be shown that

$$\begin{pmatrix} \mathbf{u} \\ \mathbf{v} \\ \mathbf{w} \end{pmatrix} = \begin{pmatrix} \sin H_0 & \cos H_0 & 0 \\ -\sin \delta_0 \cos H_0 & \sin \delta_0 \sin H_0 & \cos \delta_0 \\ \cos \delta_0 \cos H_0 & -\cos \delta_0 \sin H_0 & \sin \delta_0 \end{pmatrix} \begin{pmatrix} B_x \\ B_y \\ B_z \end{pmatrix}$$

- The u and v coordinates describe E-W and N-S components of the projected interferometer baseline.
- The w coordinate is the delay distance in wavelengths between the two antennas. The geometric delay,  $\tau_g$  is given by

$$\tau_g = \frac{\lambda}{c} w = \frac{w}{\nu}$$

- Its derivative, called the fringe frequency  $\nu_F$  is

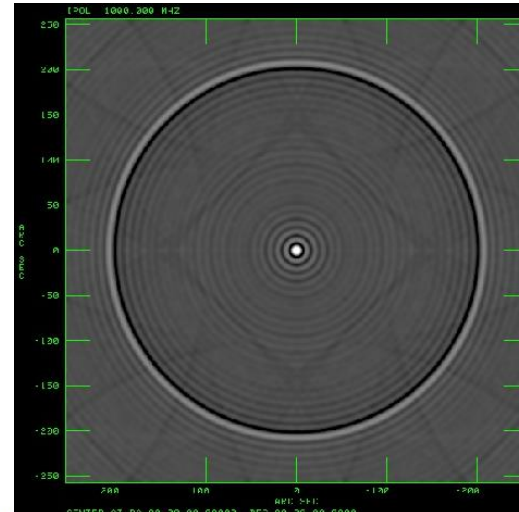
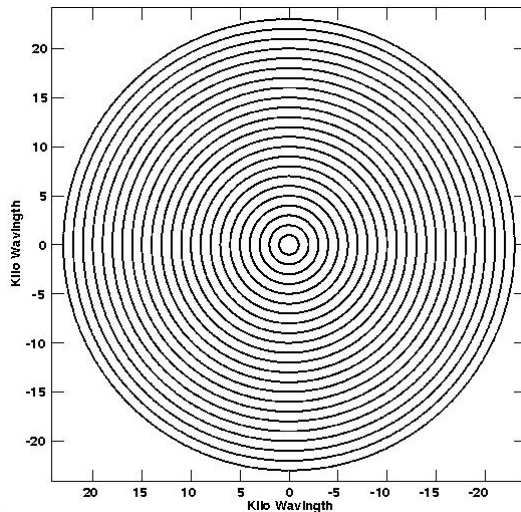
$$\nu_F = \frac{dw}{dt} = -\omega_E u \cos \delta_0$$

# E-W Array Coverage and Beams

- The simplest case is for E-W arrays, which give coplanar coverage.
- Then,  $B_x = B_z = 0$
- Consider a 'minimum redundancy array', with eight antennas located at 0, 1, 2, 11, 15, 18, 21 and 23 km along an E-W arm.

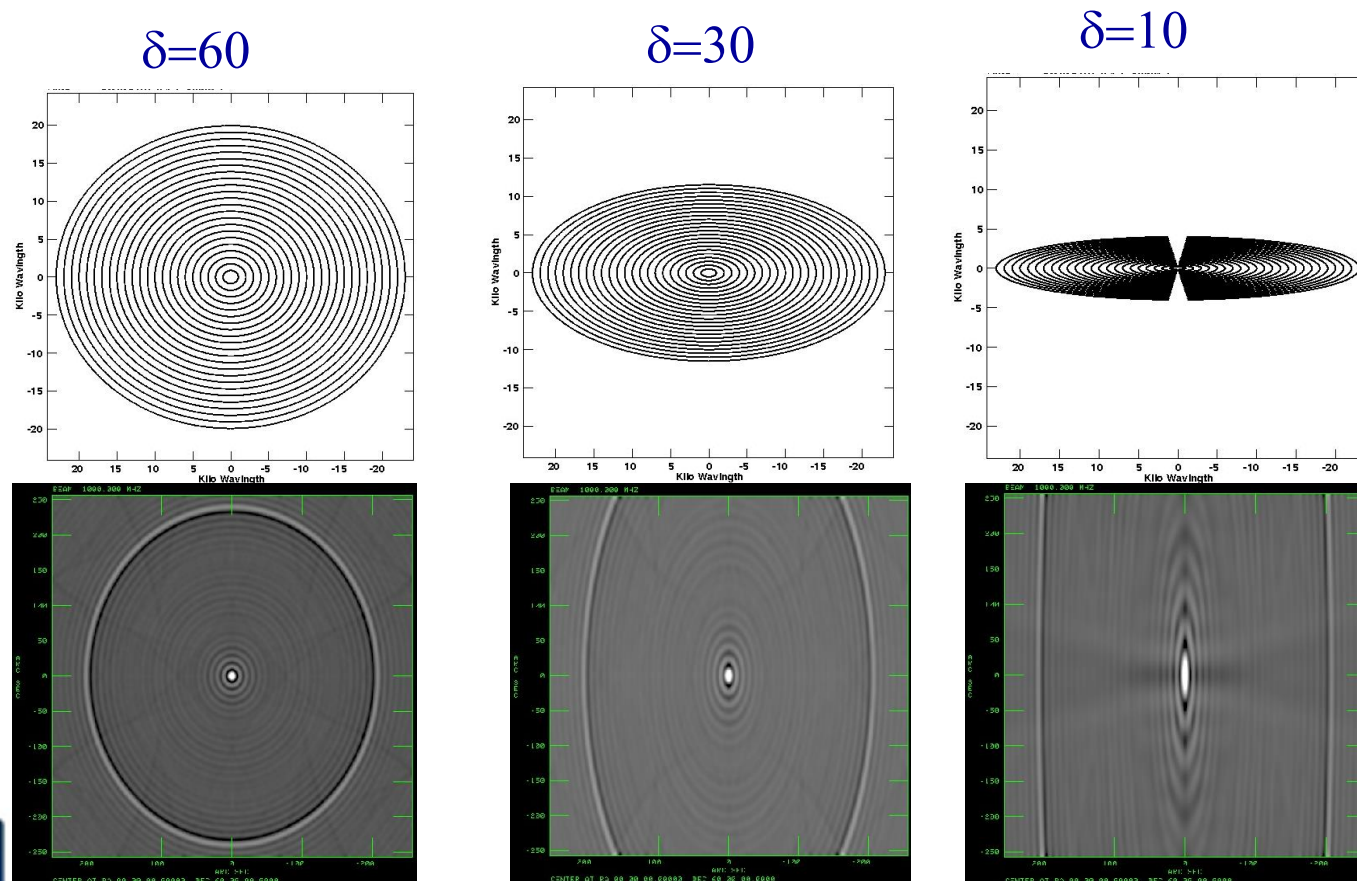


- Of the 28 simultaneous spacings, 23 are of a unique separation.
- The U-V coverage (over 12 hours) at  $\delta = 90$ , and the synthesized beam are shown below, for a wavelength of 1 m.



# E-W Arrays and Low-Dec sources.

- But the trouble with E-W arrays is that they are not suited for low-declination observing.
- At  $\delta=0$ , coverage degenerates to a line.



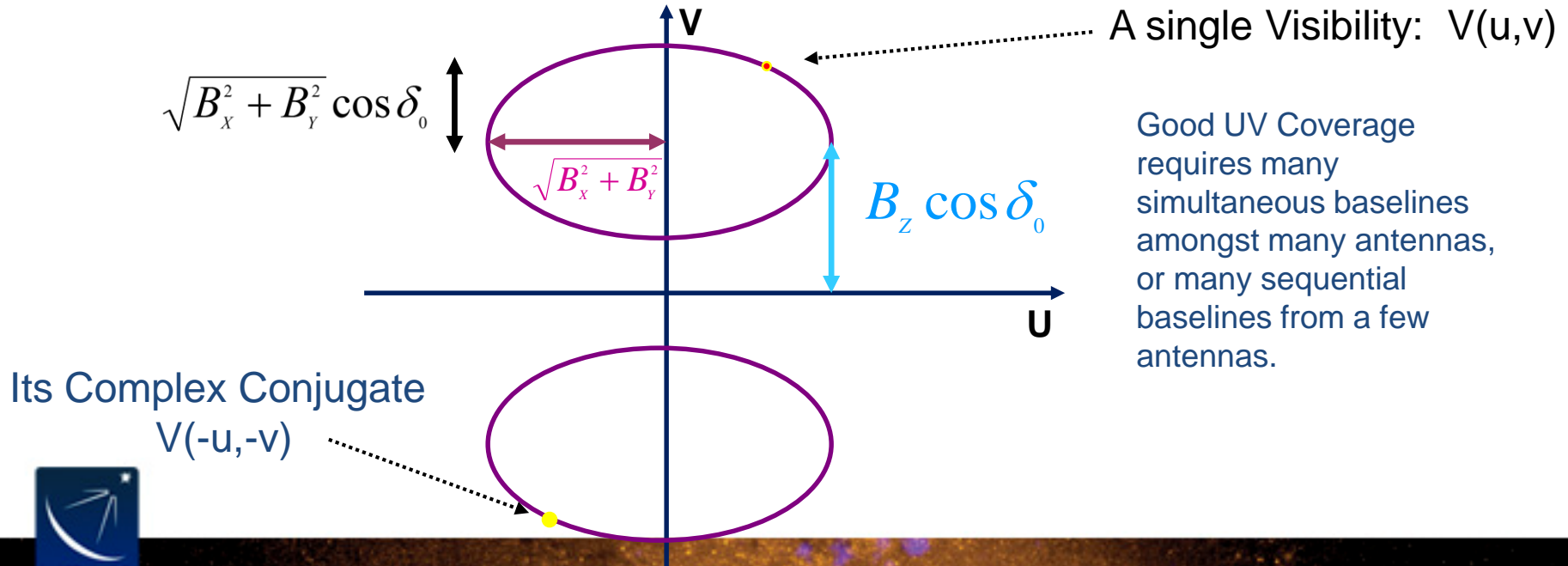


# Baseline Locus – the General Case

- Each baseline, over 24 hours, traces out an ellipse in the (u,v) plane:

$$u^2 + \left( \frac{v - B_z \cos \delta_0}{\sin \delta_0} \right)^2$$

- Because brightness is real, each observation provides us a second point, where:  $V(-u, -v) = V^*(u, v)$
- E-W baselines ( $B_x = B_z = 0$ ) have no 'v' offset in the ellipses.



Good UV Coverage requires many simultaneous baselines amongst many antennas, or many sequential baselines from a few antennas.





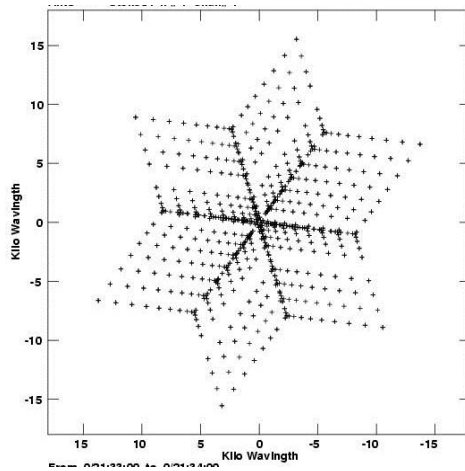
# Getting Good Coverage near $\delta = 0$

- The only means of getting good 2-d angular resolution at all declinations is to build an array with N-S spacings.
- Many more antennas are needed to provide good coverage for such geometries.
- The VLA was designed to do this, using 9 antennas on each of three equiangular arms.
- Built in the 1970s, commissioned in 1980, the VLA vastly improved radio synthesis imaging at all declinations.
- Each of the 351 spacings traces an elliptical locus on the (u,v) plane.
- Every baseline has some (N-S) component, so none of the ellipses is centered on the origin.

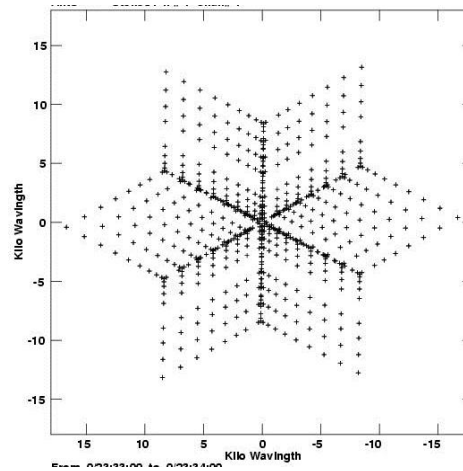


# Sample VLA (U,V) plots for 3C147 ( $\delta = 50$ )

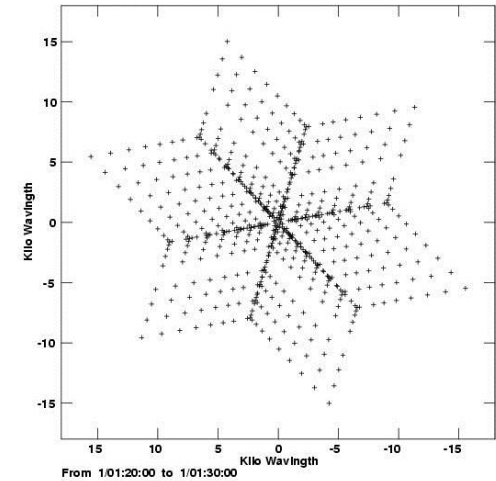
- Snapshot (u,v) coverage for HA = -2, 0, +2 (with 26 antennas).



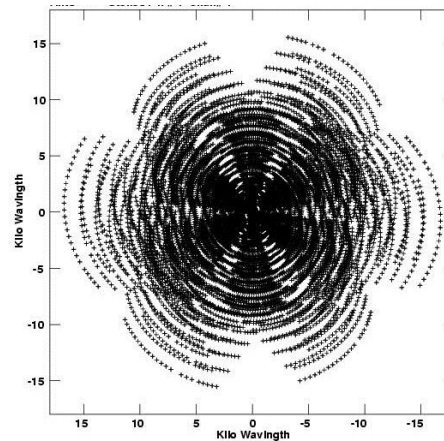
HA = -2h



HA = 0h

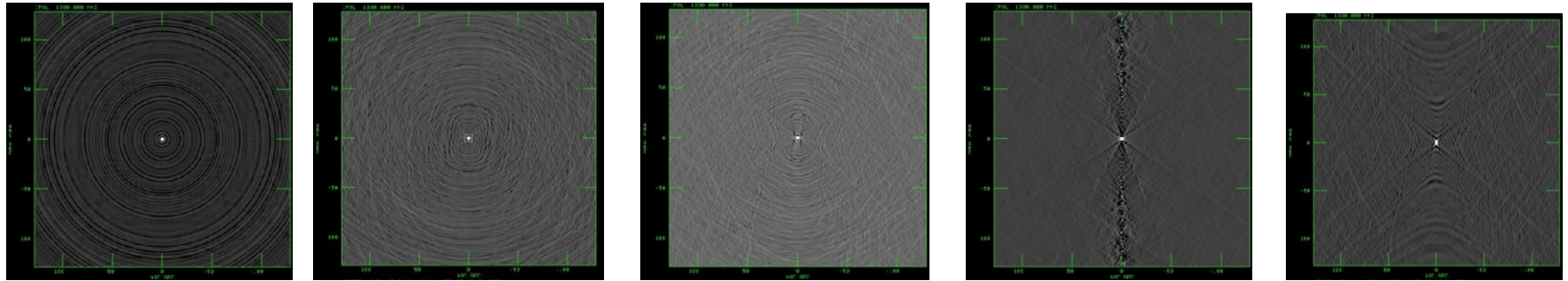
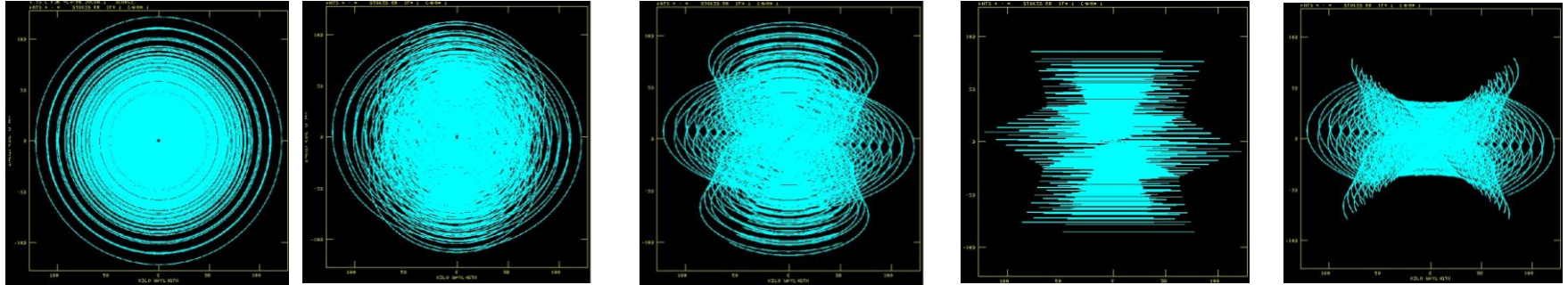


HA = 2h



Coverage over  
all four hours.

# VLA Coverage and Beams



$\delta=90$

$\delta=60$

$\delta=30$

$\delta=0$

$\delta=-30$

- Good coverage at all declinations, but troubles near  $\delta=0$  remain.



# UV Coverage and Imaging Fidelity

- Although the VLA represented a huge advance over what came before, its UV coverage (and imaging fidelity) is far from optimal.
- The high density of samplings along the arms (the 6-armed star in snapshot coverage) results in 'rays' in the images due to small errors.
- A better design is to 'randomize' the location of antennas within the span of the array, to better distribute the errors.
- Of course, more antennas would really help! :) .
- The VLA's wye design was dictated by its 220 ton antennas, and the need to move them. Railway tracks were the only answer.
- Future major arrays will utilize smaller, lighter elements which must not be positioned with any regularity.

