

GCMPCSC 266 - Formal Specification and Verification

Axiomatic Definition of Pascal

$$D0: \frac{x}{P \{x:=e\}P}$$

$$D1: \frac{P\{Q\}R, R \rightarrow T}{P\{Q\}T} \quad \frac{P\{Q\}R, T \rightarrow P}{T\{Q\}R}$$

$$D2: \frac{P\{Q1\}R1, R1\{Q2\}R}{P\{Q1;Q2\}R} \quad \frac{P_{i-1}\{S_i\}P_i \text{ for } i=1, \dots, n}{P0\{\text{begin } S1;S2; \dots; Sn \text{ end}\}Pn}$$

$$D3: \frac{P \& B\{S\}P}{P\{\text{while } B \text{ do } S\} \sim B \& P}$$

$$IF: \frac{P \& B\{S1\}Q, P \& \sim B\{S2\}Q}{P\{\text{if } B \text{ then } S1 \text{ else } S2\}Q} \quad \frac{P \& B\{S\}Q, P \& \sim B \rightarrow Q}{P\{\text{if } B \text{ then } S\}Q}$$

$$\frac{P \& B\{S1\}Q, P \& \sim B\{S2\}R}{P\{\text{if } B \text{ then } S1 \text{ else } S2\}Q|R}$$

$$CASE: \frac{P \& (x=k_i)\{S_i\}Q \text{ for } i=1, \dots, n}{x \in [k_1, \dots, k_n] \& P\{\text{case } x \text{ of } k_1:S1; \dots; k_n:S_n \text{ end}\}Q}$$

$$REPEAT: \frac{P\{S\}Q, Q \& \sim B \rightarrow P}{P\{\text{repeat } S \text{ until } B\}Q \& B}$$

Note: "&" is logical AND, "|" is logical OR, "~" is logical NOT, and "∈" is IS AN ELEMENT OF.