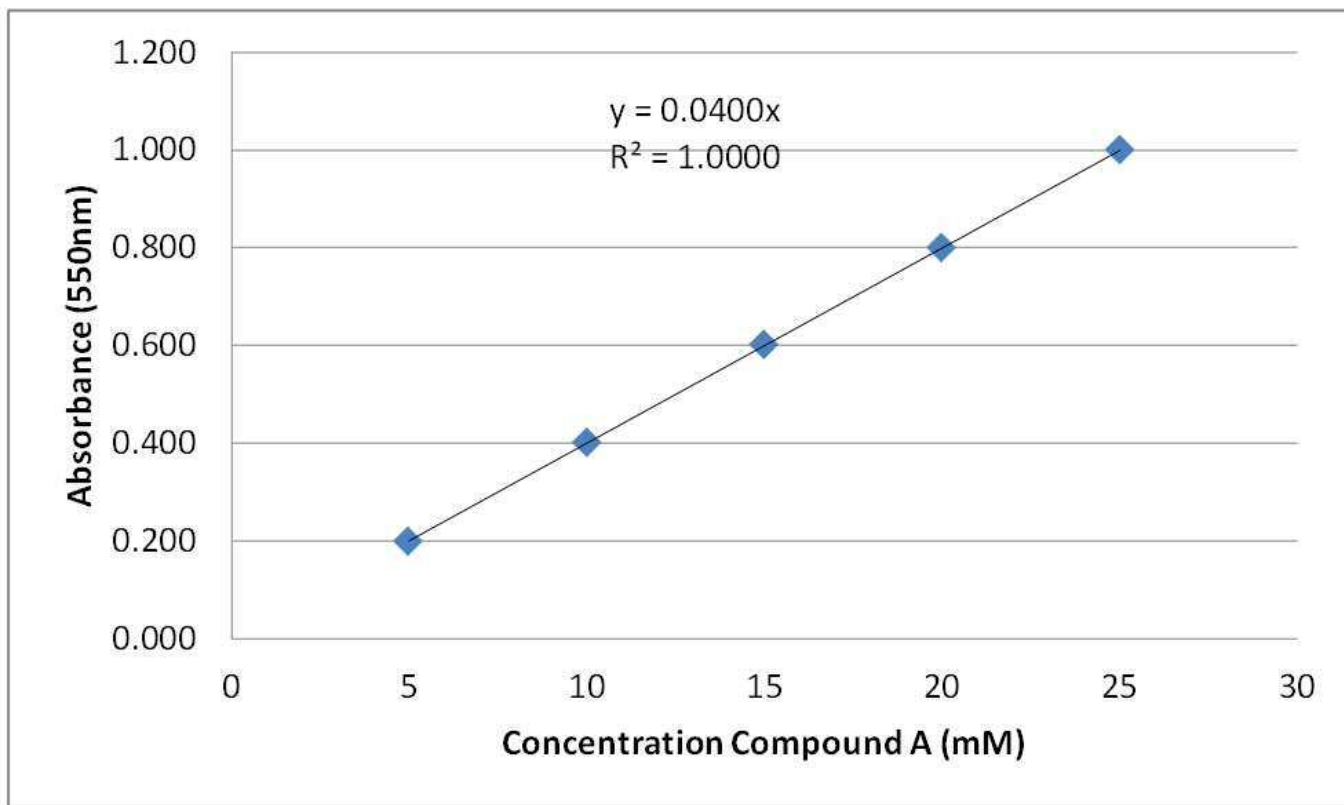


MOLAR ABSORPTIVITY

DETERMINING MOLAR ABSORPTIVITY COEFFICIENTS.

Suppose that we made a standard curve where the data obeys Beer's Law and fits a straight line. We should be able to calculate the molar absorptivity coefficient (ϵ).



Since $A = \epsilon bc$ and the graph is of A vs C (mM)

$A = (\epsilon b) c$ the slope is therefore equal to (ϵb) . We get the slope from the $y = 0.400x$.

In the above: slope = $0.0400 \text{ mM}^{-1} = \epsilon b$ where b is usually 1 cm (the pathlength of a cuvette)

Therefore we can calculate the value of ϵ :

$$\epsilon = (\text{slope} / b) = (0.0400 \text{ mM}^{-1} / 1 \text{ cm}) = 0.0400 \text{ mM}^{-1} \text{ cm}^{-1} \text{ or } 0.0400 \frac{L}{\text{mmoles cm}}$$

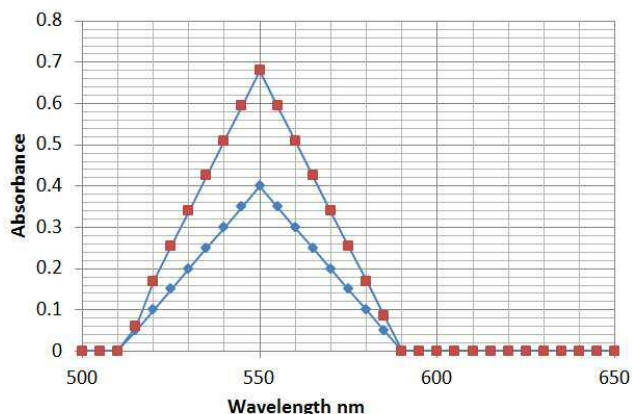
ϵ is most often written in $\text{M}^{-1} \text{ cm}^{-1}$

$$\text{so } \epsilon = 0.0400 \frac{L}{\text{mmoles cm}} \times \frac{1000 \text{ mmoles}}{\text{mole}} = 40.0 \frac{L}{\text{moles cm}} = 40.0 \text{ M}^{-1} \text{ cm}^{-1}$$

MOLAR ABSORPTIVITY

TWO COMPOUNDS ABSORBING AT THE SAME WAVELENGTH.

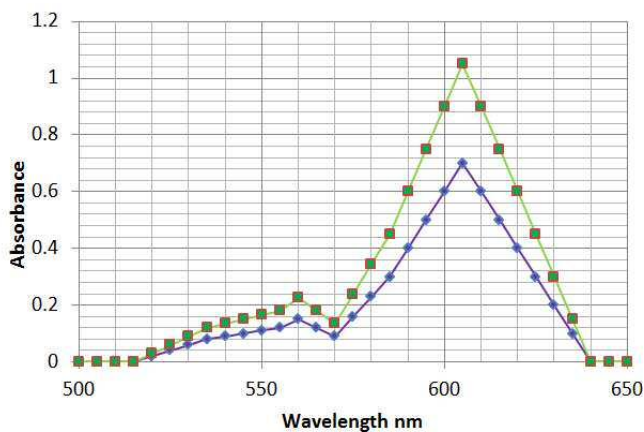
Suppose we took a scan of a sample containing 10.0 mM Compound A (blue dots) and a scan of a sample containing 17.0 mM Compound A (red dots).



We can see that this compound has a maximum wavelength at 550 nm (λ_{\max}). The higher the concentration, the greater the absorbance at 550nm. It does not absorb light above 600 nm at either concentration.

$$(\epsilon_{A,550\text{nm}} = 0.0400 \text{ L mmoles}^{-1} \text{ cm}^{-1})$$

$$(\epsilon_{A,605\text{nm}} = 0.000 \text{ L mmoles}^{-1} \text{ cm}^{-1})$$



Suppose we took a scan of 10.0 mM Compound B (blue) and a scan of 15.0 mM Compound B (green).

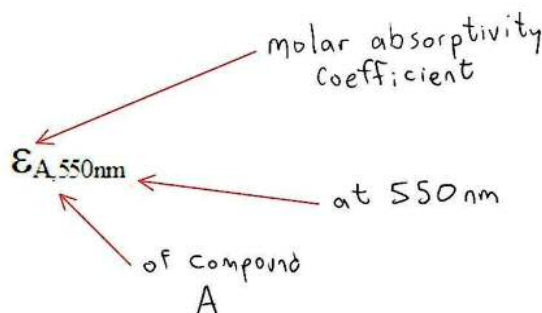
We can see that Compound B has a maximum wavelength (λ_{\max}) of 605 nm. It does absorb light below 600 nm, in the range of Compound A. The higher the concentration, the greater the absorbance at 550nm and 605nm.

$$(\epsilon_{B,605\text{nm}} = 0.0700 \text{ L mmoles}^{-1} \text{ cm}^{-1})$$

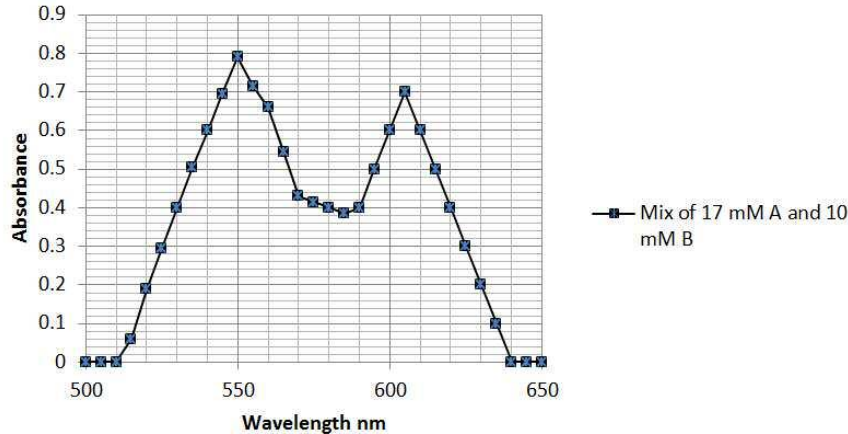
$$(\epsilon_{B,550\text{nm}} = 0.0110 \text{ L mmoles}^{-1} \text{ cm}^{-1})$$

** note usually a scan would have a curved appearance, the above scans are made up numbers for demonstration.

What does $\epsilon_{A,550\text{nm}}$ mean?



What happens if we have a mix of 17.0 mM A and 10.0 mM B in the same cuvette?
How do we calculate concentration of A and B using Beer's Law?



If we used the Absorbance at 605nm and used Beer's Law to determine Compound B using ($\epsilon_{B,605nm} = 0.0700 \text{ L mmoles}^{-1} \text{ cm}^{-1}$)

$$A = \epsilon bc$$

$$0.700 = (0.070 \text{ L mmoles}^{-1} \text{ cm}^{-1}) * (1\text{cm}) * (c)$$

$$c = 10.00 \text{ mM} = 10.0 \text{ mM}$$



We could determine the concentration of B at 605nm with $\epsilon_{B,605nm}$ alone because Compound A does not absorb at 605 nm. ($\epsilon_{A,605nm} = 0.000 \text{ L mmoles}^{-1} \text{ cm}^{-1}$)

If we used the Absorbance at 550nm and used Beer's Law to determine Compound A using ($\epsilon_{A,550nm} = 0.0400 \text{ L mmoles}^{-1} \text{ cm}^{-1}$)

$$A = \epsilon bc$$

$$0.790 = (0.040 \text{ L mmoles}^{-1} \text{ cm}^{-1}) * (1\text{cm}) * c$$

$$c = 19.75 \text{ mM} = 19.8 \text{ mM}$$

WRONG

19.8 mM would be our answer which is close to the actual, but we have overestimated the real value of 17.0 mM. The reason is because Compound B also absorbs at this wavelength. ($\epsilon_{B,550nm} = 0.0110 \text{ L mmoles}^{-1} \text{ cm}^{-1}$).

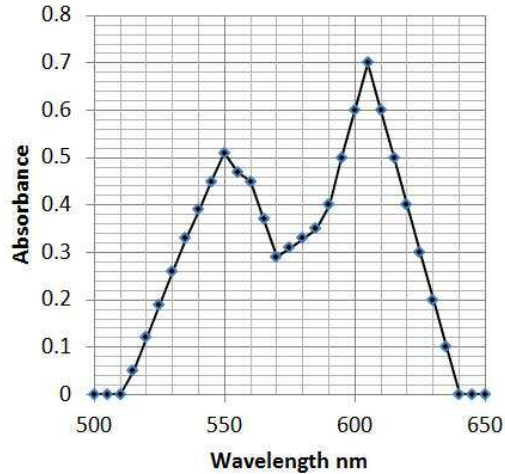
In reality you must add Beer's Law together for compound A and compound B at 550nm.

$$\begin{aligned} A_{550nm} &= \epsilon_{A,550nm}bc + \epsilon_{B,550nm}bc \\ &= (0.0400 \text{ L mmoles}^{-1} \text{ cm}^{-1} * 1\text{cm} * 17.0\text{mM}) + (0.0110 \text{ L mmoles}^{-1} \text{ cm}^{-1} * 1\text{cm} * 10.0\text{mM}) \\ &= 0.680 + 0.110 \\ &= 0.790 \end{aligned}$$



So what should you do to calculate the concentrations of Compound A and B when they are mixed??

Let's Try an Unknown



— Unknown mix of A and B

At 550 nm the mixed sample absorbs at 0.510. At 605 nm the mixed sample absorbs at 0.700. Since Compound A does not absorb at 605 nm ($\epsilon_{A,605nm} = 0.000 \text{ L mmole}^{-1} \text{ cm}^{-1}$), we should determine B's concentration first.

$$\begin{aligned}
 A_{605nm} &= 0.700 &= \epsilon_{A,605nm}bc_A + \epsilon_{B,605nm}bc_B \\
 &= 0.700 &= (0.000 \text{ L mmole}^{-1} \text{ cm}^{-1} * 1\text{cm} * c_A) + (0.0700 \text{ L mmole}^{-1} \text{ cm}^{-1} * 1\text{cm} * c_B) \\
 &= 0.700 &= 0 + (0.0700 \text{ L mmole}^{-1} \text{ cm}^{-1} * 1\text{cm} * c_B) \\
 &= 0.700 / (0.0700 \text{ L mmole}^{-1} \text{ cm}^{-1} * 1\text{cm}) = c_B
 \end{aligned}$$

$c_B = 10.0 \text{ mM}$ therefore concentration of Compound B is 10.0 mM

Compound A's concentration (c_A) is a little more difficult to determine, but since we now know B's concentration (c_B) to be 10.0 mM from the above calculation, we can determine A's next.

$$\begin{aligned}
 A_{550nm} &= 0.510 &= (\epsilon_{A,550nm} * b * c_A) + (\epsilon_{B,550nm} * b * c_B) \\
 &= 0.510 &= (0.0400 \text{ L mmole}^{-1} \text{ cm}^{-1} * 1\text{cm} * c_A) + (0.0110 \text{ L mmole}^{-1} \text{ cm}^{-1} * 1\text{cm} * 10.0\text{mM}) \\
 &= 0.510 &= (0.0400 \text{ L mmole}^{-1} \text{ cm}^{-1} * 1\text{cm} * c_A) + (0.110) \\
 &= 0.510 - 0.110 = (0.0400 \text{ L mmole}^{-1} \text{ cm}^{-1} * 1\text{cm} * c_A) \\
 &= 0.400 / (0.0400 \text{ L mmole}^{-1} \text{ cm}^{-1} * 1\text{cm}) = c_A
 \end{aligned}$$

$C_A = 10.0 \text{ mM}$ therefore concentration of Compound A is 10.0 mM.

Using multiple wavelengths in a Biochemical assay is fairly common.

- An example of this is in determining the purity of DNA. Samples are measured at 260nm and 280nm.
- Another example is the AlamarBlue assay which is used to determine cellular proliferation. This takes measurements at 570nm and 600nm.