


V. Biological Neural Networks

A. Overview

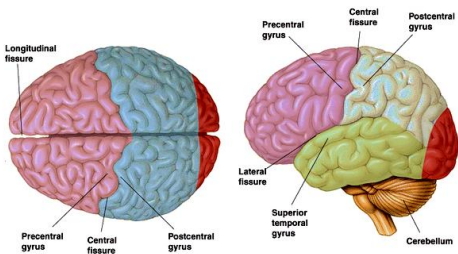
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A Very Brief Tour of Real Neurons




(and Real Brains)

► The Lobes of the Cerebral Hemispheres



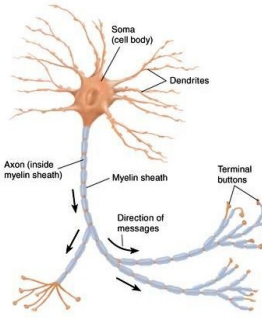
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Left Hemisphere



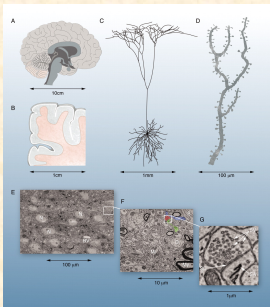
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Typical Neuron





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The brain is organized over sizes that span 6 orders of magnitude




J W Lichtman, W Denk Science 2011;334:618-623

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### Overview of Brain to Neurons



<<http://www.youtube.com/watch?v=DF04XPBj5uc>>


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### Animation of Neuron

- An animated film about nicotine addiction
- A good visualization of a single neuron
- ©2006, Hurd Studios
- Winner of NSF/AAAS Visualization Challenge
- [View flash video](#)

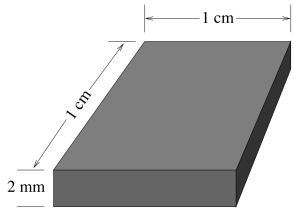
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### Grey Matter vs. White Matter



3/25/15 (fig. from Carter 1998) 9

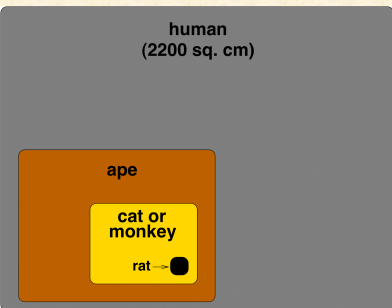
### Neural Density in Cortex



- 148 000 neurons / sq. mm
- Hence, about 15 million / sq. cm

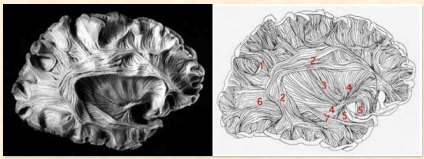
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### Cortical Areas



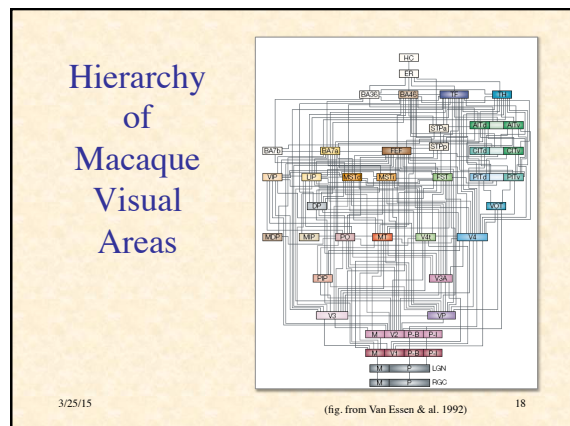
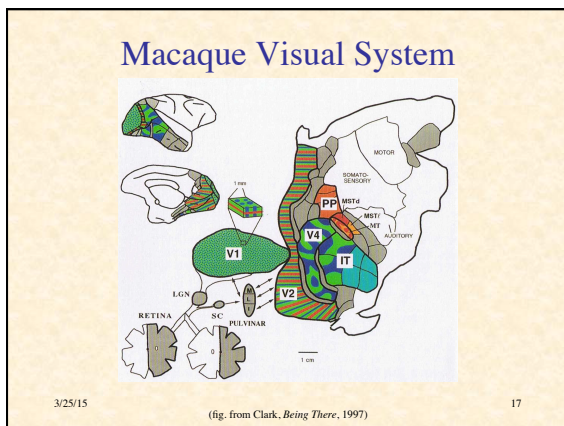
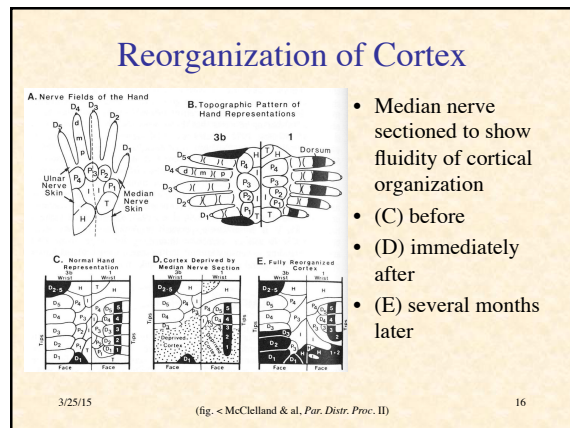
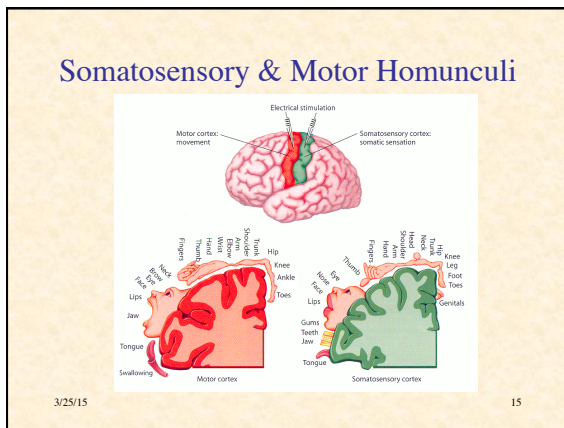
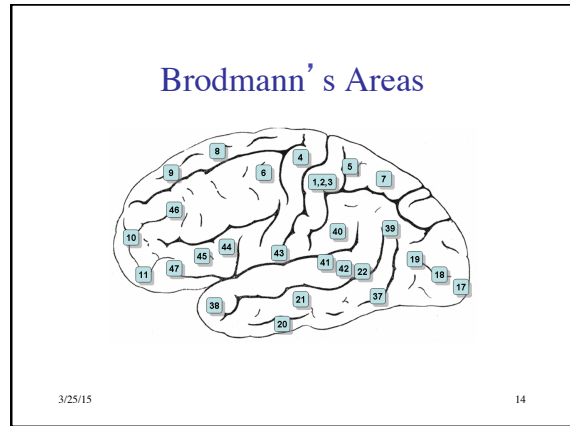
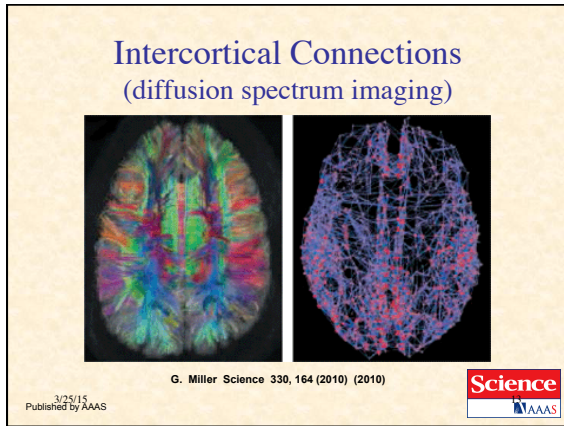
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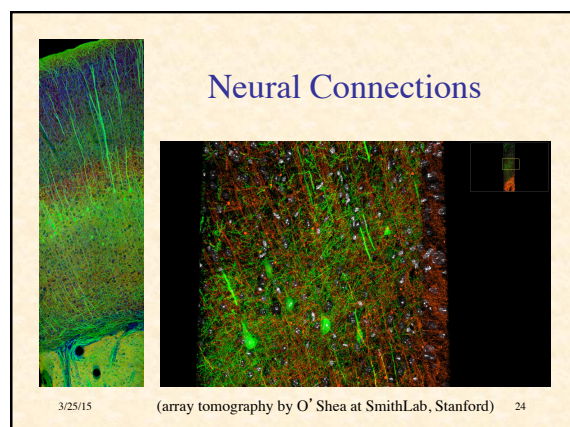
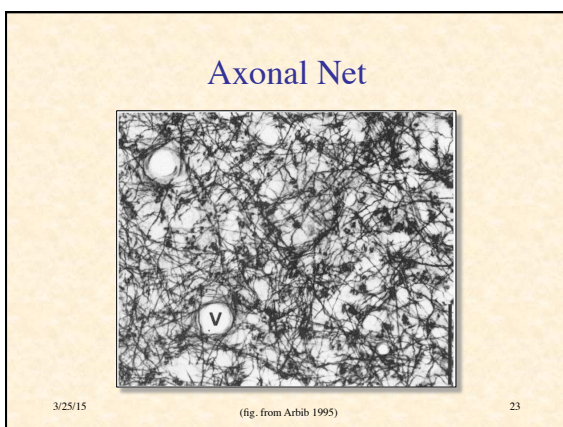
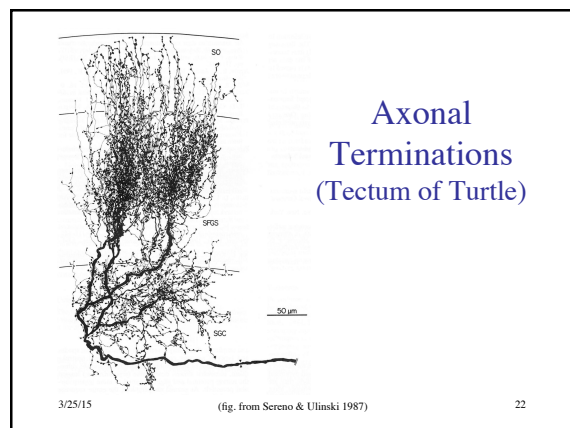
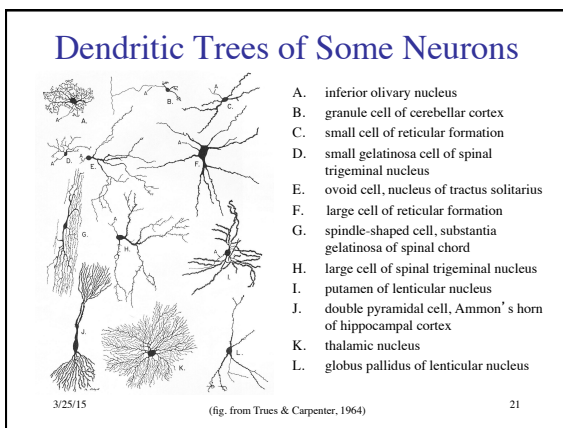
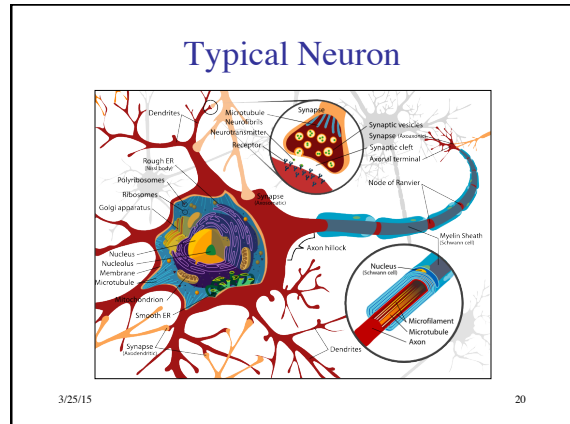
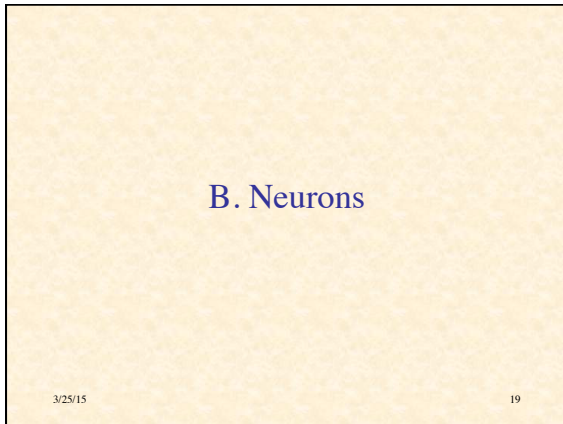
### Intercortical Connections



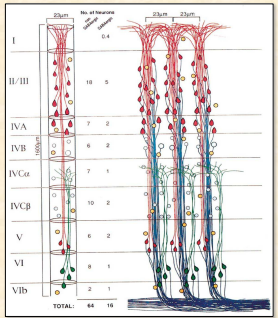
- (1) Short arcuate bundles, (2) Superior longitudinal fasciculus, (3) External capsule, (4) Inferior occipitofrontal fasciculus, (5) Uncinate fasciculus, (6) Sagittal stratum, (7) Inferior longitudinal fasciculus

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### Minicolumn

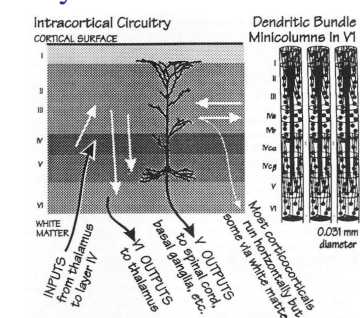


I	18	5
II/III	18	5
IVa	7	2
IVb	4	2
IVc	7	1
IVCb	10	2
V	6	2
VI	8	1
VIb	2	1
TOTAL	64	16

- Up to ~100 neurons
  - 75-80% pyramidal
  - 20-25% interneurons
- 20-50µ diameter
- Length: 0.8 (mouse) to 3mm (human)
- ~6x10<sup>5</sup> synapses
- 75-90% synapses outside minicolumn
- Interacts with 1.2x10<sup>5</sup> other minicolumns
- Mutually excitable
- Also called *microcolumn*

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### Layers and Minicolumns



**Intracortical Circuitry**  
CORTICAL SURFACE

**Dendritic Bundle Minicolumns in V1**  
0.025 mm diameter

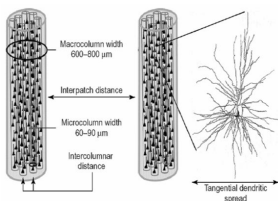
Inputs from thalamus to layer IV  
Y OUTPUTS basal ganglia, etc.  
X OUTPUTS normal via white matter

Most corticospinal axons run horizontally, but

WHITE MATTER

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(fig. from Arbib 1995, p. 270)

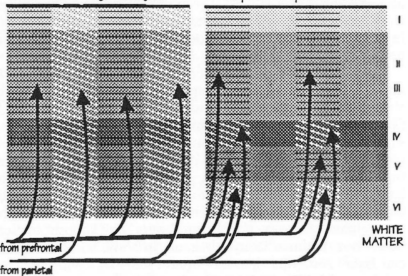
### Macrocolumns



- ~70 inhibitorily-coupled minicolumns in humans
- 70% of minicol. connections are within macrocol.
- Basket neurons provide shunting inhibition between minicolumns
- Winner-takes-all networks
- Represent microfeatures

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### Projection Macrocolumns 0.5-1.0mm wide



**Interdigitating Columns in Anterior Cingulate Gyrus**

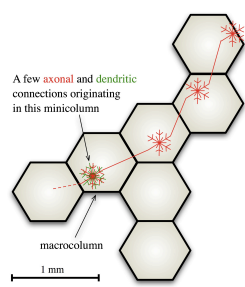
**Interleaving Input Columns in Superior Temporal Sulcus**

from prefrontal  
from parietal

WHITE MATTER

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(fig. from Arbib 1995, p. 270)

### Intracortical Connections



- Dendrites extend 2-4 minicol. diameters
- Axons extend 5x (or even 30-40x) minicol. diameter
- Periodic spacing of axon terminal clusters causes entrainment
- ~2x10<sup>7</sup> connections to macrocolumn

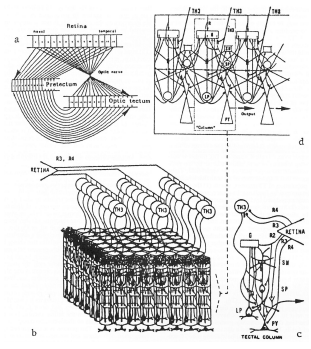
A few axonal and dendritic connections originating in this minicolumn

macrocolumn

1 mm

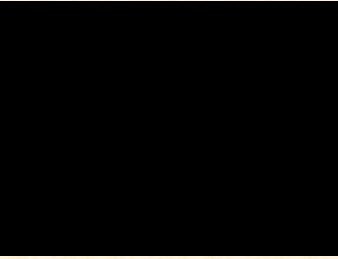
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### Neural Networks in Visual System of Frog



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(fig. from Arbib 1995, p. 1039)

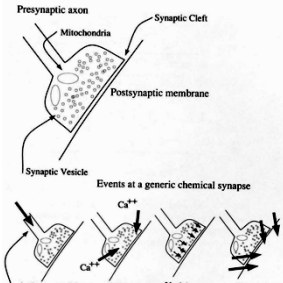
## Synapses



video by Hybrid Medical Animation

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## Chemical Synapse

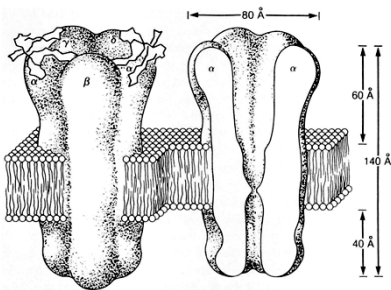


1. Action potential arrives at synapse
2. Ca ions enter cell
3. Vesicles move to membrane, release neurotransmitter
4. Transmitter crosses cleft, causes postsynaptic voltage change

(fig. from Anderson, *Intr. Neur. Nets*)

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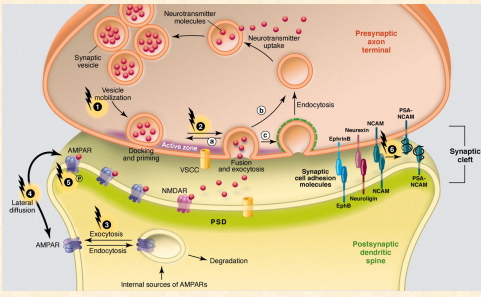
## Typical Receptor




(fig. from Anderson, *Intr. Neur. Nets*)

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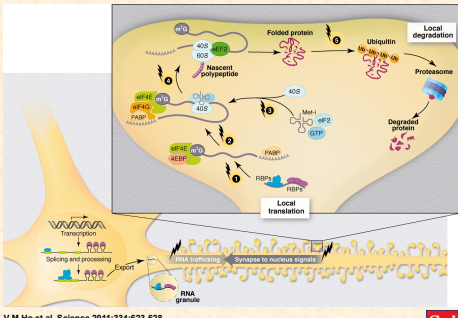
### Fig. 3 Activity-dependent modulation of pre-, post-, and trans-synaptic components.




V M Ho et al. *Science* 2011;334:623-628

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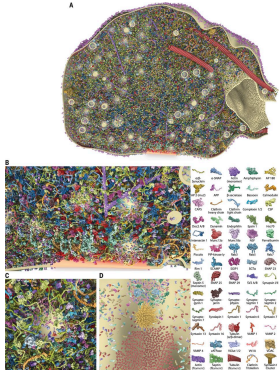
### Fig. 4 Local regulation of the synaptic proteome.



V M Ho et al. *Science* 2011;334:623-628


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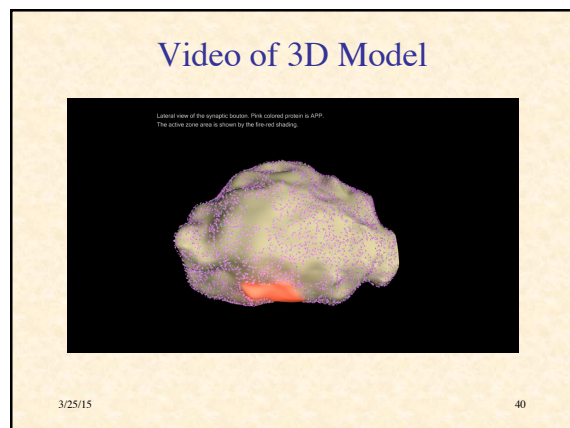
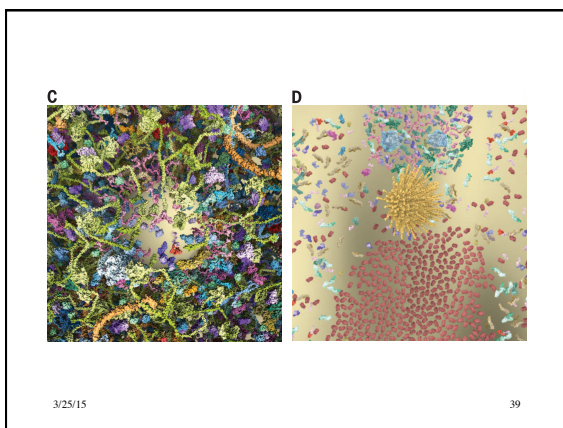
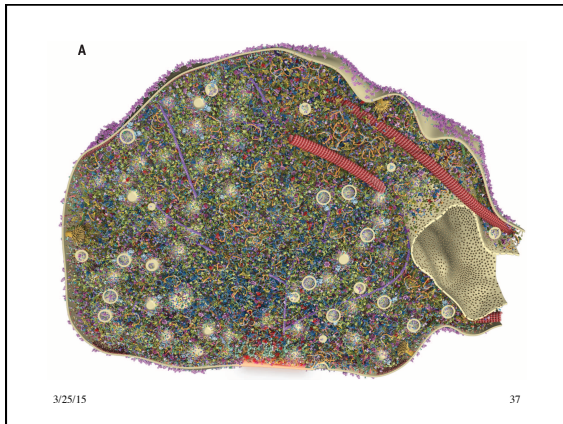
### Fig. 3: A 3D model of synaptic architecture.



- (A) A section through the synaptic bouton, indicating 60 proteins.
- (B) High-zoom view of the active zone area.
- (C) High-zoom view of one vesicle within the vesicle cluster.
- (D) High-zoom view of a section of the plasma membrane in the vicinity of the active zone. Clusters of syntaxin (yellow) and SNAP 25 (red) are visible, as well as a recently fused synaptic vesicle (top). The graphical legend indicates the different proteins (right). Displayed synaptic vesicles have a diameter of 42 nm.

B G Wilhelm et al. *Science* 2014;344:1023-1028

Published by AAAS 



### Input Signals

- Excitatory
  - about 85% of inputs
  - AMPA channels, opened by glutamate
- Inhibitory
  - about 15% of inputs
  - GABA channels, opened by GABA
  - produced by inhibitory interneurons
- Leakage
  - potassium channels
- Synaptic efficacy: net effect of:
  - presynaptic neuron to produce neurotransmitter
  - postsynaptic channels to bind it

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### Membrane Potential (Variables)

- $g_e$  = excitatory conductance
- $E_e$  = excitatory potential ( $\sim 0$  mV)
- $g_i$  = inhibitory conductance
- $E_i$  = inhibitory potential ( $-70$  mV)
- $g_l$  = leakage conductance
- $E_l$  = leakage potential
- $V_m$  = membrane potential
- $\theta$  = threshold

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### Membrane Potential

Currents:  $I_x = g_x(E_x - V_m)$ ,  $x = e, i, l$

Net current:  $I_{net} = I_e + I_i + I_l$

Change in membrane potential:  $\dot{V}_m = CI_{net}$  ( $C$  is rate constant)

$$\dot{V}_m = C[g_e(E_e - V_m) + g_i(E_i - V_m) + g_l(E_l - V_m)]$$

$$\text{Equilibrium } V_m = \frac{g_e E_e + g_i E_i + g_l E_l}{g_e + g_i + g_l}$$

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### Slow Potential Neuron

(fig. < Anderson, *Intr. Neur. Nets*)

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### Action Potential Generation

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### Frequency Coding

(fig. from Anderson, *Intr. Neur. Nets*)

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### Variations in Spiking Behavior

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### Dendritic computation in pyramidal cells.

T Branco Science 2011; 334:615-616  
Published by AAAS



### Rate Code Approximation

- Rate-coded (simulated) neurons:
  - short-time avg spike frequency  $\approx$
  - avg behavior of microcolumn (~100 neurons) with similar inputs and output behavior
- Rate not predicted well by  $V_m$
- Predicted better by  $g_e$  relative to a threshold value  $g_e^\theta$

3/25/15 (fig. < O'Reilly, *Comp. Cog. Neurosci.*) 49

### Rate Code Approximation

- $g_e^\theta$  is the conductance when  $V_m = \theta$ 

$$\theta = \frac{g_e^\theta E_e + g_i E_i + g_l E_l}{g_e^\theta + g_i + g_l}$$
- Rate is a nonlinear function of relative conductance
 
$$g_e^\theta = \frac{g_i (E_i - \theta) + g_l (E_l - \theta)}{\theta - E_e}$$
- What is  $f$ ?
 
$$y = f(g_e - g_e^\theta)$$

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### Activation Function

- Desired properties:
  - threshold (~0 below threshold)  $y = \frac{x}{x+1}$  where  $x = \eta [g_e - g_e^\theta]^+$
  - saturation  $y = \frac{1}{1 + \frac{1}{\eta [g_e - g_e^\theta]^+}}$
  - smooth
- Smooth by convolution with Gaussian to account for noise
- Activity update:
 
$$y_{t+1} = y_t + C(y - y_t)$$

3/25/15 (fig. < O'Reilly, *Comp. Cog. Neurosci.*) 51