Systems-level physiology of the human red blood cell is computed from metabolic and macromolecular mechanisms

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ABSTRACT

The human red blood cell has served as a starting point for the application and development of systems biology approaches due to its simplicity, intrinsic experimental accessibility, and importance in human health applications. Here, we present a multi-scale computational model of the human red blood cell that accounts for the full metabolic network, key proteins (>95% of proteome mass fraction), and several macromolecular mechanisms. Proteomics data are used to place quantitative constraints on individual protein complexes that catalyze metabolic reactions, as well as a total proteome capacity constraint. We explicitly describe molecular mechanisms—such as hemoglobin binding and the formation and detoxification of reactive oxygen species—and takes standard hematological variables (e.g., hematocrit, hemoglobin concentration) as input, allowing for personalized physiological predictions. This model is built from first principles and allows for direct computation of the flux state of the metabolic network. More broadly, this work represents an important step toward including the proteome and its function in whole-cell models of human cells.

INTRODUCTION

The blood is a window through which we can explore human health and disease [50]. The human red blood cell (RBC)—the most abundant human cell [46]—has historically been used as the starting point for the application and development of systems biology models due to its relative simplicity, intrinsic accessibility, and the vast amounts of data and information available on its biochemistry and physiology [52]. While the RBC lacks cellular compartments and the ability to produce energy using oxidative phosphorylation, it is heavily involved in the transport and exchange of gases throughout the body, including O₂, CO₂ [17], and NO [15]. The ability to model and compute physiological states of the RBC is thus crucial to our understanding of how our blood performs vital systems-level functions.

Since the 1970s, mathematical models have been used to study the dynamics of RBC metabolism [42]. Other modeling formalisms, like constraint-based modeling methods [51], have been used to study mechanisms underlying cellular metabolism [8, 38, 53]. These constraint-based methods have evolved to allow for the study of system dynamics [27, 48, 9], although kinetic models are best suited to exploring temporal dynamics at short time scales [20]. From the first whole-cell kinetic model of RBC metabolism in the

KEYWORDS

Systems biology Metabolism Human red blood cell Hemoglobin binding ROS detox

late 1980s [22, 23, 24, 25], researchers have examined various aspects of RBC metabolism through kinetic modeling including regulatory network structure [41], the role of 2,3-diphosphoglycerate (2,3-DPG) in binding hemoglobin [32, 34, 33], hereditary glucose-6-phosphate dehydrogenase (G6PDH) deficiency [35], and personalized pharmacodynamics [7]. There lies a gap, however, between what can be computationally modeled using kinetic approaches (limited by parameterization and network scale) and constraint-based approaches (limited by the completeness of the network structure).

Here, we address this gap with the development of a wholecell model of the metabolism of the human Red Blood Cell and Macromolecular Mechanisms (RBC-MM). This model is built from first principles and uses kinetic and thermodynamic constraints to represent macromolecular mechanisms such as O2 and CO2 binding to hemoglobin and the detoxification of reactive oxygen species (ROS). Further, we account for the limitation to maximum reaction velocity due to finite enzyme abundance and effective turnover rate through the integration of recently published targeted proteomic data [10]. We validate our model against previous computational models and experimental data, demonstrating the ability of the RBC-MM to compute physiologically meaningful quantities and phenotypes, such as the oxygen dissociation curve (ODC). We anticipate that the computational modeling framework presented here will help usher in a new frontier in metabolic modeling that integrates non-metabolic mechanisms to better represent

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the functions of complex biological systems.

RESULTS

We begin by detailing the construction and scope of the RBC-MM model. We then proceed to demonstrate its simulation capacity, providing validation of various computed phenotypes and quantities. Finally, we compute systems-level properties of the RBC network.

Model construction

The RBC-MM model is constructed starting from the iAB-RBC-283 metabolic network reconstruction of RBC metabolism. iAB-RBC-283 represents a knowledgebase which includes 283 metabolic genes, 292 reactions, and 267 metabolites [6]. These metabolites include small molecules, cofactors, and trace minerals. For a model having *n* reactions and *m* metabolites, flux balance analysis (FBA) [39] computes the optimal metabolic state of a cell. A metabolic state is defined by a vector of reaction fluxes $v \in \mathbb{R}^n$ (in mmol/gDW/h), by solving the linear program:

maximize
$$c^T v$$
 subject to $Sv = 0, l \le v \le u$, (1)

where $c \in \mathbb{R}^n$ is the vector of objective coefficients, $S \in \mathbb{R}^{m \times n}$ is the matrix of reaction stoichiometries, and $l \in \mathbb{R}^n$, $u \in \mathbb{R}^n$ are the lower and upper bounds on the fluxes.

We have expanded this model to account for macromolecules present in the RBC (Figure 1). Specifically, we (*i*) account for the limitation to maximum reaction rate due to finite enzyme abundance and effective turnover rate and (*ii*) limited total protein mass in a cell. We implement these constraints in a manner similar to previous methods [3, 2]. The FBA problem associated with this expanded model is called protein-constrained FBA ($P_{con}FBA$) [36].

In addition to fluxes, $P_{con}FBA$ also computes enzyme complex concentrations $e \in \mathbb{R}^r$ (in mmol/gDW), and protein concentrations $p \in \mathbb{R}^s$ (in mmol/gDW). We constrain the total protein mass (*P*) using the molecular weight of each protein (*w*). Each protein concentration is constrained by the measured concentration (Φ), while accounting for measurement error (ϵ). Protein concentrations are also constrained by enzyme complex stoichiometry (*a*). Given the above constraints, the P_{con}FBA problem is formulated as follows:

$$\underset{e,p,v}{\text{maximize}} \quad c^{\mathrm{T}}v \tag{2}$$

subject to
$$\mathbf{S} \cdot \mathbf{v} = 0$$
, (3)

$$\sum_{k} w_k p_k \le P,\tag{4}$$

$$p_k \le \Phi_k^{\text{meas}} + \epsilon, \quad \forall k,$$
 (5)

$$p_k \ge \Phi_k^{\text{meas}} - \epsilon, \quad \forall k,$$
 (6)

$$v_j \le \sum_{l \in \text{CPLX}(j)} e_l k_{j,l}^{\text{eff}}, \tag{7}$$

$$p_k = \sum_{l \in \text{CPLX}(p_k)} a_{k,l} e_l, \tag{8}$$

$$p_k, v_j \ge 0, \quad \forall j, k,$$
 (9)

where CPLX(j) is the index set of reactions that are catalyzed by enzyme complex *j*, and $k_{j,l}^{eff}$ is the effective rate constant for the reaction *l* being catalyzed by enzyme *j*. The model includes quantitative constraints for 306 biochemical reactions and accounts for 2,653 total proteins using published proteomic data [10].

Next, we mathematically extend this protein-constrained model with key molecular mechanisms that describe RBC physiology.

Hemoglobin mechanisms. The RBC plays a vital role in the respiratory function of blood, delivering dissolved oxygen and oxygen bound to hemoglobin (oxyhemoglobin) from the lungs to the tissues [17]. In return, tissues transport CO₂ back to the lung, where carbonic anhydrase converts biocarbonate into CO₂ and H₂O. The CO₂ can be transported dissolved in the blood or can be bound to hemoglobin, depending on the concentration of O₂ and CO₂ in the blood [29]. The Bohr Effect [44, 4] describes how the ODC shifts based on the concentrations of CO₂ and protons affect the affinity of hemologlobin for O₂; the Haldane Effect describes how the ODC shifts based on the concentration of O₂ affects the affinity of hemoglobin for CO₂ and protons. The ODC is also dependent upon the intracellular of 2,3-diphosphoglycerate (2,3-DPG), a glycolytic intermediate and competitive inhibitor of oxygen binding to Hb [28].

We model the kinetics of hemoglobin (Hb) binding with oxygen, carbon dioxide, and 2,3-DPG. We use a cooperative mechanism (i.e., the affinity for oxygen increases with more bound oxygen) with allosteric inhibition by 2,3-DPG [40]. We model the binding of CO₂ to Hb to account for the Bohr Effect. Here we use the notation Hb_i^* to denote a relaxed (i.e., active) form *i* of Hb and the notation Hb^{\dagger} to denote a tense (i.e., inactive) form; *i* indicates the number of oxygen species bound to Hb. The full reaction schema (Figure 1C) is detailed below:

$$\mathbf{H}\mathbf{b}_0^* + \mathbf{O}_2 \rightleftharpoons \mathbf{H}\mathbf{b}_1^* \tag{10}$$

$$\mathbf{Hb}_{1}^{*} + \mathbf{O}_{2} \rightleftharpoons \mathbf{Hb}_{2}^{*} \tag{11}$$

$$\mathbf{Hb}_{2}^{*} + \mathbf{O}_{2} \rightleftharpoons \mathbf{Hb}_{3}^{*} \tag{12}$$

$$\mathbf{Hb}_{3}^{*} + \mathbf{O}_{2} \rightleftharpoons \mathbf{Hb}_{4}^{*} \tag{13}$$

$$\mathbf{Hb}_0^* + 23\mathrm{DPG} \rightleftharpoons \mathbf{DHb}^\dagger \tag{14}$$

$$\mathbf{Hb}_{i}^{*}(\mathrm{CO}_{2})_{j} + \mathrm{CO}_{2} \rightleftharpoons \mathbf{Hb}_{i}^{*}(\mathrm{CO}_{2})_{j+1}$$
(15)

$$\mathbf{Hb}_{i}^{*} + \mathbf{H}^{+} \rightleftharpoons \mathbf{Hb}_{i}^{*} - \mathbf{H}^{+}$$
(16)

where $i \in \{0, 1, 2, 3, 4\}$ represents the number of bound O₂ molecules and $j \in \{0, 1, 2, 3\}$ represents the number of bound CO₂ molecules. To model these Hb binding kinetics, we introduce additional variables for the concentrations of Hb (all possible bound states), O₂, CO₂, 2,3-DPG, H₂O, OH⁻, and H⁺.

Generation and detoxification of reactive oxygen species (ROS). Hb in its alternative oxygen-bound forms is prone to autooxidation [30], resulting in the formation of ROS. We reconstructed and included the following ROS generation reactions that involved Hb [43] (Figure 1D) in the RBC-MM model:

$$\mathbf{Hb}_{2}^{*} \to \mathbf{Hb}_{1}^{*} + \mathbf{O}_{2}^{\cdot -} \tag{17}$$

$$O_2^{\cdot-} \rightarrow H_2O_2$$
 (18)

$$\mathbf{Hb}_{1}^{*} + \mathrm{H}_{2}\mathrm{O}_{2} \rightarrow \mathbf{Hb}(\mathrm{IV}) = \mathrm{O}$$

$$\tag{19}$$

$$\mathbf{Hb}(\mathrm{IV}) = \mathrm{O} + \mathrm{H}_2\mathrm{O}_2 \to \mathbf{Hb}(\mathrm{III}) \cdot \mathrm{O}_2^{-}$$
(20)

$$Hb(III)-O_2^{\cdot-} \rightarrow Heme degradation + Fe(III)$$
 (21)

where the heme degradation product results in membrane damage, particularly observed in senescent RBCs [43]. Further, we explicitly model ROS detoxification through superoxide dismutase (Equation 22) and catalase (Equation 23):

$$2 H^+ + 2 O_2^{-} \rightarrow H_2 O_2 + O_2$$
 (22)

$$2 H_2O_2 \rightarrow 2 H_2O + O_2$$
 (23)

where the rate of both reactions is extremely high [1, 43].

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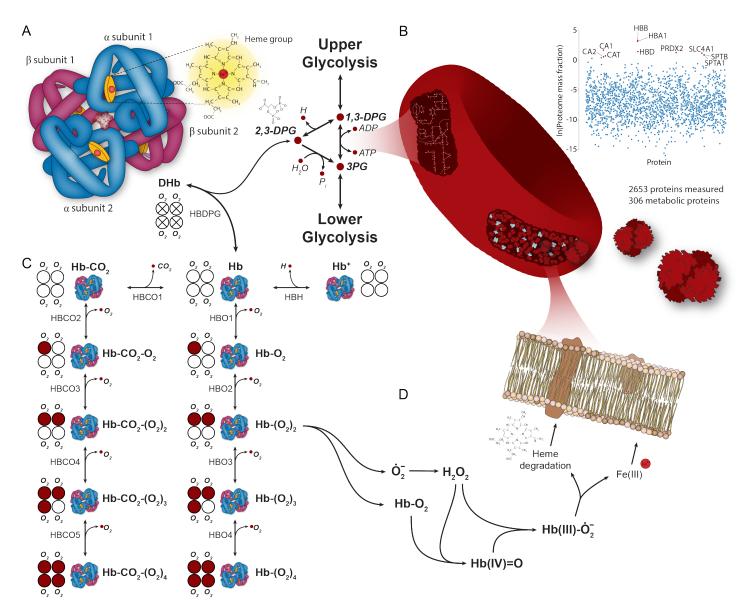


Fig. 1 Overview of the RBC-MM model's scope, including (**A**) integration of Hb reactions with the metabolic network, (**B**) quantitative protein constraints and crowding constraints (measured data from [10]), (**C**) Hb binding reactions, and (**D**) ROS detox mechanisms.

Model simulation

The modeling formalism described above for the RBC-MM model is built from first principles and takes a number of typically measured hematological variables as input (Table 1).

Computing the oxygen dissociation curve. We validated the physiological utility of the RBC-MM model by computing the oxygen dissociation curve (ODC) and comparing it to experimentally measured values. We explored three primary validations (Figure 2): (*i*) simulation of the ODC for nominal physiological values, (*ii*) qualitatively reproducing the Bohr Effect, and (*iii*) quantitatively recapitulating measured shifts due to varying concentrations of 2,3-DPG. We computed the curve using nominal baseline parameter values for the model (Table 1) according to the equation:

% saturation =
$$\frac{O_2 \text{ occupancy}}{O_2 \text{ capacity}} \times 100$$
 (24)

where the occupancy and capacity represent all binding states of Hb. We found that the curve is highly sensitive to the K_{eq} values

used for the binding of Hb to various substrates. To examine this behavior, we used values from the literature [13, 19] and also fit the those parameters to measured data [47] (Figure 2A). It is not surprising that simulations using literature parameterization does not match measured data due to the differences between *in vitro* and *in vivo* K_{eq} values (see Supplemental Data).

Next, we tested the model's ability to qualitatively reproduce the Bohr Effect—i.e., a shift of the ODC to the left with increasing pCO_2 (Figure 2B). We observed that the model did indeed reproduce this behavior, matching the same qualitative trends previously observed from Hill-type models [14, 13].

We then tested the model's ability to recapitulate the welldescribed dependence of the ODC on the intracellular concentration of 2,3-DPG [31, 26, 16]. We parameterized the model with measured values [16] using the reported hematocrit (40%), pH (7.195), and Hb concentration (14.75 g/dL blood); the osmotic coefficient of Hb [45] was used to convert the reported Hb concentrations. We performed a sweep across the five different concen-

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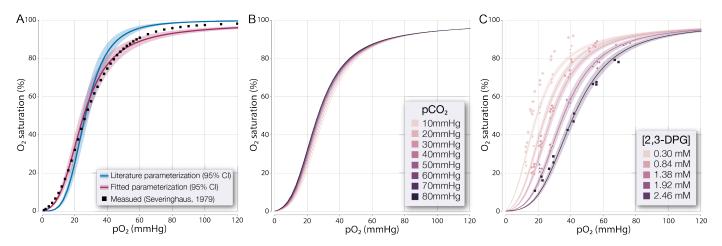


Fig. 2 Computation of the oxygen dissociation curve (ODC). (**A**) Baseline computation for physiological values; measured data from [47]. (**B**) Computing the Bohr Effect demonstrates the expected qualitative shift of the ODC to the left with increasing pCO₂. (**C**) Computing the effect of varying 2,3-DPG concentrations on the ODC; measured data from [16].

Table 1 Input parameters for the RBC-MM model; defaults are set according to literature values for hemoglobin concentration [12] and 2,3-DPG concentration [11].

Input variable	Default (physiological) value	Units	
Hemoglobin concen-	15.5	g/dL blood	
tration			
Hematocrit	45	%	
Altitude	0 (sea level)	m	
Temperature	37 (body temperature)	°C	
Partial pressure car-	40	mmHg	
bon dioxide (pCO ₂)			
Intracellular pH	7.24	-	
2,3-DPG concentra-	4.47	mmol/L	
tion			

trations of 2,3-DPG reported by Duhm [16] (Figure 2C): 0.1, 1.9, 4.4, 11.6, and 23.0 (μ moles/g RBC). These values were converted to units of mmol/L RBC before integration with the model. The model closely predicted the ODC for higher concentration values but underpredicted the saturation at lower concentrations. This result is likely due to parameterization of the K_{eq} values.

Computing the concentrations of hemoglobin bound states. In the modeling formalism described here, each Hb form is represented as a separate variable. Thus, we can compute the concentration of each bound state of Hb by solving a system of linear equations based on the K_{eq} values for each binding reaction [40]. The computed concentrations of all Hb bound states for the baseline simulation with fitted K_{eq} values (Figure 2A) are reported in Table 2. There is no experimental data with which to validate these computationally predicted values, but the values are in general agreement with estimates.

DISCUSSION

The human RBC plays a crucial role in higher-level physiological function through regulating gas exchange and transport. While a variety of modeling formalisms have been used to model some of these mechanisms, the most prevalent model type to date is a Hill-type model [13], an empirical model. We have built a model that integrates these important macromolecular mechanisms with the complete known metabolic network of the RBC to compute functional states and phenotypic properties of the RBC. These results have several primary implications.

First, the modeling formalism presented here allows for the computation of physiological-scale phenotypes using mechanistic information. Such a framework will allow for the integration of whole-body deep-phenotyping data [50] to help identify causative factors important for the onset and progression of blood disorders. While constraint-based models have previously been used to explore whole-body physiology [5], these efforts were limited to studying the metabolic network. Here, we have extended the capabilities of the model to include non-metabolic macromolecular mechanisms that perform crucial physiological functions in our cell type of interest.

Second, we have computed the ODC of the human RBC from first principles using a model parameterized with standard hematological measurements. In other words, we model the binding of Hb to its various substrates using kinetic relationships instead of empirical relationships (e.g., a Hill-type model [13]). Such a modeling formalism allows for the explicit computation of the concentration of bound Hb forms. While the technology does not yet exist to experimentally measure these compounds, the ability to computationally predict them—while validating the overall phenotypic predictions—provides insight into the functional state of the blood's gas transport and exchange system.

Third, this framework will enable the computation of personalized phenotypic responses. The use of electronic health records for personalized medical research has been increasing over the last decade [21, 49, 18], but we still need a unifying framework for the elucidation of causal biological mechanisms from such data [52]. The work presented here represents an important step in this direction, providing a computational network-based framework that integrates deep-phenotyping data typically recorded in a patient electronic health record (e.g., hematocrit, Hb concentration) to provide mechanistic predictions. By nature, these predictions offer mechanistic explanations for the observed model behavior.

Here, we have reported the most comprehensive model of the RBC to date that comprises the complete metabolic network, primary ROS detoxification, and O_2 , CO_2 , and 2,3-DPG binding to Hb. We validated this model by computing the ODC and comparing

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Table 2 Computed fractions of hemoglobin binding states (in percentages of total hemoglobin); $i \in \{0, 1, 2, 3, 4\}$ represents the number of bound CO₂ molecules.

pO ₂ (mmHg)	$\mathbf{H}\mathbf{b}_0$	\mathbf{Hb}_1	Hb_2	Hb_3	Hb_4	Hb-DPG	Hb ₀ -CO _{2,j}	Hb_1 -CO _{2,j}	Hb ₂ -CO _{2,j}	Hb ₃ -CO _{2,j}	Hb ₄ -CO _{2,j}	Нb-Н
0.00	0.90	0.00	1.00e-08	0.00	0.00	84.52	8.65	0.00	1.00e-08	0.00	0.00	5.93
12.87	0.68	3.67	3.53	2.94	2.43	63.49	6.50	4.13	3.56	2.65	1.97	4.45
25.74	0.29	3.13	6.04	10.03	16.60	27.11	2.77	3.53	6.08	9.05	13.47	1.90
38.61	0.10	1.64	4.75	11.83	29.38	9.48	0.97	1.85	4.78	10.68	23.85	0.66
51.48	0.04	0.86	3.32	11.02	36.50	3.73	0.38	0.97	3.34	9.95	29.63	0.26
64.35	0.02	0.49	2.36	9.81	40.59	1.70	0.17	0.55	2.38	8.86	32.95	0.12
77.22	0.01	0.30	1.74	8.70	43.20	0.87	0.09	0.34	1.75	7.85	35.07	0.06
90.10	0.01	0.20	1.33	7.77	45.00	0.49	0.05	0.22	1.34	7.01	36.53	0.03
102.97	0.00	0.14	1.05	7.00	46.33	0.30	0.03	0.15	1.06	6.32	37.61	0.02
115.84	0.00	0.10	0.85	6.35	47.34	0.19	0.02	0.11	0.85	5.74	38.43	0.01

with experimentally measured values under different physiological conditions. The scope of this model could yet be expanded, namely through the addition of nitric oxide signaling, which will allow for additional physiologically relevant phenotypic predictions and insights. Taken together, this work represents a step toward marrying physiological deep-phenotyping data with a mechanistic computational framework capable of providing causal insights into the physiology of human blood.

METHODS

To compute the ODC, we solve the optimization problem described in Equations (1-9) as we sweep across different pO₂ values. At each pO₂ value, we recompute the concentrations of all Hb bound states. For the baseline simulations shown in Figure 2, we selected Keq values from a normal distribution using a 15% standard error 50 simulations and report the 95% confidence intervals for the 50 simulated curves, showing the mean trajectory; for the 2,3-DPG simulations, we selected $K_{\mbox{eq}}$ values from a normal distribution using a 5% standard error for 50 simulations and report the 95% confidence intervals, showing the mean trajectory. The 2,3-DPG concentrations from [16] were converted into units of mmol/L RBC using the reported density of RBC as 1.110 g/mL [37].

Pseudo-first-order elementary rate constant (kPERC) values [40] are used to help sample the kinetically feasible flux solution space through setting constraints on reactions. We used literature values for "known" k^{cat} values and sampled remaining k^{eff} values from

$$v = \frac{k^{\text{cat}}}{K^m}[E][S] \tag{25}$$

$$\frac{k^{\text{cat}}}{K^m}[S] = \frac{v}{[E]} \tag{26}$$

where the quantity $\frac{k^{\text{cat}}}{k^{m}}[S]$ is k^{eff} . Sampling was performed with a lower bound for the objective function, sodium-potassium transport (NaKt), set to 90% of the maximum value to estimate the physiologically relevant solution space.

The concentrations of various macromolecule bound states are modeled based on Keq values where available:

$$K_{\rm eq} = \frac{k^{\rm f}}{k^{\rm r}} = \frac{\Pi[{\rm product}]}{\Pi[{\rm reactant}]}.$$
(27)

The total mass of Hb is constant,

$$\mathbf{H}\mathbf{b}_{\text{total}} = \sum \mathbf{H}\mathbf{b} \cdot S \tag{28}$$

where S represents all bound species: O_2 , CO_2 , 2,3-DPG, and H⁺. This formulation allows us to solve the system of equations represented by Equations (27) and (28) for the concentration of each bound state as previously described [40]. See the Supplemental Methods for full details on the solving procedure and model parameterization.

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