Negative density dependence promotes persistence of a globally
 rare yet locally abundant plant species (Oenothera coloradensis)

³ Supplementary Materials

4 Species Information

Oenothera coloradensis seeds are contained within small, indehiscent capsules that con-5 tain 2-5 seeds each (Burgess, Hild, & Shaw, 2005). A single adult individual can produce 6 >500 capsules. This species does not reproduce vegetatively, although seeds typically ger-7 minate near the base of the parent plant, which often results in dense patches of vegetative 8 individuals (Heidel, Tuthill, & Wallace, 2021). O. coloradensis is pollinated primarily by 9 hawkmoths (Krakos, pers. comm. to B. Heidel, 2013). Seed dispersers are unknown (Floyd 10 & Ranker, 1998; Heidel et al., 2021). Previous work established that O. coloradensis pop-11 ulation growth rate is particularly impacted by recruitment of seedlings (Floyd & Ranker, 12 1998). Recruitment increases when non-O. coloradensis community biomass is removed, in-13 dicating that surrounding grasses and forbs outcompete or shade-out seedlings (Munk, Hild, 14 & Whitson, 2002). 15

O. coloradensis commonly co-occurs with Agrostis stolonifera, Pascopyrum smithii, Poa pratensis, Glycyrrhiza lepidota, Iris missouriensis, Cirsium flodmanii, and Grindelia squarrosa (Endangered and Threatened Wildlife and Plants, 2000; Munk et al., 2002). Encroachment of woody shrubs such as Salix exigua has been correlated with declining numbers in some populations (Heidel et al., 2021).

²¹ The Wyoming Natural Diversity Database (WYNDD) began a base-wide census of re-

productive individuals in the FEWAFB population in 1986, and has repeated this census annually since 1988 (Heidel et al., 2021). The first estimate of species size after its full geographic range was identified occurred in 1998, when it was approximated that the entire species consisted of 47,300 to 50,300 reproductive individuals (Fertig, 2000).

26 Seed Production Estimation

It was not possible to measure seed production exactly because O. coloradensis seeds are 27 contained in indehiscent capsules. Additionally, buds on the same individual flower and set 28 seed with a time lag of up to several weeks, so mature seed capsules often exist at the tip of 29 a stem while un-opened buds lower down on that same stem have not vet flowered. This lag 30 makes it difficult to count the total number of capsules produced by an individual. However, 31 seed capsules leave a noticeable scar on the stem, so we used the number of seed capsule scars 32 on reproductive stems as an estimate of capsule production. Counting scars is extremely 33 time-intensive since a single plant can produce several hundred capsules, so we used Poisson 34 generalized linear regression to estimate the relationship between the length of stem bearing 35 capsule scars and the number of capsules produced by that stem. A Poisson regression model 36 fit to stem measurements and capsule counts from 106 individuals in 2018 indicated that 37 the number of capsules produced by an individual (C) can be predicted by $e^{(1.843+0.119 \times S))}$, 38 where S is the stem length in cm (pseudo $R^2 = 0.42$, P < 0.01, Residual deviance = 186.98, 39 df = 104) (Fig. S2). We used this relationship to estimate capsule production for each 40 reproductive individual. Previous work indicated that each capsule contained an average of 41 4 seeds, so we multiplied the estimated number of capsules produced by an adult plant by 4 42 to estimate seed production (Burgess et al., 2005). 43

44 Discrete Vital Rate Parameters

Previously-published data from a greenhouse experiment using O. coloradensis seed cap-45 sules collected from the FEWAFB populations determined that viable seeds had an average 46 germination rate of 20.3% after cold-stratification, and did not identify a consistent decline 47 in germination rate over five years (Burgess et al., 2005). This study also found that 58.5%48 of seeds produced were viable. We conducted an additional seed study to determine if over-49 wintering in natural conditions lead to a lower germination rate than was identified in the 50 previous greenhouse study. We buried 60 field-collected seed capsules in mesh bags at 6 51 locations near our demographic study plots at FEWAFB, and then recovered the seed bags 52 after one winter. An average of 10% of seed capsules were not recoverable, likely because 53 they were non-viable and withered away or were eaten. We planted the recovered capsules 54 in standard greenhouse conditions, and found a mean germination rate of 6.8%. This germi-55 nation rate was much lower than that identified by Burgess et al., however our seed study 56 had a much smaller sample size, reducing the reliability of our result (Burgess et al., 2005). 57 However, it is still likely that true germination rates are much lower than those identified in 58 greenhouse conditions, so we reduced the germination rate identified by Burgess et al. by 59 20%. 60

61 Seedling Data

Although seedlings (above-ground plants < 3 cm in leaf length) were only tallied in each plot quadrant and year instead of tagged and measured, we incorporated them into the dataset for continuous, above-ground plants by assigning them a random size drawn from a continuous, uniform probability distribution (seedling size ~ U(0.1, 3)). Each new recruit to the > 3 cm stage in year t + 1 was randomly assigned to a seedling within the same plot quadrant in year t. Seedlings in year t that were assigned a recruit in year t + 1 survived, while those without an assigned recruit died. Incorporating seedlings into the continuous dataset in this fashion allowed us to create IPMs using only one discrete stage.

⁷⁰ Table S1: Permanent Plot Locations and subpopulation-level sample sizes for each year and

 $_{\rm 71}~$ individual type (seedling vs. non-seedling). GPS coordinates listed in decimal degrees, map

⁷² datum and spheroid: WGS 84.

					Sample Size					
					20	18	20	19	2020)
Site	Subpopulation	Plot	Ν	W	non-seedling	seedling	non-seedling	seedling	non-seedling	seedling
		Name	Coord.	Coord.						
	Unnamed Creek	U3	41.13642	-104.87209						
	Unnamed Creek	U4	41.13634	-104.87183	740	525	528	417	406	530
~	Unnamed Creek	U6	41.13647	-104.87132						
AFE	Diamond Creek	D7	41.14340	-104.88380						
CW/	Diamond Creek	D10	41.14441	-104.88303	235 20	209	347	149	275	81
Ц	Diamond Creek	D11	41.14431	-104.88094						
	Crow Creek	C4	41.15540	-104.87497	203 127		214 98		150	160
	Crow Creek	C5	41.15477	-104.87474				98		
	Crow Creek	C8	41.15534	-104.87487						
	Pasture HQ5	S1	40.99297	-105.00925						
	Pasture HQ5	S2	40.99318	-105.00935	283 772		714	813	641	423
CD	Pasture HQ5	S3	40.99342	-105.00937						
ton	Pasture HQ3	S4	40.98623	-105.01691						
aps	Pasture HQ3	S5	40.98639	-105.01671	102	138	158 1'	173	117	104
$\overset{\circ}{\mathrm{So}}$	Pasture HQ3	S6	40.98650	-105.01656						
	Meadow	S7	40.98753	-105.02148						
	Meadow	S8	40.98747	-105.02179	44	31	47	28	48	12
	Meadow	$\mathbf{S9}$	40.98724	-105.02145						



Figure S1: (A) The current known distribution of *O. coloradensis*, shown in dark blue, extends into Wyoming, Colorado, and Nebraska. The historical distribution included the current distribution area as well as some additional locations shown in pale blue. Distribution information comes from Everson, 2019. Black dots show the relative locatino of the FEWAFB and Soapstone prairie populations included in this study. Colored dots show the location of plots in each subpopulation at FEWAFB (**B**) and Soapstone Prairie (**C**).

Table S2: Continuous vital rate functions used in each IPM. In the functions below, $size_t$ indicates plant longest leaf length in the previous year, N_t indicates number of individuals in a plot in the previous year, T_G indicates mean temperature in the previous year's growing season, and T_W indicates the mean temperature in winter of the previous year.

IPM	Vital Rate	Equation
A & B	Survival	$logit(s(z)) = -0.21 + 0.37(ln(size_t))$
	Flowering	$logit(Pb(z)) = -34.06 + 27.67(ln(size_t)) - 5.78(ln(size_t)^2)$
	Growth	$G(z', z) = N(\mu_s, \sigma_s); \ \mu_s = 1.57 + 0.18(ln(size_t)); \ \sigma_s = 0.51$

	Seed prod.	$exp(b(z)) = 3.35 + 1.19(ln(size_t))$
	Recruit size	$c_o(z') = N(\mu_r, \sigma_r); \ \mu_r = 0.21; \ \sigma_r = 0.77$
С	Survival	$logit(s(z)) = -0.73 + 0.45(ln(size_t))$
	Flowering	$logit(Pb(z)) = -40.31 + 33.40(ln(size_t)) - 7.09(ln(size_t)^2)$
	Growth	$G(z', z) = N(\mu_s, \sigma_s); \ \mu_s = 1.64 + 0.11(ln(size_t)); \ \sigma_s = 0.42$
	Seed prod.	$exp(b(z)) = 3.73 + 1.01(ln(size_t))$
	Recruit size	$c_o(z') = N(\mu_r, \sigma_r); \ \mu_r = 0.19; \ \sigma_r = 0.76$
D	Survival	$logit(s(z)) = 1.01 + -0.01(ln(size_t))$
	Flowering	$logit(Pb(z)) = -44.52 + 36.73(ln(size_t)) - 7.69(ln(size_t)^2)$
	Growth	$G(z', z) = N(\mu_s, \sigma_s); \ \mu_s = 1.84 + 0.26(ln(size_t)); \ \sigma_s = 0.52$
	Seed prod.	$exp(b(z)) = 3.80 + 1.11(ln(size_t))$
	Recruit size	$c_o(z') = N(\mu_r, \sigma_r); \ \mu_r = 0.22; \ \sigma_r = 0.78$
Ε	Survival	$logit(s(z)) = 0.21 + 0.18(ln(size_t))$
	Flowering	$logit(Pb(z)) = -18.73 + 15.84(ln(size_t)) - 3.63(ln(size_t)^2)$
	Growth	$G(z', z) = N(\mu_s, \sigma_s); \ \mu_s = 1.74 + 0.24(ln(size_t)); \ \sigma_s = 0.49$
	Seed prod.	$exp(b(z)) = 3.83 + 0.92(ln(size_t))$
	Recruit size	$c_o(z') = N(\mu_r, \sigma_r); \ \mu_r = 0.19; \ \sigma_r = 0.80$
F	Survival	$logit(s(z)) = 0.54 + 0.24(ln(size_t))$
	Flowering	$logit(Pb(z)) = -27.49 + 20.83(ln(size_t)) - 4.04(ln(size_t)^2)$
		$O(I)$ $N(I)$ $1.62 \pm 0.16(I(I))$ 0.44
	Growth	$G(z', z) = N(\mu_s, \sigma_s); \ \mu_s = 1.62 + 0.16(ln(size_t)); \ \sigma_s = 0.44$
	Growth Seed prod.	$G(z', z) = N(\mu_s, \sigma_s); \ \mu_s = 1.62 + 0.16(ln(size_t)); \ \sigma_s = 0.44$ $exp(b(z)) = 1.72 + 1.51(ln(size_t))$
	Growth Seed prod. Recruit size	$G(z', z) = N(\mu_s, \sigma_s); \ \mu_s = 1.62 + 0.16(ln(size_t)); \ \sigma_s = 0.44$ $exp(b(z)) = 1.72 + 1.51(ln(size_t))$ $c_o(z') = N(\mu_r, \sigma_r); \ \mu_r = 0.15; \ \sigma_r = 0.80$
G	Growth Seed prod. Recruit size Survival	$G(z', z) = N(\mu_s, \sigma_s); \ \mu_s = 1.62 \pm 0.16(ln(size_t)); \ \sigma_s = 0.44$ $exp(b(z)) = 1.72 \pm 1.51(ln(size_t))$ $c_o(z') = N(\mu_r, \sigma_r); \ \mu_r = 0.15; \ \sigma_r = 0.80$ $logit(s(z)) = -0.19 \pm 0.30(ln(size_t)))$
G	Growth Seed prod. Recruit size Survival Flowering	$G(z', z) = N(\mu_s, \sigma_s); \ \mu_s = 1.62 \pm 0.16(ln(size_t)); \ \sigma_s = 0.44$ $exp(b(z)) = 1.72 \pm 1.51(ln(size_t))$ $c_o(z') = N(\mu_r, \sigma_r); \ \mu_r = 0.15; \ \sigma_r = 0.80$ $logit(s(z)) = -0.19 \pm 0.30(ln(size_t))$ $logit(Pb(z)) = -32.72 \pm 23.50(ln(size_t)) - 4.23(ln(size_t)^2)$
G	Growth Seed prod. Recruit size Survival Flowering Growth	$\begin{split} G(z',z) &= N(\mu_s,\sigma_s); \ \mu_s = 1.62 \pm 0.16(\ln(size_t)); \ \sigma_s = 0.44 \\ exp(b(z)) &= 1.72 \pm 1.51(\ln(size_t)) \\ c_o(z') &= N(\mu_r,\sigma_r); \ \mu_r = 0.15; \ \sigma_r = 0.80 \\ logit(s(z)) &= -0.19 \pm 0.30(\ln(size_t)) \\ logit(Pb(z)) &= -32.72 \pm 23.50(\ln(size_t)) - 4.23(\ln(size_t)^2) \\ G(z',z) &= N(\mu_s,\sigma_s); \ \mu_s = 1.42 \pm 0.21(\ln(size_t)); \ \sigma_s = 0.42 \end{split}$
G	Growth Seed prod. Recruit size Survival Flowering Growth Seed prod.	$\begin{split} G(z',z) &= N(\mu_s,\sigma_s); \ \mu_s = 1.62 \pm 0.16(ln(size_t)); \ \sigma_s = 0.44\\ exp(b(z)) &= 1.72 \pm 1.51(ln(size_t))\\ c_o(z') &= N(\mu_r,\sigma_r); \ \mu_r = 0.15; \ \sigma_r = 0.80\\ logit(s(z)) &= -0.19 \pm 0.30(ln(size_t))\\ logit(Pb(z)) &= -32.72 \pm 23.50(ln(size_t)) - 4.23(ln(size_t)^2)\\ G(z',z) &= N(\mu_s,\sigma_s); \ \mu_s = 1.42 \pm 0.21(ln(size_t)); \ \sigma_s = 0.42\\ exp(b(z)) &= 0.83 \pm 2.06(ln(size_t)) \end{split}$
G	Growth Seed prod. Recruit size Survival Flowering Growth Seed prod. Recruit size	$\begin{split} G(z',z) &= N(\mu_s,\sigma_s); \ \mu_s = 1.62 \pm 0.16(\ln(size_t)); \ \sigma_s = 0.44 \\ exp(b(z)) &= 1.72 \pm 1.51(\ln(size_t)) \\ c_o(z') &= N(\mu_r,\sigma_r); \ \mu_r = 0.15; \ \sigma_r = 0.80 \\ logit(s(z)) &= -0.19 \pm 0.30(\ln(size_t)) \\ logit(Pb(z)) &= -32.72 \pm 23.50(\ln(size_t)) - 4.23(\ln(size_t)^2) \\ G(z',z) &= N(\mu_s,\sigma_s); \ \mu_s = 1.42 \pm 0.21(\ln(size_t)); \ \sigma_s = 0.42 \\ exp(b(z)) &= 0.83 \pm 2.06(\ln(size_t)) \\ c_o(z') &= N(\mu_r,\sigma_r); \ \mu_r = 0.21; \ \sigma_r = 0.77 \end{split}$
G	Growth Seed prod. Recruit size Survival Flowering Growth Seed prod. Recruit size Survival	$\begin{split} G(z',z) &= N(\mu_s,\sigma_s); \ \mu_s = 1.62 \pm 0.16(ln(size_t)); \ \sigma_s = 0.44 \\ exp(b(z)) &= 1.72 \pm 1.51(ln(size_t)) \\ c_o(z') &= N(\mu_r,\sigma_r); \ \mu_r = 0.15; \ \sigma_r = 0.80 \\ logit(s(z)) &= -0.19 \pm 0.30(ln(size_t)) \\ logit(Pb(z)) &= -32.72 \pm 23.50(ln(size_t)) - 4.23(ln(size_t)^2) \\ G(z',z) &= N(\mu_s,\sigma_s); \ \mu_s = 1.42 \pm 0.21(ln(size_t)); \ \sigma_s = 0.42 \\ exp(b(z)) &= 0.83 \pm 2.06(ln(size_t)) \\ c_o(z') &= N(\mu_r,\sigma_r); \ \mu_r = 0.21; \ \sigma_r = 0.77 \\ logit(s(z)) &= -0.32 \pm 0.62(ln(size_t)) \end{split}$
G	Growth Seed prod. Recruit size Survival Flowering Growth Seed prod. Recruit size Survival Flowering	$\begin{split} G(z',z) &= N(\mu_s,\sigma_s); \ \mu_s = 1.62 \pm 0.16(ln(size_t)); \ \sigma_s = 0.44 \\ exp(b(z)) &= 1.72 \pm 1.51(ln(size_t)) \\ c_o(z') &= N(\mu_r,\sigma_r); \ \mu_r = 0.15; \ \sigma_r = 0.80 \\ logit(s(z)) &= -0.19 \pm 0.30(ln(size_t)) \\ logit(Pb(z)) &= -32.72 \pm 23.50(ln(size_t)) - 4.23(ln(size_t)^2) \\ G(z',z) &= N(\mu_s,\sigma_s); \ \mu_s = 1.42 \pm 0.21(ln(size_t)); \ \sigma_s = 0.42 \\ exp(b(z)) &= 0.83 \pm 2.06(ln(size_t)) \\ c_o(z') &= N(\mu_r,\sigma_r); \ \mu_r = 0.21; \ \sigma_r = 0.77 \\ logit(s(z)) &= -0.32 \pm 0.62(ln(size_t)) \\ logit(Pb(z)) &= -31.04 \pm 23.96(ln(size_t)) - 4.71(ln(size_t)^2) \end{split}$
G	Growth Seed prod. Recruit size Survival Flowering Growth Seed prod. Recruit size Survival Flowering Growth	$\begin{split} G(z',z) &= N(\mu_s,\sigma_s); \ \mu_s = 1.62 \pm 0.16(ln(size_t)); \ \sigma_s = 0.44 \\ exp(b(z)) &= 1.72 \pm 1.51(ln(size_t)) \\ c_o(z') &= N(\mu_r,\sigma_r); \ \mu_r = 0.15; \ \sigma_r = 0.80 \\ logit(s(z)) &= -0.19 \pm 0.30(ln(size_t)) \\ logit(Pb(z)) &= -32.72 \pm 23.50(ln(size_t)) - 4.23(ln(size_t)^2) \\ G(z',z) &= N(\mu_s,\sigma_s); \ \mu_s = 1.42 \pm 0.21(ln(size_t)); \ \sigma_s = 0.42 \\ exp(b(z)) &= 0.83 \pm 2.06(ln(size_t)) \\ c_o(z') &= N(\mu_r,\sigma_r); \ \mu_r = 0.21; \ \sigma_r = 0.77 \\ logit(s(z)) &= -0.32 \pm 0.62(ln(size_t)) \\ logit(Pb(z)) &= -31.04 \pm 23.96(ln(size_t)) - 4.71(ln(size_t)^2) \\ G(z',z) &= N(\mu_s,\sigma_s); \ \mu_s = 1.50 \pm 0.05(ln(size_t)); \ \sigma_s = 0.43 \end{split}$
G	Growth Seed prod. Recruit size Survival Flowering Growth Seed prod. Survival Flowering Growth Seed prod.	$\begin{split} G(z',z) &= N(\mu_s,\sigma_s); \ \mu_s = 1.62 \pm 0.16(ln(size_t)); \ \sigma_s = 0.44 \\ exp(b(z)) &= 1.72 \pm 1.51(ln(size_t)) \\ c_o(z') &= N(\mu_r,\sigma_r); \ \mu_r = 0.15; \ \sigma_r = 0.80 \\ logit(s(z)) &= -0.19 \pm 0.30(ln(size_t)) \\ logit(Pb(z)) &= -32.72 \pm 23.50(ln(size_t)) - 4.23(ln(size_t)^2) \\ G(z',z) &= N(\mu_s,\sigma_s); \ \mu_s = 1.42 \pm 0.21(ln(size_t)); \ \sigma_s = 0.42 \\ exp(b(z)) &= 0.83 \pm 2.06(ln(size_t)) \\ c_o(z') &= N(\mu_r,\sigma_r); \ \mu_r = 0.21; \ \sigma_r = 0.77 \\ logit(s(z)) &= -0.32 \pm 0.62(ln(size_t)) \\ logit(Pb(z)) &= -31.04 \pm 23.96(ln(size_t)) - 4.71(ln(size_t)^2) \\ G(z',z) &= N(\mu_s,\sigma_s); \ \mu_s = 1.50 \pm 0.05(ln(size_t)); \ \sigma_s = 0.43 \\ exp(b(z)) &= 2.53 \pm 1.59(ln(size_t)) \end{split}$
G	Growth Seed prod. Recruit size Survival Flowering Growth Seed prod. Survival Flowering Growth Seed prod. Seed prod.	$\begin{split} G(z',z) &= N(\mu_s,\sigma_s); \ \mu_s = 1.62 \pm 0.16(\ln(size_t)); \ \sigma_s = 0.44 \\ exp(b(z)) &= 1.72 \pm 1.51(\ln(size_t)) \\ c_o(z') &= N(\mu_r,\sigma_r); \ \mu_r = 0.15; \ \sigma_r = 0.80 \\ logit(s(z)) &= -0.19 \pm 0.30(\ln(size_t)) \\ logit(Pb(z)) &= -32.72 \pm 23.50(\ln(size_t)) - 4.23(\ln(size_t)^2) \\ G(z',z) &= N(\mu_s,\sigma_s); \ \mu_s = 1.42 \pm 0.21(\ln(size_t)); \ \sigma_s = 0.42 \\ exp(b(z)) &= 0.83 \pm 2.06(\ln(size_t)) \\ c_o(z') &= N(\mu_r,\sigma_r); \ \mu_r = 0.21; \ \sigma_r = 0.77 \\ logit(s(z)) &= -0.32 \pm 0.62(\ln(size_t)) \\ logit(Pb(z)) &= -31.04 \pm 23.96(\ln(size_t)) - 4.71(\ln(size_t)^2) \\ G(z',z) &= N(\mu_s,\sigma_s); \ \mu_s = 1.50 \pm 0.05(\ln(size_t)); \ \sigma_s = 0.43 \\ exp(b(z)) &= 2.53 \pm 1.59(\ln(size_t)) \\ c_o(z') &= N(\mu_r,\sigma_r); \ \mu_r = 0.23; \ \sigma_r = 0.76 \end{split}$

	Flowering	$logit(Pb(z)) = -41.36 + 33.73(ln(size_t)) - 7.21(ln(size_t)^2) + 0.0008(N_t)$
	Growth	$G(z', z) = N(\mu_s, \sigma_s); \ \mu_s = 2.19 + 0.14(ln(size_t)) - 0.0005(N_t); \ \sigma_s = 0.42$
	Seed prod.	$exp(b(z)) = 3.73 + 1.01(ln(size_t))$
	Recruit size	$c_o(z') = N(\mu_r, \sigma_r); \ \mu_r = 0.19; \ \sigma_r = 0.76$
J	Survival	$logit(s(z)) = 17.59 + 0.05(ln(size_t)) - 0.03(N_t)$
	Flowering	$logit(Pb(z)) = -46.27 + 37.38(ln(size_t)) - 7.83(ln(size_t)^2) +$
		$0.002(N_t)$
	Growth	$G(z', z) = N(\mu_s, \sigma_s); \ \mu_s = 3.70 + 0.28(ln(size_t)) - 0.004(N_t); \ \sigma_s = 0.004($
		0.51
	Seed prod.	$exp(b(z)) = 3.80 + 1.11(ln(size_t))$
	Recruit size	$c_o(z') = N(\mu_r, \sigma_r); \ \mu_r = 0.22; \ \sigma_r = 0.78$
Κ	Survival	$logit(s(z)) = -13.85 + 0.20(ln(size_t)) + 0.04(N_t)$
	Flowering	$logit(Pb(z)) = -21.21 + 15.50(ln(size_t)) - 3.55(ln(size_t)^2) +$
		$0.009(N_t)$
	Growth	$G(z',z) = N(\mu_s,\sigma_s); \ \mu_s = -0.49 + 0.24(ln(size_t)) + 0.006(N_t);$
		$\sigma_s = 0.48$
	Seed prod.	$exp(b(z)) = 3.83 + 0.92(ln(size_t))$
	Recruit size	$c_o(z') = N(\mu_r, \sigma_r); \ \mu_r = 0.19; \ \sigma_r = 0.80$
L	Survival	$logit(s(z)) = 33.06 + 0.24(ln(size_t)) - 0.44(N_t)$
	Flowering	$logit(Pb(z)) = -26.23 + 21.0(ln(size_t)) - 4.01(ln(size_t)^2) - 0.02(N_t))$
	Growth	$G(z', z) = N(\mu_s, \sigma_s); \ \mu_s = 15.89 + 0.17(ln(size_t)) - 0.19(N_t); \ \sigma_s = 0.19(N_t)$
		0.43
	Seed prod.	$exp(b(z)) = 1.72 + 1.51(ln(size_t))$
	Recruit size	$c_o(z') = N(\mu_r, \sigma_r); \ \mu_r = 0.15; \ \sigma_r = 0.80$
М	Survival	$logit(s(z)) = 5.39 + 0.37(ln(size_t)) - 0.02(N_t)$
	Flowering	$logit(Pb(z)) = -32.79 + 24.02(ln(size_t)) - 4.34(ln(size_t)^2) -$
		$0.002(N_t)$
	Growth	$G(z', z) = N(\mu_s, \sigma_s); \ \mu_s = 2.26 + 0.23(ln(size_t)) - 0.003(N_t); \ \sigma_s = 0.003($
		0.39
	Seed prod.	$exp(b(z)) = 0.83 + 2.06(ln(size_t))$
	Recruit size	$c_o(z') = N(\mu_r, \sigma_r); \ \mu_r = 0.21; \ \sigma_r = 0.77$
Ν	Survival	$logit(s(z)) = 4.30 + 0.87(ln(size_t)) - 0.004(N_t)$

	Flowering	$logit(Pb(z)) = -28.50 + 25.52(ln(size_t)) - 4.93(ln(size_t)^2) - 0.004(N_t)$
	Growth	$G(z', z) = N(\mu_s, \sigma_s); \ \mu_s = 2.76 + 0.16(ln(size_t)) - 0.001(N_t); \ \sigma_s = 0.004(N_t); \ \sigma_s = 0.004($
		0.36
	Seed prod.	$exp(b(z)) = 2.53 + 1.59(ln(size_t))$
	Recruit size	$c_o(z') = N(\mu_r, \sigma_r); \ \mu_r = 0.23; \ \sigma_r = 0.77$
\mathbf{S}	Survival	$logit(s(z)) = 1.11 + 0.49(ln(size_t)) + 0.005(N_t) - 0.28(T_G)$
	Flowering	$logit(Pb(z)) = -47.12 + 33.70(ln(size_t)) - 7.21(ln(size_t)^2) +$
		$0.0004(N_t) + 0.42(T_G) - 0.23(T_W)$
	Growth	$G(z',z) = N(\mu_s,\sigma_s); \ \mu_s = 4.12 + 0.14(ln(size_t)) + 0.0009(N_t) - 0.0009(N_t))$
		$0.20(T_G); \ \sigma_s = 0.41$
	Seed prod.	$exp(b(z)) = 3.52 + 0.90(ln(size_t)) + 0.0008(N_t) + 0.01(T_G) + 0.10(T_W)$
	Recruit size	$c_o(z') = N(\mu_r, \sigma_r); \ \mu_r = -0.38 + 0.00005(N_t) + 0.04(T_G) + 0.03(T_W);$
		$\sigma_r = 0.76$
Т	Survival	$logit(s(z)) = -27.59 + 0.21(ln(size_t)) - 0.0006(N_t) + 1.91(T_G)$
	Flowering	$logit(Pb(z)) = -70.28 + 35.37(ln(size_t)) - 7.45(ln(size_t)^2) -$
		$0.003(N_t) + 1.83(T_G) - 0.95(T_W)$
	Growth	$G(z', z) = N(\mu_s, \sigma_s); \ \mu_s = -2.88 + 0.27(ln(size_t)) + 0.0002(N_t) + 0.0002(N_t)$
		$0.32(T_G); \sigma_s = 0.49$
	Seed prod.	$exp(b(z)) = -12.0 + 0.80(ln(size_t)) - 0.002(N_t) + 1.07(T_G) -$
		$0.94(T_W)$
	Recruit size	$c_o(z') = N(\mu_r, \sigma_r); \ \mu_r = -0.65 - 0.0007(N_t) + 0.06(T_G) - 0.16(T_W);$
		$\sigma_r = 0.77$
U	Survival	$logit(s(z)) = -14.02 + 0.39(ln(size_t)) + 0.006(N_t) + 0.87(T_G)$
	Flowering	$logit(Pb(z)) = -22.83 + 16.0(ln(size_t)) - 3.66(ln(size_t)^2) +$
		$0.002(N_t) + 0.19(T_G) - 1.01(T_W)$
	Growth	$G(z', z) = N(\mu_s, \sigma_s); \ \mu_s = 0.40 + 0.25(ln(size_t)) - 0.001(N_t) +$
		$0.10(T_G); \sigma_s = 0.46$
	Seed prod.	$exp(b(z)) = -14.33 + 0.59(ln(size_t)) + 0.001(N_t) + 1.18(T_G) -$
		$1.17(T_W)$
	Recruit size	$c_o(z') = N(\mu_r, \sigma_r); \ \mu_r = -0.56 - 0.00002(N_t) + 0.05(T_G) + 0.09(T_W);$
		$\sigma_r = 0.81$
V	Survival	$logit(s(z)) = -6.78 + 0.24(ln(size_t)) - 0.08(N_t) + 0.69(T_G)$

	Flowering	$logit(Pb(z)) = -36.50 + 18.80(ln(size_t)) - 3.57(ln(size_t)^2) -$
		$0.02(N_t) + 0.79(T_G) + 0.09(T_W)$
	Growth	$G(z', z) = N(\mu_s, \sigma_s); \ \mu_s = -1.83 + 0.17(ln(size_t)) + 0.0003(N_t) + 0.0003(N_t)$
		$0.23(T_G); \sigma_s = 0.42$
	Seed prod.	$exp(b(z)) = 8.44 + 1.32(ln(size_t)) + 0.003(N_t) - 0.43(T_G) - 0.18(T_W)$
	Recruit size	$c_o(z') = N(\mu_r, \sigma_r); \ \mu_r = -2.01 + 0.006(N_t) + 0.13(T_G) - 0.01(T_W);$
		$\sigma_r = 0.80$
W	Survival	$logit(s(z)) = -32.30 + 0.38(ln(size_t)) + 0.0008(N_t) + 2.19(T_G)$
	Flowering	$logit(Pb(z)) = -311.80 + 18.72(ln(size_t)) - 3.56(ln(size_t)^2) -$
		$0.002(N_t) + 17.93(T_G) - 20.46(T_W)$
	Growth	$G(z',z) = N(\mu_s,\sigma_s); \ \mu_s = -2.73 + 0.22(ln(size_t)) - 0.0006(N_t) + 0.0006(N_t) +$
		$0.29(T_G); \sigma_s = 0.39$
	Seed prod.	$exp(b(z)) = -7.07 + 1.47(ln(size_t)) + 0.003(N_t) + 0.63(T_G)$
	Recruit size	$c_o(z') = N(\mu_r, \sigma_r); \ \mu_r = 1.75 + 0.006(N_t) - 0.10(T_G) + 0.17(T_W);$
		$\sigma_r = 0.77$
Х	Survival	$logit(s(z)) = -34.59 + 0.88(ln(size_t)) + 0.001(N_t) + 2.26(T_G)$
	Flowering	$logit(Pb(z)) = -43.64 + 28.21(ln(size_t)) - 5.35(ln(size_t)^2) -$
		$0.001(N_t) + 0.57(T_G) + 1.33(T_W)$
	Growth	$G(z', z) = N(\mu_s, \sigma_s); \ \mu_s = -7.65 + 0.16(ln(size_t)) - 0.0000004(N_t) + 0.00000004(N_t)) + 0.00000004(N_t) + 0.00000004(N_t) + 0.00000004(N_t)) + 0.00000004(N_t) + 0.00000004(N_t)) + 0.000000004(N_t) + 0.00000004(N_t)) + 0.00000004(N_t) + 0.00000004(N_t) + 0.00000004(N_t)) + 0.00000004(N_t) + 0.00000004(N_t) + 0.00000004(N_t) + 0.000000004(N_t)) + 0.00000000004(N_t) + 0.00000004(N_t) + 0.0000000000000000000000000000000000$
		$0.61(T_G); \sigma_s = 0.36$
	Seed prod.	$exp(b(z)) = -28.65 + 0.62(ln(size_t)) + 0.0005(N_t) + 2.15(T_G) -$
		$1.64(T_W)$
	Recruit size	$c_o(z') = N(\mu_r, \sigma_r); \ \mu_r = 0.48 - 0.00004(N_t) - 0.01(T_G) + 0.005(T_W);$
		$\sigma_r = 0.77$
AA	Survival	$logit(s(z)) = -0.26 + 0.54(ln(size_t))$
	Flowering	$logit(Pb(z)) = -28.96 + 21.71(ln(size_t)) - 4.14(ln(size_t)^2)$
	Growth	$G(z', z) = N(\mu_s, \sigma_s); \ \mu_s = 1.48 + 0.10(ln(size_t)); \ \sigma_s = 0.44$
	Seed prod.	$exp(b(z)) = 3.12 + 1.24(ln(size_t))$
	Recruit size	$c_o(z') = N(\mu_r, \sigma_r); \ \mu_r = 0.23; \ \sigma_r = 0.77$
BB	Survival	$logit(s(z)) = -0.18 + 0.29(ln(size_t))$
	Flowering	$logit(Pb(z)) = -32.70 + 26.93(ln(size_t)) - 5.73(ln(size_t)^2)$
	Growth	$G(z', z) = N(\mu_s, \sigma_s); \ \mu_s = 1.72 + 0.18(ln(size_t)); \ \sigma_s = 0.51$
	Seed prod.	$exp(b(z)) = 3.45 + 1.17(ln(size_t))$
	Recruit size	$c_o(z') = N(\mu_r, \sigma_r); \ \mu_r = 0.19; \ \sigma_r = 0.77$

CC	Survival	$logit(s(z)) = -1.23 + 0.76(ln(size_t))$
	Flowering	$logit(Pb(z)) = -45.81 + 38.00(ln(size_t)) - 8.03(ln(size_t)^2)$
	Growth	$G(z', z) = N(\mu_s, \sigma_s); \ \mu_s = 1.57 + 0.12(ln(size_t)); \ \sigma_s = 0.44$
	Seed prod.	$exp(b(z)) = 3.21 + 1.22(ln(size_t))$
	Recruit size	$c_o(z') = N(\mu_r, \sigma_r); \ \mu_r = 0.13; \ \sigma_r = 0.77$
DD	Survival	$logit(s(z)) = 2.43 - 0.23(ln(size_t))$
	Flowering	$logit(Pb(z)) = -86.83 + 71.52(ln(size_t)) - 14.65(ln(size_t)^2)$
	Growth	$G(z', z) = N(\mu_s, \sigma_s); \ \mu_s = 1.93 + 0.25(ln(size_t)); \ \sigma_s = 0.56$
	Seed prod.	$exp(b(z)) = 6.01 + 0.34(ln(size_t))$
	Recruit size	$c_o(z') = N(\mu_r, \sigma_r); \ \mu_r = 0.30; \ \sigma_r = 0.69$
EE	Survival	$logit(s(z)) = 0.65 + 0.15(ln(size_t))$
	Flowering	$logit(Pb(z)) = -24.35 + 17.91(ln(size_t)) - 3.49(ln(size_t)^2)$
	Growth	$G(z', z) = N(\mu_s, \sigma_s); \ \mu_s = 1.85 + 0.20(ln(size_t)); \ \sigma_s = 0.52$
	Seed prod.	$exp(b(z)) = 2.51 + 1.54(ln(size_t))$
	Recruit size	$c_o(z') = N(\mu_r, \sigma_r); \ \mu_r = 0.09; \ \sigma_r = 0.86$
\mathbf{FF}	Survival	$logit(s(z)) = 1.50 - 0.32(ln(size_t))$
	Flowering	$logit(Pb(z)) = -70.62 + 54.30(ln(size_t)) - 10.46(ln(size_t)^2)$
	Growth	$G(z', z) = N(\mu_s, \sigma_s); \ \mu_s = 1.65 + 0.21(ln(size_t)); \ \sigma_s = 0.46$
	Seed prod.	$exp(b(z)) = 1.91 + 1.39(ln(size_t))$
	Recruit size	$c_o(z') = N(\mu_r, \sigma_r); \ \mu_r = 0.10; \ \sigma_r = 0.92$
GG	Survival	$logit(s(z)) = 0.99 + 0.12(ln(size_t))$
	Flowering	$logit(Pb(z)) = -50.32 + 36.50(ln(size_t)) - 6.54(ln(size_t)^2)$
	Growth	$G(z', z) = N(\mu_s, \sigma_s); \ \mu_s = 1.48 + 0.28(ln(size_t)); \ \sigma_s = 0.38$
	Seed prod.	$exp(b(z)) = 3.06 + 1.22(ln(size_t))$
	Recruit size	$c_o(z') = N(\mu_r, \sigma_r); \ \mu_r = 0.18; \ \sigma_r = 0.81$
HH	Survival	$logit(s(z)) = 0.74 + 0.33(ln(size_t))$
	Flowering	$logit(Pb(z)) = -50.91 + 40.17(ln(size_t)) - 7.81(ln(size_t)^2)$
	Growth	$G(z', z) = N(\mu_s, \sigma_s); \ \mu_s = 1.62 + 0.18(ln(size_t)); \ \sigma_s = 0.39$
	Seed prod.	$exp(b(z)) = 4.20 + 0.97(ln(size_t))$
	Recruit size	$c_o(z') = N(\mu_r, \sigma_r); \ \mu_r = 0.24; \ \sigma_r = 0.76$
II	Survival	$logit(s(z)) = -0.26 + 0.06(ln(size_t))$
	Flowering	$logit(Pb(z)) = -41.11 + 36.347(ln(size_t)) - 8.31(ln(size_t)^2)$
	Flowering Growth	$logit(Pb(z)) = -41.11 + 36.347(ln(size_t)) - 8.31(ln(size_t)^2)$ $G(z', z) = N(\mu_s, \sigma_s); \ \mu_s = 1.67 + 0.16(ln(size_t)); \ \sigma_s = 0.38$

	Recruit size	$c_o(z') = N(\mu_r, \sigma_r); \ \mu_r = 0.22; \ \sigma_r = 0.71$
JJ	Survival	$logit(s(z)) = 0.07 + 0.16(ln(size_t))$
	Flowering	$logit(Pb(z)) = -24.83 + 19.82(ln(size_t)) - 4.20(ln(size_t)^2)$
	Growth	$G(z', z) = N(\mu_s, \sigma_s); \ \mu_s = 1.63 + 0.32(ln(size_t)); \ \sigma_s = 0.44$
	Seed prod.	$exp(b(z)) = 4.63 + 0.66(ln(size_t))$
	Recruit size	$c_o(z') = N(\mu_r, \sigma_r); \ \mu_r = 0.09; \ \sigma_r = 0.82$
KK	Survival	$logit(s(z)) = -0.26 + 0.25(ln(size_t))$
	Flowering	$logit(Pb(z)) = -27.90 + 27.66(ln(size_t)) - 7.00(ln(size_t)^2)$
	Growth	$G(z', z) = N(\mu_s, \sigma_s); \ \mu_s = 1.56 + 0.30(ln(size_t)); \ \sigma_s = 0.41$
	Seed prod.	$exp(b(z)) = 5.72 - 0.09(ln(size_t))$
	Recruit size	$c_o(z') = N(\mu_r, \sigma_r); \ \mu_r = 0.80; \ \sigma_r = 0.79$
LL	Survival	$logit(s(z)) = -0.22 + 0.77(ln(size_t))$
	Flowering	$logit(Pb(z)) = -147.87 + 121.01(ln(size_t)) - 24.82(ln(size_t)^2)$
	Growth	$G(z', z) = N(\mu_s, \sigma_s); \ \mu_s = 1.61 + 0.10(ln(size_t)); \ \sigma_s = 0.39$
	Seed prod.	$exp(b(z)) = 1.98 + 1.57(ln(size_t))$
	Recruit size	$c_o(z') = N(\mu_r, \sigma_r); \ \mu_r = 0.16; \ \sigma_r = 0.68$
MM	Survival	$logit(s(z)) = -1.13 + 0.60(ln(size_t))$
	Flowering	$logit(Pb(z)) = -45.56 + 39.31(ln(size_t)) - 8.64(ln(size_t)^2)$
	Growth	$G(z', z) = N(\mu_s, \sigma_s); \ \mu_s = 1.34 + 0.14(ln(size_t)); \ \sigma_s = 0.40$
	Seed prod.	$exp(b(z)) = 0.71 + 2.00(ln(size_t))$
	Recruit size	$c_o(z') = N(\mu_r, \sigma_r); \ \mu_r = 0.32; \ \sigma_r = 0.64$
NN	Survival	$logit(s(z)) = -1.74 + 1.39(ln(size_t))$
	Flowering	$logit(Pb(z)) = -27.89 + 20.50(ln(size_t)) - 3.99(ln(size_t)^2)$
	Growth	$G(z', z) = N(\mu_s, \sigma_s); \ \mu_s = 1.17 + 0.13(ln(size_t)); \ \sigma_s = 0.33$
	Seed prod.	$exp(b(z)) = 5.49 + 0.14(ln(size_t))$
	Recruit size	$c_o(z') = N(\mu_r, \sigma_r); \ \mu_r = 0.24; \ \sigma_r = 0.78$



Figure S2: As the stem length of an *Oenothera coloradensis* flowering individual increases, the number of capsules it produces increases as well. The red line shows the fit from a Poisson generalized linear model, and the grey ribbon shows the 95% confidence interval around the fitted relationship. Model equation: Number of capsules = $e^{(1.843+0.119\times S))}$, where *S* is stem length in cm (pseudo R-squared = 0.42, P = < 0.01, Residual deviance = 186.98, df = 104).

Table S3: Comparison of vital rate models with and without density dependence. The 85 "DI" and "DD" rows contain AIC values for each vital rate model in each subpopulation 86 for models that are density-independent (DI) and density-dependent (DD). The difference 87 between the AIC of DI and DD models is shown in the Δ AIC column. Bold text indicates 88 that the $|\Delta|$ AIC value is > 3, which means that including a term for density dependence 89 substantially changed that vital rate model. A positive $|\Delta|$ AIC indicates that including 90 density dependence improved the model, while a negative value indicates that including 91 density dependence made model fit worse. AIC values for DI and DD values can be found 92 in Table S3. 93

Vital Rate Model		Subpopulation					
		Crow	Diamond	Unnamed	HQ5	HQ3	Meadow
		Creek	Creek	Creek			
Survival	DI	776.58	1012.68	2684.34	3242.63	716.66	166.13
	DD	757.84	905.39	26848.74	2922.91	637.84	166.83
	ΔAIC	18.74	107.28	-0.41	320.33	78.82	-0.70
Growth	DI	510.34	953.29	1098.95	1570.93	300.18	116.54
	DD	506.61	931.15	1068.14	1112.78	269.73	113.88
	ΔAIC	3.73	22.15	30.811	458.15	30.45	2.66
Flowering	DI	371.68	523.30	1087.93	538.52	191.46	104.24
	DD	373.31	523.74	1087.48	483.99	193.22	106.96
	ΔAIC	-1.63	-0.44	0.45	54.52	-1.76	-1.72
Seed production	DI	842.00	1580.85	2815.89	1423.02	598.75	280.09
	DD	835.59	1566.83	2817.19	1419.32	594.63	281.45
	ΔAIC	6.41	14.02	-1.29	3.71	4.12	-1.35
Recruit size	DI	921.31	1028.23	3378.43	4629.87	967.83	173.03
	DD	923.24	1026.63	3380.53	4631.84	969.06	175.02
	ΔAIC	-1.93	1.61	-1.93	-1.97	-1.23	-1.99

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