Bottom Up Parsing

Right Sentential Forms

- Recall the definition of a derivation and a rightmost derivation
- Each of the lines is a (right) sentential form
- A form of the parsing problem is finding the correct RHS in a rightsentential form to reduce to get the previous rightsentential form in the derivation

5 F -> (E) 6 F -> id E+F*id E+id*id T+id*id F+id*id id+id*id

Motivation

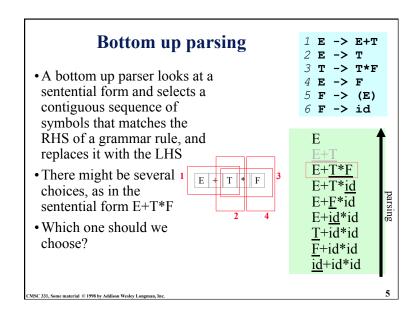
- In the last lecture we looked at a table driven, top-down parser
 - -A parser for LL(1) grammars
- In this lecture, we'll look a a table driven, bottom up parser
 - -A parser for LR(1) grammars
- In practice, bottom-up parsing algorithms are used more widely for a number of reasons

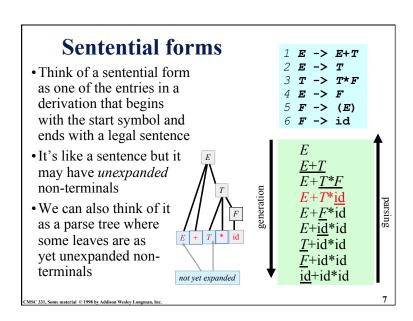
Right Sentential Forms

Consider this example

- We start with id+id*id
- What rules can apply to some portion of this sequence?
- Only rule 6: **F** -> id
- Are there more than one way to apply the rule?
- Yes, three
- Apply it so the result is part of a "right most derivation"
 - If there is a derivation, there is a right most one
- If we always choose that, we can't get into trouble

6 F -> id E F+id*id id+id*id





Bottom up parsing

- If the wrong one is chosen, it leads to failure
- •E.g.: replacing E+T with E in E+T*F yields E+F, which can't be further reduced using the given grammar
- •The **handle** of a sentential form is the RHS that should be rewritten to yield the next sentential form in the <u>right</u> most derivation

1 E -> E+T
2 E -> T
3 T -> T*F
4 E -> F
5 F -> (E)
6 F -> id

error
E*F
E+T*F
E+T*id
E+F*id
E+F*id
E+id*id
T+id*id
F+id*id
id+id*id

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Handles

- A handle of a sentential form is a substring α such that :
 - a matches the RHS of some production A -> α ; and
 - replacing α by the LHS **A** represents a step in the reverse of a rightmost derivation of s.
- For this grammar, the rightmost derivation for the input abbcde is
 S => aABe => aAde => aAbcde => abbcde

1: S -> aABe 2: A -> Abc 3: A -> b 4: B -> d

a A b c d e

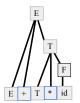
- The string **aAbcde** can be reduced in two ways:
 - (1) aAbcde => aAde (using rule 2)
 - (2) aAbcde => aAbcBe (using rule 4)
- But (2) isn't a rightmost derivation, so Abc is the only handle.
- Note: the string to the right of a handle will only contain terminals (why?)

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Phrases

- A phrase is a subsequence of a sentential form that is eventually "reduced" to a single non-terminal.
- A simple phrase is a phrase that is reduced in a single step.
- The **handle** is the leftmost simple phrase.



For sentential form E+T*id what are the •phrases: E+T*id,

T*id, id

•simple phrases: id

•handle: id

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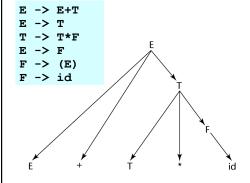
Phrases, simple phrases and handles

- **Def:** β is the *handle* of the right sentential form $\gamma = \alpha \beta w$ if and only if $S = *rm \alpha Aw = *\alpha \beta w$
- **Def:** β is a *phrase* of the right sentential form γ if and only if $S = \gamma + \alpha 1 A \alpha 2 = \beta + \alpha 1 B \alpha 2$
- **Def:** β is a *simple phrase* of the right sentential form γ if and only if $S = >* \gamma = \alpha 1 A \alpha 2 => \alpha 1 \beta \alpha 2$
- The handle of a right sentential form is its leftmost simple phrase
- Given a parse tree, it is now easy to find the handle
- Parsing can be thought of as handle pruning

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Phrases, simple phrases and handles



E E+T E+T*F E+T*id E+F*id E+id*id T+id*id F+id*id id+id*id

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On to shift-reduce parsing

- How to do it w/o having a parse tree in front of us?
- Look at a shift-reduce parser the kind that *yacc* uses
- A shift-reduce parser has a queue of input tokens & an initially empty stack. It takes one of 4 possible actions:
 - Accept: if the input queue is empty and the start symbol is the only thing on the stack
 - -Reduce: if there is a handle on the top of the stack, pop it off and replace it with the rule's RHS
 - -**Shift:** push the next input token onto the stack
 - -Fail: if the input is empty and we can't accept
- In general, we might have a choice of (1) shift, (2) reduce, or (3) maybe reducing using one of several rules
- The algorithm we next describe is deterministic

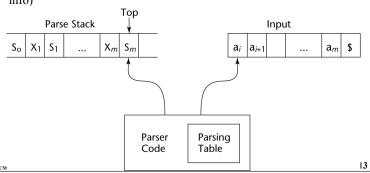
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Shift-Reduce Algorithms

A shift-reduce parser scans input, at each step decides to:

- •Shift next token to top of parse stack (along with state info) or
- •Reduce the stack by POPing several symbols off the stack (& their state info) and PUSHing the corresponding non-terminal (& state info)



LR parser table

LR shift-reduce parsers can be efficiently implemented by precomputing a table to guide the processing

				Goto					
State	id	+	*	()	S	E	Т	F
0	S5		S4				1	2	3
1		S6				accept			
2		R2	S7		R2	R2			
3		R4	R4		R4	R4			
4	S5			S4			8	2	3
5		R6	R6		R6	R6			
6	S5			S4				9	3
7	S5			S4					10
8		56			S11				
9		R1	S7		R1	R1			
10		R3	R3		R3	R3			
11		R5	R5		R5	R5			

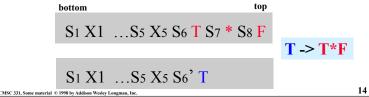
More on this Later . . .

Shift-Reduce Algorithms

The stack is always of the form



 A reduction step is triggered when we see the symbols corresponding to a rule's RHS on the top of the stack



When to shift, when to reduce

- Key problem in building a shift-reduce parser is deciding whether to shift or to reduce
- repeat: reduce if a handle is on top of stack, shift otherwise
- Succeed if there is only S on the stack and no input
- A grammar may not be appropriate for a LR parser because there are <u>conflicts</u> which can not be resolved
- Conflict occurs when the parser can't decide whether to:
- shift or reduce the top of stack (a shift/reduce conflict), or
- reduce the top of stack using one of two possible productions (a reduce/reduce conflict)
- There are several varieties of LR parsers (LR(0), LR(1), SLR and LALR), with differences depending on amount of lookahead and on construction of the parse table

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Conflicts

Shift-reduce conflict: can't decide whether to shift or to reduce

• Example : "dangling else"

Stmt -> if Expr then Stmt

| if Expr then Stmt else Stmt

• What to do when else is at the front of the input?

Reduce-reduce conflict: can't decide which of several possible reductions to make

• Example:

```
Stmt -> id ( params )
| Expr := Expr
| ...
Expr -> id ( params )
```

• Given the input a(i, j) the parser does not know whether it is a procedure call or an array reference.

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	Action							Goto			
State	id	+	*	()	\$	E	Т	F		
0	S5		S4				1	2	3		
If in state		S6				accept					
the next		R2	S7		If in state						
and go to	state 5	R4	R4		no more we are d	input, one R4					
4	\$5			S4			8	2	3		
5		R6	R6		R6	R6					
	If in state 5 a			S4				9	3		
7	6. Use goto t	able and	exposed	S4					10		
8	state to selec	S6	te	J	S11				1: E ·	 -> E+T	
9		R1	S7		R1	R1			2: E	-> T	
10		R3	R3		R3	R3				-> T*F -> F	
11		R5	R5		R5	R5				-> (E) -> id	
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LR Table

- An LR configuration stores the state of an LR parser (S0X1S1X2S2...XmSm, aiai+1...an\$)
- LR parsers are table driven, where the table has two components, an ACTION table and a GOTO table
- The ACTION table specifies the action of the parser (shift or reduce) given the parser state and next token
 - -Rows are state names; columns are terminals
- The GOTO table specifies which state to put on top of the parse stack after a reduce
 - -Rows are state names; columns are non-terminals

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Parser actions

Initial configuration: (S0, a1...an\$)

Parser actions:

- 1 If ACTION[Sm, ai] = Shift S, the next configuration is: (S0X1S1X2S2...XmSmaiS, ai+1...an\$)
- 2 If ACTION[Sm, ai] = Reduce $A \rightarrow \beta$ and S = GOTO[Sm-r, A], where r = the length of β , the next configuration is

(S0X1S1X2S2...Xm-rSm-rAS, aiai+1...an\$)

- 3 If ACTION[Sm, ai] = Accept, the parse is complete and no errors were found
- 4 If ACTION[Sm, ai] = Error, the parser calls an error-handling routine

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1: E -> E+T 2: E -> T **Example** 3: T -> T*F 4: T -> F 5: $F \rightarrow (E)$ 6: F -> id Stack Input action Id + id * id \$ Shift 5 0 id 5 + id * id \$ Reduce 6 goto(0,F) 0 F 3 + id * id \$ Reduce 4 goto(0,T) 0 т 2 + id * id \$ Reduce 2 goto(0,E) 0 E 1 + id * id \$ Shift 6 0 E 1 + 6 id * id \$ Shift 5 0 E 1 + 6 id 5 * id \$ Reduce 6 goto(6,F) 0 E 1 + 6 F 3 * id \$ Reduce 4 goto(6,T) * id \$ Shift 7 0 E 1 + 6 T 9 0 E 1 + 6 T 9 * 7 id \$ Shift 5 0 E 1 + 6 T 9 * 7 id 5 Reduce 6 goto(7,E) 0 E 1 + 6 T 9 * 7 F 10 Reduce 3 goto(6,T) 0 E 1 + 6 T 9 Reduce 1 goto(0,E) 0 E 1 Accept 21 CMSC 331, Some material © 1998 by Addison Wesley Longman, Inc

Yacc as a LR parser

- The Unix yacc utility is just such a parser.
- It does the heavy lifting of computing the table
- To see the table information, use the –v flag when calling yacc, as in yacc –v test.y

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```
0 $accept : E $end
  1 E : E '+' T
  3 T:T'*'F
  5 F: '(' E')'
      | "id"
       $accept : . E $end (0)
       '(' shift 1
"id" shift 2
       . error
       E goto 3
       T goto 4
       F goto 5
state 1
       F: '(' . E')' (5)
       '(' shift 1
       "id" shift 2
       . error
       E goto 6
       T goto 4
       F goto 5
```

			Goto						
State	id	+	*	()	\$	E	Т	F
0	S5		S4				1	2	3
1		S6				accept			
2		R2	S7		R2	R2			
3		R4	R4		R4	R4			
4	S5			S4			8	2	3
5		R6	R6		R6	R6			
6	S5			S4				9	3
7	S5			S4					10
8		S6			S11				
9		R1	S7		R1	R1			
10		R3	R3		R3	R3			
11		R5	R5		R5	R5			

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