## Converting Returns:

## Effective rates, APR's and

## Continuously Compounded rates

Question 1: A stock was bought for $\$ 10$ and sold one month later for \$10.50.
a) What is the effective monthly rate of return?
$V_{0}=\frac{V_{t}}{\left(1+r_{e f f}\right)^{t}}$
b) What is the APR compounding per month?
$r_{A P R, \text { comp monthly }}=$
c) What is the effective annual rate of return?
$r_{\text {eff,annual }}=$
d) What is the continuously compounded monthly rate of return?
$r_{c c, \text { monthly }}=$
e) What is the continuously compounded annual rate of return?
$r_{c c, a n n u a l}=$

Question 2: A credit card advertises an interest rate of $24 \%$.
Note that credit cards are paid monthly so the interest rate is quoted as an Annualised Percentage Rate (APR) compounding per month.
a) Find the effective monthly rate.
$r_{e f f, \text { monthly }}=$
b) Find the effective annual rate.
$r_{\text {eff,annual }}=$
c) Find the effective 6 month rate.
$r_{e f f, 6 m t h}=$
d) Find the effective quarterly rate.
$r_{e f f, q t r l y}=$
e) Find the Annualised Percentage Rate (APR), compounding every 6 months ( $r_{A P R, \text { comp per } 6 \mathrm{mths}}$ ).
$r_{\text {APR,comp per 6mths }}=$
f) Find the APR compounding per day ( $r_{A P R, \text { comp daily }}$ ). Assume 30 days in a month and 360 days in a year.
$r_{A P R, \text { comp daily }}=$
g) Find the continuously compounded rate per year ( $r_{\text {cc annual }}$ ). Assume 30 days in a month and 360 days in a year.
h) Find the continuously compounded rate per month ( $r_{c c}$ monthly $)$. Assume 30 days in a month and 360 days in a year.
i) Find the continuously compounded rate per day ( $r_{c c}$ daily $)$. Assume 30 days in a month and 360 days in a year.

Question 3: A bond is advertised with a coupon rate of 7\%, paid semiannually. The yield of the bond is $6 \%$.

Note that the bond pays semi-annual coupons so the yield is quoted as an Annualised Percentage Rate (APR) compounding every 6 months.
a) Find the effective six-month rate.
$r_{e f f, 6 m t h}=$
b) Find the effective annual rate.
$r_{\text {eff,annual }}=$
c) Find the effective monthly rate.
$r_{\text {eff,monthly }}=$
d) Find the effective quarterly rate.
$r_{e f f, q t r l y}=$
e) Find the Annualised Percentage Rate (APR), compounding every week. Assume 52 weeks per year. ( $r_{A P R, c o m p ~ w e e k l y}$ ).
$r_{A P R, \text { comp weekly }}=$
f) Find the APR compounding per day. Assume 30 days in a month and 360 days in a year.
$r_{A P R, \text { comp daily }}=$
g) Find the continuously compounded rate per year ( $r_{\text {cc annual }}$ ). Assume 30 days in a month and 360 days in a year.
h) Find the continuously compounded rate per month ( $r_{c c}$ monthly $)$. Assume 30 days in a month and 360 days in a year.
i) Find the continuously compounded rate per day ( $r_{c c}$ daily). Assume 30 days in a month and 360 days in a year.

