

**PLEM1****PURPOSE**

Compute the real component of the first derivative of the Weierstrass P elliptic function of a complex number (lemniscatic case with unit period parallelogram).

**DESCRIPTION**

The Weierstrass elliptic function is described in detail in the Handbook of Mathematical Functions (see REFERENCE section below).

**SYNTAX 1**

LET <ar> = PLEM1(<xr>,<xc>) <SUBSET/EXCEPT/FOR qualification>  
 where <xr> is a number, parameter, or variable that specifies the the real component of the input;  
 <xc> is a number, parameter, or variable that specifies the the complex component of the input;  
 <ar> is a variable or a parameter (depending on what <xr> and <xc> are) where the computed values are stored;  
 and where the <SUBSET/EXCEPT/FOR qualification> is optional.

This syntax computes the real component.

**SYNTAX 2**

LET <ac> = PLEM1I(<xr>,<xc>) <SUBSET/EXCEPT/FOR qualification>  
 where <xr> is a number, parameter, or variable that specifies the the real component of the input;  
 <xc> is a number, parameter, or variable that specifies the the complex component of the input;  
 <ac> is a variable or a parameter (depending on what <xr> and <xc> are) where the computed values are stored;  
 and where the <SUBSET/EXCEPT/FOR qualification> is optional.

This syntax computes the complex component.

**EXAMPLES**

```
LET AR = PLEM1(2,1)
LET AC = PLEM1I(2,1)
LET AR = PLEM1(X,4)
LET AC = PLEM1I(X,4)
```

**NOTE 1**

The Weierstrass elliptic functions are computed using algorithm 549 from the ACM Transactions on Mathematical Software (see the REFERENCE section below).

**NOTE 2**

If the input value corresponds to a lattice point, an error message is printed and the output value is set to the largest real number on the machine.

**DEFAULT**

None

**SYNONYMS**

None

**RELATED COMMANDS**

PEQ	=	Compute the real component of the Weierstrass elliptic function (equianharmonic case).
PEQ1	=	Compute the real component of the first derivative of the Weierstrass elliptic function (equianharmonic case).
PLEM	=	Compute the real component of the Weierstrass elliptic function (lemniscatic case).
SN	=	Compute the Jacobi elliptic function sn.
RF	=	Compute the Carlson elliptic integral of the first kind.
RD	=	Compute the Carlson elliptic integral of the second kind.
ELLIP1	=	Compute the Legendre elliptic integral of the first kind.

## REFERENCE

“Algorithm 549: Weierstrass’ Elliptic Functions,” Eckhardt, ACM Transactions on Mathematical Software, vol. 6 (pp. 112-120).

“Handbook of Mathematical Functions, Applied Mathematics Series, Vol. 55,” Abramowitz and Stegun, National Bureau of Standards, 1964 (chapter 18).

## APPLICATIONS

Special Functions

## IMPLEMENTATION DATE

94/11

## PROGRAM

```
X2LABEL DASH = COMPLEX COMPONENT
TITLE WEIERSTRASS ELLIPTIC FUNCTIONS
LINE SOLID DASH
MULTIPLY 2 2; MULTIPLY CORNER COORDINATES 0 0 100 100
LET C = 0.1
PLOT PLEM1(X,C) FOR X = 0.1 0.01 0.9 AND
PLOT PLEM1I(X,C) FOR X = 0.1 0.01 0.9
LET C = -0.1
PLOT PLEM1(X,C) FOR X = 0.1 0.01 0.9 AND
PLOT PLEM1I(X,C) FOR X = 0.1 0.01 0.9
LET C = 0.25
PLOT PLEM1(X,C) FOR X = 0.1 0.01 0.9 AND
PLOT PLEM1I(X,C) FOR X = 0.1 0.01 0.9
LET C = -0.25
PLOT PLEM1(X,C) FOR X = 0.1 0.01 0.9 AND
PLOT PLEM1I(X,C) FOR X = 0.1 0.01 0.9
END OF MULTIPLY
```

