

# Fire sales, price-mediated contagion and systemic risk.

Financial Risk & Network Theory - Cambridge September 2016  
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Joint work with Rama Cont<sup>a</sup>

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## Disclaimer

This presentation should not be reported as representing the views of Norges Bank. The views expressed are mine only and do not necessarily reflect those of Norges Bank (or my co-authors).

# Overview

- 1 Introduction: Price-mediated contagion and endogenous risk
- 2 Modelling fire sales
- 3 Empirical application: European Banking Network
- 4 Conclusion

# Stress testing 3.0

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**Goal:** Develop models for macro stress testing that can quantify such second round effects in a realistic and robust way.

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  - ⑤ The price impact function and liquidity models (Klye & Obizhaeva (2011 - 2016), BoE: RAMSI)

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## Mechanism:

- 1 **Shock** to illiquid assets
- 2 **Deleveraging** of marketable assets by some institutions
- 3 **Feedback effects** via price-mediated contagion  
 $\rightarrow$  potentially triggers more deleveraging (cascade).

# Model balancesheet

<b>Illiquid assets</b>
Residential mortgage exposures Commercial real estate exposure Retail exposures: Revolving credits, SME, Other Indirect sovereign exposures in the trading book Defaulted exposures Residual exposures
<b>Marketable assets</b>
Corporate bonds Sovereign debt Direct sovereign exposures in derivatives Institutional client exposures: interbank, CCPs,...

Table: Stylized representation of asset classes in bank balance sheets.

- A stress scenario is defined by a vector  $\epsilon \in [0, 1]^K$  whose components  $\epsilon_\mu$  are the percentage shocks to asset class  $\mu$ .
- Gradual increase of the shock from 0% to 20%.
- Four scenarios:
  1. Spanish residential and commercial real estate losses
  2. Northern Europe residential losses
  3. Southern Europe commercial real estate losses
  4. Eastern Europe commercial real estate losses



# Response functions

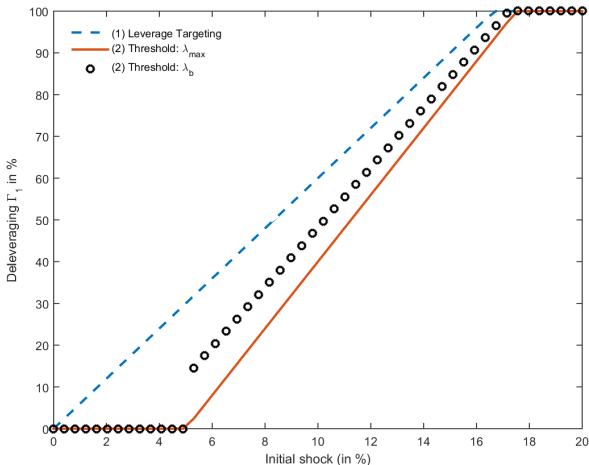


Figure: Leverage targeting response function (dashed) and two variants of the threshold (full and circles) response functions.

## Price impact

The price of an asset undergoing a forced liquidation at  $t$ :

$$S_{t+1}^{\mu} = S_t^{\mu} \exp \left( -\delta_{\mu}^{-1} \sum_{j=1}^M \Pi_t^{j\mu} \Gamma_{t+1}^j \right) \quad (1)$$

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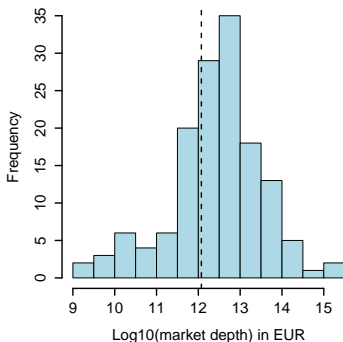
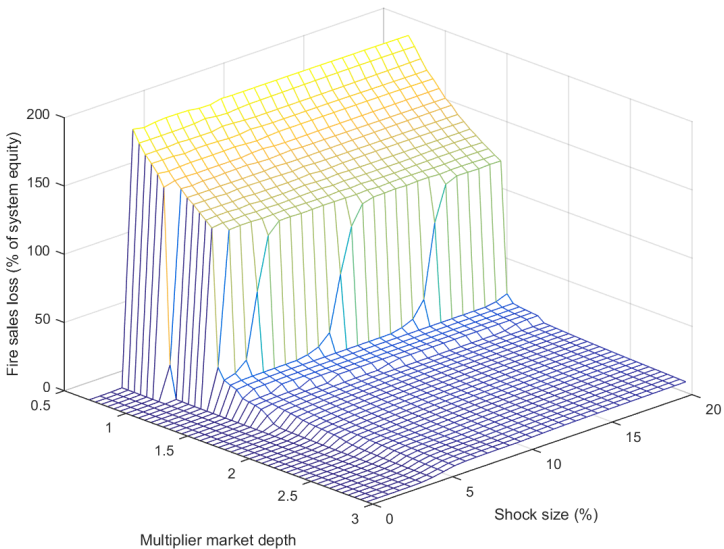


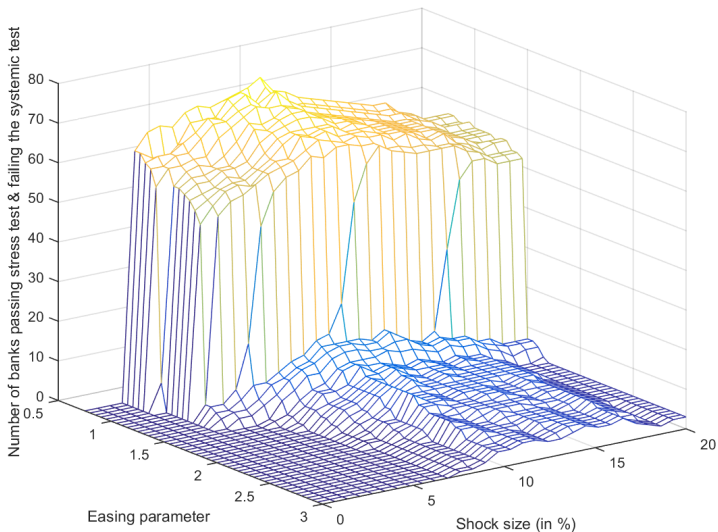
Figure: Large variation in estimated liquidity of different assets.

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# Fire sales losses and market depth



# Indirect exposures and stress test outcomes



# Liquidity weighted overlap

Our model shows that losses are proportional to the liquidity weighted overlap

$$\omega_{ij} := \sum_{\mu=1}^M \frac{\Pi_{i\mu} \Pi_{j\mu}}{\delta_{\mu}} \quad (2)$$

This leads to a network of portfolio overlaps:

$$\Omega := \Pi D^{-1} \Pi^{\top}, \quad (3)$$

which can be studied with network analysis tools.

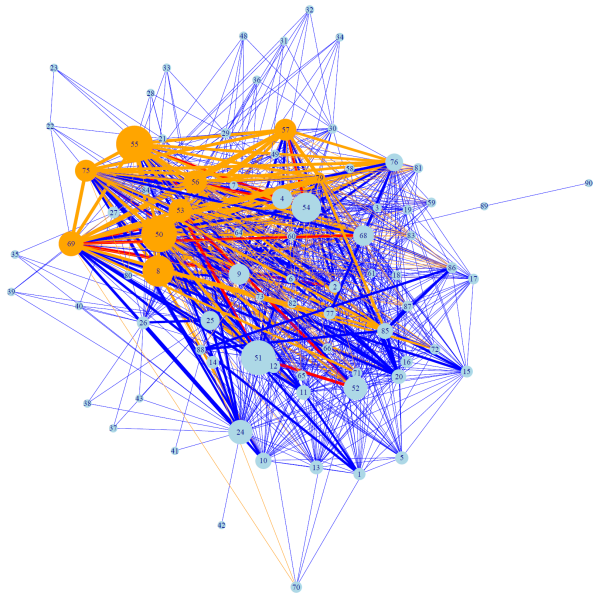


Figure: European banking system: liquidity weighted overlap network



Omega1: EV 1

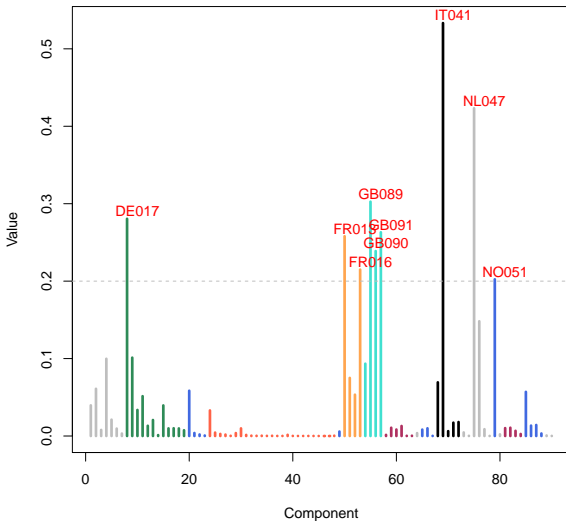


Figure: European banking system: Liquidity weighted overlaps

## Omega2: EV 1

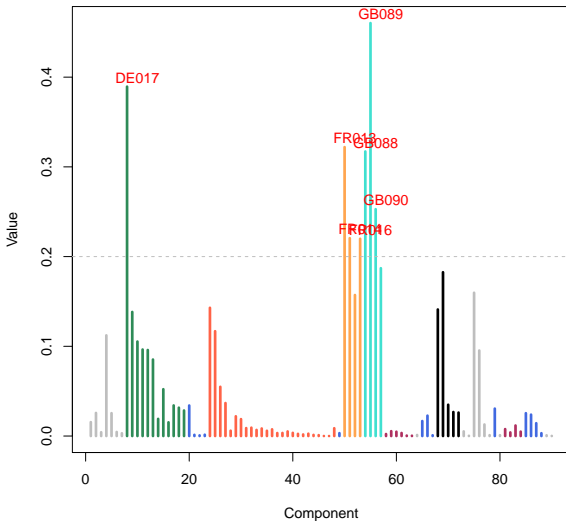


Figure: European banking system: Nominal overlaps

# Distribution of fire sales losses

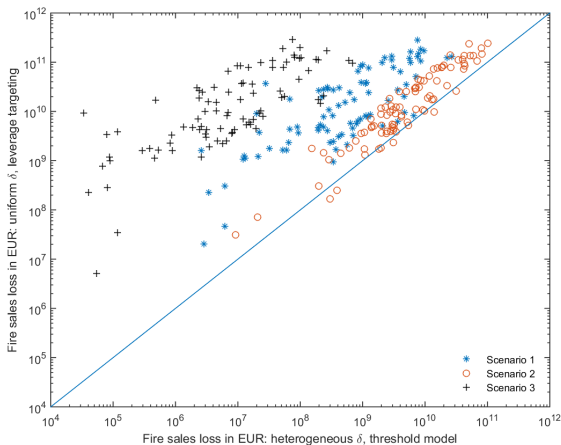


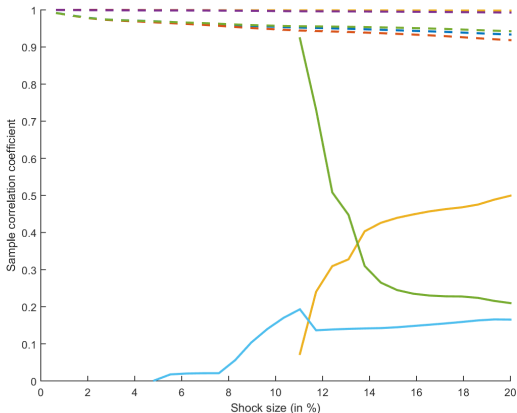
Figure:  $\log_{10}$ (fire sales loss) for different scenarios and different model combinations.

# Sensitivity to initial stress scenario

Scenario combination	Sample correlation coefficient
1 & 2	0.0840
1 & 3	0.2130
1 & 4	-0.1449
2 & 3	-0.0509
2 & 4	0.0394
3 & 4	-0.0149

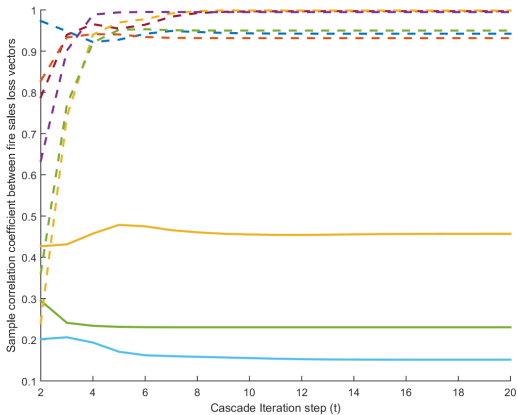
**Table:** Sample correlations between the initial loss vectors from the stress scenarios. The four stress scenarios are very different in terms of which banks are hit by the corresponding shock.

# Sensitivity to initial stress scenario



**Figure:** The pairwise sample correlation between the fire sales loss vectors of different scenarios as a function of the initial shock. Threshold model full lines - leverage targeting dashed lines.

# Sensitivity to initial stress scenario



**Figure:** The evolution of the pairwise sample correlation during the fire sales cascade for a given scenario. Threshold full - leverage targeting dashed.

## Risk management for whales (Cont and Wagalath 2016)

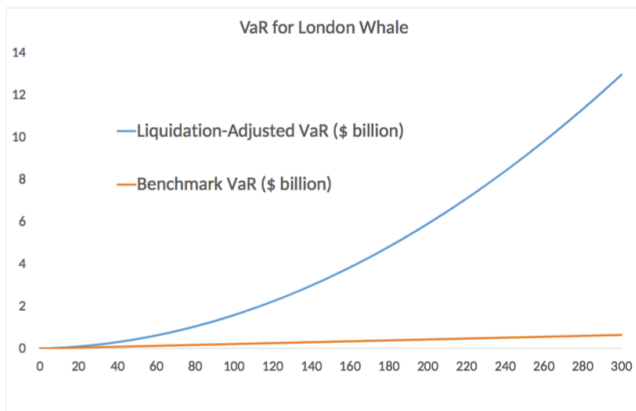


Figure 6: 95% 5-month VaR for positions in CDX IG9 (size in Bn \$).

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- The risk of fire sales generates indirect exposures. These can be quantified but depend on the entire network of portfolio holdings.
- Including fire sales and endogenous mechanisms (with realistic parameter estimates) can change the outcome of stress tests: Next generation stress testing models must include such feedback effects.
- Seemingly innocent modelling choices on response functions and liquidity estimates have a significant effect on results!

## Conclusions for modelling

- Important to account for heterogeneity in agent resilience and asset liquidity. Any meaningful fire sales stress test needs to include a sensitivity analysis on the market depth parameter.

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- The threshold model generates more realistic short term dynamics under stress. Leverage targeting models seem better suited to capture long term dynamics.
- Leverage targeting models produce counter-intuitive short term dynamics.
- Singular value decompositions of liquidity weighted overlap matrices can provide valuable information for monitoring purposes and policy responses.





Thank you!











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