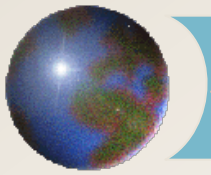


# *Pressure Gradients*

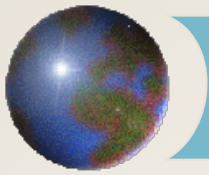
GEOG/ENST 2331 – Lecture 7  
Ahrens: Chapter 8  
Lab 2



# *Mechanics: $F = ma$*

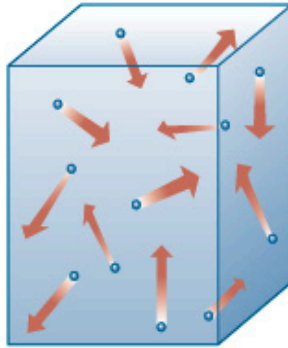
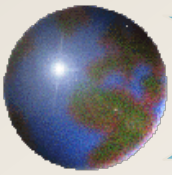
✦ What exerts force in the atmosphere?

- ✦ Pressure gradients
- ✦ Gravity
- ✦ Coriolis effect
- ✦ Friction

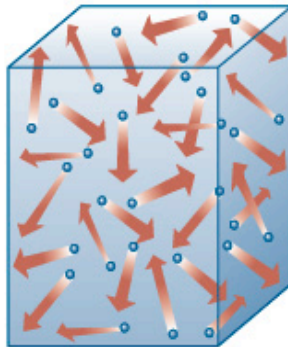


## *Review: Pressure*

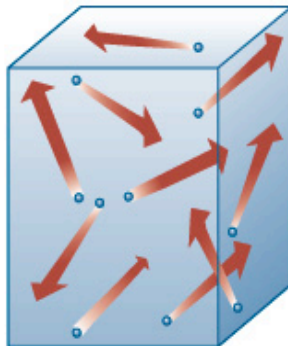
- ⊕ Atmospheric pressure is force per unit area exerted by atmospheric gases (all directions)
- ⊕ Commonly expressed in *millibars* or *hectopascals*
  - ⊞ *1 hPa = 100 Pa = 1 mb*
- ⊕ Surface pressure is close to 1000 hPa
  - ⊞ Varies with time and place



(a)



(b)



(c)

## *Ideal Gas Law*

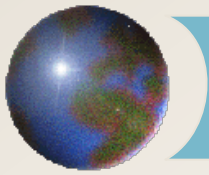
- ✦ Pressure, density and temperature of air are related by the Ideal Gas Law:

- ✦  $P = \rho TC$

- ✦  $C$  is the gas constant

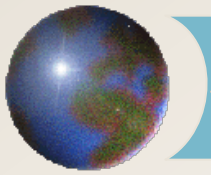
- ✦ For air,  $C = 287$  [J/kg·K]

- ✦ See Ahrens pp. 228-229



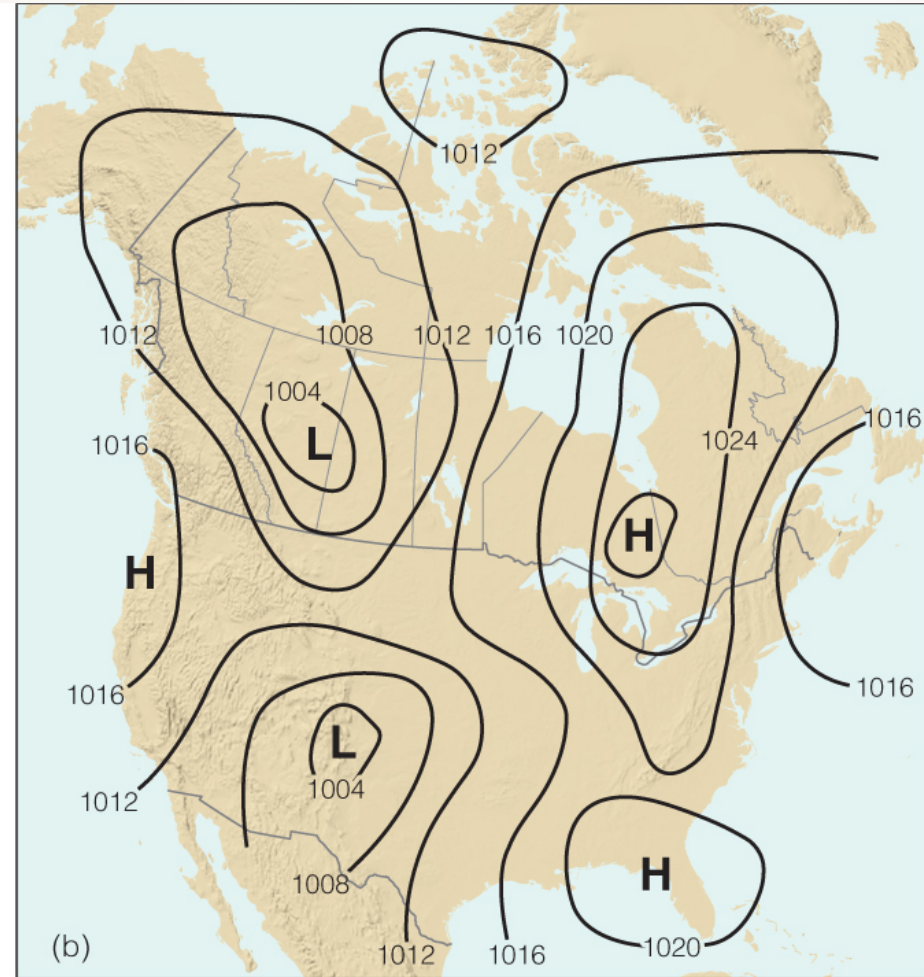
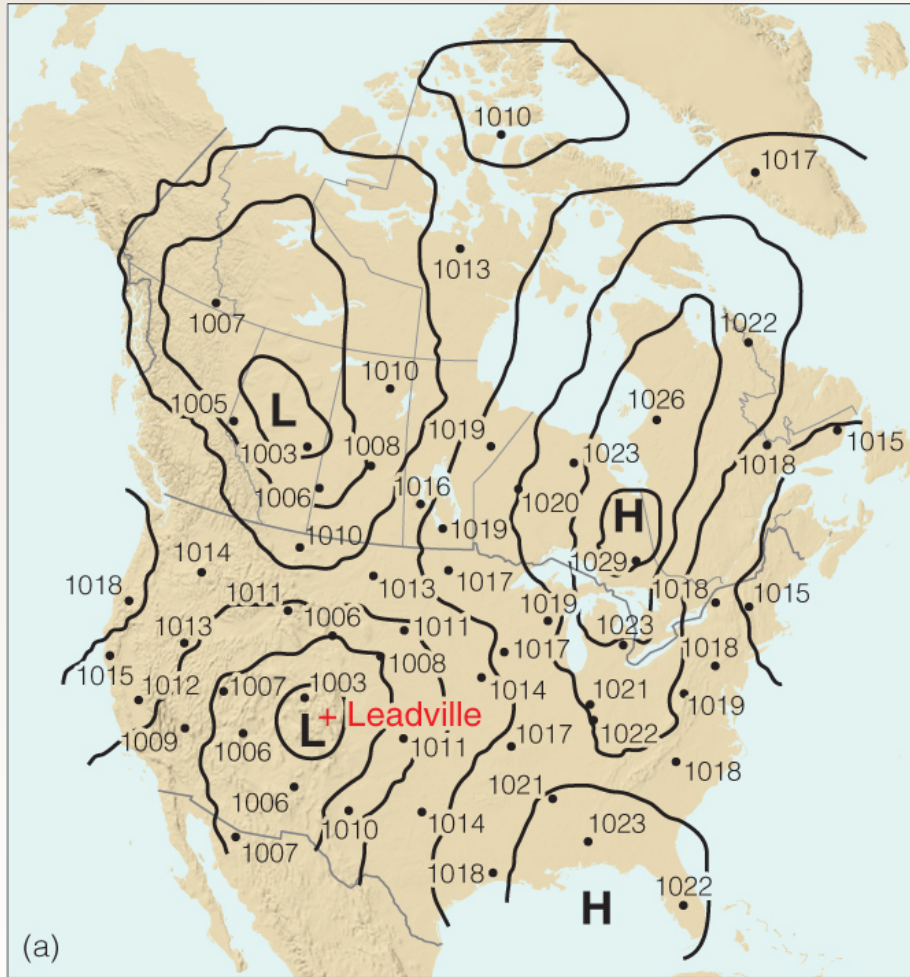
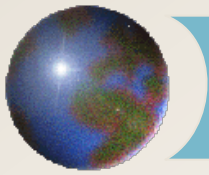
# *Partial Pressures*

- ✦ In a mixture of gases, each individual gas exerts its own *partial pressure*
  - ▣ E.g.  $p\text{CO}_2$  or  $p\text{H}_2\text{O}$
- ✦ Dalton's Law: the sum of the partial pressures equals the total pressure

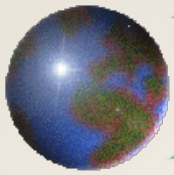


# *Charting pressure*

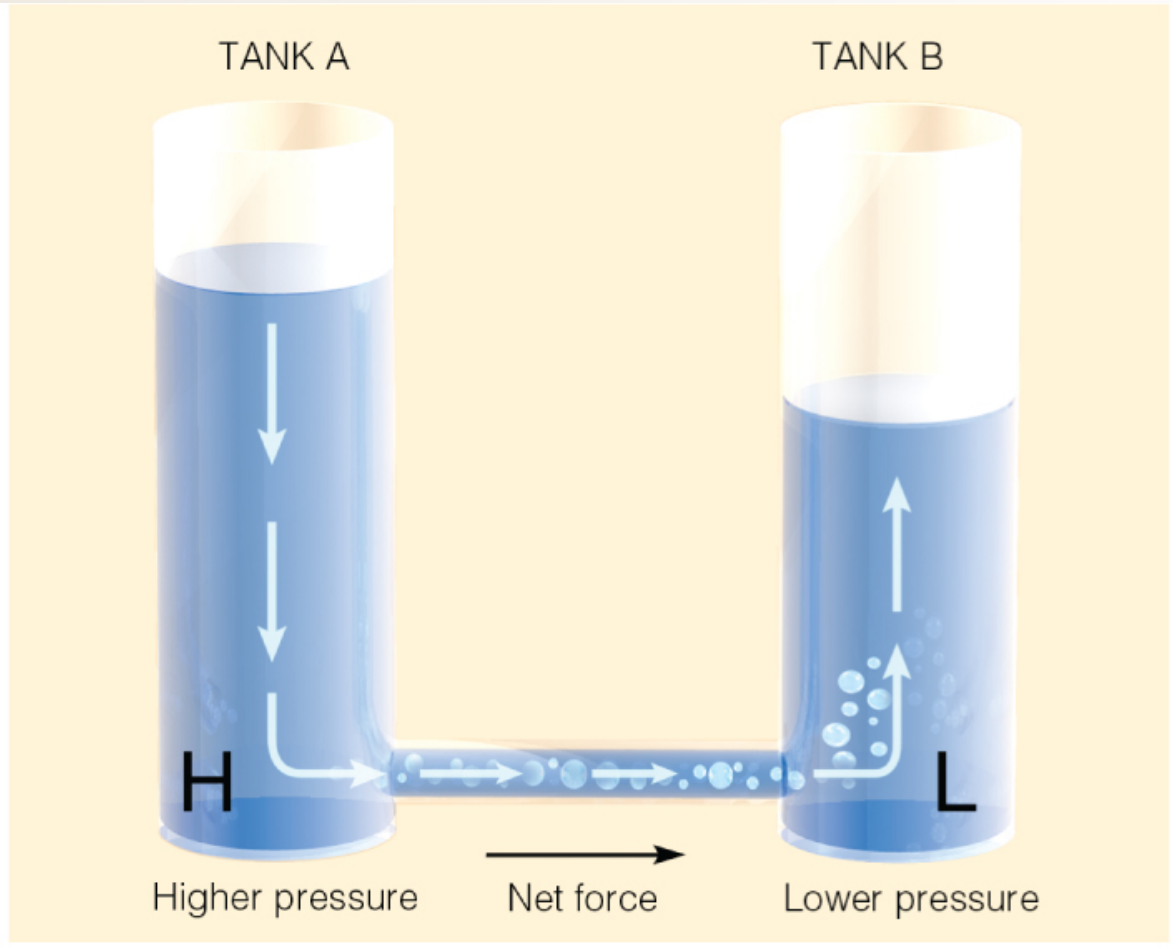
- ✦ *Isobars* – lines of constant pressure
  
- ✦ *Pressure Gradient* – the change in pressure over distance
  - ✦ Zonal
  - ✦ Meridional
  - ✦ or Vertical
  
- ✦ Blocking situations



Ahrens: Figure 8.10



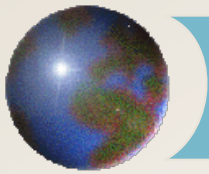
# *Pressure gradient force*



- ➊ Tendency for fluids to flow from high pressure to low pressure

Ahrens: Fig. 8.17



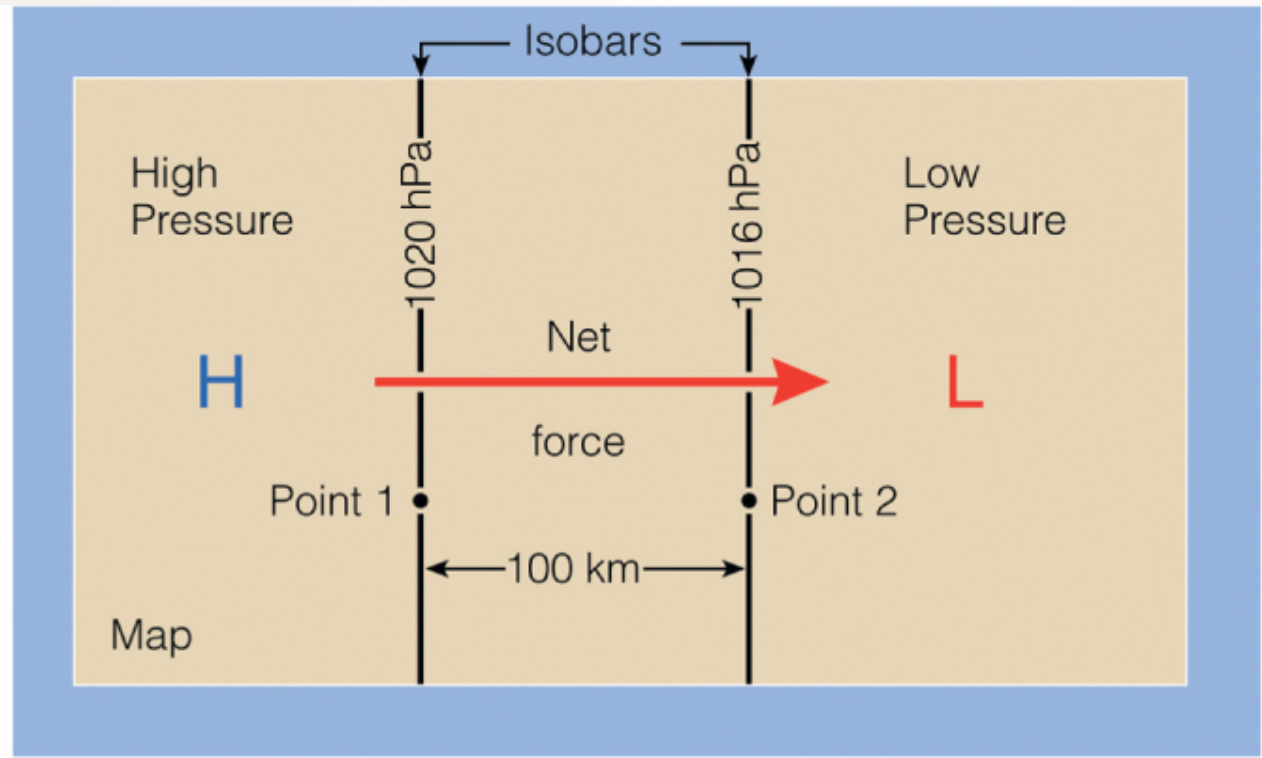


# *Horizontal pressure gradient force*

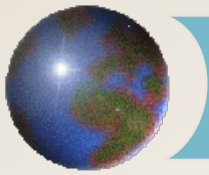
Horizontal pressure differences are usually slight.

Strong pressure gradients indicate strong winds and storms.

Ahrens: Fig. 8.18



$$\text{PGF} = -\frac{1}{\rho} \frac{\Delta P}{\Delta x}$$

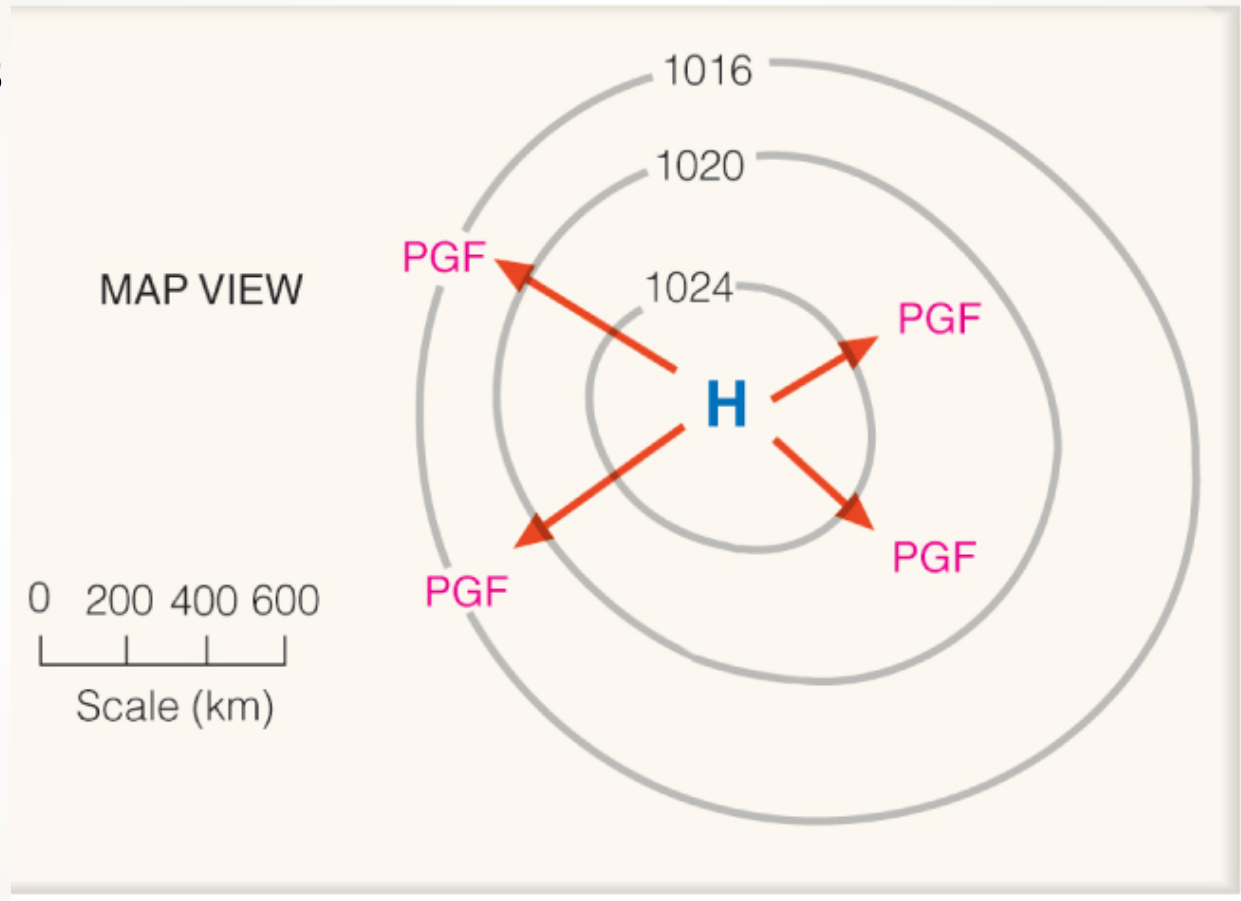


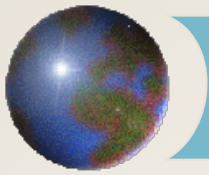
# *PGF*

PGF is always  
perpendicular to isobars

Closely spaced isobars  
indicate stronger PGF

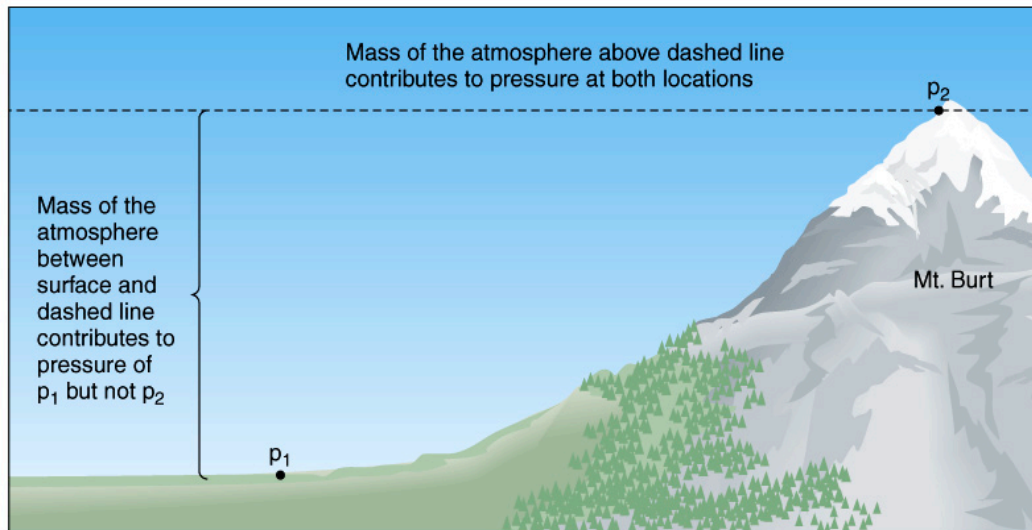
Ahrens: Fig. 8.19



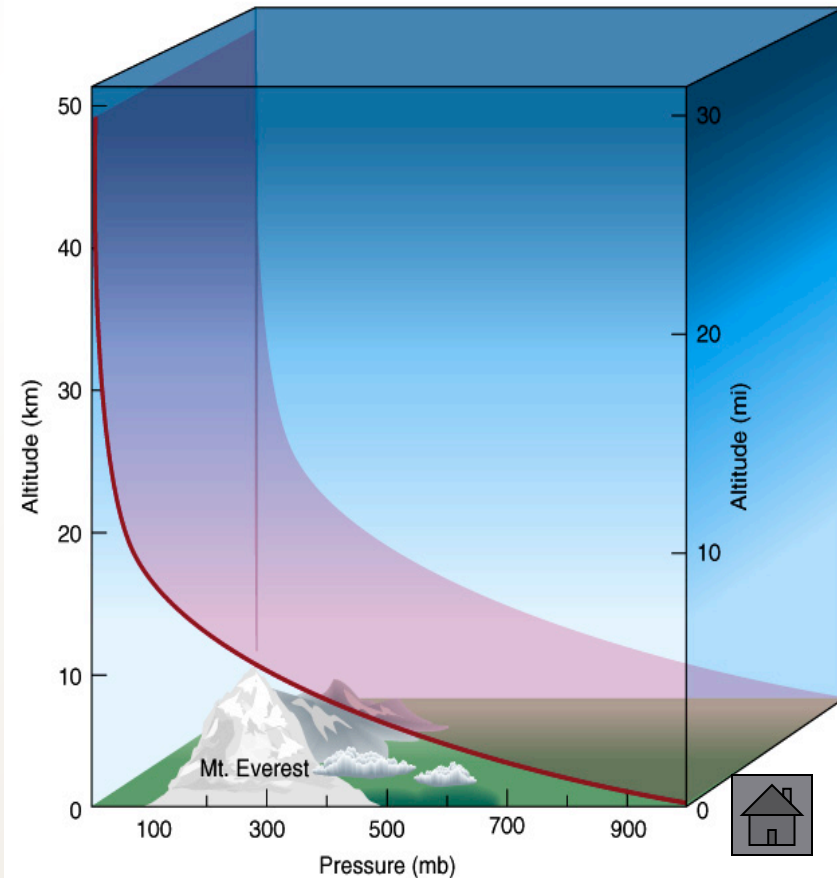


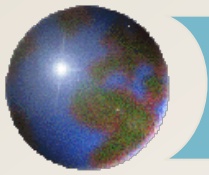
# Vertical Changes in Pressure

- ✦ Pressure decreases with height
- ✦ Exponential: roughly 50% every 5.5 km



A&B: Figures 4-2 and 4-3





# *Coordinate system*

## Cartesian system $(x, y)$

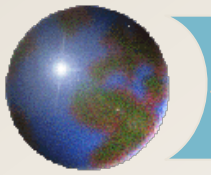
$x$  – zonal (East/West) direction – East is positive

$y$  – meridional (North/South) direction – North is positive

$z$  – vertical – up is positive

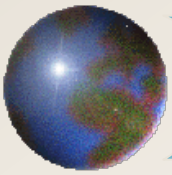
$u$  – velocity in the  $x$  direction

$v$  – velocity in the  $y$  direction



# *Gravitational force*

- ✚ Force of attraction between two masses
- ✚ Earth approximation:
  - ▣  $GF = mg, g = 9.8 \text{ N/kg}$
- ✚ Vertical force (always pulls 'down')

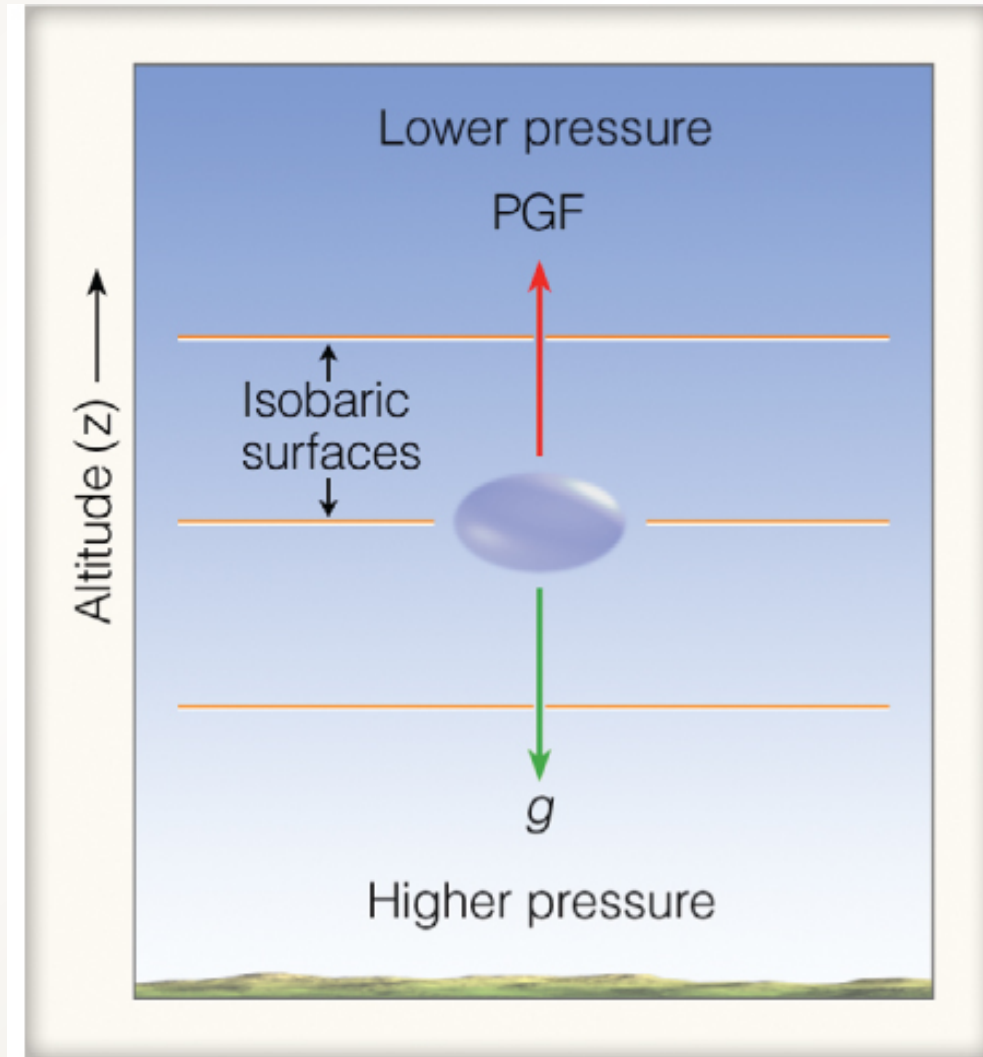


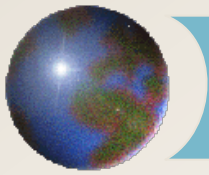
# *Hydrostatic Balance*

A vertical balance of forces

- Pressure gradient force and gravity are equal
- No net vertical acceleration

$$\Delta P = -\rho g \Delta z$$





# *Vertical pressure gradients*

Pressure always decreases with height  
Vertical pressure gradients are  
balanced by gravity

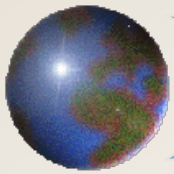
$$P = \rho C T$$

$$\Delta P = -\rho g \Delta z$$

**Scale height,  $H$ ,** is a vertical distance  
over which the pressure drops by a  
constant factor

$$H = \frac{C T}{g}$$

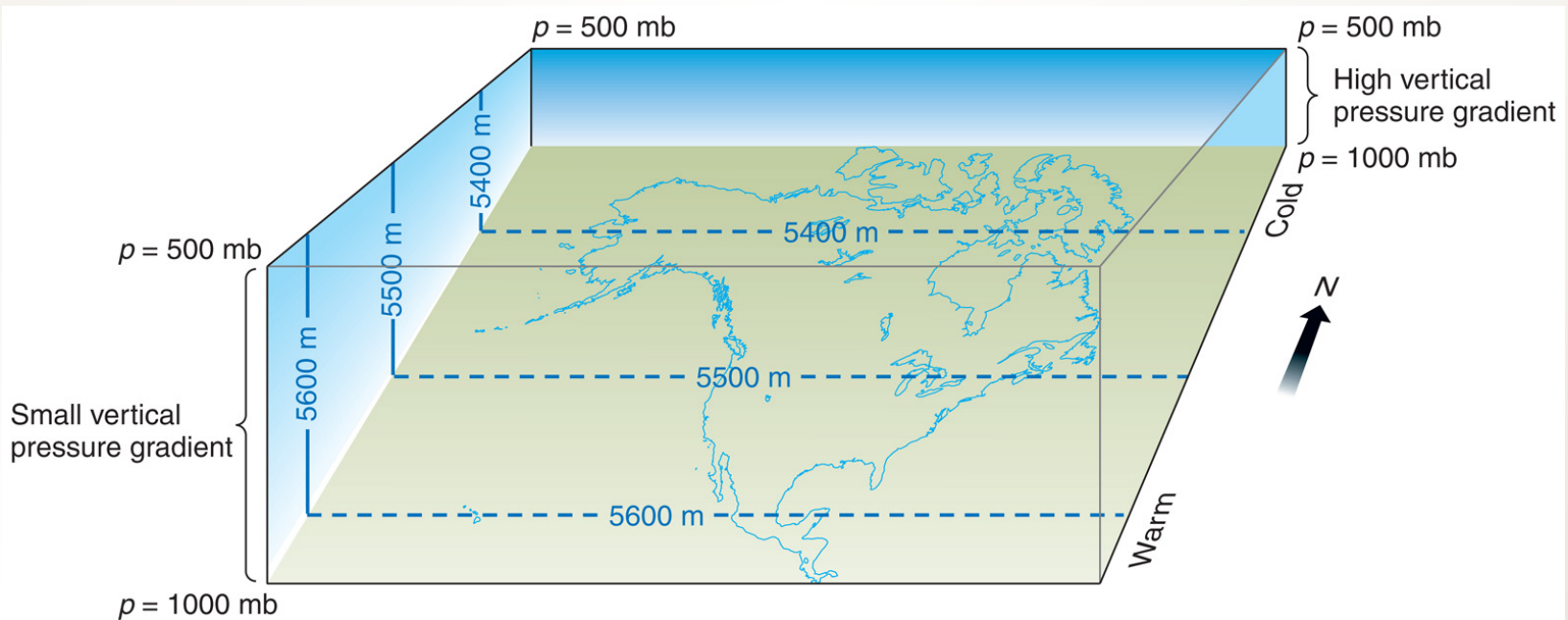
$T$  is the average temperature in the  
column of height  $H$



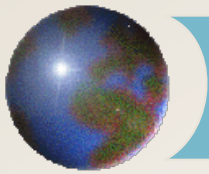
# Scale Height

- ✦ If  $T$  is large, then  $H$  is large and the pressure reduces more slowly with height.
  - ✦ If  $T$  is small the opposite is true.
- ✦ For example, the tropopause occurs at 250 hPa. The height of the tropopause is 8 km at the poles and 13 km at the equator.
  - ✦ This is consistent with the scale height analysis

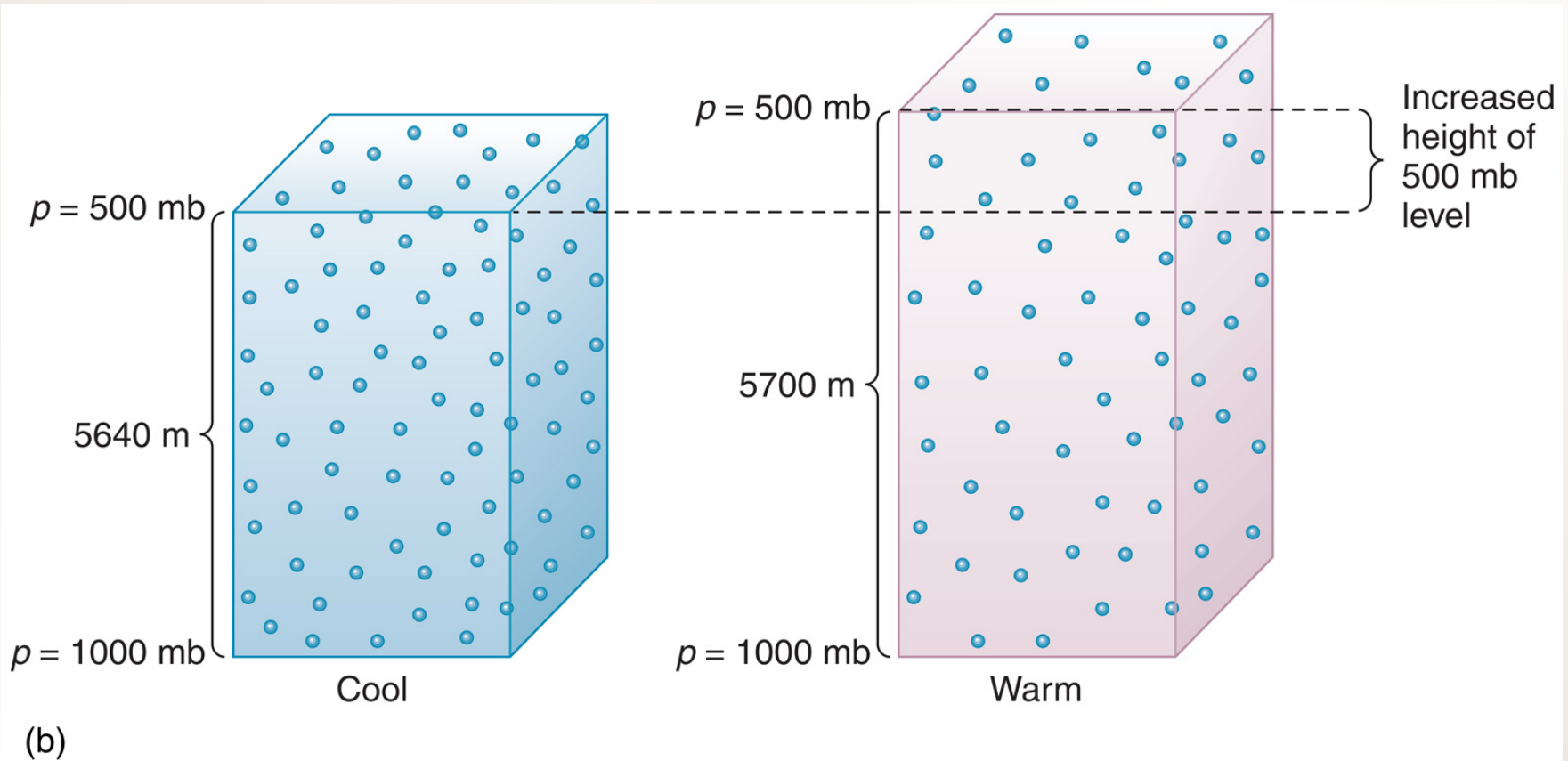
$$H = \frac{CT}{g}$$





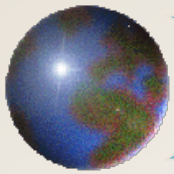


# *Temperature and scale height*



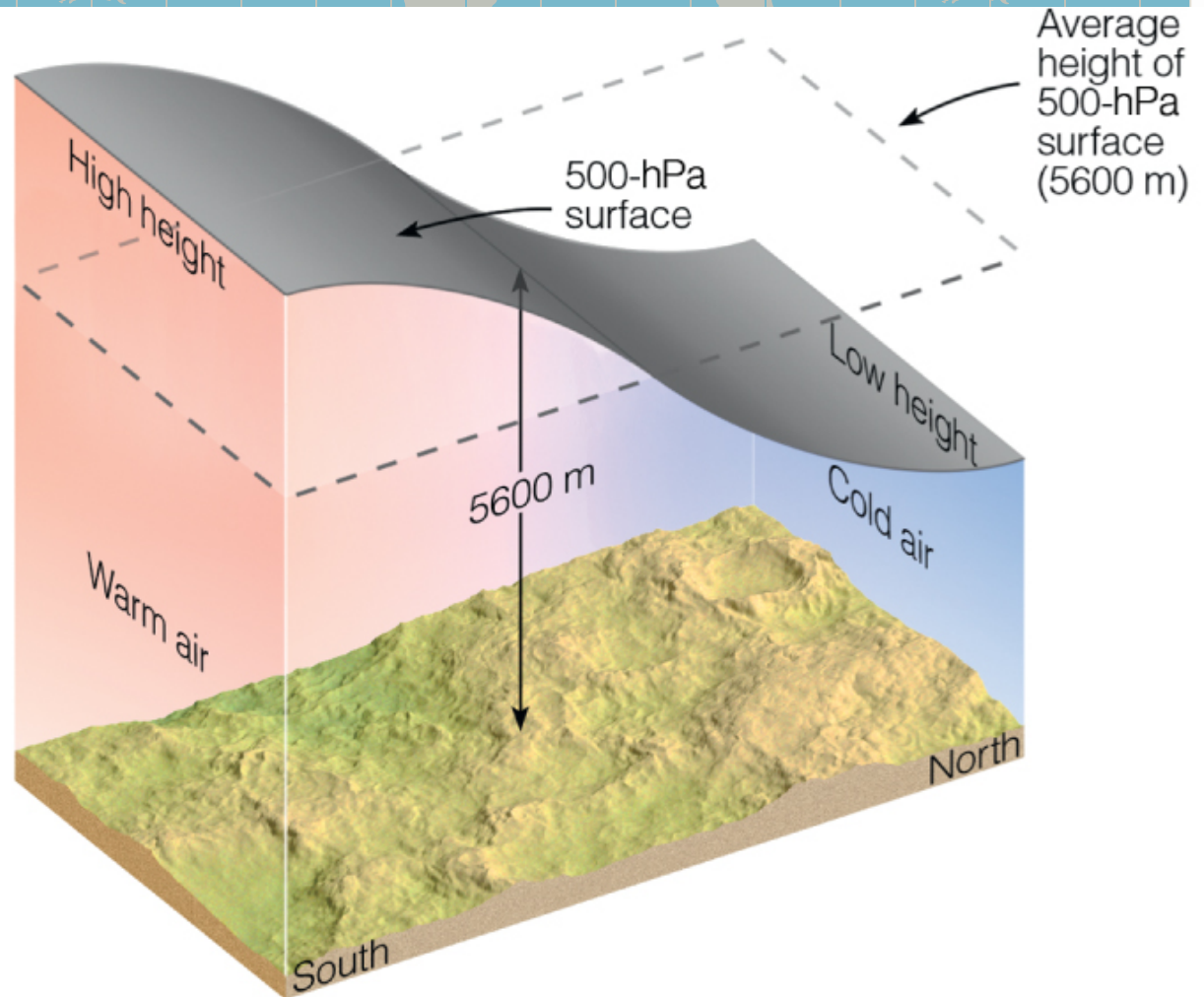
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**A&B: Figure 4-7**

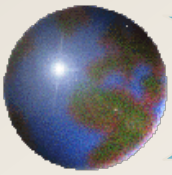


# Upper air

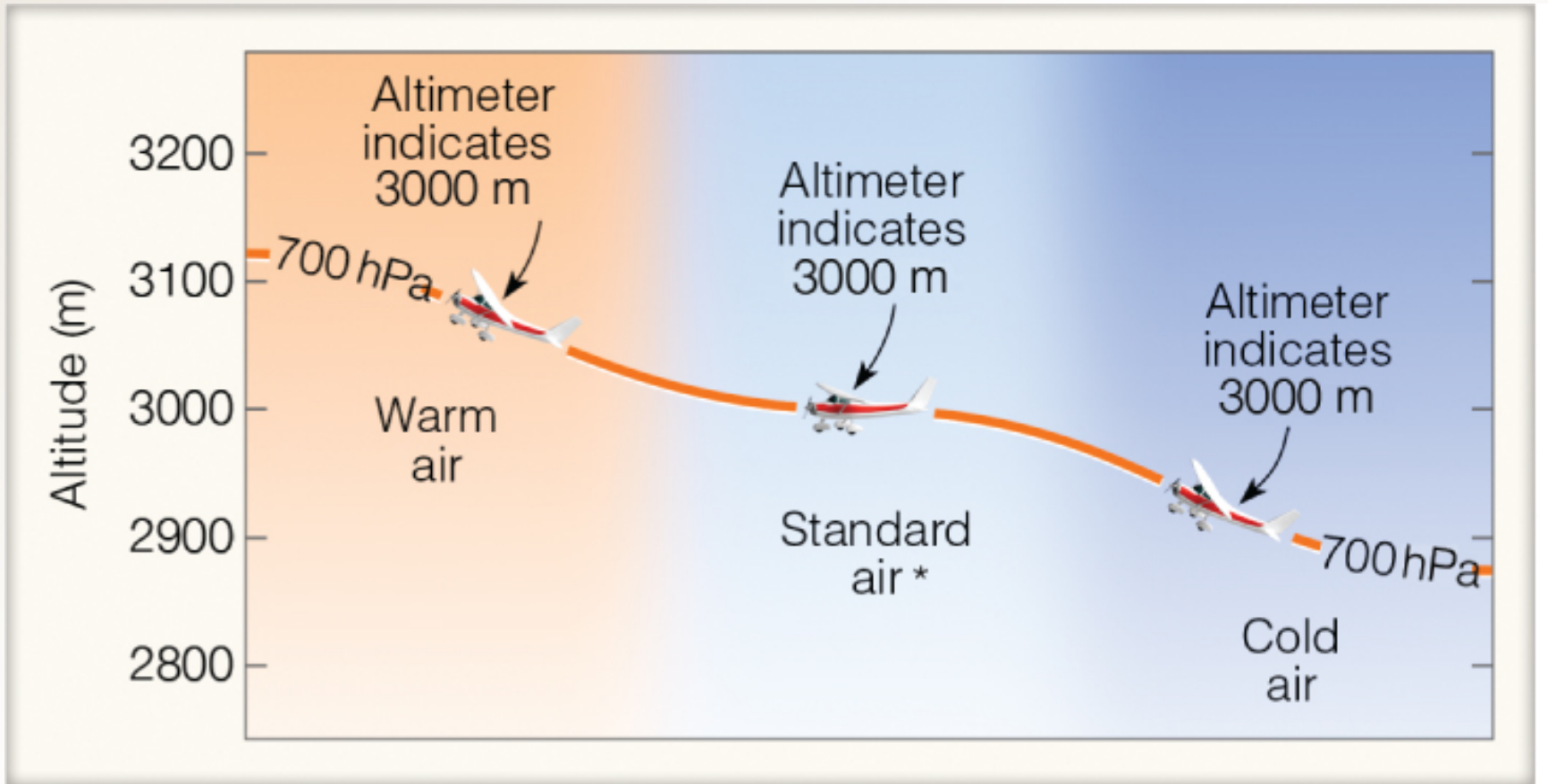
Height of constant pressure decreases with temperature



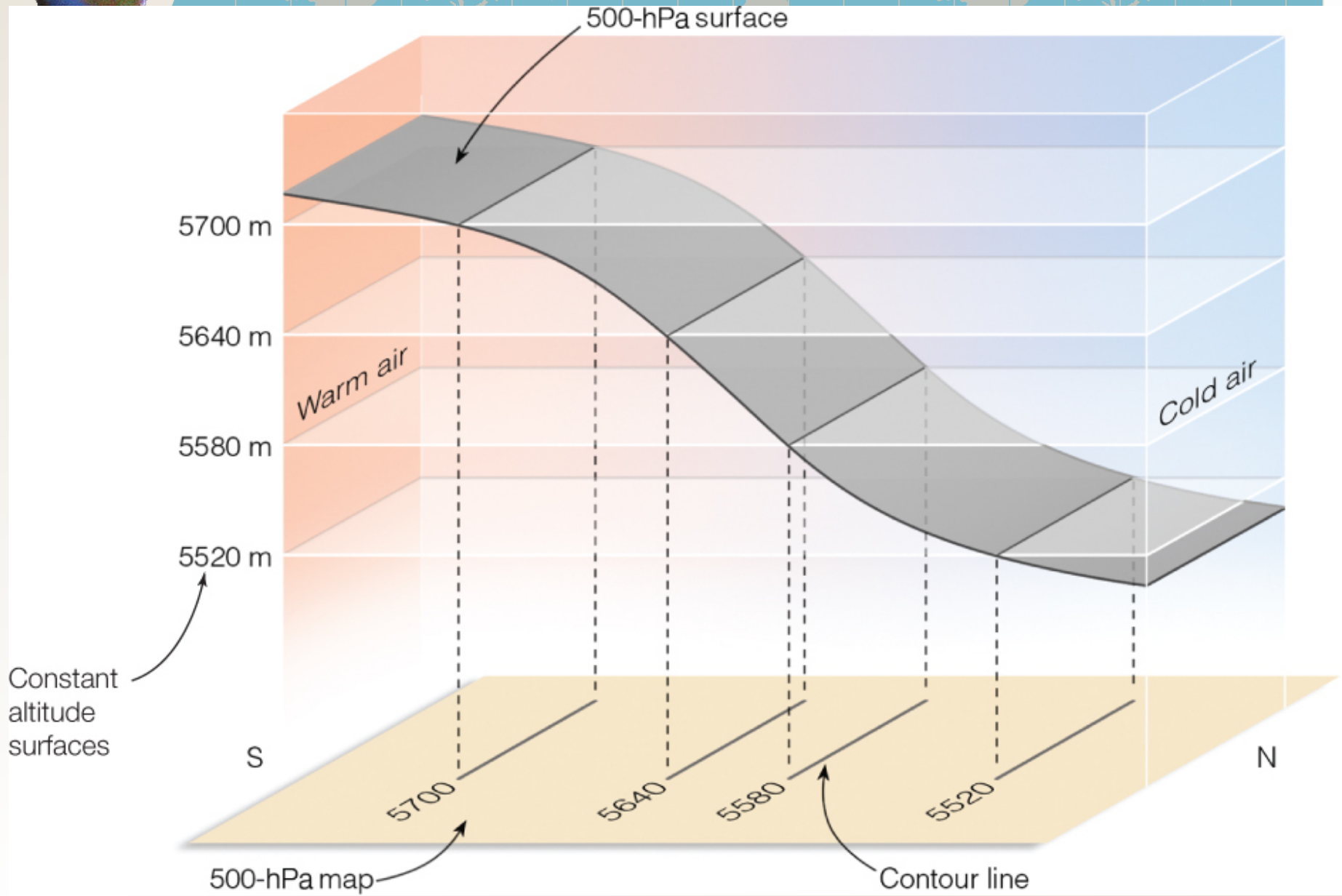
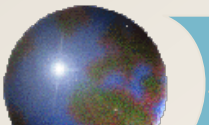
Ahrens: Figure 8.13



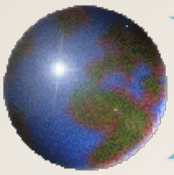
# *Altimeters*



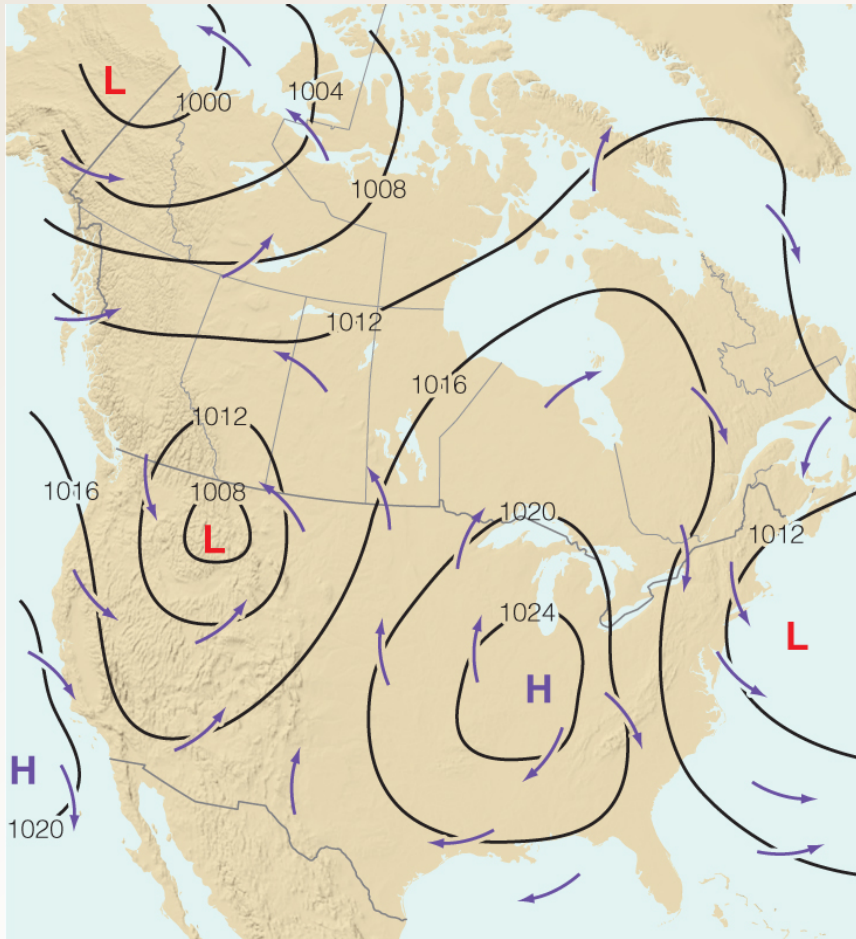
Ahrens: Fig. 2, p. 237



Ahrens: Figure 8.14

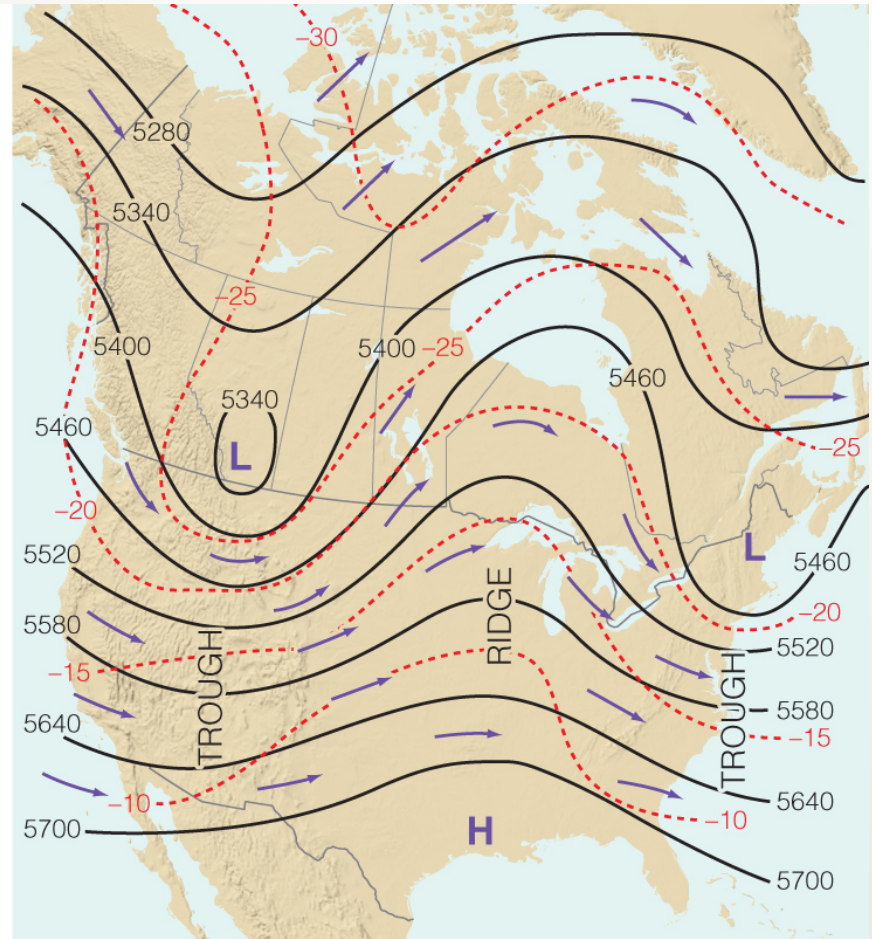


# Isobaric charts



(a) Surface map

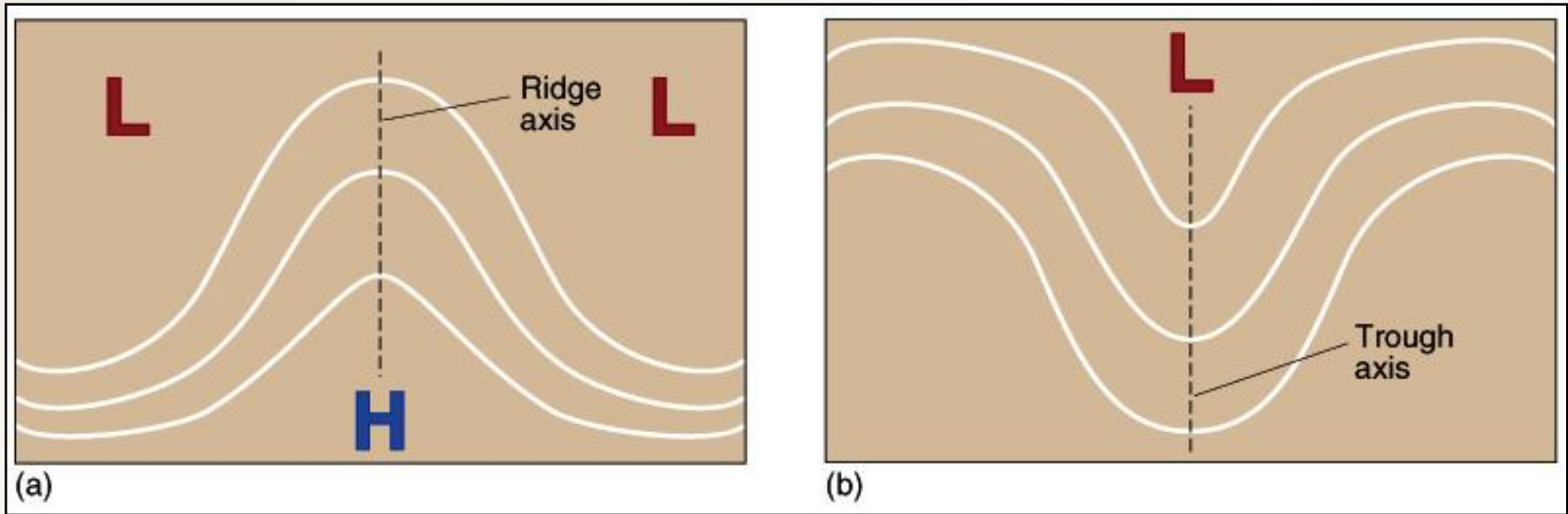
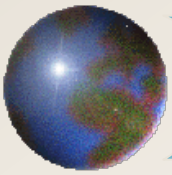
***Pressure (in hPa)***



(b) Upper-air map (500 hPa)

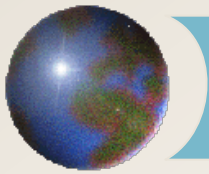
***500 hPa height contours (in m).***

Ahrens: Figure 8.16b

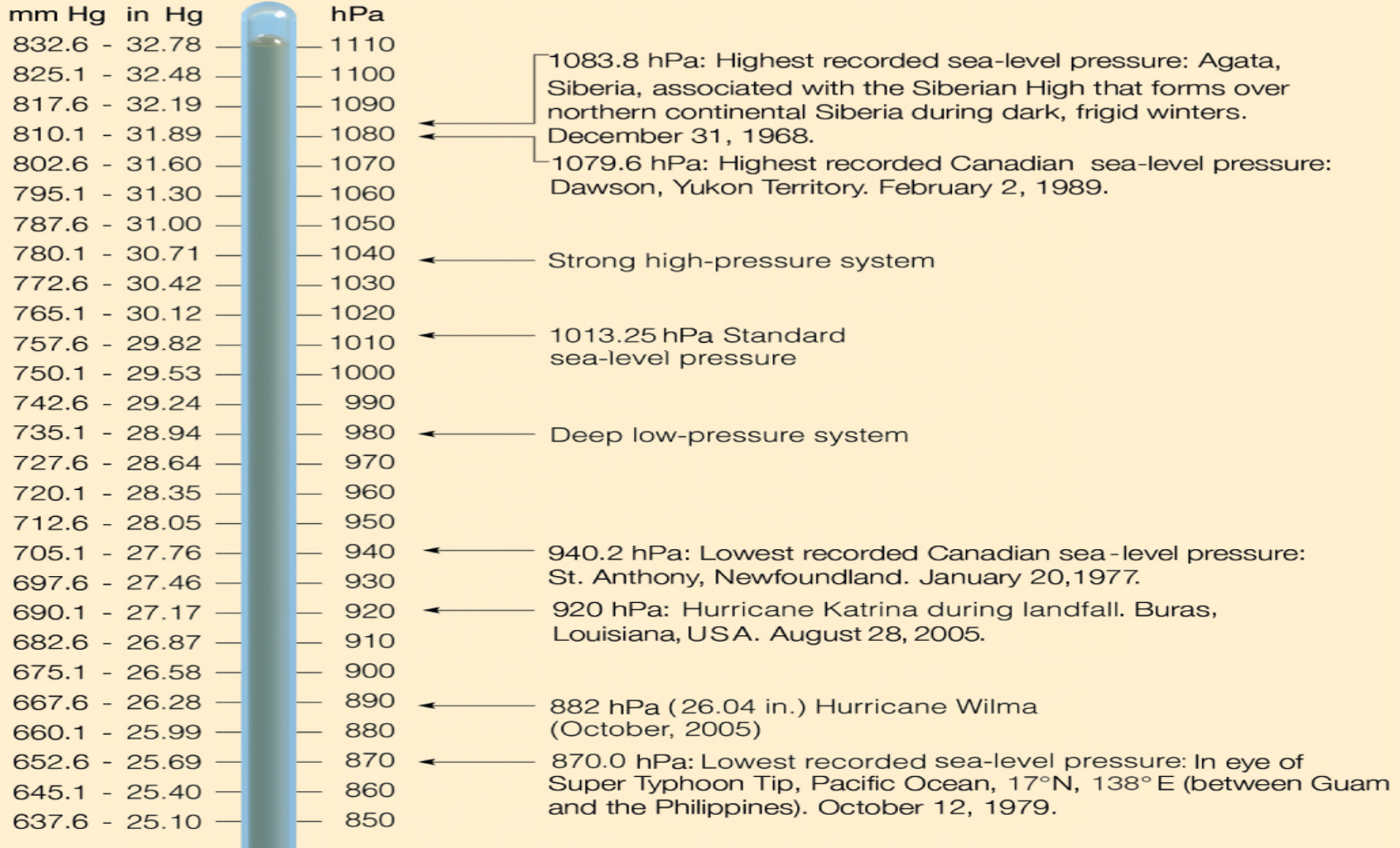


***Elongated zones of high and low pressure are called ridges (a) and troughs (b), respectively.***

A&B: Figure 4-20

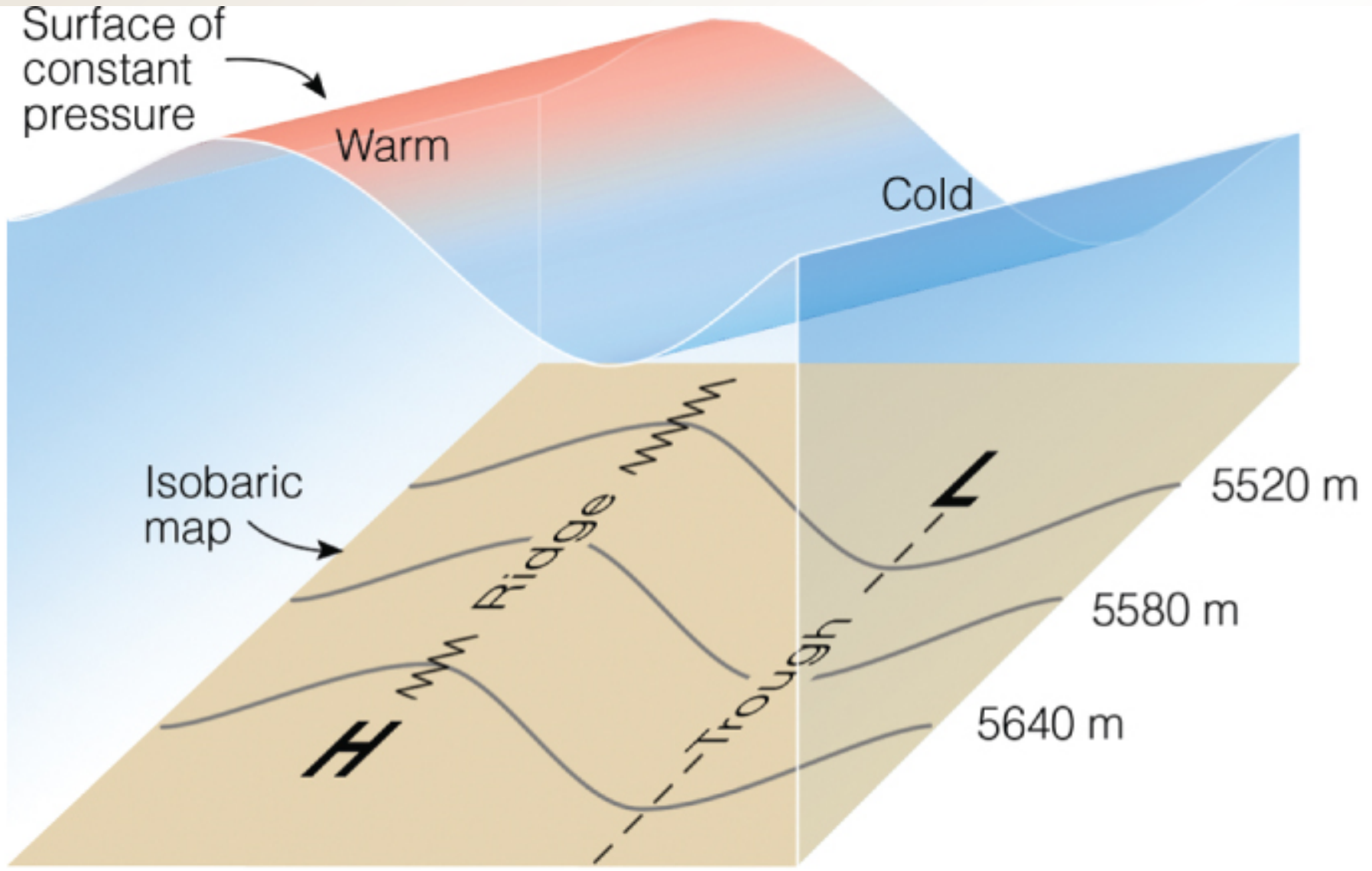
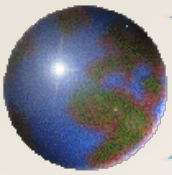


# Atmospheric Pressure Examples

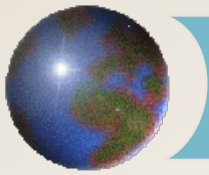






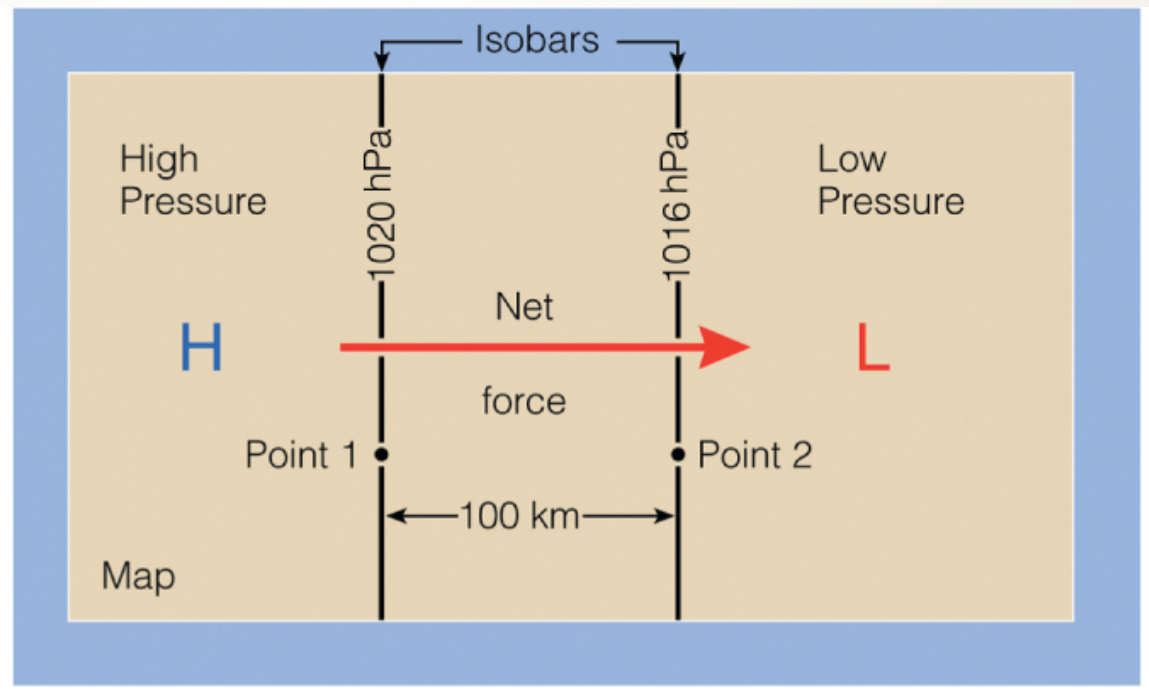


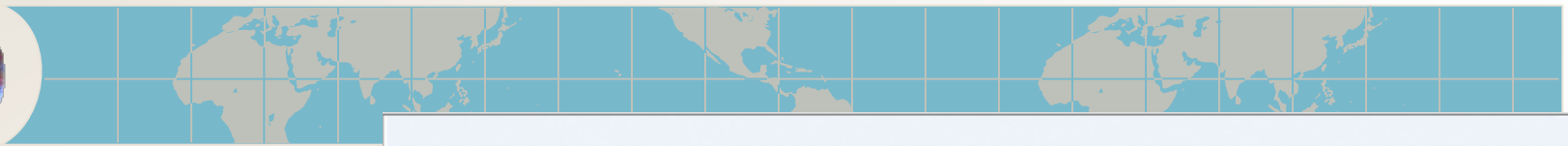
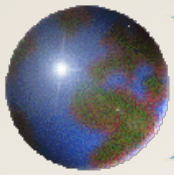
Ahrens: Figure 8.15



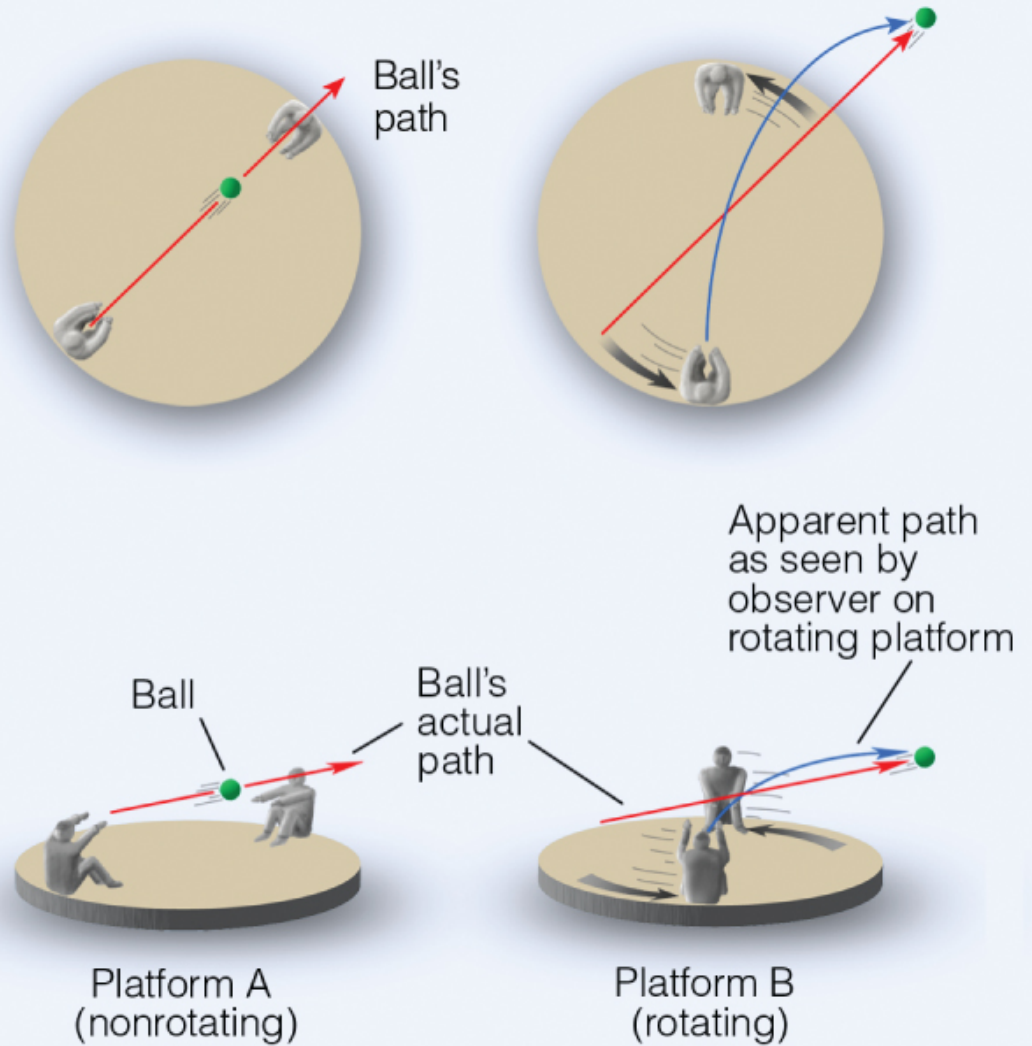
# *Put the air in motion*

- ✚ Horizontal pressure gradients cause the air to move
- ✚ The Earth's surface is a spinning frame of reference
- ✚ Push an object within that reference and it will not appear to travel in a straight line

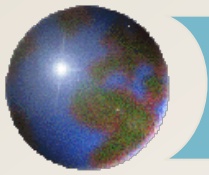




# *The Coriolis Effect*



Ahrens: Fig. 8.21



## *Next lecture*

- ✦ Coriolis “force”
- ✦ Geostrophic winds
- ✦ Cyclones and anticyclones
- ✦ More of Ahrens et al., Chapter 8