## CLASS Third Units

## PURE SUBSTANCE

- Pure substance: A substance that has a fixed chemical composition throughout.
- Air is a mixture of several gases, but it is considered to be a pure substance.


Nitrogen and gaseous air are pure substances.

(a) $\mathrm{H}_{2} \mathrm{O}$

(b) AIR

A mixture of liquid and gaseous water is a pure substance, but a mixture of liquid and gaseous air is not.

## PHASES OF A PURE SUBSTANCE



The molecules in a solid are kept at their positions by the large springlike inter-molecular forces.


In a solid, the attractive and repulsive forces between the molecules tend to maintain them at relatively constant distances from each other.
(a)

(b)

(c)

The arrangement of atoms in different phases: (a) molecules are at relatively fixed positions in a solid, (b) groups of molecules move about each other in the liquid phase, and (c) molecules move about at random in the gas phase.

## PHASE-CHANGE PROCESSES OF PURE SUBSTANCES

- Compressed liquid (subcooled liquid): A substance that it is not about to vaporize.
- Saturated liquid: A liquid that is about to vaporize.


At 1 atm and $20^{\circ} \mathrm{C}$, water exists in the liquid phase (compressed liquid).

At 1 atm pressure and $100^{\circ} \mathrm{C}$, water exists as a liquid that is ready to vaporize (saturated liquid).


- Saturated vapor: A vapor that is about to condense.
- Saturated liquid-vapor mixture: The state at which the liquid and vapor phases coexist in equilibrium.
- Superheated vapor: A vapor that is not about to condense (i.e., not a saturated vapor).


As more heat is transferred, part of the saturated liquid vaporizes (saturated liquidvapor mixture).


At 1 atm pressure, the temperature remains constant at $100^{\circ} \mathrm{C}$ until the last drop of liquid is vaporized (saturated vapor).


As more heat is transferred, the temperature of the vapor starts to rise (superheated vapor).

If the entire process between state 1 and 5 described in the figure is reversed by cooling the water while maintaining the pressure at the same value, the water will go back to state 1 , retracing the same path, and in so doing, the amount of heat released will exactly match the amount of heat added during the heating process.

$T-v$ diagram for the heating process of water at constant pressure.

## Saturation Temperature and Saturation Pressure

- The temperature at which water starts boiling depends on the pressure; therefore, if the pressure is fixed, so is the boiling temperature.
- Water boils at $100^{\circ} \mathrm{C}$ at 1 atm pressure.
- Saturation temperature $T_{\text {sat }}$ : The temperature at which a pure substance changes phase at a given pressure.
- Saturation pressure $P_{\text {sat }}$ : The pressure at which a pure substance changes phase at a given temperature.


|  | Saturation (boiling) pressure of water at various temperatures |  |
| :---: | :---: | :---: |
|  | Temperature, $T,{ }^{\circ} \mathrm{C}$ | Saturation pressure, $P_{\text {sat }}, \mathrm{kPa}$ |
|  | -10 | 0.26 |
|  | -5 | 0.40 |
| The liquid- | 0 | 0.61 |
| The liquia- | 5 | 0.87 |
| vapor | 10 | 1.23 |
| saturation | 15 | 1.71 |
| saturation | 20 | 2.34 |
| curve of a | 25 | 3.17 |
|  | 30 | 4.25 |
| pure | 40 | 7.39 |
| substance | 50 | 12.35 |
| (numerical | 100 | 101.4 |
| (numerical | 200 | 1555 |
| values are for | 250 | 3976 |
| water). | 300 | 8588 |

- Latent heat: The amount of energy absorbed or released during a phasechange process.
- Latent heat of fusion: The amount of energy absorbed during melting. It is equivalent to the amount of energy released during freezing.
- Latent heat of vaporization: The amount of energy absorbed during vaporization and it is equivalent to the energy released during condensation.
- The magnitudes of the latent heats depend on the temperature or pressure at which the phase change occurs.
- At 1 atm pressure, the latent heat of fusion of water is $333.7 \mathrm{~kJ} / \mathrm{kg}$ and the latent heat of vaporization is $2256.5 \mathrm{~kJ} / \mathrm{kg}$.
- The atmospheric pressure, and thus the boiling temperature of water, decreases with elevation.

Variation of the standard atmospheric pressure and the boiling (saturation) temperature of water with altitude

| Elevation, <br> m | Atmospheric <br> pressure, <br> kPa | Boiling <br> tempera- <br> ture, ${ }^{\circ} \mathrm{C}$ |
| ---: | ---: | ---: |
| 0 | 101.33 | 100.0 |
| 1,000 | 89.55 | 96.5 |
| 2,000 | 79.50 | 93.3 |
| 5,000 | 54.05 | 83.3 |
| 10,000 | 26.50 | 66.3 |
| 20,000 | 5.53 | 34.7 |

## Some Consequences of $T_{\text {sat }}$ and $P_{\text {sat }}$ Dependence



The temperature of liquid nitrogen exposed to the atmosphere remains constant at $-196^{\circ} \mathrm{C}$, and thus it maintains the test chamber at $-196^{\circ} \mathrm{C}$.

The variation of the temperature of fruits and vegetables with pressure during vacuum cooling from $25^{\circ} \mathrm{C}$ to $0^{\circ} \mathrm{C}$.



## PROPERTY DIAGRAMS FOR PHASECHANGE PROCESSES

- The variations of properties during phase-change processes are best studied and understood with the help of property diagrams such as the $T-v, P-v$, and $P-T$ diagrams for pure substances.

- saturated liquid line
- saturated vapor line
- compressed liquid region
- superheated vapor region
- saturated liquid-vapor mixture region (wet region)


At supercritical pressures ( $P>P_{\mathrm{cr}}$ ), there is no distinct phase-change (boiling) process.

$T-v$ diagram of a pure substance.
Critical point: The point at which the saturated liquid and saturated vapor states are identical.


$$
\begin{aligned}
& P=1 \mathrm{MPa} \\
& T=150^{\circ} \mathrm{C}
\end{aligned}
$$

$\xrightarrow[V]{ }$
$P-v$ diagram of a pure substance.
The pressure in a piston-cylinder device can be reduced by reducing the weight of the piston.

## Extending the Diagrams to Include the Solid Phase


$P-v$ diagram of a substance that contracts on freezing.

For water,
$T_{\text {tp }}=0.01^{\circ} \mathrm{C}$ $P_{\mathrm{tp}}=0.6117 \mathrm{kPa}$

At triple-point pressure and temperature, a substance exists in three phases in equilibrium.


Sublimation: Passing from the solid phase directly into the vapor phase.


At low pressures (below the triple-point value), solids evaporate without melting first (sublimation).

## Phase Diagram


$P-T$ diagram of pure substances.

The $P-v-T$ surfaces present a great deal of information at once, but in a thermodynamic analysis it is more convenient to work with two-dimensional diagrams, such as the $P-v$ and $T-v$ diagrams.

$P-V-T$ surface of a substance that contracts on freezing.

$P-v-T$ surface of a substance that expands on freezing (like water).

## PROPERTY TABLES

- For most substances, the relationships among thermodynamic properties are too complex to be expressed by simple equations.
- Therefore, properties are frequently presented in the form of tables.
- Some thermodynamic properties can be measured easily, but others cannot and are calculated by using the relations between them and measurable properties.
- The results of these measurements and calculations are presented in tables in a convenient format.


## Enthalpy-A Combination Property

$$
\begin{align*}
& h=u+P V \quad(\mathrm{~kJ} / \mathrm{kg}) \\
& H=U+P V \quad(\mathrm{~kJ}) \tag{kJ}
\end{align*}
$$

The


$$
\begin{aligned}
\mathrm{kPa} \cdot \mathrm{~m}^{3} & \equiv \mathrm{~kJ} \\
\mathrm{kPa} \cdot \mathrm{~m}^{3} / \mathrm{kg} & \equiv \mathrm{~kJ} / \mathrm{kg} \\
\mathrm{bar} \cdot \mathrm{~m}^{3} & \equiv 100 \mathrm{~kJ} \\
\mathrm{MPa} \cdot \mathrm{~m}^{3} & \equiv 1000 \mathrm{~kJ} \\
\mathrm{psi} \cdot \mathrm{ft}^{3} & \equiv 0.18505 \mathrm{Btu}
\end{aligned}
$$

$u+P v$ is frequently encountered in the analysis of control volumes.

## Saturated Liquid and Saturated Vapor States

- Table A-4: Saturation properties of water under temperature.
- Table A-5: Saturation properties of water under pressure.

A partial list of Table A-4.



## Saturated Liquid-Vapor Mixture

Quality, $x$ : The ratio of the mass of vapor to the total mass of the mixture. Quality is between 0 and $1 \rightarrow 0$ : sat. liquid, 1: sat. vapor
The properties of the saturated liquid are the same whether it exists alone or in a mixture with saturated vapor.
$x=\underline{m_{\text {vapor }}} m_{\text {total }}=m_{\text {liquid }}+m_{\text {vapor }}=m_{f}+m_{g}$

Temperature and pressure are dependent properties for a mixture.


The relative amounts of liquid and vapor phases in a saturated mixture are specified by the quality $\boldsymbol{x}$.


$$
\begin{aligned}
& v_{\mathrm{avg}}=v_{f}+x \mathrm{v}_{f g} \quad\left(\mathrm{~m}^{3} / \mathrm{kg}\right) \\
& x=m_{g} / m_{t} \quad x=\frac{v_{\mathrm{avg}}-v_{f}}{v_{f g}} \\
& u_{\mathrm{avg}}=u_{f}+x u_{f g} \quad(\mathrm{~kJ} / \mathrm{kg}) \\
& h_{\mathrm{avg}}=h_{f}+x h_{f g} \quad(\mathrm{~kJ} / \mathrm{kg})
\end{aligned} \begin{aligned}
& \boldsymbol{y} \rightarrow \mathrm{v}, u, \mathrm{or} h . \\
& y_{\mathrm{avg}}=y_{f}+x y_{f g} \\
& y_{f} \leq y_{\mathrm{avg}} \leq y_{g}
\end{aligned}
$$




## Examples: Saturated liquid-vapor

## mixture states on $T-v$ and $P-v$ diagrams.




In the region to the right of the saturated vapor line and at temperatures above the critical point temperature, a substance exists as superheated vapor. In this region, temperature and pressure are independent properties.

| $T,{ }^{\circ} \mathrm{C}$ | $v$ <br> $\mathrm{~m}^{3} / \mathrm{kg}$ | $\mathrm{kJ} / \mathrm{kg}$ | $\mathrm{kJ} / \mathrm{kg}$ |
| :---: | :---: | :---: | :---: |
|  | $P=0.1 \mathrm{MPa}\left(99.61{ }^{\circ} \mathrm{C}\right)$ |  |  |
|  | 1.6941 | 2505.6 | 2675.0 |
|  | 1.6959 | 2506.2 | 2675.8 |
| 150 | 1.9367 | 2582.9 | 2776.6 |
| $\vdots$ | $\vdots$ | $\vdots$ | $\vdots$ |
| 1300 | 7.2605 | 4687.2 | 5413.3 |
|  | $P=0.5 \mathrm{MPa}\left(151.83{ }^{\circ} \mathrm{C}\right)$ |  |  |
| Sat. | 0.37483 | 2560.7 | 2748.1 |
| 200 | 0.42503 | 2643.3 | 2855.8 |
| 250 | 0.47443 | 2723.8 | 2961.0 |
|  |  |  |  |

## Superheated Vapor

Compared to saturated vapor, superheated vapor is characterized by
Lower pressures ( $P<P_{\text {sat }}$ at a given $T$ )
Higher tempreatures ( $T>T_{\text {sat }}$ at a given $P$ )
Higher specific volumes ( $v>\mathrm{v}_{g}$ at a given $P$ or $T$ )
Higher internal energies $\left(u>u_{g}\right.$ at a given $P$ or $\left.T\right)$
Higher enthalpies $\left(h>h_{g}\right.$ at a given $P$ or $\left.T\right)$
At a specified ${ }^{T 4}$
$P$, superheated
vapor exists at
a higher $h$ than
the saturated
vapor.
A partial
listing of
Table A-6.

The compressed liquid properties depend on temperature much more strongly than they do on pressure.
$y \cong y_{f @ T} \quad \boldsymbol{y} \rightarrow v, u$, or $h$
A more accurate relation for $h$
$h \cong h_{f @ T}+V_{f @ T}\left(P-P_{\text {sat @T }}\right)$

## Compressed Liquid

Compressed liquid is characterized by
Higher pressures $\left(P>P_{\text {sat }}\right.$ at a given $\left.T\right)$
Lower tempreatures ( $T<T_{\text {sat }}$ at a given $P$ )
Lower specific volumes $\left(v<v_{f}\right.$ at a given $P$ or $\left.T\right)$
Lower internal energies $\left(u<u_{f}\right.$ at a given $P$ or $\left.T\right)$
Lower enthalpies ( $h<h_{f}$ at a given $P$ or $T$ )

## Given: $P$ and $T$

$$
\begin{aligned}
& v \cong v_{f} @ T \\
& u \cong u_{f} @ T \\
& h \cong h_{f} @ T
\end{aligned}
$$

A compressed liquid may be approximated as a saturated liquid at the given temperature.


## Reference State and Reference Values

- The values of $u, h$, and $s$ cannot be measured directly, and they are calculated from measurable properties using the relations between properties.
- However, those relations give the changes in properties, not the values of properties at specified states.
- Therefore, we need to choose a convenient reference state and assign a value of zero for a convenient property or properties at that state.
- The referance state for water is $0.01^{\circ} \mathrm{C}$ and for $\mathrm{R}-134 \mathrm{a}$ is $-40^{\circ} \mathrm{C}$ in tables.
- Some properties may have negative values as a result of the reference state chosen.
- Sometimes different tables list different values for some properties at the same state as a result of using a different reference state.
- However, In thermodynamics we are concerned with the changes in properties, and the reference state chosen is of no consequence in calculations.

Saturated water-Temperature table

| Temp.,$T^{\circ} \mathrm{C}$ | Sat. press., $P_{\text {sat }} \mathrm{kPa}$ | Specific volume,$\mathrm{m}^{3} / \mathrm{kg}$ |  | Internal energy, $\mathrm{kJ} / \mathrm{kg}$ |  |  | Enthalpy, kJ/kg |  |  | Entropy, <br> kJ/kg • K |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Sat. liquid, $v_{f}$ | Sat. vapor, $v_{g}$ | Sat. liquid, $u_{f}$ | Evap., $u_{f g}$ | Sat. vapor, $u_{g}$ | Sat. liquid, $h_{f}$ | Evap., $h_{f g}$ | Sat. vapor, $h_{g}$ | Sat. liquid, $s_{f}$ | $\begin{aligned} & \text { Evap., } \\ & s_{f g} \end{aligned}$ | Sat. vapor, $s_{g}$ |
| 0.01 | 0.6117 | 0.001000 | 206.00 | 0.000 | 2374.9 | 2374.9 | 0.001 | 2500.9 | 2500.9 | 0.0000 | 9.1556 | 9.1556 |
| 5 | 0.8725 | 0.001000 | 147.03 | 21.019 | 2360.8 | 2381.8 | 21.020 | 2489.1 | 2510.1 | 0.0763 | 8.9487 | 9.0249 |

Saturated refrigerant-134a-Temperature table

| Temp.,$T^{\circ} \mathrm{C}$ | Sat. press., $P_{\text {sat }} \mathrm{kPa}$ | Specific volume, $\mathrm{m}^{3} / \mathrm{kg}$ |  | Internal energy, $\mathrm{kJ} / \mathrm{kg}$ |  |  | Enthalpy, $\mathrm{kJ} / \mathrm{kg}$ |  |  | Entropy, <br> kJ/kg • K |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Sat. <br> liquid, $v_{f}$ | Sat. vapor, $v_{g}$ | Sat. liquid, $u_{f}$ | Evap., $u_{f g}$ | Sat. vapor, $u_{g}$ | Sat. <br> liquid, $h_{f}$ | Evap., $h_{f g}$ | Sat. <br> vapor, $h_{g}$ | Sat. <br> liquid, $s_{f}$ | Evap., $S_{f g}$ | Sat. vapor, $s_{g}$ |
| -40 | 51.25 | 0.0007054 | 0.36081 | -0.036 | 207.40 | 207.37 | 0.000 | 225.86 | 225.86 | 0.00000 | 0.96866 | 0.96866 |

## Exercises:

1. What is the difference between saturated liquid and compressed liquid?
2. What is the difference between saturated vapor and superheated vapor?
3. Why are the temperature and pressure dependent properties in the saturated mixture region.
4. What is the physical significance of $h_{f g}$ ? Can it be obtained from a knowledge of $h_{f}$ and $h_{g}$ ? How?
5. Is it true that it takes more energy to vaporize 1 kg of saturated liquid water at $100^{\circ} \mathrm{C}$ than it would at $120^{\circ} \mathrm{C}$ ?

## Quiz

- Which is the energy quantity necessary to vaporize 1 Kg of saturated liquid water at 75 Kpa .


## Exercices

Complete this table for $\mathrm{H}_{2} \mathrm{O}$ :

| $T,{ }^{\circ} \mathrm{C}$ | $P, \mathrm{kPa}$ | $v, \mathrm{~m}^{3} / \mathrm{kg}$ | Phase description |
| :--- | :--- | :--- | :--- |
| 50 |  | 4.16 |  |
|  | 200 |  | Saturated vapor |
| 250 | 400 |  |  |
| 110 | 600 |  |  |


| Complete this table for $\mathrm{H}_{2} \mathrm{O}:$ |  |  |  |
| :--- | :--- | :--- | :--- |
| $T,{ }^{\circ} \mathrm{F}$ | $P$, psia | $u$, Btu/lbm | Phase description |
| 300 |  | 782 |  |
|  | 40 |  | Saturated liquid |
| 500 | 120 |  |  |
| 400 | 400 |  |  |

## THE IDEAL-GAS EQUATION OF STATE

- Equation of state: Any equation that relates the pressure, temperature, and specific volume of a substance.
- The simplest and best-known equation of state for substances in the gas phase is the ideal-gas equation of state. This equation predicts the $P-v-T$ behavior of a gas quite accurately within some properly selected region.

$$
\begin{aligned}
& P=R\left(\frac{T}{v}\right) P V=R T \begin{array}{l}
\text { Ideal gas e } \\
\text { of state }
\end{array} \\
& R=\frac{R_{u}}{M} \quad\left(\mathrm{~kJ} / \mathrm{kg} \cdot \mathrm{~K} \text { or } \mathrm{kPa} \cdot \mathrm{~m}^{3} / \mathrm{kg} \cdot \mathrm{~K}\right)
\end{aligned}
$$

R: gas constant
M: molar mass (kg/kmol)
$R_{u}$ : universal gas constant
$R_{u}=\left\{\begin{array}{l}8.31447 \mathrm{~kJ} / \mathrm{kmol} \cdot \mathrm{K} \\ 8.31447 \mathrm{kPa} \cdot \mathrm{m}^{3} / \mathrm{kmol} \cdot \mathrm{K} \\ 0.0831447 \mathrm{bar} \cdot \mathrm{m}^{3} / \mathrm{kmol} \cdot \mathrm{K} \\ 1.98588 \mathrm{Btu} / \mathrm{lbmol} \cdot \mathrm{R} \\ 10.7316 \mathrm{psia} \cdot \mathrm{ft}^{3} / \mathrm{lbmol} \cdot \mathrm{R} \\ 1545.37 \mathrm{ft} \cdot \mathrm{lbf} / \mathrm{lbmol} \cdot \mathrm{R}\end{array}\right.$


Different substances have different gas constants.

$$
\begin{gathered}
\text { Mass }=\text { Molar mass } \times \text { Mole number } \frac{P_{1} V_{1}}{T_{1}}=\frac{P_{2} V_{2}}{T_{2}} \text { Ideal gas equation at two } \\
\text { states for a fixed mass }
\end{gathered}
$$

$$
\begin{aligned}
& V=m V \longrightarrow P V=m R T \\
& m R=(M N) R=N R_{u} \longrightarrow P V=N R_{u} T \begin{array}{l}
\text { Various } \\
\text { expressions } \\
\text { of ideal gas } \\
\text { equation }
\end{array}
\end{aligned}
$$

Real gases behave as an ideal gas at low densities (i.e., low pressure, high temperature).


Properties per unit mole are denoted with a bar on the top.


## Is Water Vapor an Ideal Gas?



- At pressures below 10 kPa , water vapor can be treated as an ideal gas, regardless of its temperature, with negligible error (less than 0.1 percent).
- At higher pressures, however, the ideal gas assumption yields unacceptable errors, particularly in the vicinity of the critical point and the saturated vapor line.
- In air-conditioning applications, the water vapor in the air can be treated as an ideal gas. Why?
- In steam power plant applications, however, the pressures involved are usually very high; therefore, ideal-gas relations should not be used.

Percentage of error ( $\left[\left|v_{\text {table }}-v_{\text {ideal }}\right| / v_{\text {table }}\right] \times 100$ ) involved in assuming steam to be an ideal gas, and the region where steam can be treated as an ideal gas with less than 1 percent error.

# COMPRESSIBILITY FACTOR-A MEASURE OF DEVIATION FROM IDEAL-GAS BEHAVIOR 

Compressibility factor Z A factor that accounts for the deviation of real gases from ideal-gas behavior at a given temperature and pressure.

$$
P v=Z R T
$$

$$
Z=\frac{P V}{R T} \quad Z=\frac{V_{\text {actual }}}{V_{\text {ideal }}}
$$



The compressibility factor is unity for ideal gases.

The farther away $Z$ is from unity, the more the gas deviates from ideal-gas behavior.
Gases behave as an ideal gas at low densities (i.e., low pressure, high temperature).

Question: What is the criteria for low pressure and high temperature?
Answer: The pressure or temperature of a gas is high or low relative to its critical temperature or pressure.


At very low pressures, all gases approach ideal-gas behavior (regardless of their temperature).

