## Experiment No. 13

Lenses

## Objective:

(a) To determine the focal length of a convex lens by plane mirror method.
(b) To determine the focal length of a convex lens and the focal length of a concave lens by conjugate foci method.

## Apparatus:

An optical bench, 2 convex lenses, a concave lens, a plane mirror, object and image pins, light source and ground glass screen.

## Theory:

A lens (Figs. 13-1 and 13-2) consists of a refracting medium bounded by two spherical surfaces. A lens has two principal foci ( $F_{1}$ and $F_{2}$ ). The line passing through $F_{1}$ and $F_{2}$ is known as the principal axis of the lens. Point $O$ is called the optical center of the lens. The following rules define the optical center $O$, and, the two principal foci $F_{1}$ and $F_{2}$ :


Fig. 13-1

(1) An incident ray of light passing through the optical center is not deviated. (See rays marked 1 in the above figures.)
(2) If an incident ray is parallel to the principal axis (rays marked 2 in the above figures), then the refracted ray passes through the first principal focus $F_{1}$ (as in Fig. 13-1) or appears to come from the first principal focus $\mathrm{F}_{1}$ (as in Fig. 13-2).
(3) If an incident ray passes through the second principal focus $F_{2}$ (as in Fig. 13-1) or is directed towards the second principal focus $\mathrm{F}_{2}$ (as in Fig. 13-2), the refracted is parallel to the principal axis. (See rays marked 3 in Figs. 13-1 and 13-2.)

The above rules are used to draw ray diagrams and to locate the positions of images as shown in Figs. 13-3 and 13-4.

Focal length: The distance of the first principal focus from the optical center (which is also numerically equal to the distance of the second principal focus from the optical center) is defined as the focal length (f) of the lens. The focal length $f$ is positive for a convex (converging) lens and it is negative for a concave (diverging) lens.


Fig. 13-3


Fig. 13-4
In Fig. 13-3, the rays starting from the point $A$ (of the object $A B$ ) pass through the point $A_{1}$ after refraction through the lens. Thus the image $A_{1}$ which is formed by the actual intersection of the refracted rays, is the real image of the point A. Similarly, $\mathrm{B}_{1}$ is the real image of point $B$.

In Fig. 13-4, the rays starting from the point $A$ (of the object $A B$ ) appear to come from the point $A_{1}$ after refraction through the lens. Thus the image $A_{1}$ which is not formed by the actual intersection of the refracted rays, is the virtual image of the point $A$. Similarly, $B_{1}$ is the virtual image of point $B$.
The path of a ray is reversible. Thus if a real object is placed at $\mathrm{B}_{1}$ (Fig. 13-3) a real image is obtained at $B$. Thus $B$ and $B_{1}$ are known as conjugate foci. Similarly, if in Fig. 13-4, a virtual object is placed at $B_{1}$, a real image will be formed at B . Thus B and $\mathrm{B}_{1}$ are conjugate foci.

The distance BO is known as the object distance ( p ) and the distance O $\mathrm{B}_{1}$ is known as the image distance ( q ).

## Convention of signs:

The distances which are actually traversed by the rays are taken to be positive and those which are not actually traversed by the rays are taken to be negative. Thus the focal length of a convex lens (in Fig. 13-1) and the object distances in Figs. 13-3 and 13-4 which are actually traversed by light rays are positive. The image distance (q) in Fig. 13-3 is also positive because the rays actually travel from the lens to the image $A_{1} B_{1}$. The focal length of the concave lens (Fig. 132 ) is negative and the image distance (q) in Fig. 13-4 is negative because the rays appear to come from the virtual image $\mathrm{A}_{1} \mathrm{~B}_{1}$.

The relationship between the object distance (p), the image distance (q) and the focal length ( $f$ ) is

$$
\begin{equation*}
1 / \mathrm{p}+1 / \mathrm{q}=1 / \mathrm{f} . \tag{1}
\end{equation*}
$$

This formula is used to find the focal length (f) by the conjugate foci method.

The magnification (m) is defined by

$$
\begin{equation*}
m=(\text { size of image }) /(\text { size of object })=-q / p \tag{2}
\end{equation*}
$$

If two lenses of focal lengths $f_{1}$ and $f_{2}$ are placed in contact, the focal length of the combination ( $f$ ) is given by

$$
\begin{equation*}
1 / \mathrm{f}=1 / \mathrm{f}_{1}+1 / \mathrm{f}_{2} . \tag{3}
\end{equation*}
$$

Plane mirror method of determining the focal length of a convex lens:

This m-thod is especially suitable for determining the focal length of a convex lens of large focal length. If an object $A B$ (Fig. 13-5) is placed in the focal plane of the convex lens such that the point $A$ is at the principal focus, then all the rays starting from A will become parallel to the principal focus after refraction through the convex lens.

This beam of parallel rays is incident normally on the plane mirror $M$ and thus it is reflected back along its own path. The reflected beam is parallel to the principal axis of the lens and thus it is brought to a focus at the principal focus of the lens (point A). Thus the image of $A B$ is formed at $A^{\prime} B^{\prime}$ such that the point $A^{\prime}$ of the image coincides with the point $A$ of the object.


The method of no parallax is adopted to locate the position of images. Parallax is the relative motion observed between two objects (or between an object and an image) which are not situated at the same point, due to the motion of the observer. For example, consider the image $A_{1}$ (Fig. 13-6). If the image pin is placed at $A_{2}{ }^{\prime}$ (or $A_{3}{ }^{\prime}$ ), points $A_{1}$ and $A_{2}{ }^{\prime}$ (or $A_{1}$ and $A_{3}{ }^{\prime}$ ) will appear to move relative to each other when the observer moves sideways. Thus parallax will be observed between $A_{1}$ and $A_{2}{ }^{\prime}$ (and, $A_{1}$ and $A_{3}{ }^{\prime}$ ). However, if the tip of the image pin is at $A_{1}$ ' (coinciding with $A_{1}$ ), there no parallax will be observed between $A_{1}$ and $A_{1}$.


Fig. 13-6

Conjugate foci method of determining the focal length of a convex lens:

In Fig. 13-6, $A B$ is an object whose image is $A_{1} B_{1}$. Thus points $A$ and $A_{1}$ are the conjugate foci. Further, in Fig. 13-6, the image $A_{1} B_{1}$ is real. Thus the method of no parallax can be employed for determining the object distance (p) and the image distance (q). Then the focal length $f$ can be calculated from Eq. (1). Alternatively, a well-defined image of a source of light (placed at AB) can be obtained on a ground glass screen (placed at $\mathrm{A}_{1}{ }^{\prime} \mathrm{B}_{1}$ '). Thus the object and image distances can be measured.

Conjugate foci method of determining the focal length of a concave lens:

The image of a real object in a concave (diverging) lens is always virtual. Thus its focal length can not be determined by the methods adopted for determining the focal length of convex lenses described above. However, the image of a virtual object formed by a concave lens is real. Therefore, the focal length of a concave lens can be determined by the method described below (Fig. 13-7)


Fig. 13-7
The real image of the object $A B$ is formed by the convex lens $L_{1}$ at $A_{1} B_{1}$. This image is located by the image pin $A_{1}{ }^{\prime} B_{1}$. Alternatively, a light source can be placed at AB and its real image can be obtained by placing a screen at $A_{1}$. Now let a concave lens $L_{2}$ be placed between the convex lens $L_{1}$ and the image $A_{1} B_{1}$. In such a case, the real image $A_{1} B_{1}$ (of the object $A B$ formed by the convex lens $L_{1}$ ) serves as a virtual object for refraction through the concave lens $L_{2}$. This is because the rays refracted by lens $\mathbf{L}_{1}$ pass through lens $\mathrm{L}_{2}$ before
they actually meet at the real image $A_{1} B_{1}$. The concave lens forms a real image $A_{2} B_{2}$ of the virtual object $A_{1} B_{1}$. This real image can be located by the method of no parallax by using the image pin $A_{2}{ }^{\prime} \mathrm{B}_{2}{ }^{\prime}$ or the image can be located by using a light source (placed at $A B$ ) and a screen (placed at $A_{2} B_{2}$ ). Obviously, for the concave lens $L_{2}$, the object distance ( $p$ ) is the distance from $\mathrm{O}_{2}$ to $\mathrm{A}_{1}$, and the image distance ( $q$ ) is the distance from $\mathrm{O}_{2}$ to $\mathrm{A}_{2}$. Thus the focal length of the concave lens can be calculated from Eq. (1).

There is another way of looking at the situation depicted in Fig. 13-7. Let an object pin be placed at $\mathrm{A}_{2}{ }^{\prime} \mathrm{B}_{2}{ }^{\prime}$. The concave lens $\mathrm{L}_{2}$ produces a virtual image $A_{1}{ }^{\prime} B_{1}$ ' of this object $A_{2}{ }^{\prime} B_{2}{ }^{\prime}$. This virtual image serves as a real object for refraction through the convex lens $L_{1}$ and thus a real image is formed by the convex lens at $\mathrm{A}^{\prime} \mathrm{B}^{\prime}$.

## Procedure:

Unit 1. Determination of the focal length of a convex lens by plane mirror method:
(a) Mount the plane mirror, a convex lens and a pin on the optical bench as shown in Fig. 13-5. Rotate the plane of the mirror so as to have the tip of the pin, the tip of the image and the optical center of the lens in a straight line.
(b) Adjust the position of the pin along the optical bench and remove the parallax between the tip of the pin and the tip of the image.
(c) Record the position of the lens and the position of the pin.
(d) Repeat steps (a), (b) and (c) twice.

Units 2 \& 3. Determination of the focal length of a convex lens and the focal length of a concave lens by the ronjugate foci method:
(e) Mount the light source $S$ (Fig. 13-8) near one end of the optical bench. Mount the convex lens $\mathrm{L}_{1}$ such that the object distance $\mathrm{SL}_{1}$ lies between $f_{1}$ and $2 f_{1}$, where $f_{1}$ is the approximate focal length of the convex lens. Mount the screen $\mathrm{G}_{1}$ as shown in Fig. 13-8. Adjust the position of the screen (and of the lens, if necessary) to obtain a sharp image of the light source on the screen.


Fig. 13-8
(f) Record the positions of the lens $L_{1}$, of the light source $S$ and of the screen $G_{1}$. The distance between $S$ and $L_{1}$ is the object distance ( $p_{1}$ ) and the distance between $L_{1}$ and $G_{1}$ is the image distance $\left(q_{1}\right)$ for the convex lens.
(g) Keep the positions of the source and convex lens $L_{1}$ fixed in the following steps.
(h) Now mount the concave lens $\mathrm{L}_{2}$ between the convex lens $\mathrm{L}_{1}$ and the screen $G_{1}$. Move the screen to position $G_{2}$ so as to obtain a sharp image of the light source $S$ on the screen. Thus the image of the light source is formed at $G_{2}$ by the two lenses $L_{1}$ and $L_{2}$.
(i) Note that for the concave lens $L_{2}$, the image formed by the convex lens $L_{1}$ is the virtual object whose image is formed by the concave lens $L_{2}$ at the new position of the screen $G_{2}$. Thus for the concave lens, the distance between $L_{2}$ and $G_{1}$ is the object distance ( $p_{2}$ ) and the distance between $L_{2}$ and $G_{2}$ is the image distance $\left(q_{2}\right)$.
(j) Record the positions of $L_{2}$ and $G_{2}$.
(k) Change the object distance for the convex lens by about 1.5 cm and repeat steps (e) through (j) twice.

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| Physics 11 | Name: |
| Experiment No. 13: Pre-Lab Questionnaire |  |

1. In a converging lens, if an incident ray is parallel to the principal axis, the refracted ray
2. In a diverging lens, if an incident ray is parallel to the principal axis, the refracted ray $\qquad$
3. Can a real image be obtained by means of a diverging lens? If yes, how?
4. Draw a clearly labeled diagram showing the objects and images formed by a combination of a converging and diverging lenses.

| Name: | Experiment No. 13 |
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| Partner: | Marks: |
| Section: | Remarks: |
| Date Submitted: |  |
| Title: |  |
| Objective: |  |

## DATA SHEET

## Unit 1:

A. Focal length of a convex lens by plane mirror method:

| No. | Position of |  | focal length f |
| :---: | :---: | :---: | :---: |
|  | convex lens | pin |  |
| 1. |  |  |  |
| 2. |  |  |  |
| 3. |  |  |  |

## Units 2 \& 3:

B. Focal lengths of a convex lens and a concave lens by conjugate foci method:

| No. | Position of |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Light source S | Lens $L_{1}$ | Screen $\mathrm{G}_{1}$ | Lens $\mathrm{L}_{2}$ | Screen $\mathrm{G}_{2}$ |
| 1. |  |  |  |  |  |
| 2. |  |  |  |  |  |
| 3. |  |  |  |  |  |


| No. Convex lens | $\mathrm{f}_{1}$ |  |  | Concave lens |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathrm{p}_{1}$ | $\mathrm{q}_{1}$ | $p_{2}$ | $\mathrm{q}_{2}$ | $\mathrm{f}_{2}$ |  |
| 1. |  |  |  |  |  |  |
| 2. |  |  |  |  |  |  |
| 3. |  |  |  |  |  |  |

## Questions:

1. Define focal length, object distance and image distance.
2. Distinguish between a real and a virtual image.
3. What is meant by parallax?
4. What is the convention of signs for $f, p$ and $q$ ?
5. Is the object distance for $\mathrm{L}_{2}$ in Fig. 7 positive or negative? Explain.
