

ME 222: Kinematics of Machines and Mechanisms

[L13] Path Generation 1

Overview

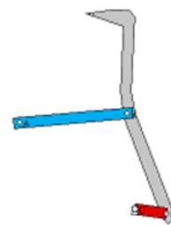
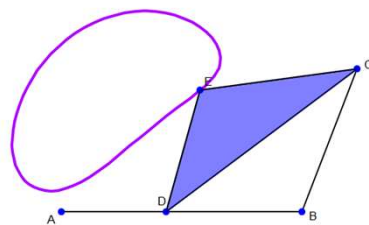
- Path generation
- Coupler Curve
- Cognates
- Parallel motion

Path Generation

- The control of a **point** in the plane such that it follows some prescribed path

Coupler curve

- Coupler: most interesting link of four bar

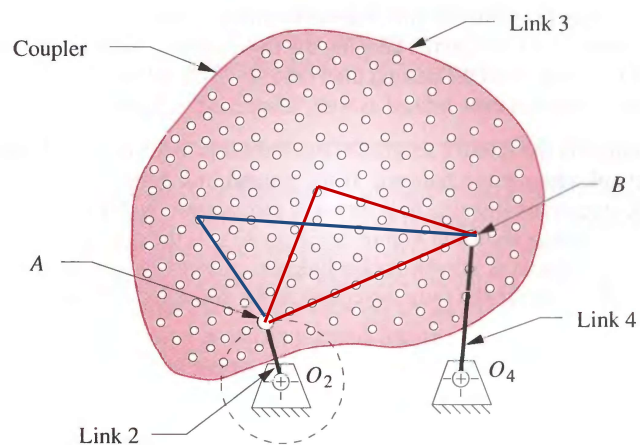


Coupler curve

- A slider-crank can generate curve with max order $m=4$.
- four-bar mechanism can generate curve with max order $m=6$.
- n -link revolute jointed can have maximum order

$$m = 2 \cdot 3^{(n/2-1)}$$

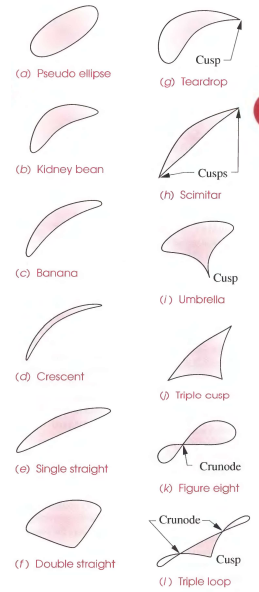
Coupler curve



Coupler curves

FOURBAR COUPLER CURVES can be crudely categorized as

- Cusp
- Crunode

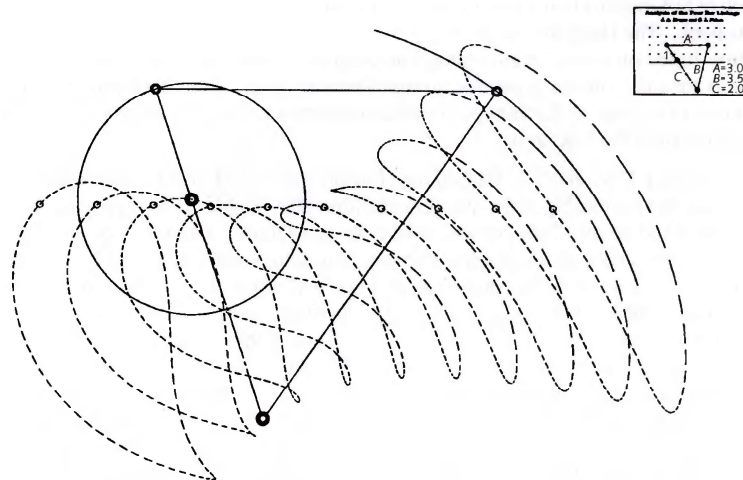


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Hrones and Nelson (H&N) atlas

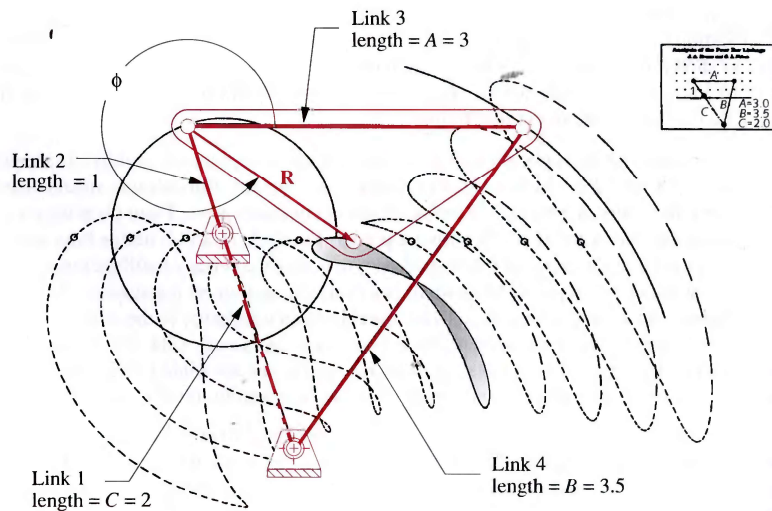
- Atlas of fourbar coupler curves (7000)



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Hrones and Nelson (H&N) atlas



Hrones, J. A., and G. L. Nelson. (1951). *Analysis of the Fourbar Linkage*. MIT Technology Press:Cambridge, MA.

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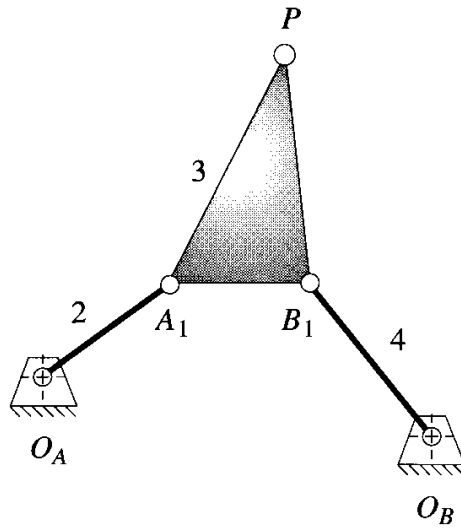
Cognates

- Good solution that satisfies path generation constraints but inappropriate fixed pivots
- **Cognate** can be helpful in such situations.
- **Cognate** : A linkage, of different geometry, which generates the same coupler curve.
- **Roberts-Chebyshev Theorem**: Three different planar, pin-jointed fourbar linkages will trace identical coupler curves.

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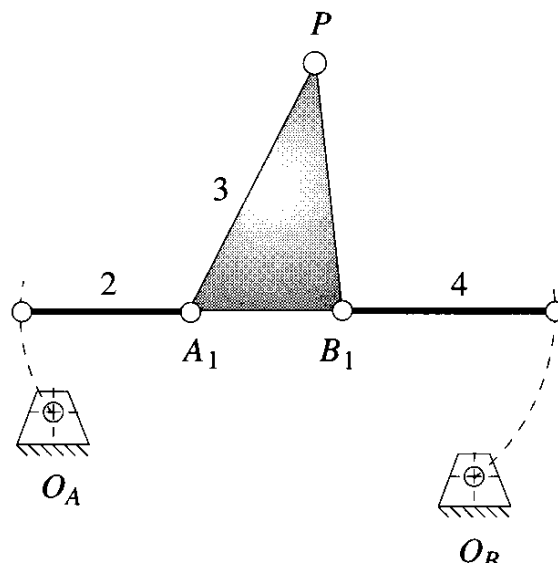
Cayley Diagram



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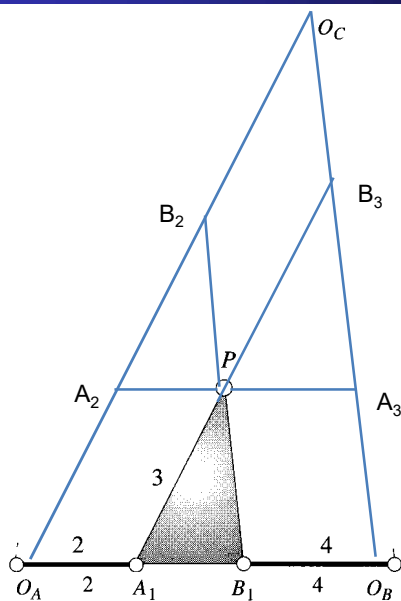
Cayley Diagram



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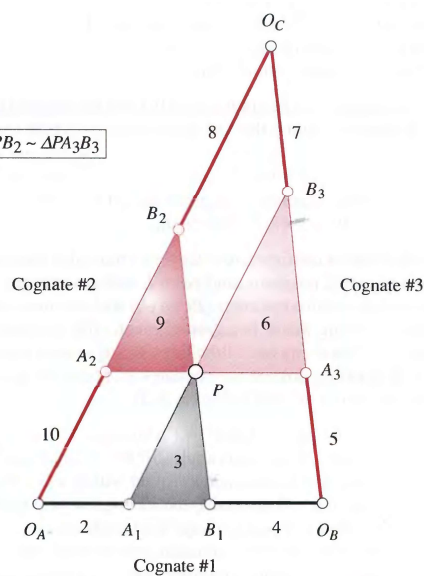
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Cayley Diagram

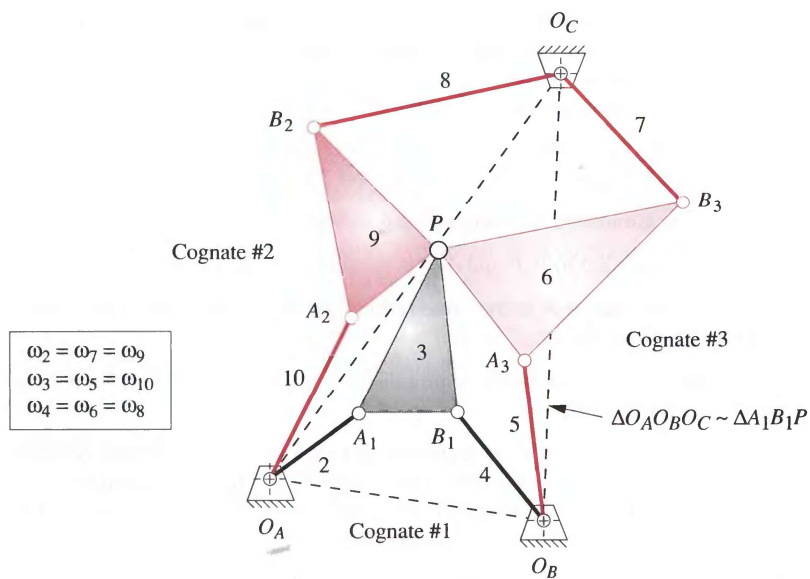


Cayley Diagram

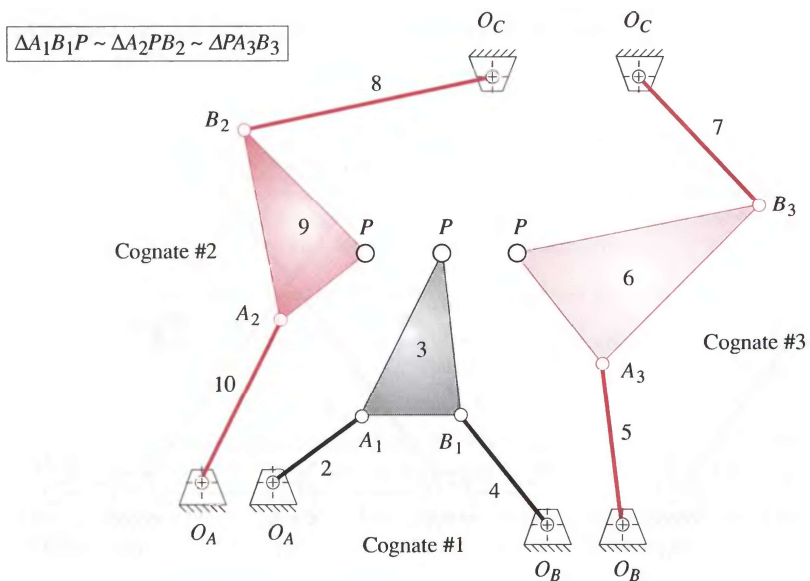
$$\Delta A_1B_1P \sim \Delta A_2PB_2 \sim \Delta PA_3B_3$$



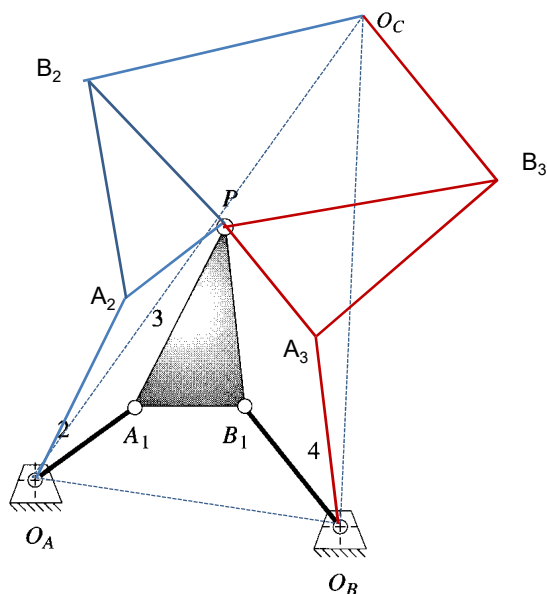
Roberts Diagram



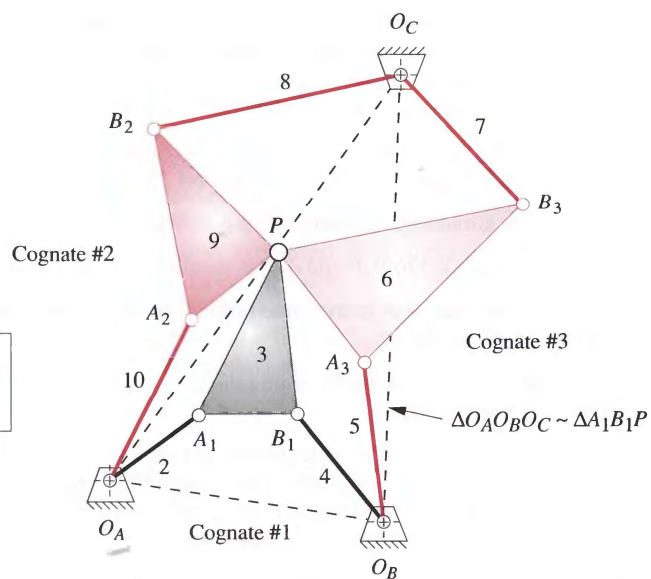
3-Cognates



Robert's Diagram



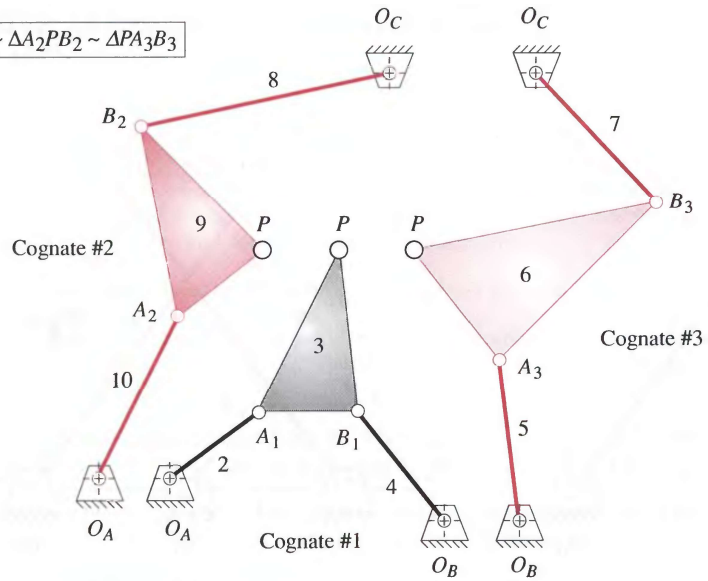
Robert's Diagram



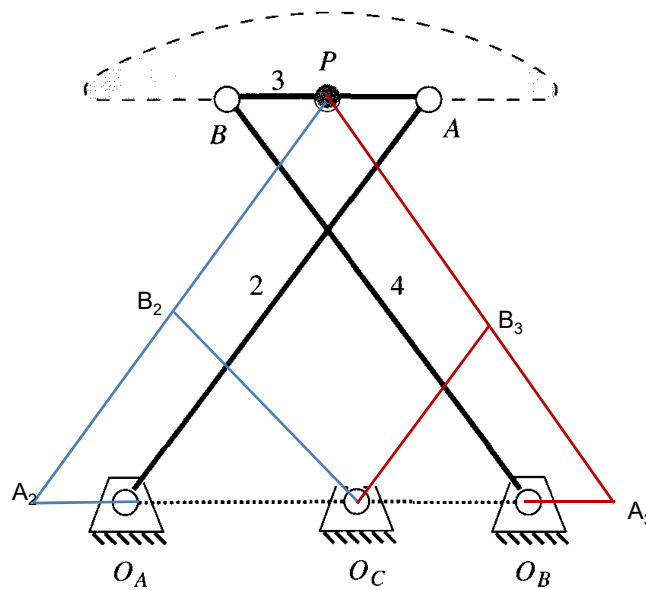
$$\begin{aligned} \omega_2 &= \omega_7 = \omega_9 \\ \omega_3 &= \omega_5 = \omega_{10} \\ \omega_4 &= \omega_6 = \omega_8 \end{aligned}$$

3-Cognates

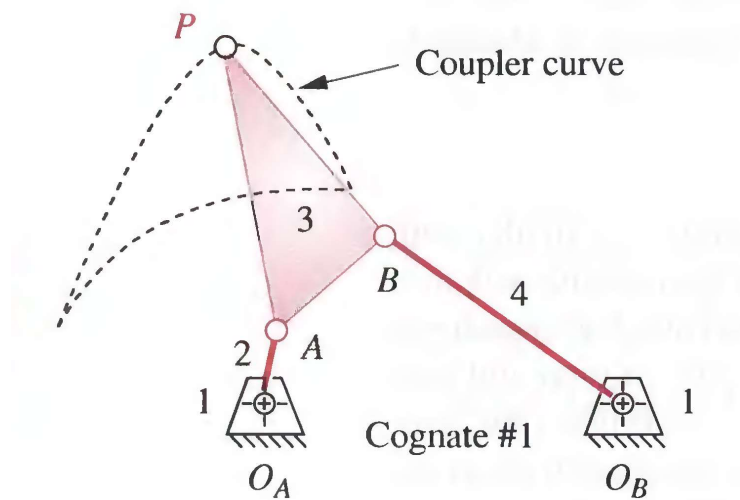
$$\Delta A_1 B_1 P \sim \Delta A_2 P B_2 \sim \Delta P A_3 B_3$$



Coupler point on link-3

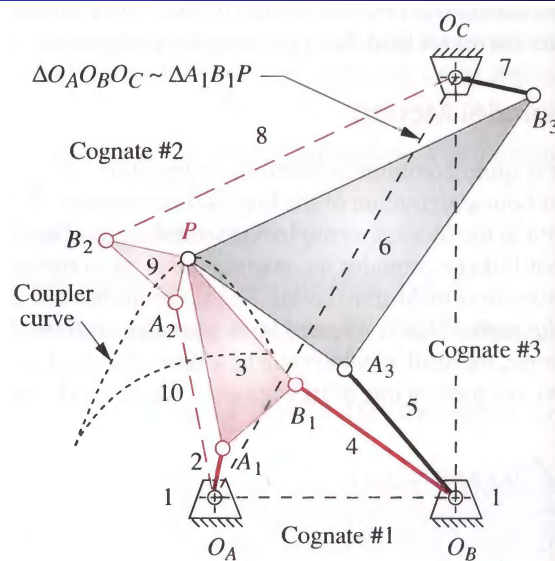


Parallel motion



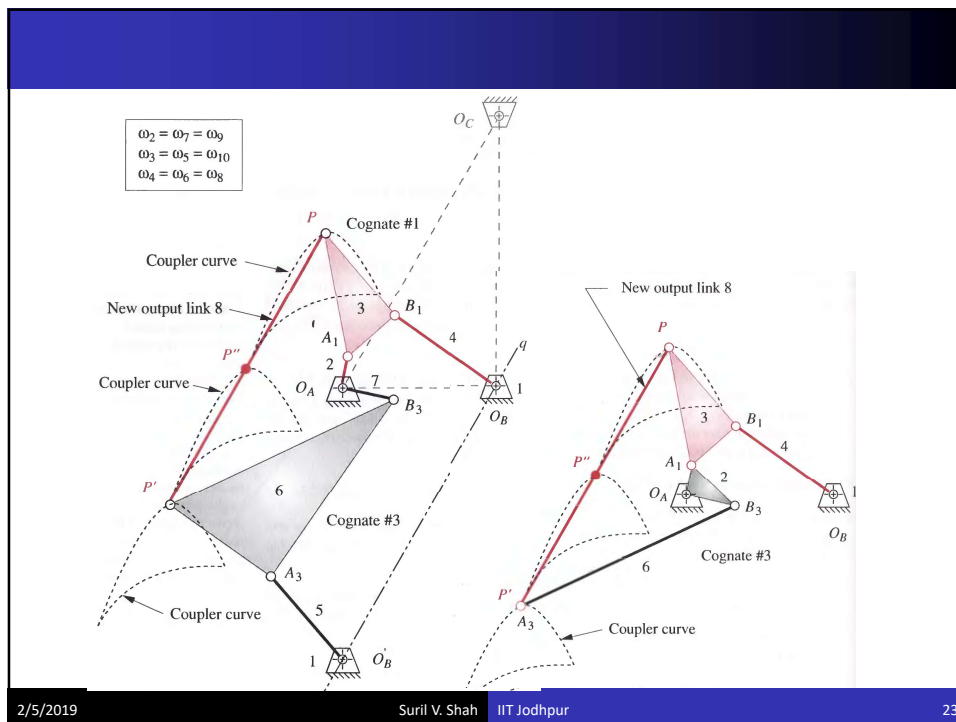
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Thank you

Next Class: **Parallel motion**