

1 **Title:** Cardinal models to describe the effect of temperature and pH on the growth of
2 *Anoxybacillus flavithermus* & *Bacillus licheniformis*.

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9 **Abstract**

10 *Anoxybacillus flavithermus* and *Bacillus licheniformis* are among the predominant spore-
11 formers of heat-processed foods. To our knowledge, no systematic analysis of growth kinetic
12 data of *A. flavithermus* or *B. licheniformis* is currently available. In the present study, the
13 growth kinetics of *A. flavithermus* and *B. licheniformis* in broth at various temperature and pH
14 conditions were studied. Cardinal models were used to model the effect of the above-
15 mentioned factors on the growth rates. The estimated values for the cardinal parameters
16 T_{min} , T_{opt} , T_{max} , pH_{min} and $pH_{1/2}$ for *A. flavithermus* were 28.70 ± 0.26 , 61.23 ± 0.16 and
17 71.52 ± 0.32 °C 5.52 ± 0.01 and 5.73 ± 0.01 , respectively, while for *B. licheniformis* were 11.68
18 ± 0.03 , 48.05 ± 0.15 , 57.14 ± 0.01 °C, 4.71 ± 0.01 and 5.670 ± 0.08 , respectively. The growth
19 behaviour of these spoilers was also investigated in a pea beverage at 62 and 49 °C,
20 respectively, to adjust the models to this product. The adjusted models were further validated
21 at static and dynamic conditions and demonstrated good performance with 85.7 and 97.4 %
22 of predicted populations for *A. flavithermus* and *B. licheniformis*, respectively, being within the
23 -10 % to 10 % relative error (RE) zone. The developed models can be useful tools in assessing
24 the potential of spoilage of heat-processed foods including plant-based milk alternatives.

25 **Keywords**

26 *Anoxybacillus flavithermus*; *Bacillus licheniformis*; cardinal model; growth kinetics; climate
27 change; plant-based milk alternatives

28 **1. Introduction**

29 Thermophilic and thermotolerant spore-forming bacteria are responsible for spoilage of a wide
30 range of non-refrigerated heat-processed food products, including milk and dairy products.
31 Among the different species found in dairy powders, *Geobacillus stearothermophilus*,
32 *Anoxybacillus flavithermus* and *Bacillus licheniformis* are the predominant spore-formers
33 (Delaunay et al., 2019; Lindsay et al., 2022). *A. flavithermus* is a facultative thermophilic spore-
34 forming bacterium used by the dairy powders industry as a poor hygiene indicator (Remize,
35 2017). Its optimum temperature of growth, around 60 °C, can be reached in different sections
36 of the production line, including the preheating phase in milk evaporators (Flint et al., 2011).
37 *A. flavithermus* is rarely found in raw and pasteurized milk, with a prevalence from 0.8 to 1.6
38 and 1.6%, respectively (Chauhan et al., 2013; Kable et al., 2019). However, during summer
39 season *A. flavithermus* has been isolated from 40% of the selected samples of raw milk (Kable
40 et al., 2019). Regarding its enzymatic activity, *A. flavithermus* has been found to produce
41 lipase and β -galactosidase, which may lead to significant spoilage of dairy products (Lücking
42 et al., 2013; Sadiq et al., 2016).

43 Besides the facultative thermophilic spore-forming bacilli, moderate thermophilic and
44 thermotolerant bacilli are equally important for the food industry. Among these groups,
45 *B. licheniformis*, is considered of great interest for the dairy industry due to its ability to survive
46 and multiply at moderate and high temperatures and at the same time form heat resistant
47 spores (Ivy et al., 2012; Li et al., 2019). Many studies have reported the presence of
48 *B. licheniformis* both in bulk tank milk kept under refrigerated temperature and ultrafiltration
49 plants (Boor et al., 2017; Eijlander et al., 2019). Interestingly, *B. licheniformis* has also been
50 associated with food poisoning (Fernández-No et al., 2011; Mikkola et al., 2000; Salkinoja-
51 Salonen et al., 1999). Regarding food spoilage, some strains of *B. licheniformis* are capable
52 of producing a slimy extracellular substance that can affect the quality of pasteurised milk and

53 cream (Gilmour and Rowe, 1990), while the majority of strains demonstrate β -galactosidase,
54 lipolysis, and proteolysis activity (De Jonghe et al., 2010; Lücking et al., 2013).

55 The potential of thermophilic and thermotolerant spore-forming bacteria, including
56 *A. flavithermus* and dairy originated strains of *B. licheniformis*, to form biofilms has been
57 demonstrated in many studies (Burgess et al., 2009; Flint et al., 2011; Seale et al., 2008;
58 Ostroy et al., 2019). Temperature applied during processes and the presence of divalent
59 cations in milk have been found to positively influence the formation of biofilms (Burgess et
60 al., 2014, 2009), indicating that dairy manufacturing plants could be an ideal harbour for
61 entrapped spores. Thus, thermophilic bacilli could be found in various final dairy and non-dairy
62 products due to formation of biofilms in the lines.

63 In the past few years, consumers' demand for plant-based alternatives has increased
64 worldwide due to special dietary needs and behavioural changes. According to Nielsen data,
65 plant-based consumption across Europe has increased by 49% in two years, reaching total
66 sales values of €3.6 billion in 2020 (Nielsen, 2021). Following this tremendous growth, the
67 dairy (food) industry has focused on producing many innovative plant-based milk alternatives
68 from nuts, cereals and legumes, such as oat, soy and pea.

69 Considering that soil constitutes the harbour of spore-forming bacteria (Carlin, 2011), plant-
70 based proteins used as raw material might be contaminated with various thermophilic and
71 thermotolerant bacilli. Plant-based milk alternatives are usually low acid products and are
72 therefore sterilized by ultra-high temperature (UHT) treatment (Sethi et al., 2016), which is
73 primarily designed to eliminate spores of *Clostridium botulinum* (Membré and van Zuijlen,
74 2011). Nevertheless, this thermal process has been proven insufficient in eliminating spores
75 of thermophilic and thermotolerant spore-forming bacteria that exhibit extreme heat
76 resistance, such as *Bacillus sporothermodurans* and *Geobacillus stearothermophilus* (Alonso
77 et al., 2021; André et al., 2016; Burgess et al., 2010; Wells-Bennik et al., 2016). The surviving
78 spores may cause spoilage issues in non-refrigerated food products when the products
79 storage temperature exceed their minimum growth temperature for a certain time and allow

80 germination and outgrowth. While the minimum growth temperature is usually relatively high,
81 these products are distributed and stored at ambient temperature. Current environmental
82 conditions, particularly temperature, generally do not allow extensive growth of thermophilic
83 bacilli and therefore ensure their microbiological stability (Misiou et al., 2021a). However,
84 several studies have already highlighted the emerging risk of spoilage in hot climate regions
85 and temperate climates, due to climate change and global warming (Kakagianni and
86 Koutsoumanis, 2018; Misiou et al., 2021b; Misiou and Koutsoumanis, 2021).

87 In order to assess the potential risk of spoilage, the growth behaviour of thermophilic bacteria
88 as a function of the environment should first be described. Predictive microbiology modelling
89 can be used as a tool to predict the bacterial behaviour as function of extrinsic and intrinsic
90 factors, such as temperature and pH. In this sense, several secondary and primary models
91 have already been developed for thermophilic spore-forming bacteria. More specifically, the
92 effects of temperature and pH on the maximum specific growth rate (μ_{max}) of *Geobacillus*
93 *stearothermophilus*, *Bacillus coagulans* and *Alicyclobacillus acidoterrestris* has been
94 described by means of cardinal parameter models (Mtimet et al., 2015; Kakagianni et al.,
95 2018; Misiou et al., 2021a; Misiou et al., 2021b). Although *A. flavithermus* and *B. licheniformis*
96 are responsible for the spoilage of a wide range of non-refrigerated foods, the scientific
97 literature lacks quantitative kinetic data and models that could be used by the food industry to
98 predict their growth.

99 Against this background, the objective of the present study was to model the effect of
100 temperature and pH on the growth of *Anoxybacillus flavithermus* and *Bacillus licheniformis*
101 and validate the developed models against observed growth in a pea-based milk alternative
102 under static and dynamic temperature conditions.

103 **2. Materials and methods**

104 **2.1 Bacterial strain and culture conditions**

105 Type strain *B. licheniformis* DSM 13 and stain *A. flavithermus* DSM 21510 were used in the
106 present study. The strains were maintained as working culture onto Microbank™ porous beads
107 (Pro-Lab Diagnostics, Ontario, Canada) and stored at -20 °C. All experiments were performed
108 using the strains harvested in their stationary phase. Therefore, *A. flavithermus* strain was
109 cultured by inoculation of 10 mL Brain Heart Infusion (BHI; Thermofisher™ Diagnostics
110 CM1135B Waltham, MA, U.S) with a bead from the working culture, incubating aerobically at
111 55 °C for 8 h. After 8 h, 0.1 mL of the sub-culture were transferred into a fresh 9.9 mL BHI
112 tube and incubated at the same conditions for 18 h. The same procedure was followed for
113 *B. licheniformis* strain, with the exemption that the culture was inoculated into Tryptone Soy
114 Broth (TSB; Thermofisher™ Diagnostics, CM0129B) and incubated at 37 °C. The initial
115 concentration of the suspension of both microorganisms was determined by spread plating on
116 tryptone soy agar (TSA; Thermofisher™ Diagnostics, CM0131B).

117 **2.2 Growth experiments in broth**

118 The *A. flavithermus* working cultures were decimally diluted in BHI for temperature
119 experiments or pH-adjusted BHI, based on the experimental set-up for the pH experiments, to
120 a concentration of approximately 10⁶ CFU/mL. The same was applied for *B. licheniformis* with
121 the exemption that cultures were diluted in TSB or pH-adjusted TSB, respectively.

122 **2.2.1 Effect of temperature on maximum specific growth rate (μ_{max})**

123 The effect of temperature on the maximum specific growth rate (μ_{max}) of *A. flavithermus* was
124 studied in BHI with pH 7.4 ± 0.2. In order to cover the growth range to the greatest possible
125 extent, a step of 2 °C was used and 17 temperature levels between 33 and 68 °C were
126 selected. Concerning the effect of temperature on (μ_{max}) of *B. licheniformis*, experiments were
127 conducted in TSB with pH 7.2 ± 0.2 at 22 temperature levels between 15 and 57 °C.

128 **2.2.2 Effect of pH on maximum specific growth rate (μ_{max})**

129 The effect of pH on maximum specific growth rates (μ_{max}) of *A. flavithermus* and
130 *B. licheniformis* was evaluated in BHI and TSB, respectively, at suboptimal temperature
131 conditions (55 and 43 °C, respectively), following the recommendation of Le Marc et al., 2021.
132 The pH adjustment was performed by adding NaOH 1 N (HC73325137, Merck, Darmstadt,
133 Germany) or HCl 1 N (HC67744657, Merck) to sterilized BHI or TSB by using a pre-sterilized
134 0.22 μm filter unit until the pH reached the necessary level; from 4.8 to 7.0 with a step of 0.2.
135 The pH measurements were performed at 25 °C with a pH meter with a glass electrode
136 (SevenMulti, Mettler Toledo, Ohio, USA).

137 2.2.3 Automated optical density measurements

138 To estimate the maximum specific growth rate (μ_{max}) values reached in the different pH levels
139 and temperatures between 30 and 59 °C, the automated turbidimetric system BioScreen C
140 (Oy Growth Curves Ab Ltd., Raisio, Finland) was used, following the method described by
141 Lianou and Koutsoumanis, 2011. The method adjusted as follows. Except for the first and fifth
142 rows that will receive the inoculum, the BioScreen plate wells were pre-filled with 180 μL of the
143 appropriate broth, based on the experimental set-up. The first and fifth rows were inoculated
144 with 200 μL of 10^6 CFU/mL from the 26-h culture, prepared as described in **Section 2.1**. To
145 avoid evaporation, the outer columns of the plate were filled with 200 μL of the selected broth
146 but were not used for sample inoculation. Decimal dilutions of the inoculum were performed
147 across the BioScreen plate by transferring 20 μL from one well to the other, while 20 μL of the
148 fifth dilution was discarded to keep the same culture volume (180 μL). Thus, the range of initial
149 concentrations obtained throughout the BioScreen plate was approximately $10^6 - 10^2$ CFU/mL.
150 Optical density (OD) measurements were automatically measured at standard time intervals
151 (10 min) using the wideband filter (600 nm) of the instrument, at temperatures between 30 and
152 59 °C, for a total period during which a considerable OD increase (0.2) for all five decimally
153 diluted cultures was observed. For the assessment of the effect of pH and on μ_{max}
154 experiments were conducted at sub-optimal growth temperature for each microorganism (55
155 and 43 °C), based on the results obtained for the temperature experiments. The BioScreen

156 plates were agitated for 30 sec to stop 5 sec prior to the OD measurements in all experiments.
157 One independent experiment was conducted for each selected pH level, and eight samples
158 (e.g., quadruple wells of five serially diluted cultures) were analysed (n=8), while for each
159 temperature level one independent experiment with 16 samples was analysed (n=16).

160 **2.2.4 Manual optical density measurements and plate count experiments**

161 BioScreen C instrument can operate up to 59 °C. However, thermophilic bacteria can grow to
162 much higher temperature levels. Since a precise harmonized methodology for the estimation
163 of cardinal values does not exist, two different protocols were applied in parallel for
164 temperature levels above 59 °C.

165 In the first protocol, the BioScreen plate inoculated with *A. flavithermus* was incubated into a
166 high-precision oven (Heratherm oven, ThermoScientific™) set to the studied temperature. The
167 temperature was monitored during incubation using electronic temperature-monitoring
168 devices (iButton; iButtonLink, Thermochron, Whitewater, WI, USA). The BioScreen plate was
169 prepared as described in **Section 2.2.3** and transferred manually to the BioScreen C, where
170 OD measurements were taken every 0.3 h for a total period such that a considerable OD
171 increase for all five decimally diluted cultures was observed.

172 In the second protocol, the BioScreen plate was inoculated with 200 µL of 10² CFU/well,
173 except for the wells in the outer columns, and incubated in the same oven. 0.1 mL were taken
174 every half an hour from a different well. After the appropriate serial decimal dilutions, samples
175 were spread plated on TSA agar plates and incubated aerobically at 55 °C for 24 h. Following
176 the plate count method, one experiment per temperature level was conducted (n=1).

177 **2.3 Growth experiments in plant-based milk alternative**

178 The growth kinetic behaviour of *A. flavithermus* and *B. licheniformis* was investigated
179 individually in a shelf stable, ready-to-eat food product, namely a pea-based beverage. This
180 product was selected based on the high frequency and high level of contamination of pea
181 isolates with thermoresistant and thermophilic spores, compared to other plant-based raw

182 materials (NIZO, 2022). The pea-based beverage contained 2.1 g proteins, 1.4 g fat and 5.7
183 g carbohydrates per 100 mL. The initial pH and water activity values of this product were 7.01
184 \pm 0.01 and 0.996 ± 0.02 , respectively. For this set of experiments, the samples were
185 artificially and independently contaminated with vegetative cells of *B. licheniformis* and
186 *A. flavithermus*. The inoculum of both microorganisms was prepared as described in **Section**
187 **2.1**. Portions of 200 mL of the samples were transferred into pre-sterilized 250 mL Duran
188 bottles and pre-heated in a water bath (ThermoScientific™, Haake w26 Fisons, Digitana AG)
189 at the selected temperature; 62 °C for *A. flavithermus* and at 49 °C for *B. licheniformis*,
190 respectively. After the appropriate dilutions of the inoculum, samples were aseptically
191 inoculated with approximately 10^2 - 10^3 CFU/mL and submerged again in the pre-heated water
192 bath at static conditions. The selected temperatures constitute the optimum temperature for
193 *A. flavithermus* and *B. licheniformis* growth, respectively, based on the optical density
194 experiments performed in broth. Three independent experiments were performed for each
195 microorganism (n=3).

196 For the enumeration of *B. licheniformis* and *A. flavithermus* concentration, samples were taken
197 every 30 min for the first four hours and every 1 h for the rest of the experimental duration.
198 Appropriate serial decimal dilutions of the samples were performed in TS solution before
199 surface plating on TSA plates. Before counting, plates were incubated aerobically at 37 and
200 55 °C for 24 h, respectively. At the same time span, monitoring of pH and visual observation
201 of the macroscopic changes in the structure of the samples were performed. The data derived
202 from this set of experiments were used to estimate the maximum specific growth rates of *B.*
203 *licheniformis* and *A. flavithermus* and then deduce their optimum specific growth rates in the
204 tested product (see **Section 2.4**).

205 The developed growth models of *A. flavithermus* and *B. licheniformis* were validated in the
206 pea beverage under static conditions at 55 and 42 °C, respectively. The validation
207 temperatures were selected, taking into account the temperature applied during UHT products'
208 quality control to detect insterility defaults caused by thermophilic spore-forming bacteria,

209 based on the recommendations (Cordier, 1990), and the applied industrial practices. The
210 developed models were further validated under non-isothermal conditions. The temperature
211 profiles were designed taking into account, the “worst case scenario” during distribution and
212 storage at a retail and domestic level. Hence, experiments were performed within a
213 temperature range from 12 to 55 °C. More specifically, the pea beverages inoculated with *A.*
214 *flavithermus* were stored at 25 °C for 12 h, 55 °C for 5 h, 30 °C for 24 h and 37 °C for 24 h,
215 while samples inoculated with *B. licheniformis* were stored at 12 °C for 12 h, 55 °C for 5 h, 30
216 °C for 24 h and 37 °C for 24 h. The temperature fluctuation was electronically monitored using
217 cox tracer data loggers (Cox Tracer, Cox Technologies, Belmont, NC, USA). Temperature
218 data were obtained with a time interval of 15 min. Samples were prepared and treated
219 following the same procedure as the one applied for the development of the model. For each
220 microorganism one independent experiment with two technical replicates was performed
221 (n=2).

222 **2.4 Data analysis**

223 Regarding the OD method experiments, the detection times of the five serial decimal dilutions
224 were plotted against the natural logarithm of their initial concentrations and the μ_{max} values
225 were determined by linear regression, according to the following equation as proposed by
226 Dalgaard and Koutsoumanis, 2001:

$$227 \quad \ln N_i = k - \mu_{max} \cdot DT_i \quad (1)$$

228 where DT_i is being generally defined as the time required for OD increase to 0.20 to be
229 observed.

230 For the plate count method experiments, the μ_{max} values were determined by fitting the
231 primary model of Baranyi and Roberts, 1994 (Eq. (2) and (3)) to the data by using the DMFit
232 Microsoft Excel add-in downloadable from the www.combase.cc.

$$233 \quad \frac{dN(t)}{dt} = \frac{Q(t)}{Q(t)+1} \cdot \mu_{max} \cdot \left(1 - \frac{N(t)}{N_{max}}\right) \cdot N(t) \quad (2)$$

234
$$\frac{dQ(t)}{dt} = \mu_{max} \cdot Q(t) \quad (3)$$

235

236 where N_t is the number of cell concentration at time t (CFU/mL); μ_{max} is the maximum specific
 237 growth rate of the cell population (1/h); N_{max} is the maximum cell density (CFU/mL).

238 The parameter Q denotes the concentration of a substance critical to growth, which is
 239 assumed to be synthesised during the lag phase, and is related to the physiological parameter
 240 h_0 as follows:

241
$$h_0 = \ln \left(1 + \frac{1}{Q_0} \right) = \mu_{max} \cdot \lambda$$

242 The effects of temperature and pH on μ_{max} of each microorganism were modelled individually
 243 using the Cardinal Model for temperature (Rosso et al., 1993) and pH (Aryani et al., 2015):

244
$$\mu_{max} = \mu_{opt-T} \cdot CM(T) \quad (4)$$

245 with

246
$$CM(T) = \begin{cases} 0, & T \leq T_{min} \\ \frac{(T-T_{min})^2(T-T_{max})}{(T_{opt}-T_{min})[(T_{opt}-T_{min})(T-T_{opt})-(T_{opt}-T_{max})(T_{opt}+T_{min}-2T)]}, & T_{min} \leq T \leq T_{max} \\ 0, & T \geq T_{max} \end{cases} \quad (5)$$

247 and

248
$$\mu_{max} = \mu_{opt-pH} \cdot CM(pH) \quad (6)$$

249 with

250
$$CM(pH) = 1 - 2 \frac{(pH-pH_{min})}{(pH_{min}-pH_{1/2})} \quad (7)$$

251

252 Where μ_{opt} is the value for the maximum specific growth rate when $T = T_{opt}$ and $pH = pH_{opt}$,
 253 T_{min} , T_{opt} and T_{max} are the theoretical minimum, optimum and maximum values of T enabling
 254 growth, pH_{min} is the theoretical minimum and $pH_{1/2}$ is the pH at which the μ_{max} is the half of
 255 the μ_{opt} .

256 The cardinal values (T_{\min} , T_{opt} , T_{\max} , pH_{\min} and $\text{pH}_{1/2}$) were determined by fitting the obtained
257 μ_{\max} values for *A. flavithermus* and *B. licheniformis* to the above model using the CardinalFit
258 software (Cadavez and Gonzales-Barron, 2020). The goodness of fit was evaluated by a
259 graphical comparison between the observed and the predicted values, the coefficient of
260 determination (R^2) and Root Mean Square Error (RMSE) (Ratkowsky, 2004).

261 The combined effect of temperature and pH on μ_{\max} , was predicted based on the following
262 equation, as proposed by Rosso et al., 1995:

$$263 \mu_{\max} = \mu_{\text{opt}} \cdot CM(T) \cdot CM(\text{pH}) \quad (8)$$

264

265 The above secondary model was adjusted for the tested plant-based alternative as following:

266

$$267 \mu_{\max} = \mu_{\text{ref}} \cdot \frac{CM(T) \cdot CM(\text{pH})}{CM(T_{\text{ref}}) \cdot CM(\text{pH}_{\text{ref}})} \quad (9)$$

268

269 Where rate μ_{ref} is the maximum specific growth rate in the plant-based alternative estimated
270 based on the growth data obtained from the experiments in this product at static conditions
271 and $CM(T_{\text{ref}})$, $CM(\text{pH}_{\text{ref}})$ are the cardinal model parameters (Eq. (5) and (7), respectively) for
272 the reference conditions ($\text{pH}=7.01$ and $T=62$ °C for *A. flavithermus* and $T=49$ °C for *B.*
273 *licheniformis*.. To estimate the growth kinetic parameters, the primary model of Baranyi and
274 Roberts, 1994 (Eq. (2) and (3)) was fitted to the above-mentioned data by using the DMFit
275 add-in in Microsoft Excel.

276 For the prediction of growth of *A. flavithermus* and *B. licheniformis* at 55 and 42 °C,
277 respectively, the parameter h_0 referring to the “work” required by the cells to adjust to the new
278 environment (Baranyi and Roberts, 1994), was estimated as the product of $\lambda^* \mu_{\max}$ based on
279 the values of the growth kinetic parameters obtained from the experiments performed in the
280 pea-based milk alternative (at 62 and 49 °C). Since h_0 constitutes a “characteristic” of the

281 cell culture and remains constant and independent from the storage temperature when the
282 pre-history of the culture is the same, (Baranyi and Roberts, 1995, 1994; Gougouli and
283 Koutsoumanis, 2016; Koutsoumanis et al., 2006; Pin and Baranyi, 2006) the parameter was
284 set on the same value for all predictions of growth.

285 The growth predictions of *A. flavithermus* and *B. licheniformis* in the selected food products
286 were estimated using the multiplicative secondary model (Eq. (8)) and primary model (Eq. (2)
287 and (3)). The prediction of growth at dynamic temperature conditions drew on the assumption
288 that the growth rate is adapted directly to the new temperature environment after a
289 temperature change and the equations (2) and (3) were numerically integrated based on time.
290 For the calculation of the “momentary” μ_{max} the multiplicative secondary model (Eq. (8)) was
291 used. The parameter μ_{opt} used in the secondary model (Eq. (8)) was calculated for the pea-
292 based milk alternative through the primary model (Eq. (2) and (3)), based on the estimated
293 μ_{max} determined from fitting the primary model (Eq. (2) and (3)) into the growth data obtained
294 from the experiments that were performed under static conditions.

295 The performance of the developed models in both static and dynamic temperature conditions
296 was evaluated using the percent relative errors (Koutsoumanis et al., 2006):

$$297 \quad \% \text{ Relative Error (RE)} = \frac{(\text{Log}(N_{t_{observed}}) - \text{Log}(N_{t_{predicted}}))}{\text{Log}(N_{t_{observed}})} \times 100 \quad (10)$$

298 **3. Results**

299 **3.1 Growth experiments in broth**

300 The effect of temperature (range: 33-68 °C) and pH (range: 5.6-7.0) on *A. flavithermus* growth
301 rate is presented in **Figures 1 and 2**. For the effect of temperature the growth rate increased
302 from 0.118 1/h (\pm 0.004) at T=33 °C to a maximum value of 3.393 1/h (\pm 0.09) at T=60 °C,
303 while at T levels above 60 °C a gradual reduction of μ_{max} was observed down to 2.319 1/h (\pm
304 0.10) at 68 °C. Accordingly, the μ_{max} (1/h) when studying the pH effect, increased from 0.847

305 1/h (± 0.002) at pH 5.6 to a maximum value of 1.805 1/h (± 0.04) at pH 6.4 where it reached
306 the plateau.

307 The effect of temperature (range: 15-57 °C) and pH (range: 4.8-7.0) on *B. licheniformis* growth
308 rate is presented in **Figures 3 and 4**. The growth rate increased from 0.068 1/h (± 0.003) at
309 T=15 °C to a maximum value of 3.083 1/h (± 0.04) at T=49 °C, while at T levels above this
310 level, a gradual reduction of μ_{max} was observed down to 0.178 1/h (± 0.009) at 57 °C.
311 Accordingly, for the effect of pH, the μ_{max} (1/h) increased from 0.516 1/h (± 0.01) at pH 4.8
312 and reached a plateau at 6.4 with a maximum value of 1.662 1/h (± 0.03).

313 The above experimental data (μ_{max}) were modelled as a function of temperature and pH using
314 CM for both microorganisms separately. The graphical evaluation of the fitting (**Figure 1-4**),
315 along with the statistical factors (**Table 1**) indicated a satisfactory performance of all models
316 in describing the effect of temperature and pH on the μ_{max} of *A. flavithermus* and
317 *B. licheniformis*. **Table 1** shows the estimated values for the cardinal parameters T_{min} ,
318 T_{opt} and T_{max} of *A. flavithermus* and *B. licheniformis* being 28.70, 61.23 and 71.52 °C and
319 11.68, 48.05 and 57.14 °C, respectively. Likewise, the estimated values for the parameters
320 pH_{min} and $pH_{1/2}$ of *A. flavithermus* and *B. licheniformis* were 5.52 and 5.73 and 4.71 and 5.67,
321 respectively. The goodness of fit was demonstrated graphically and by using the low values
322 of Root Mean Square Error (RMSE) (**Table 1**).

323 **3.2 Model development and validation in plant-based milk alternative**

324 In an attempt to adjust the models, the growth kinetics of *A. flavithermus* and *B. licheniformis*
325 were investigated in a pea-based milk alternative.

326 **Figures 5a and 5b** depict representative fittings of the primary model (Eq. (2) and (3)) to the
327 growth data obtained in the pea beverage under static conditions at 62 °C for *A. flavithermus*
328 and at 49 °C for *B. licheniformis*, respectively. As illustrated in **Figures 5a and 5b**, the
329 observed growth of *A. flavithermus* and *B. licheniformis* in the same plant-based milk
330 alternative showed a lag phase in both cases, estimated to 1.08 ± 0.15 and 1.36 ± 0.02 h,

331 respectively. Based on the latter observation, for predictions of *A. flavithermus* and
332 *B. licheniformis* growth in plant-based milk alternatives the parameter h_0 was set at 2.78 and
333 3.76, respectively. The maximum specific growth rates (μ_{max}) of *A. flavithermus* and
334 *B. licheniformis* in the pea beverage were estimated at 2.555 ± 0.09 and 2.229 ± 0.13 1/h,
335 respectively, while the optimum rates (μ_{opt}) were determined at 2.581 ± 0.09 and 2.764 ± 0.13
336 1/h, respectively. The maximum population concentration (N_{max}) was set at $10^{6.8}$ CFU/mL for
337 prediction of *A. flavithermus* growth and at $10^{7.5}$ CFU/mL for prediction of *B. licheniformis*
338 growth, based on the observed growth data obtained from the experiments performed for the
339 model development (see **Figure 5a** and **5b**).

340 In order to test the performance of the developed models in plant-based milk alternatives, the
341 model predictions were validated against the observed growth of *A. flavithermus* and
342 *B. licheniformis* at two static temperatures that were not used during the model development
343 stage, namely 55 and 42 °C, respectively, as well as under non-isothermal conditions. The
344 growth was predicted by using a combination of the secondary model (Eq. (4)) with the Baranyi
345 and Roberts primary model (Eq. (2) and (3)), following the method described in **Section 2.4**.

346 The performance of the model was first graphically evaluated as depicted in **Figures 6 - 9**. As
347 illustrated in **Figure 6**, *A. flavithermus* in the selected plant-based milk alternative exhibited
348 an approximately 5 log increase when exposed at 55 °C for 10 h; that was predicted by the
349 model. *B. licheniformis* reached its maximum concentration when the tested products were
350 stored at 42 °C for 10 h (**Figure 7**), and it was accurately predicted by the model. **Figures 8**
351 and **9** depict the observed growth of *A. flavithermus* and *B. licheniformis*, respectively, along
352 with the predicted growth under non-isothermal conditions. The developed models predicted
353 growth satisfactory under dynamic temperatures suggesting that the assumptions made for
354 growth prediction were valid. The results showed that the bacterium adapts instantaneously
355 to the new environment without presenting any additional lag phase and grow with the
356 expected μ_{max} . Even after a storage period of about 12 h at temperatures below T_{min} , both
357 bacteria were able to initiate growth when temperature increased to levels within the biokinetic

358 range with a lag phase and a growth rate very close to those predicted by the model. The
359 performance of the models was further evaluated through the estimation of the percent relative
360 error (%RE). Based on the combined growth data obtained from the validation experiments,
361 %RE values were estimated for each developed model. As presented in **Figure 10**, for
362 *A. flavithermus* 85.7% of the predictions were within -10 and 10 % RE zone, while for
363 *B. licheniformis* percentage of predictions within the same zone was 97.4 %. In addition, for
364 both models none of the predictions were outside the -20 and 20 % RE zone.

365 **4. Discussion**

366 The estimated cardinal values of the temperature and pH of *B. licheniformis* are comparable
367 with the values reported by Trunet et al., 2015, who modelled the recovery of heat-treated
368 *Bacillus licheniformis* spores at suboptimal temperature and pH using growth limits. In
369 particular, the authors reported slightly higher optimum (49.01°C), maximum temperature
370 values (57.87°C) and lower minimum pH values (4.63) compared to the ones obtained in the
371 present study (see **Table 1**). The above differences could be attributed mainly to strain
372 variability (Lianou and Koutsoumanis, 2013), since in the Trunet et al.'s study a different strain
373 of *B. licheniformis* (Ad978) was used. At the same time the observed difference might also be
374 explained by the different model fitted to the data. The experiments for the estimation of
375 cardinal pH values presented in this study were conducted at a temperature lower than the
376 optimum one since temperature has a markable effect on the estimation of pH_{min} parameter
377 (Le Marc et al., 2002; Martinez-Rios et al., 2019). The above-described relationship between
378 temperature and minimum pH values has already been highlighted for mesophilic *B. cereus*
379 *sensu lato* (Le Marc et al., 2021). However, in the present study the effect of and extrinsic (T)
380 and intrinsic factors (pH) on the μ_{max} was studied individually without including any interaction
381 term, based on the gamma concept and the hypothesis that each factor has an independent
382 effect on the growth rate (Zwietering et al., 1992).

383 To our knowledge, this study provides the first attempt to estimate the cardinal temperature
384 and pH values of *A. flavithermus* DSM 21510. However, the estimated cardinal temperature

385 values are in line with the temperature growth range (30-72 °C) and the optimum temperature
386 range (60-65 °C) of *A. flavithermus* DSM 2641 reported by Ellis and Magnuson, 2012.
387 Interestingly, the results of the present study indicated that both optical density and the plate
388 count method provide comparable μ_{max} values, since the μ_{max} values obtained through the
389 plate count method fall within the “cloud” of μ_{max} values obtained through optical density
390 method (data not shown). The above observation suggests that experiments at high
391 temperature (above 59 °C) for the estimation of cardinal temperature values of thermophilic
392 bacteria can be conducted using any of the above methodologies.

393 The accuracy of the developed models in the plant-based milk alternative was graphically
394 evaluated by comparing the observed with predicted values. In addition, the performance of
395 the models was statistically evaluated by using the percent relative error (% RE). Considering
396 that % RE for *A. flavithermus* and *B. licheniformis* models ranged between -15.46 and 13.24
397 % and from -12.73 to 9.79 %, respectively, the ability of the models to predict growth was
398 deemed satisfactory. Moreover, no specific over- or underestimating trend was observed.

399 Food spoilage challenges emerge from innovative raw materials and food products. In similar
400 vein, the vast majority of plant-based proteins used as raw materials are known for their poor
401 solubility properties during dissolution which can hamper the effectiveness of the heat process
402 (Akharume et al., 2021; Sim et al., 2021), allowing the survival of spores. The models
403 developed in the present study can be used to evaluate the risk of microorganisms surviving
404 the heat process to grow to levels that can cause spoilage. In particular, the developed models
405 can be incorporated in a quantitative microbial spoilage risk assessment model to estimate
406 the growth during transportation and storage and the associated risk of spoilage. While the
407 effect of temperature and pH on the growth rate of these microorganisms has been described,
408 the quantitative risk assessment model can be also applied to control growth, by providing
409 alternatives that can mitigate the risk of spoilage.

410 For the evaluation of the risk, it is of great importance to investigate the prevalence and
411 contamination level of several thermophilic and thermotolerant bacteria in plant-based

412 proteins that are not currently available in the literature. The NIZO institute reported that less
413 than 100 CFU/g might be found in pea proteins (NIZO, 2021). When a low number of surviving
414 spores are expected in the products, cell heterogeneity should be taken into consideration as
415 a significant variability source (Baranyi and Pin, 2004; Kakagianni et al., 2017; Koutsoumanis
416 and Lianou, 2013). Nonetheless, the present deterministic form of the model does not take
417 into account the variability of individual spore behaviour. Future data and information on
418 individual spore heterogeneity as affected by the heat treatment can allow a stochastic
419 modelling approach and provide more precise growth predictions (Koutsoumanis & Lianou,
420 2013). This data shall include the likelihood of individual spore outgrowth in a finished product
421 after exposure to the heat treatment. In addition, the performance of the models developed in
422 the present study can be further improved by taking into account strain variability. Considering
423 the diversity of strains that may be present in the final product, “feeding” the models with
424 additional research data on the intra-species differences in the growth kinetics of *A.*
425 *flavithermus* and *B. licheniformis* are certainly expected to increase their accuracy in predicting
426 the risk of spoilage (Lianou and Koutsoumanis, 2013).

427 **5. Conclusions**

428 To our knowledge, this is the first study on the development and validation of a predictive
429 model for the effect of temperature and pH on the growth of *Anoxybacillus flavithermus* and
430 *Bacillus licheniformis* in plant-based milk alternatives. Validation studies showed that the
431 developed models satisfactorily predicted the growth behaviour of both spoilage bacteria in
432 the selected pea beverage. Hence, the models developed in the present study could be
433 applied for an effective spoilage risk assessment to ensure microbial stability of plant-based
434 milk alternatives.

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438 **CRedit authorship statement**

439 **Ourania Misiou**: Conceptualization, Data curation, Investigation, Writing - Original Draft,
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441 Review & Editing. **Konstantinos Koutsoumanis**: Conceptualization, Funding acquisition,
442 Methodology, Writing - Review & Editing.

443 **Declaration of competing interest**

444 The authors declare that they have no known conflict of financial interests or personal
445 relationships that could have appeared to influence the work reported in this paper

446 **References**

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Table 1. Estimated values and fitting statistics for the cardinal parameter model describing the effect of temperature and pH on the maximum specific growth rate (μ_{max}) of *Anoxybacillus flavithermus* DSM 21510 and *Bacillus licheniformis* DSM 13 in brain heart infusion and tryptone soy broth, respectively.

Parameter	Estimated value ^a	95 % Confidence Limits		RMSE ^b	R ^{2c}
		Upper	Lower		
<i>Anoxybacillus flavithermus</i>					
Temperature cardinal values					
μ_{opt-T} (pH= 7.4) (1/h)	3.471 ± 0.04				
T_{min}	28.70 ± 0.26	28.69	28.71	0.08	0.974
T_{opt}	61.23 ± 0.16	58.05	65.00		
T_{max}	71.52 ± 0.32	71.51	71.53		
pH cardinal values					
μ_{opt-pH} (T= 55 °C) (1/h)	3.242 ± 0.06				
pH_{min}	5.52 ± 0.01	5.51	5.53	0.07	0.946
$pH_{1/2}$	5.73 ± 0.01	5.72	5.73		
<i>Bacillus licheniformis</i>					
Temperature cardinal values					
μ_{opt-T} (pH= 7.2) (1/h)	2.836 ± 0.03				
T_{min}	11.68 ± 0.26	11.67	11.69	0.09	0.972
T_{opt}	48.05 ± 0.15	45.50	51.19		
T_{max}	57.14 ± 0.01	57.13	57.15		
pH cardinal values					
μ_{opt-pH} (T= 43 °C) (1/h)	3.195 ± 0.15				
pH_{min}	4.71 ± 0.01	4.70	4.71	0.07	0.969
$pH_{1/2}$	5.67 ± 0.08	5.652	5.69		

^a ±: Standard Error

^b RMSE: Root Mean Square Error

^c R²: Coefficient of determination

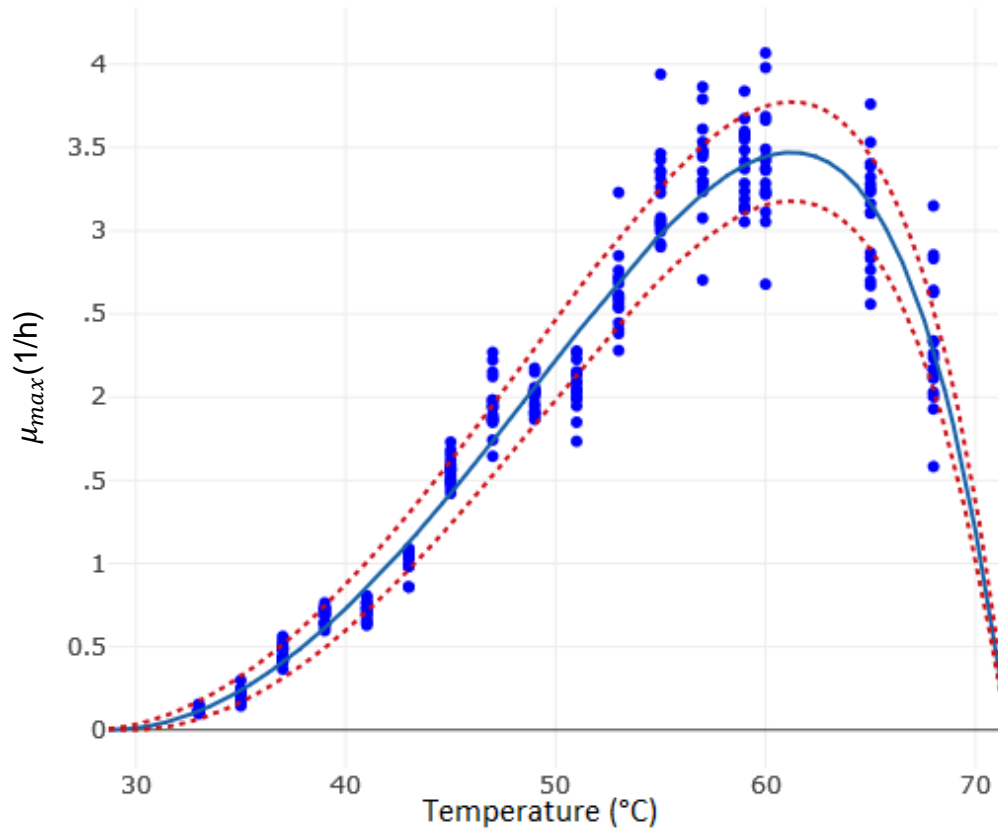


Figure 1. Effect of temperature on the maximum specific growth rate (μ_{max}) of *Anoxybacillus flavithermus* DSM 21510 in brain heart infusion broth. Data are fitted to the Cardinal Model (—). Points (○) represent observed values of the μ_{max} . The dashed red lines (--) indicate the 95% confidence limits.

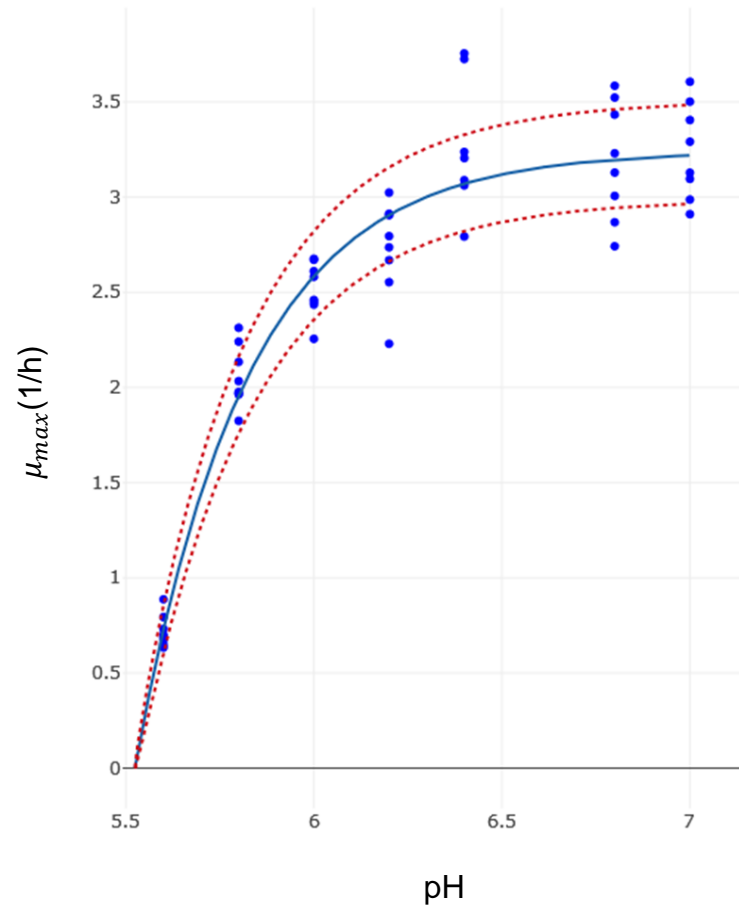


Figure 2. Effect of pH on the maximum specific growth rate (μ_{max}) of *Anoxybacillus flavithermus* DSM 21510 in brain heart infusion broth. Data are fitted to the Cardinal Model (—). Points (○) represent observed values of the μ_{max} . The dashed red lines (--) indicate the 95% confidence limits.

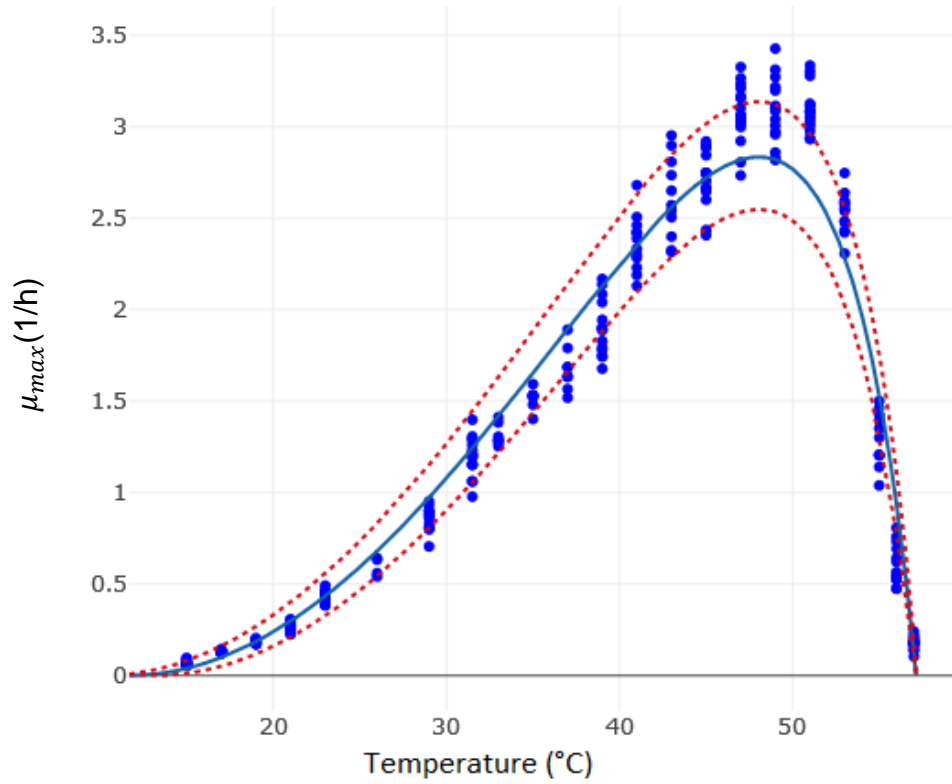


Figure 3. Effect of temperature on the maximum specific growth rate (μ_{max}) of *Bacillus licheniformis* DSM 13 in tryptone soy broth. Data are fitted to the Cardinal Model (—). Points (○) represent observed values of the μ_{max} . The dashed red lines (--) indicate the 95% confidence limits.

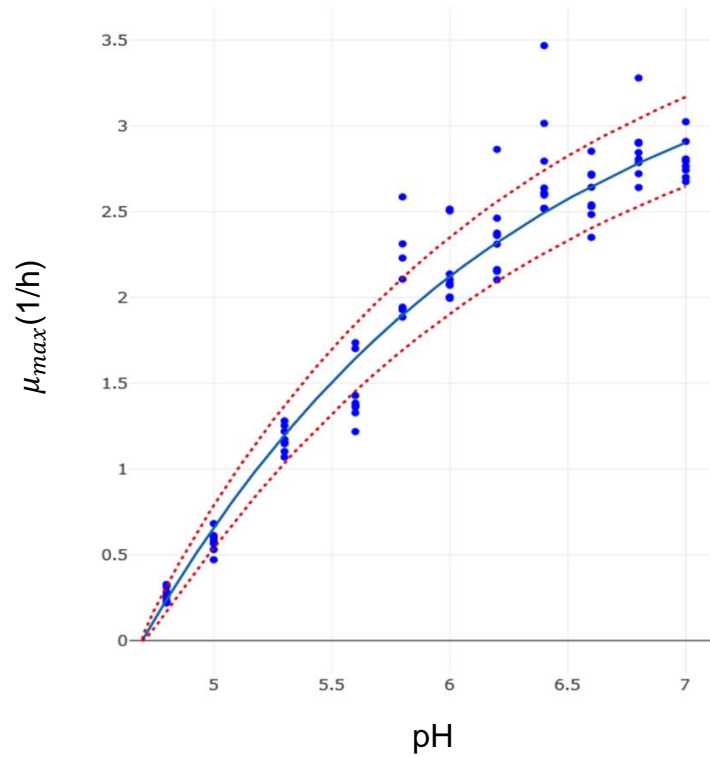
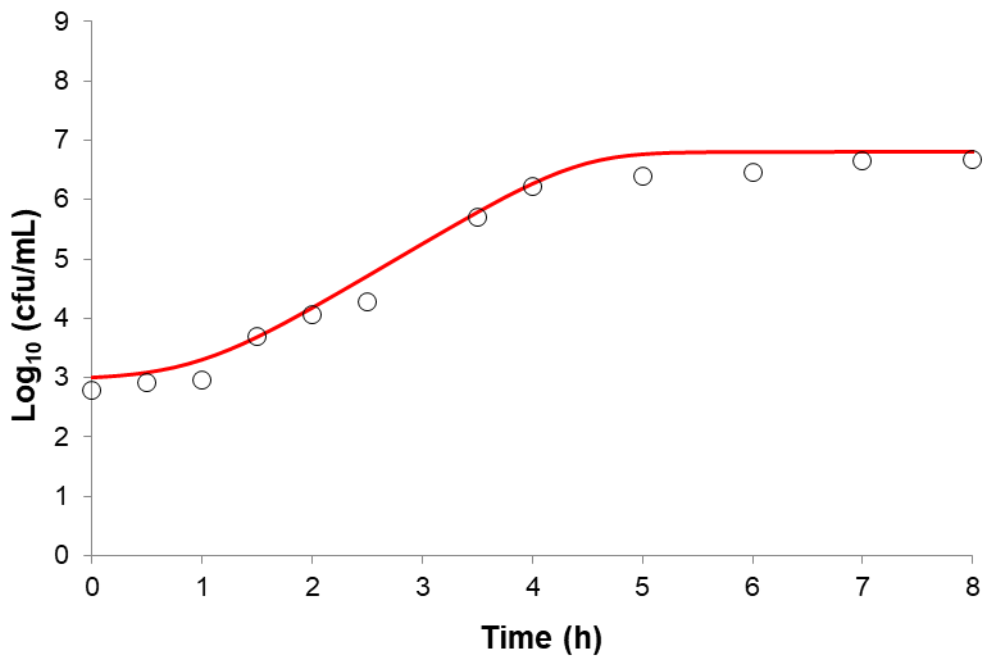
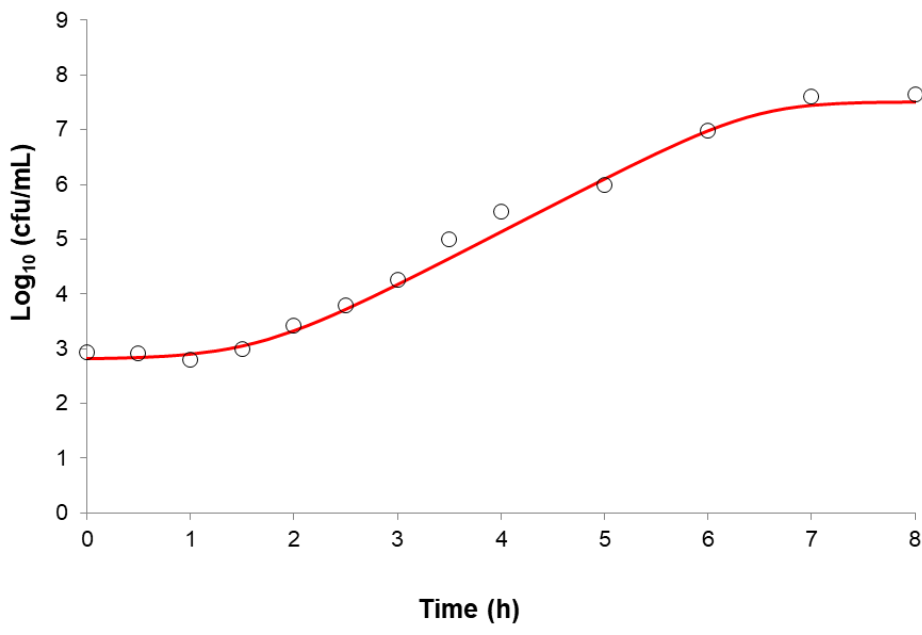


Figure 4. Effect of pH on the maximum specific growth rate (μ_{max}) of *Bacillus licheniformis* DSM 13 in tryptone soy broth. Data are fitted to the Cardinal Model (—). Points (○) represent observed values of the μ_{max} . The dashed red lines (--) lines the 95% confidence limits.



(a)



(b)

Figure 5. Growth kinetics of *Anoxybacillus flavithermus* DSM 21510 (a) and *Bacillus licheniformis* DSM 13 (b) in plant-based milk alternative during storage at optimum growth temperature at 62 and 49 °C, respectively. The red solid lines (-) indicate the fitting of the Baranyi and Roberts model to the growth data. One representative fitting of each spoilage bacterium is shown.

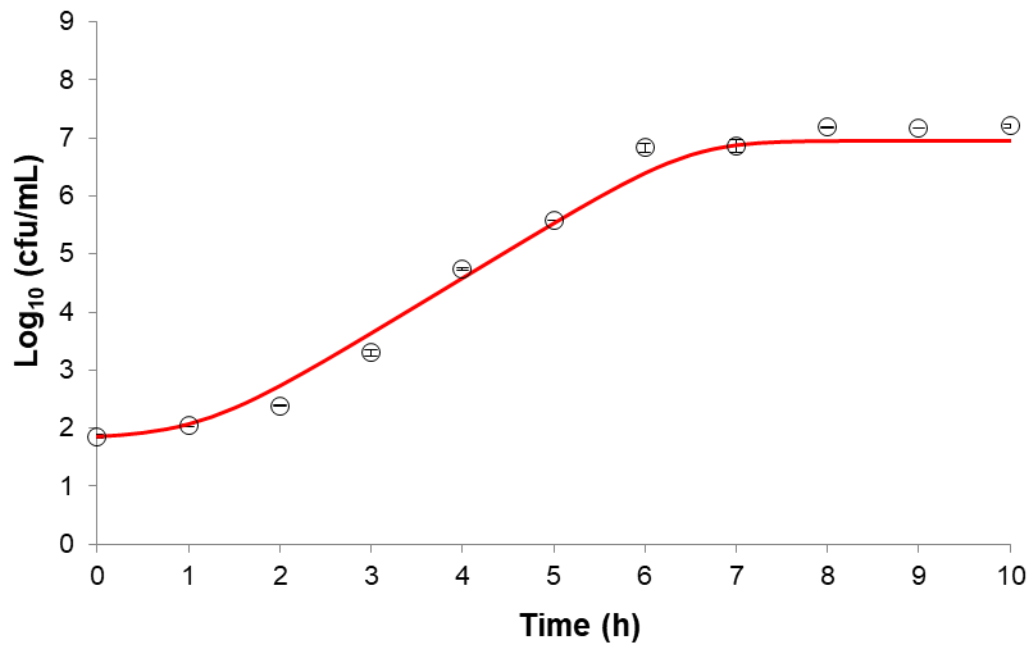


Figure 6. Comparison between observed (\circ) and predicted growth ($-$) of *Anoxybacillus flavithermus* DSM 21510 with time (h) in plant-based milk alternative when stored at 55 °C. Mean values \pm standard deviation of one independent experiment with two replicates are shown.

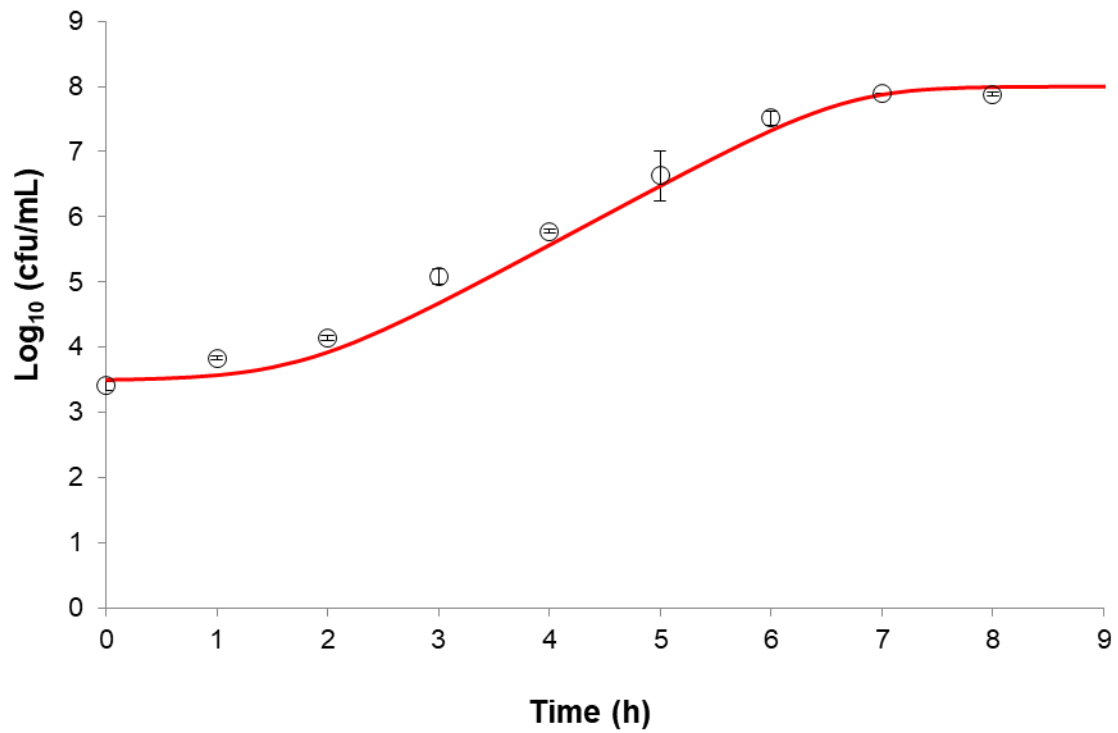


Figure 7. Comparison between observed (\circ) and predicted growth (-) of *Bacillus licheniformis* DSM 13 in plant-based milk alternative stored at 42 °C. Mean values \pm standard deviation of one independent experiment with two replicates are shown.

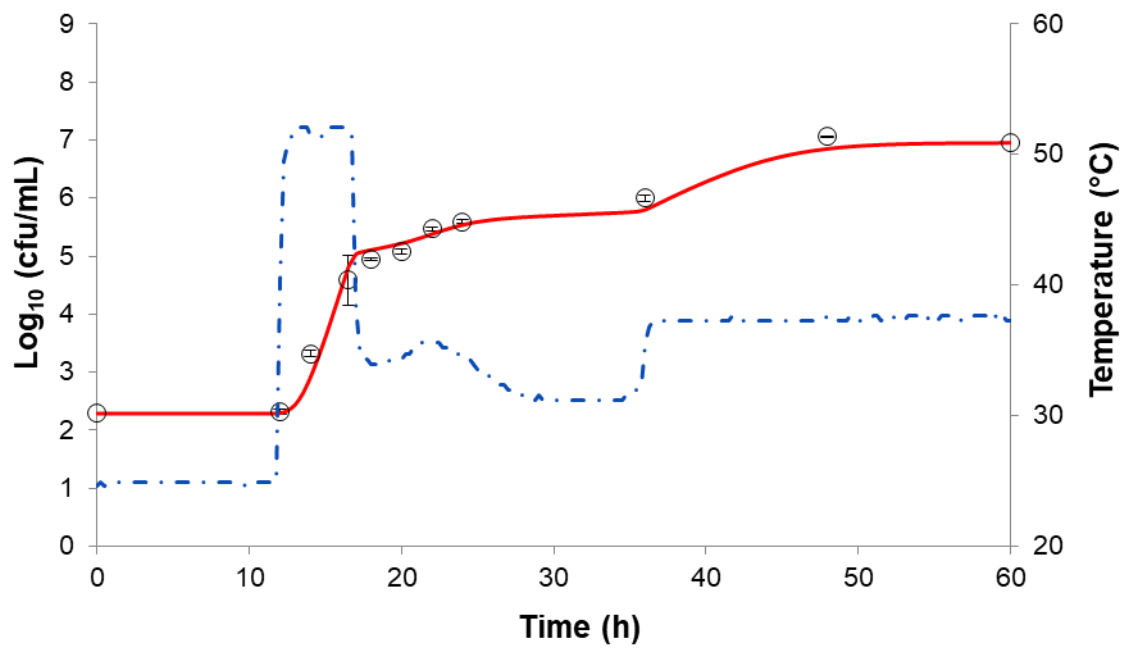


Figure 8. Comparison between observed (○) and predicted growth (-) of *Anoxybacillus flavithermus* DSM 21510 with time (h) in plant-based milk alternative stored at 25 °C for 12h, 55 °C for 5 h, 30 °C for 24 h and 37 °C for 24 h. Dashed dot blue line (--) indicates temperature changes. Mean values ± standard deviation of one independent experiment with two replicates are shown.

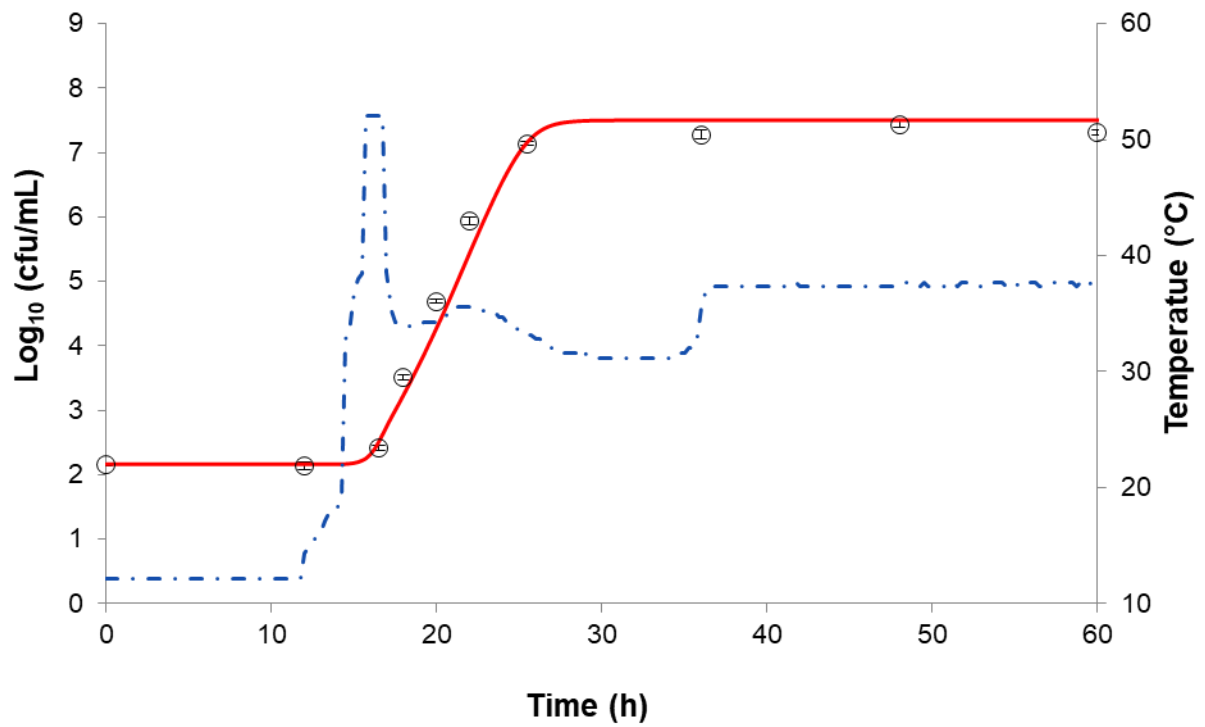


Figure 9. Comparison between observed (○) and predicted growth (-) of *Bacillus licheniformis* DSM 13 with time (h) in plant-based milk alternative stored at 12 °C for 12h, 55 °C for 5 h, 30 °C for 24 h and 37 °C for 24 h. Dashed dot blue line (--) indicates temperature changes. Mean values ± standard deviation of one independent experiment with two replicates are shown.

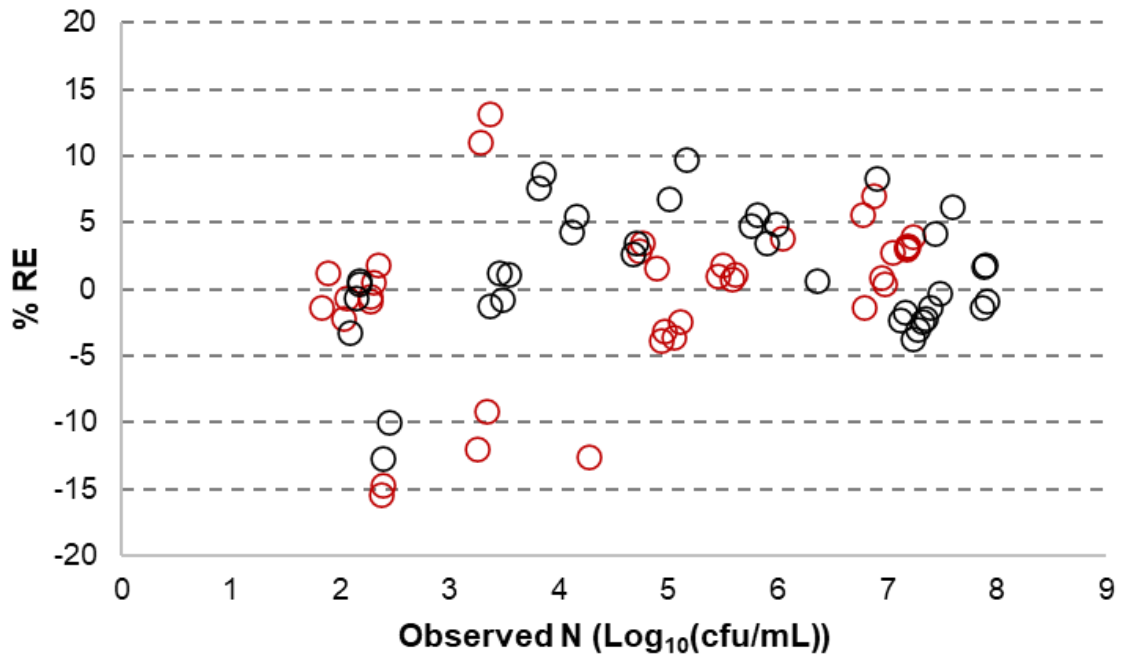


Figure 10. Relative error values (%RE) (Eq. (10)) for the comparison between observed and predicted population (Log CFU/mL) of *Anoxybacillus flavithermus* DSM 21510 (○) and *Bacillus licheniformis* DSM 13 (○) in plant-based milk alternative stored under static and dynamic temperature conditions.