

# Antimatter in the lab

Lecture 2

Jack Devlin

CERN

25/7/2023

# Recap

## Lecture 1

1. What is antimatter?

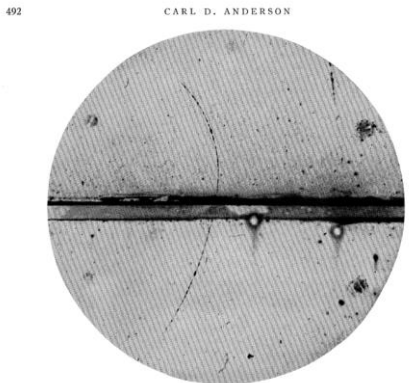
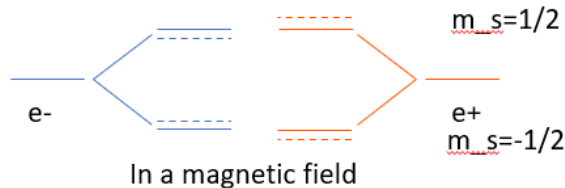
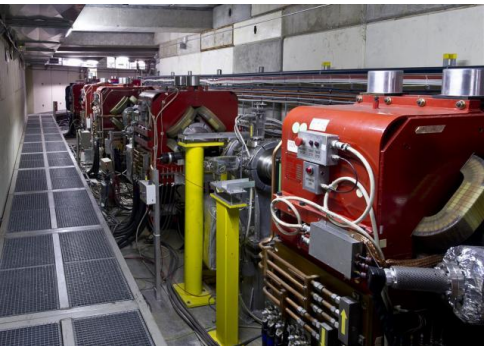
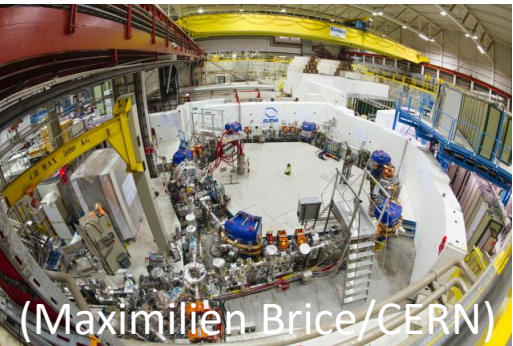


FIG. 1. A 63 million volt positron ( $H_0=2.1 \times 10^6$  gauss-cm) passing through a 6 mm lead plate and emerging as a 23 million volt positron ( $H_0=7.5 \times 10^6$  gauss-cm). The length of this latter path is at least ten times greater than the possible length of a proton path of this curvature.

2. Why study antimatter?



3. How do we make antimatter at CERN?

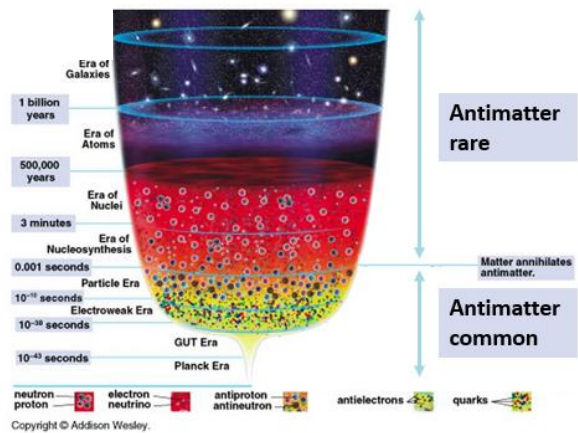


$$(i\gamma^\mu \partial_\mu - m) \Psi(x, t) = 0$$

$$E = +E_p = +\sqrt{p^2 + m^2} \quad E = -E_p = -\sqrt{p^2 + m^2}$$

$$\Psi_1 = A \begin{pmatrix} 1 \\ 0 \\ p \\ m+E_p \end{pmatrix} e^{-ip^\mu x_\mu} \quad \Psi_3 = A \begin{pmatrix} -p \\ E_p+m \\ 0 \\ 1 \end{pmatrix} e^{-ip^\mu x_\mu}$$

$$\Psi_2 = A \begin{pmatrix} 0 \\ 1 \\ 0 \\ -p \\ E_p+m \end{pmatrix} e^{-ip^\mu x_\mu} \quad \Psi_4 = A \begin{pmatrix} 0 \\ p \\ E_p+m \\ 0 \\ 1 \end{pmatrix} e^{-ip^\mu x_\mu}$$



Antimatter rare

SHOULD NOT EXIST (according to known physics)

Problem: one billion times more matter left over than expected

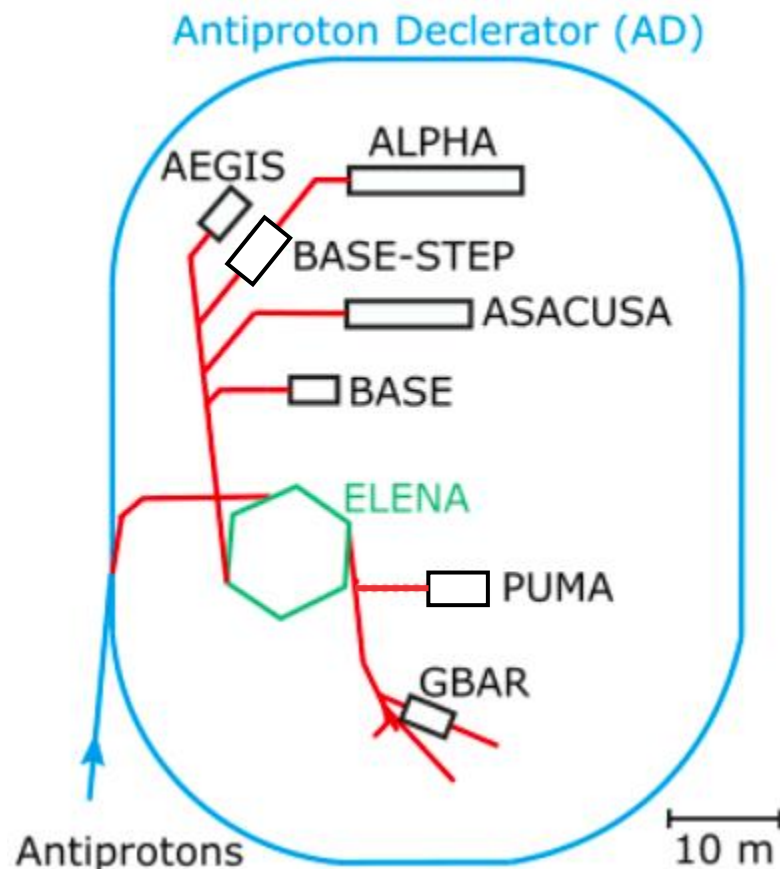
Antimatter common

Figure adapted from "The Essential Cosmic Perspective", by Bennett, Voit, and Donahue

# Overview

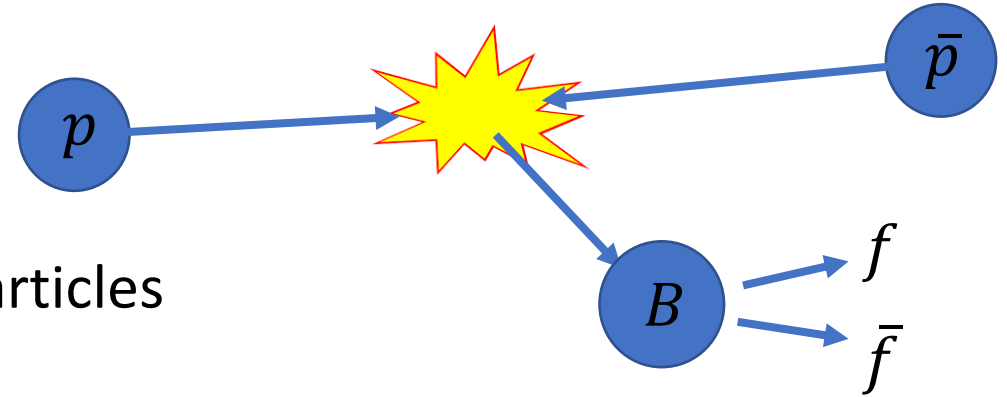
## Lecture 2: Experiments at the Antimatter Factory

1. Catching and storing antimatter
2. Measurements on antiprotons
3. Spectroscopy of anti-atoms
4. Gravity and antihydrogen
5. Taking antimatter out of the lab (and into another lab..)



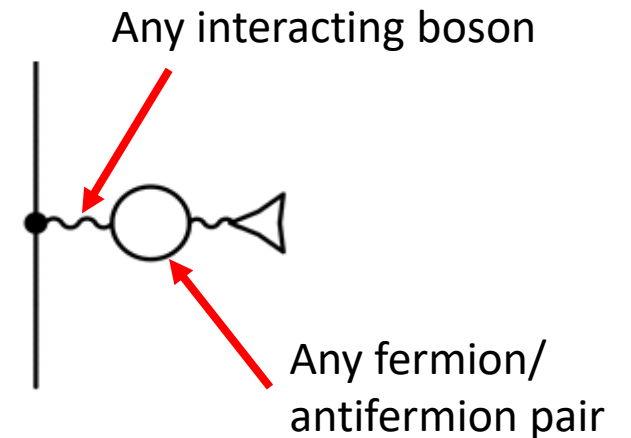
# Low energy physics

- High energy experiments (direct search)
  - Produce and detect new particles in high energy particle collisions
  - High energies needed to make non-virtual particles
- Precision experiments: (indirect search)



$$\frac{g_{electron}}{2} = 1 + a_{QED} + a_{\mu,\tau} + a_{weak} + a_{hadrons} + a_{New\ physics}$$

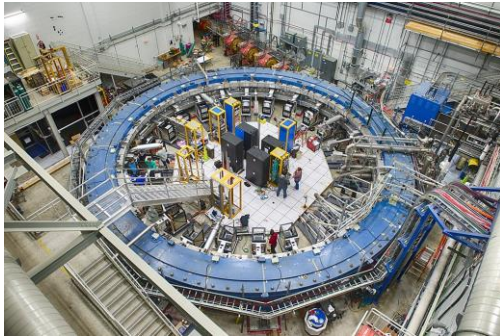
So far, all low energy CPT tests have been consistent with no CPT breaking



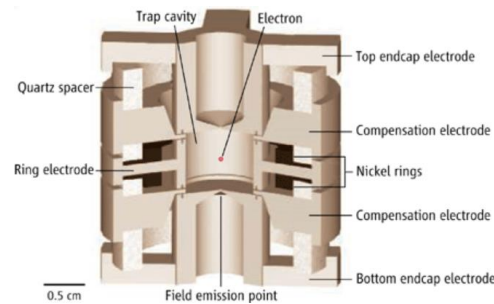
# Other efforts

Many groups studying antimatter. Some notable ones are:

**Positron-electron magnetic moment** University of Washington/Harvard, new effort at Northwestern  
Van Dyke & Dehmelt / Gabrielse



Reidar Hahn

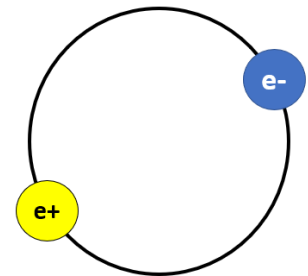


Gabrielse /Harvard

**Muon-antimuon magnetic moment** Fermilab, formerly Brookhaven

**Positronium, muonium**, bound states of electrons/positron and antimuon+ electron: many groups

**Kaons, B mesons, other collider searches**



D. Hanneke et al. Phys. Rev. Lett. **100** (2008)

R.S. Van Dyke, Jr., P.B. Schwinberg, and H.G. Dehmelt, Phys. Rev. Lett. **59**, 26 (1987)

G.W. Bennett et al., Phys. Rev. Lett. **89**, 101804 (2002)

B. Abi et al. (Muon  $g-2$  Collaboration) Phys. Rev. Lett. **126**, (2021)

# Why many efforts?

## Minimal Standard Model Extension (SME)

$$\mathcal{L}_{\text{lepton}}^{\text{CPT-even}} = \frac{1}{2}i(c_L)_{\mu\nu AB}\bar{L}_A\gamma^\mu\overleftrightarrow{D}^\nu L_B + \frac{1}{2}i(c_R)_{\mu\nu AB}\bar{R}_A\gamma^\mu\overleftrightarrow{D}^\nu R_B \quad , \quad (9)$$

$$\mathcal{L}_{\text{lepton}}^{\text{CPT-odd}} = -(a_L)_{\mu AB}\bar{L}_A\gamma^\mu L_B - (a_R)_{\mu AB}\bar{R}_A\gamma^\mu R_B \quad , \quad (10)$$

$$\mathcal{L}_{\text{quark}}^{\text{CPT-even}} = \frac{1}{2}i(c_Q)_{\mu\nu AB}\bar{Q}_A\gamma^\mu\overleftrightarrow{D}^\nu Q_B + \frac{1}{2}i(c_U)_{\mu\nu AB}\bar{U}_A\gamma^\mu\overleftrightarrow{D}^\nu U_B + \frac{1}{2}i(c_D)_{\mu\nu AB}\bar{D}_A\gamma^\mu\overleftrightarrow{D}^\nu D_B \quad , \quad (11)$$

$$\mathcal{L}_{\text{quark}}^{\text{CPT-odd}} = -(a_Q)_{\mu AB}\bar{Q}_A\gamma^\mu Q_B - (a_U)_{\mu AB}\bar{U}_A\gamma^\mu U_B - (a_D)_{\mu AB}\bar{D}_A\gamma^\mu D_B \quad . \quad (12)$$

$$\mathcal{L}_{\text{Yukawa}}^{\text{CPT-even}} = -\frac{1}{2}[(H_L)_{\mu\nu AB}\bar{L}_A\phi\sigma^{\mu\nu}R_B + (H_U)_{\mu\nu AB}\bar{Q}_A\phi^c\sigma^{\mu\nu}U_B + (H_D)_{\mu\nu AB}\bar{Q}_A\phi\sigma^{\mu\nu}D_B] + \text{h.c.} \quad (13)$$

$$\mathcal{L}_{\text{Higgs}}^{\text{CPT-even}} = \frac{1}{2}(k_{\phi\phi})^{\mu\nu}(D_\mu\phi)^\dagger D_\nu\phi + \text{h.c.} - \frac{1}{2}(k_{\phi B})^{\mu\nu}\phi^\dagger\phi B_{\mu\nu} - \frac{1}{2}(k_{\phi W})^{\mu\nu}\phi^\dagger W_{\mu\nu}\phi \quad , \quad (14)$$

$$\mathcal{L}_{\text{Higgs}}^{\text{CPT-odd}} = i(k_\phi)^\mu\phi^\dagger D_\mu\phi + \text{h.c.} \quad . \quad (15)$$

$$\mathcal{L}_{\text{gauge}}^{\text{CPT-even}} = -\frac{1}{2}(k_G)_{\kappa\lambda\mu\nu}\text{Tr}(G^{\kappa\lambda}G^{\mu\nu}) - \frac{1}{2}(k_W)_{\kappa\lambda\mu\nu}\text{Tr}(W^{\kappa\lambda}W^{\mu\nu}) - \frac{1}{4}(k_B)_{\kappa\lambda\mu\nu}B^{\kappa\lambda}B^{\mu\nu} \quad . \quad (16)$$

$$\mathcal{L}_{\text{gauge}}^{\text{CPT-odd}} = (k_3)_\kappa\epsilon^{\kappa\lambda\mu\nu}\text{Tr}(G_\lambda G_\mu + \frac{2}{3}ig_3G_\lambda G_\mu G_\nu) + (k_2)_\kappa\epsilon^{\kappa\lambda\mu\nu}\text{Tr}(W_\lambda W_\mu + \frac{2}{3}igW_\lambda W_\mu W_\nu) + (k_1)_\kappa\epsilon^{\kappa\lambda\mu\nu}B_\lambda B_\mu + (k_0)_\kappa B^\kappa \quad . \quad (17)$$

CPT breaking coefficients proportional to (energy)<sup>(-order)</sup>

Measurement	Energy scale	Fractional precision	Measurement in energy units
$K_0 - \bar{K}_0$ mass difference	Mass of two Kaons ~1 GeV	$4.8 \times 10^{-19}$	$4.8 \times 10^{-19}$ GeV
$\bar{H}$ 1S-2S	~2500 THz	$2 \times 10^{-12}$	$2 \times 10^{-20}$ GeV
$\bar{p}$ magnetic moment	Larmor frequency ~81 MHz at 1.95 T	$1.5 \times 10^{-9}$	$5 \times 10^{-25}$ GeV

## Non-minimal Standard Model Extension (SME)

18 pages to write down

Don't know a priori where to look!

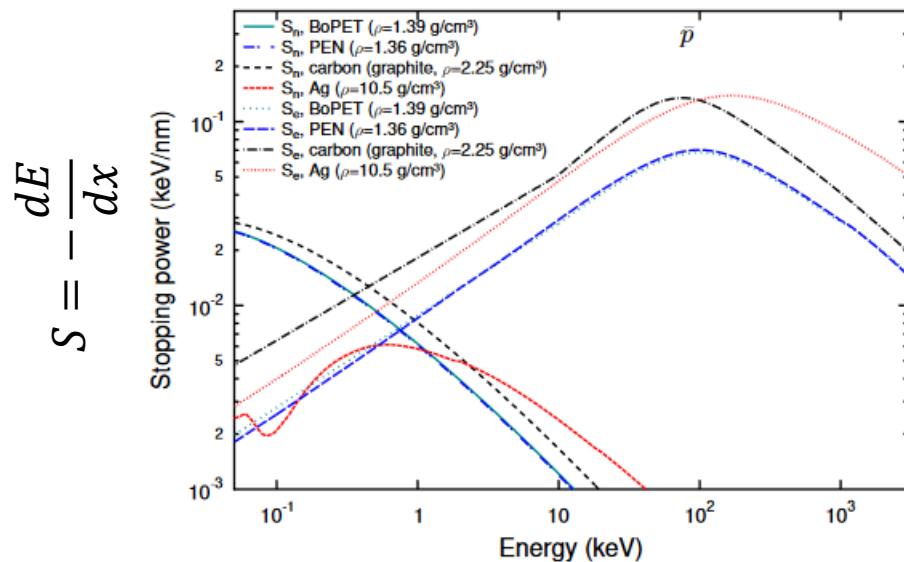
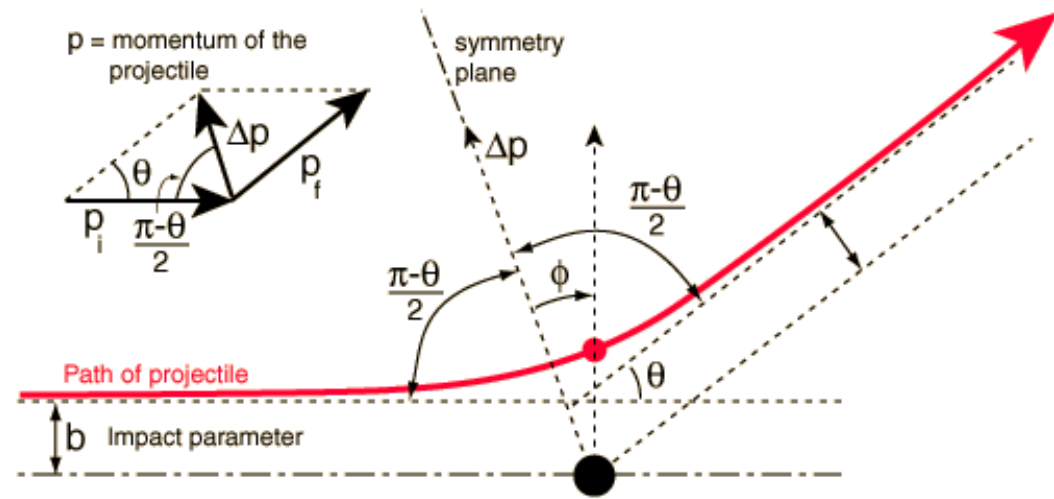
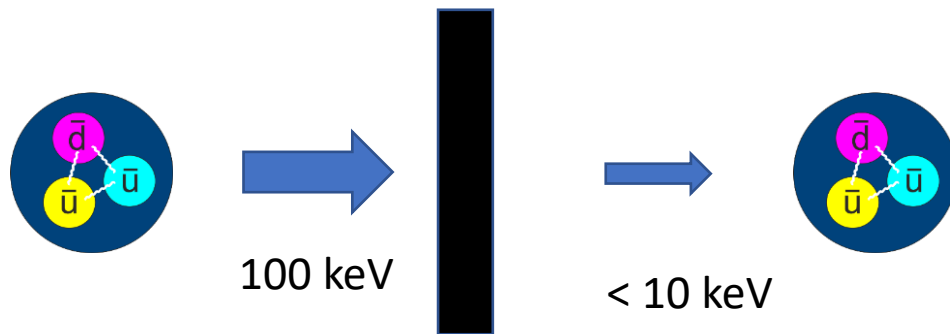
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# Catching and storing antimatter

# Final step of slowing

Final ELENA energy 100 keV, need a final step to reach trappable energies

Degrader foil



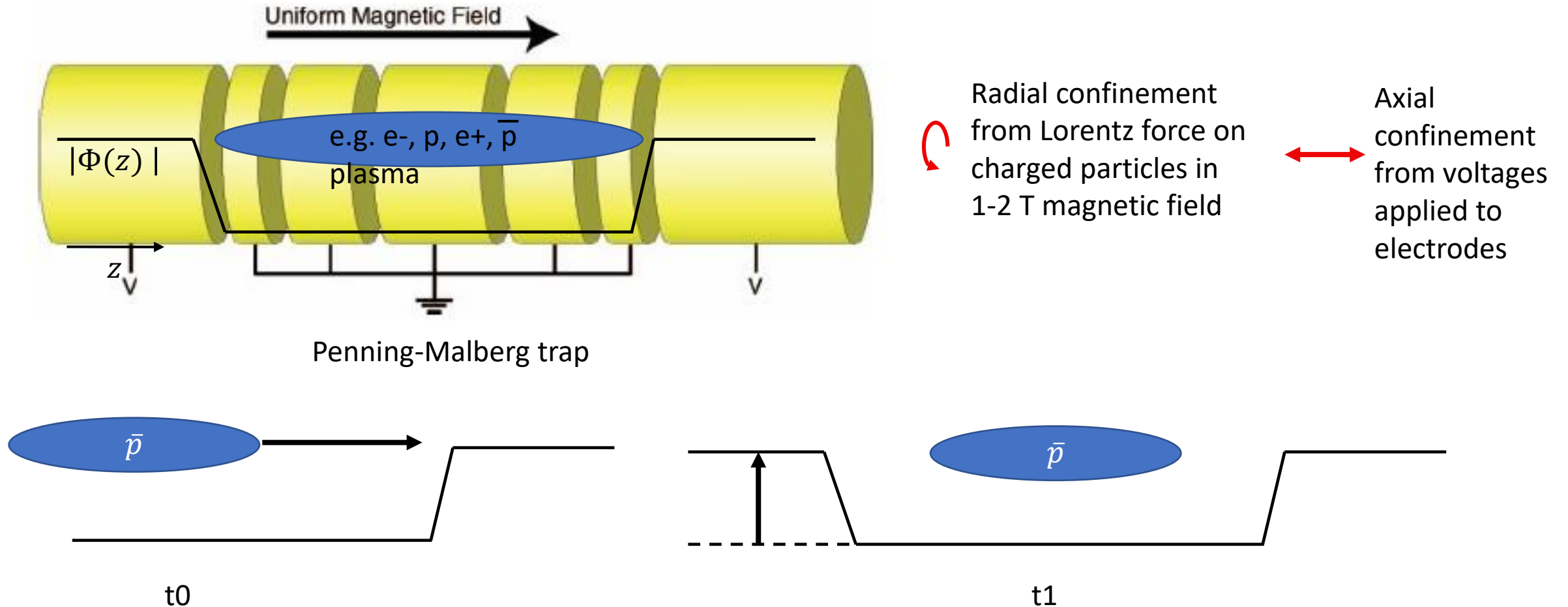
Sum of scattering from electrons and Rutherford scattering from nuclei

Up to ~50% antiprotons transmitted



# Catching antiprotons

Strong magnetic and moderate electric fields used



Can co-trap with electrons and use these to sympathetically cool

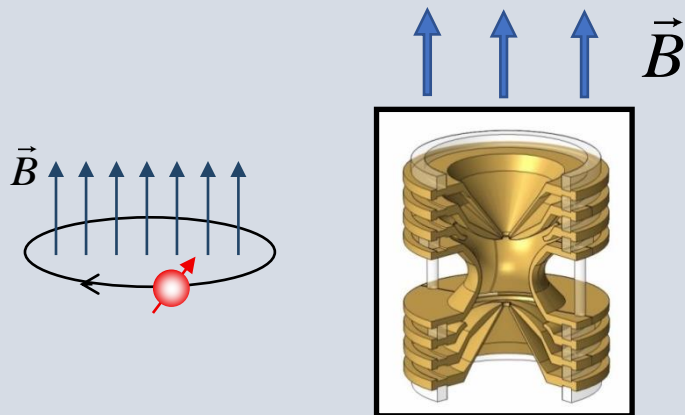
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# Measurements on antiprotons

# Properties

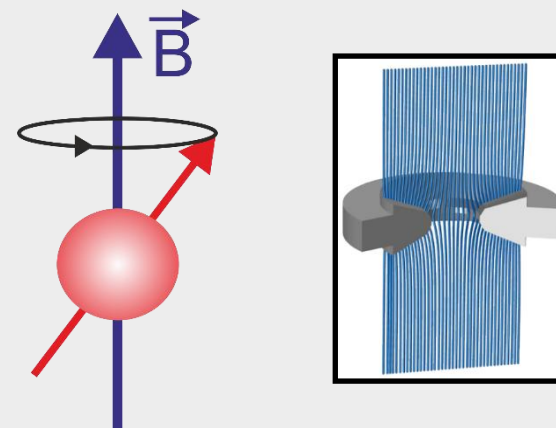
Measurements

## Cyclotron Frequency



$$\omega_c = \frac{q}{m} B$$

## Larmor Frequency



$$\omega_L = g \frac{e}{2m_p} B$$

## Trap loss rate



CPT Tests

$$\frac{\omega_{c,\bar{p}}}{\omega_{c,p}} = \frac{q_{\bar{p}}/m_{\bar{p}}}{q_p/m_p} \text{ Charge to mass comparison}$$

$$\frac{\omega_{c,\bar{p}}}{\omega_{c,p}} \text{ (Year)} \text{ Gravity, clock comparison}$$

$$\frac{\omega_L}{\omega_c} = \frac{g}{2} = \frac{\mu}{\mu_N}$$

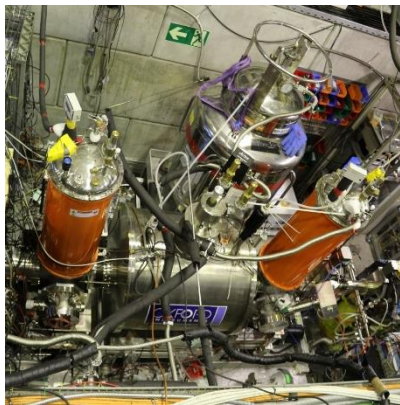
Magnetic moment

$t_{\bar{p}}$

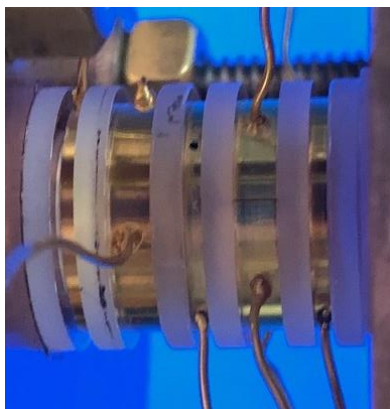
Lifetime

# Frequency measurements in a Penning trap

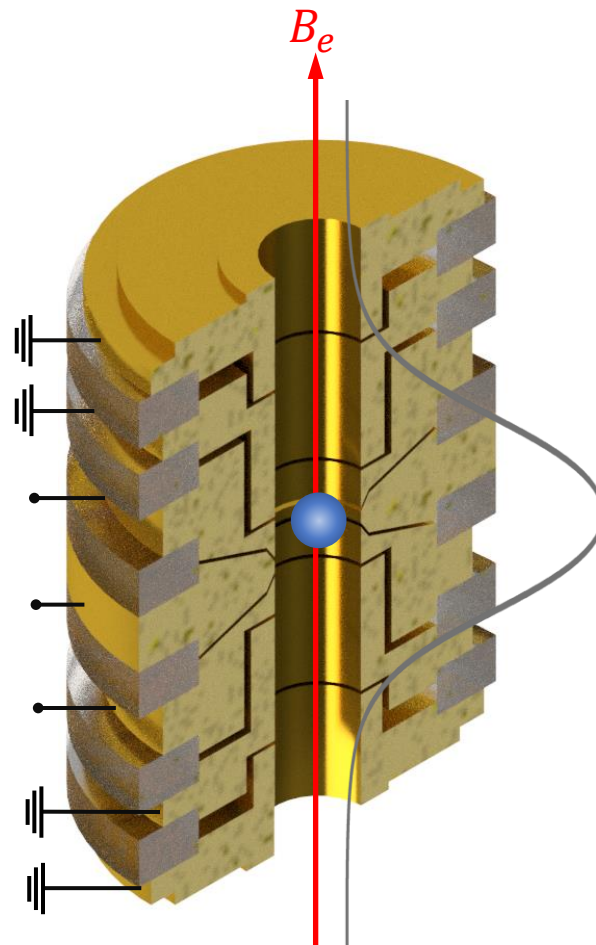
1.95 T B field from solenoid



Voltages applied to ring-shaped electrodes

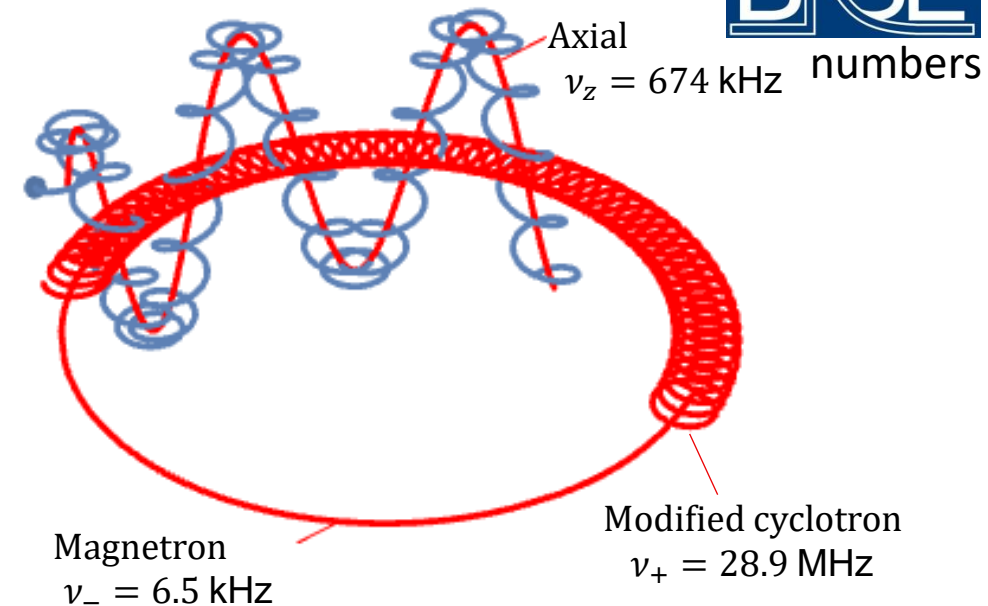


A Penning trap



$$\Phi(0, z)$$

$$\Phi(\rho, z) = V_0 C_2 \left( z^2 - \frac{\rho^2}{2} \right)$$



$$\sqrt{\nu_z^2 + \nu_+^2 + \nu_-^2} = \nu_c = \frac{q}{2\pi m} B_e$$

Orbit is sum of three normal modes

Measure frequencies and get access to charge-to-mass ratio and magnetic field

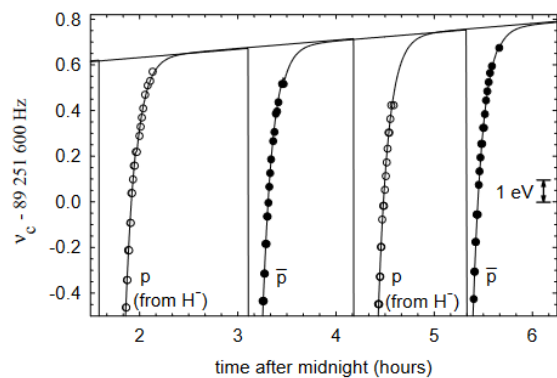
# Charge-to-mass ratio comparisons

$$R = \frac{v_{c,\bar{p}}}{v_{c,H^-}} = \frac{(q/m)_{\bar{p}}}{(q/m)_{H^-}} \times \frac{B/2\pi}{B/2\pi} = \frac{(q/m)_{\bar{p}}}{(q/m)_{H^-}}$$

$$m_{H^-} = m_p \left( 1 + 2 \frac{m_e}{m_p} - \frac{E_b}{m_p} - \frac{E_a}{m_p} + \frac{\alpha_{\text{pol},H^-} B_0^2}{m_p} \right)$$

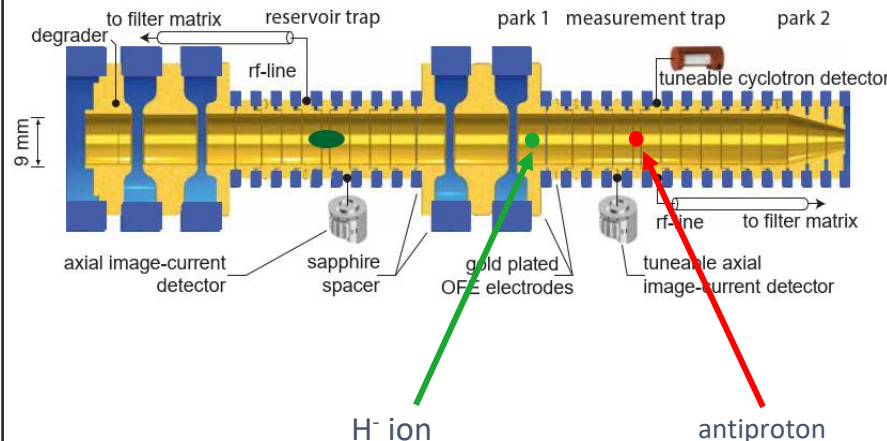
$$R_{\text{theo}} = 1.001\,089\,218\,754\,2(2)$$

Multiyear campaign performed by G. Gabrielse and collaborators at CERN's LEAR Decelerator 1990's



Single trap, 2 hrs to exchange particles, 90 ppt reached

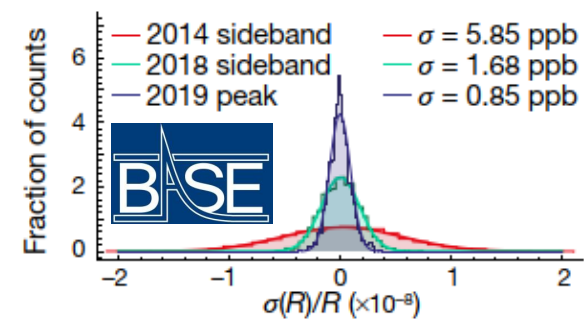
2 measurements by BASE at CERN's AD



Multi trap, 2 minutes to exchange particles,

$$\frac{(q/m)_{\bar{p}}}{(q/m)_p} = 1.0000000000003(16)$$

16 ppt reached

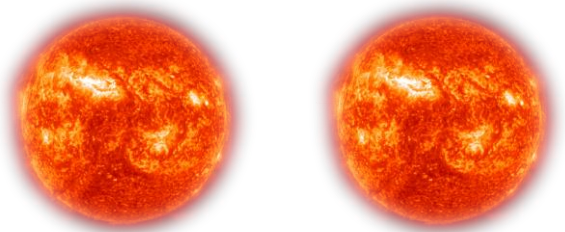
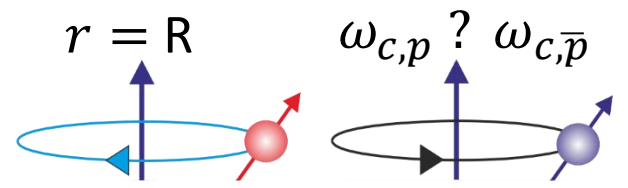
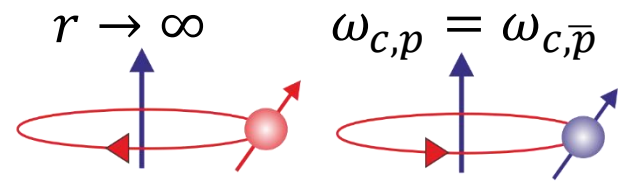
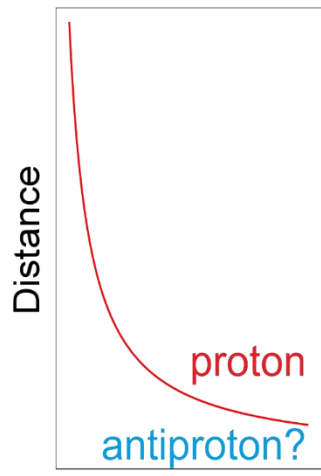


# Gravity

Clock comparison between matter and antimatter clocks in a gravitational potential

Relies on assumptions about CPT

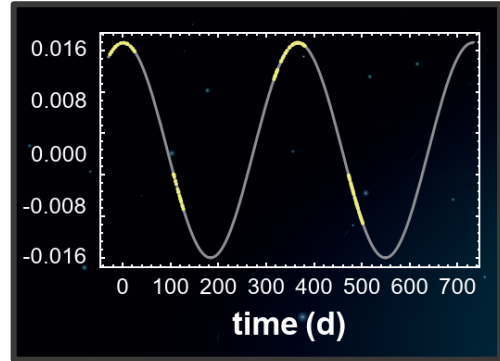
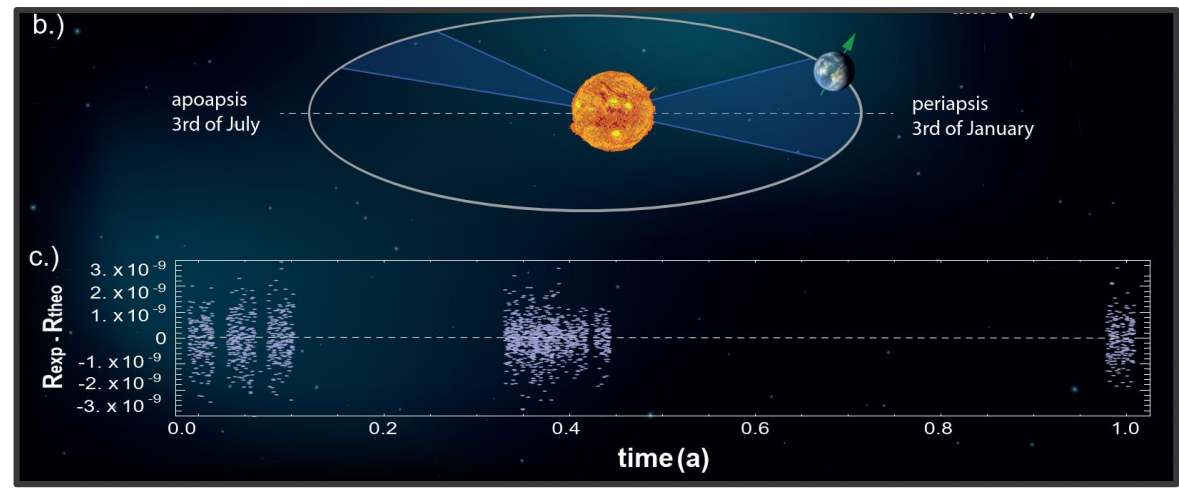
Gravitation Potential



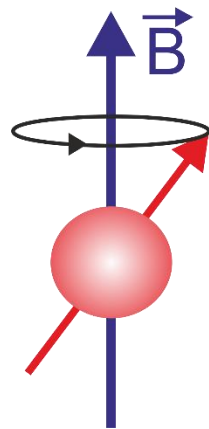
Variation in distance modulates effect

$$\frac{\Delta R(t)}{R_{avg}} = \frac{3GM_{sun}}{c^2} (\alpha_{g,D} - 1) \left( \frac{1}{O(t)} - \frac{1}{O(t_0)} \right)$$

Property	Limit
$\alpha_g - 1$	$< 1.8 * 10^{-7}$
$\alpha_{g,D} - 1$	$< 0.03$



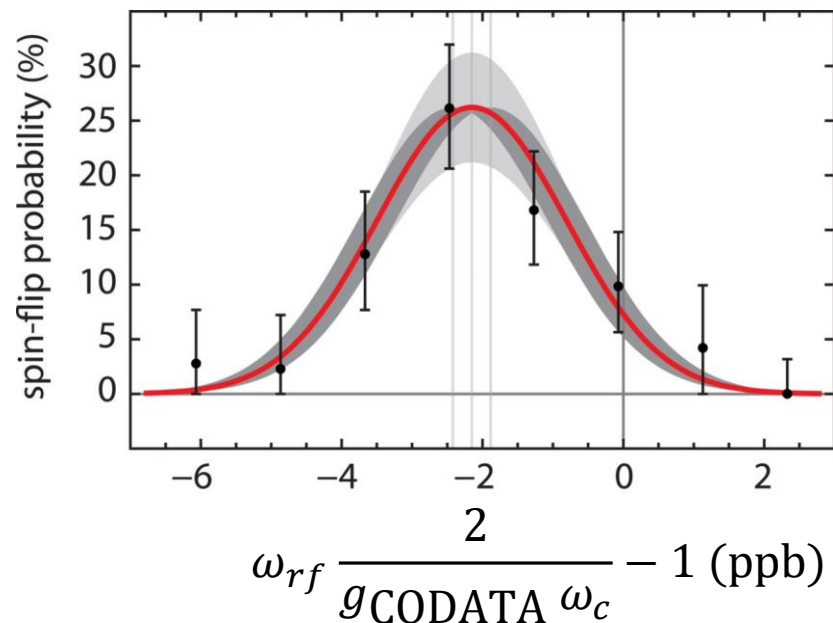
# Measuring the magnetic moment



$$\omega_L = g \frac{e}{2m_p} B$$

$$\frac{g}{2} = \frac{\mu}{\mu_N} = \frac{\omega_L}{\omega_c}$$

How to measure the Larmor frequency  $\omega_L$ ?



Weak radiofrequency magnetic field most likely to flip antiproton spin at  $\omega_L$

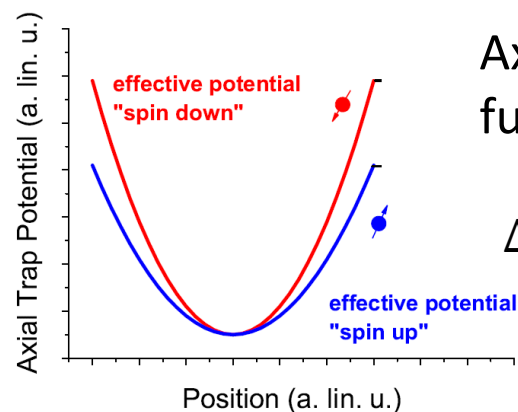
How to measure spin?

Continuous Stern-Gerlach effect

$$H_M = -(\vec{\mu}_p \cdot \vec{B})$$

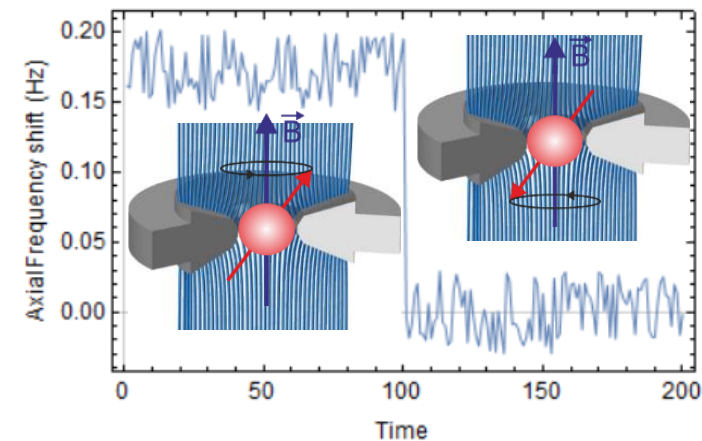
Energy of magnetic dipole in magnetic field

$$B_z = B_0 + B_2 \left( z^2 - \frac{\rho^2}{2} \right)$$



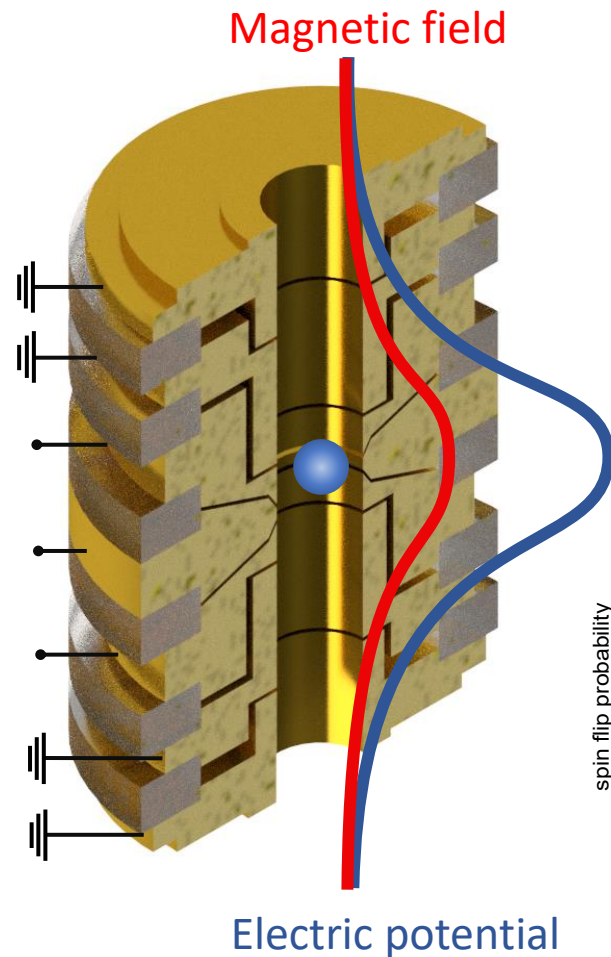
Axial frequency becomes function of spin state

$$\Delta v_z \sim \frac{\mu_p B_2}{m_p v_z} := \alpha_p \frac{B_2}{v_z}$$



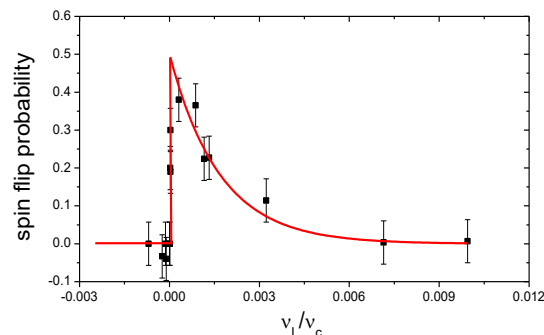
# Method

## Single trap method



Measure  $\omega_L$  and  $\omega_C$  and spin states in the same trap

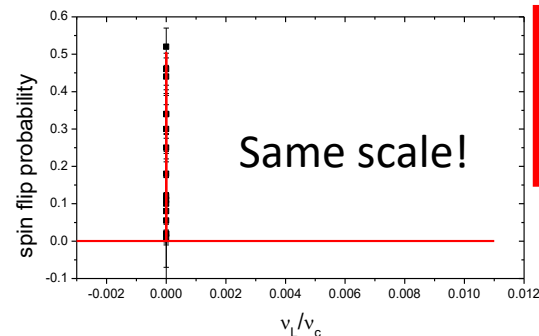
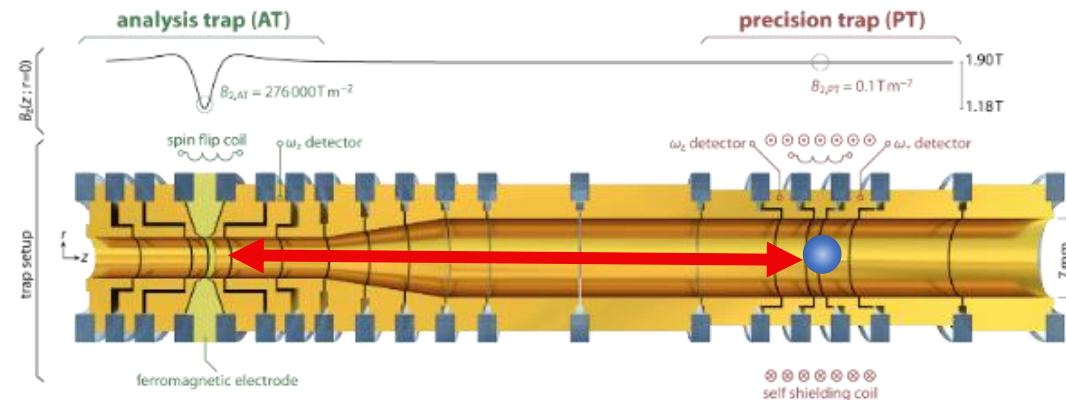
Works well for electrons, but large quadratic B field adds temperature broadening, limits measurements



Proton: 2.5 ppm  
Antiproton: 0.8 ppm  
Electron: 0.28 ppt  
Positron: 4.3 ppt

## Double trap method

Separate spin state identification from measuring  $\omega_L$  and  $\omega_C$



Same scale!

Proton: 0.3 ppb  
Antiproton: 1.2 ppb

H Häffner et al., *The European Physical Journal D* **22** 2 (2003)  
DiSciacca, J. & Gabrielse, G. *Phys. Rev. Lett.* **108**, 153001 (2012)  
H. Nagahama et al. *Nature Communications* **8** (2017)  
Hanneke et al., *Phys. Rev. Lett.* **100** (2008)  
Van Dyck, R.S., Jr.; Schwinberg, P.B.; Dehmelt, H.G. *Phys. Rev. Lett.* **59** (1987)



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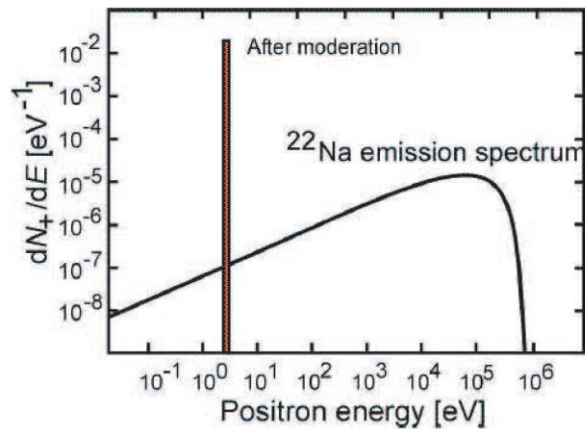
# Spectroscopy of anti-atoms

# What about the positrons?

Need positrons to make antihydrogen

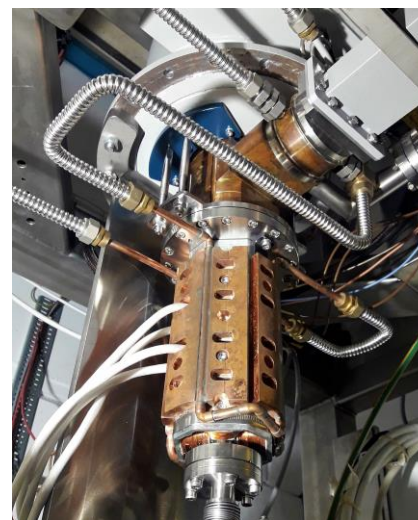


Radioactive source and moderation with frozen noble gas



(CERN/ALPHA)

~ 5 million slow  
e+ per second



(CERN/GBAR/Comini)

~ 40 million slow e+  
per second

e- accelerated 10 MeV  
onto a water-cooled  
tungsten target to form  
positrons by pair  
production, moderated  
by tungsten mesh

# Producing antihydrogen

- 1) Recombination  $\bar{p} + e^+ \rightarrow \bar{H} + \text{UV photon}$
- 2) Three body recombination  $\bar{p} + e^+ + e^+ \rightarrow \bar{H} + e^+$

rate 2)  $\gg$  rate 1) typically



ATRAP

ALPHA:  $2.6 \pm 0.2$  detected  $\bar{H}$   
trapped per minute



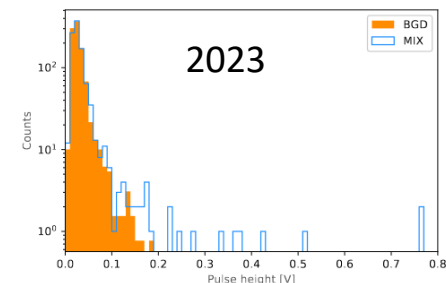
ASACUSA

- 3) Charge transfer  $\bar{p} + \text{positronium} \rightarrow \bar{H} + e^-$



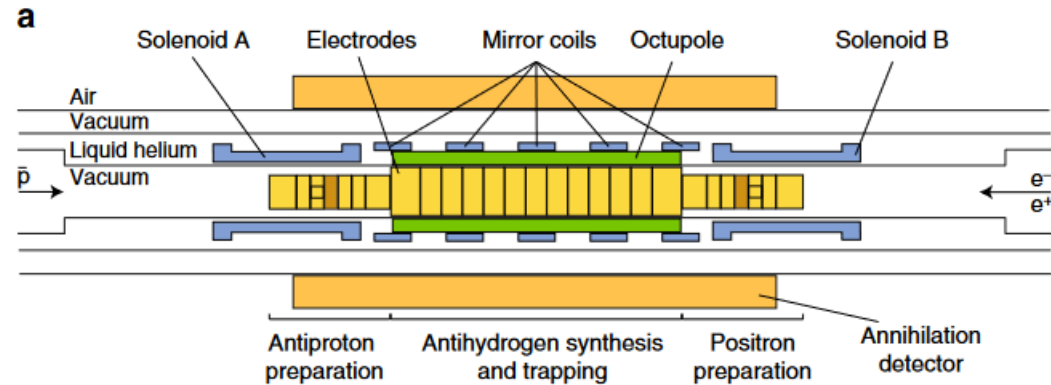
AEGIS:  $0.021(5)$   $\bar{H}$  per attempt,  
 $\sim 15$  minutes per attempt

M. Ahmadi, Nature Communications **8** (2017)  
C. Amsler et al., Nature Communications Physics **4** (2021)  
F Robicheaux J. Phys. B: At. Mol. Opt. Phys. **41** (2008)  
[arXiv:2306.15801](https://arxiv.org/abs/2306.15801) [hep-ex] (2023)

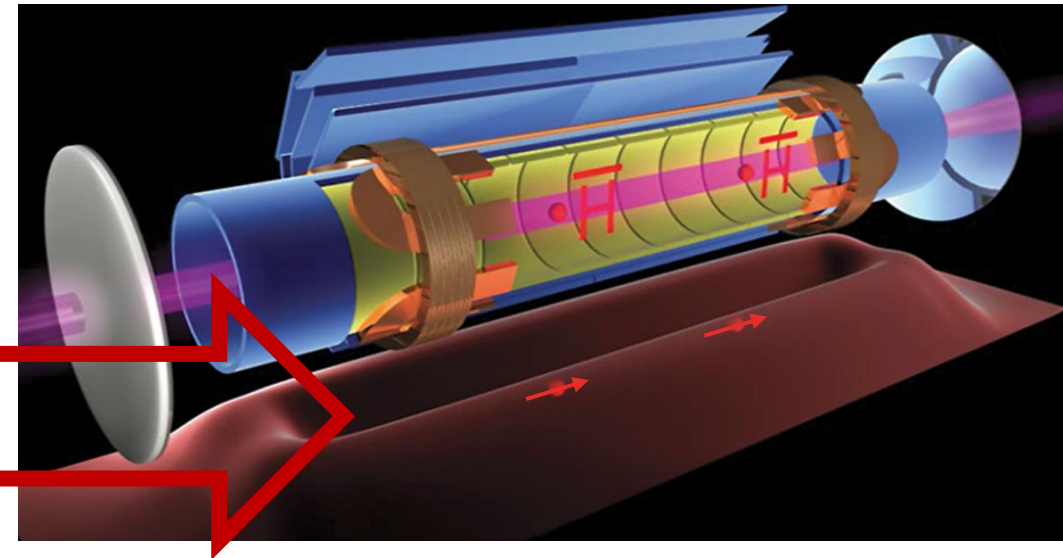
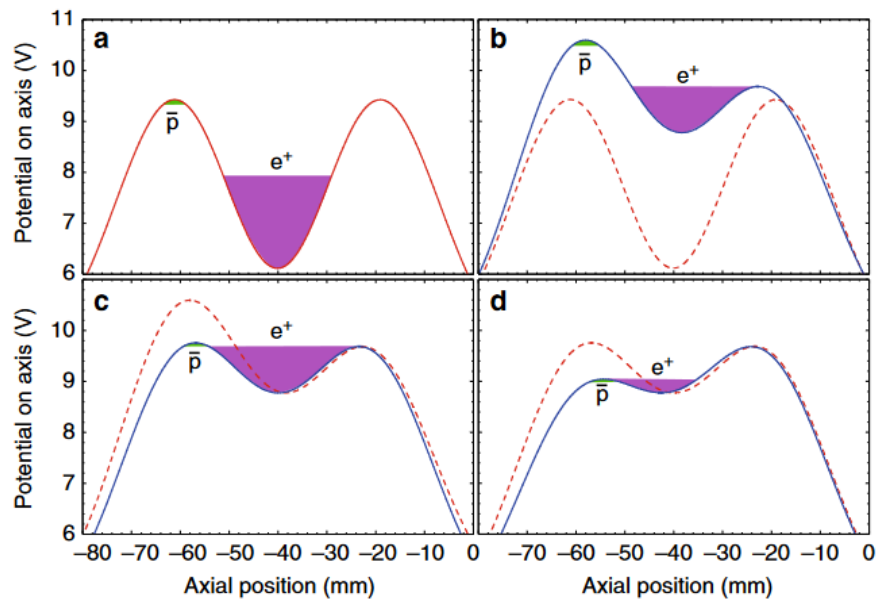


GBAR:  $0.0089$   $\bar{H}$  per  
antiproton pulse  
 $\sim 112$  s per pulse

# Antihydrogen production in ALPHA

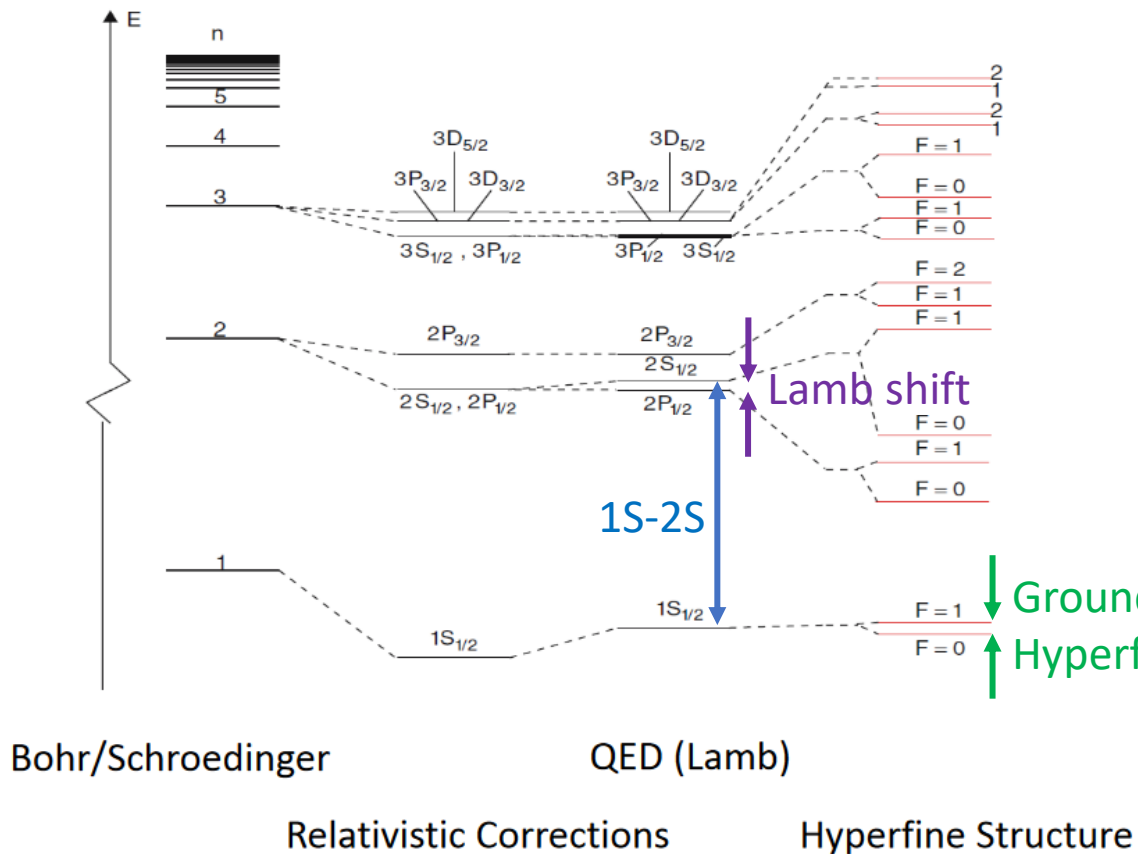


Careful control of antiproton and positron temperatures and densities



Antihydrogen magnetically trapped

# (anti)hydrogen



**Bohr / Schroedinger: L degeneracy**

$$E_n = -\frac{mZ^2e_0^4}{2\hbar^2n^2} = -\frac{(Ze_0)^2}{2an^2} = -\frac{mc^2}{2}\alpha^2\frac{Z^2}{n^2}$$

**Dirac: J degeneracy**

$$\langle H_1 + H_2 \rangle_{n,j=l\pm 1/2,l} = \frac{mc^2(Z\alpha)^2}{2n^2} \frac{(Z\alpha)^2}{n^2} \left\{ \frac{3}{4} - \frac{n}{j+1/2} \right\}$$

**QED: Lamb Shift**

$$\Delta E_{\text{Lamb}} \approx \frac{4}{3\pi} \frac{mc^2 Z^4 \alpha^5}{n^3} \log \frac{1}{\alpha Z} \delta_{l,0}$$

↓ Ground State

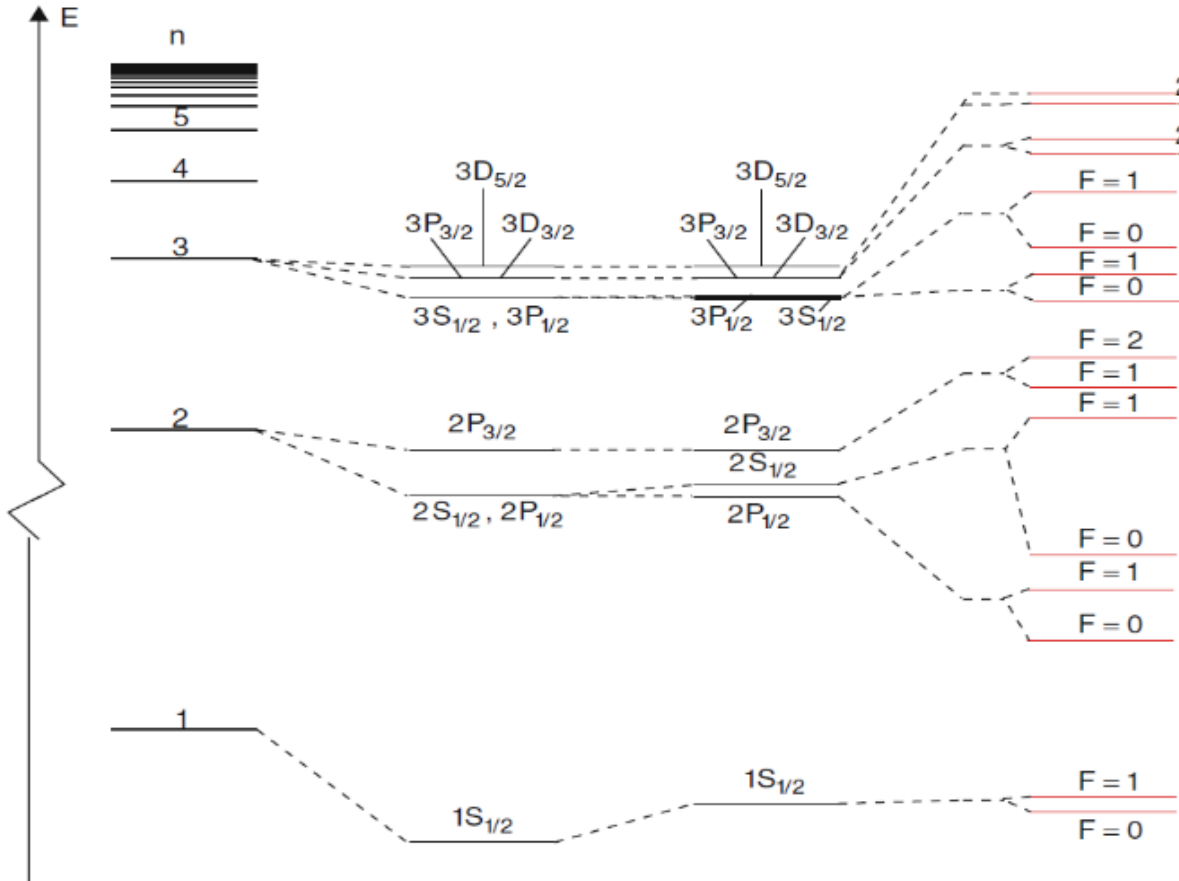
↑ Hyperfine Splitting

**Hyperfine Structure:**

$$\Delta E_{n,1/2,0}^{\text{Hyp}} = \frac{4}{3} g_K \frac{m}{M_K} (Z\alpha)^4 \frac{mc^2}{n^3} \frac{(2I+1)}{2}$$

Analytically calculable energy levels, high precision hydrogen measurements (4.5 ppt for 1S-2S) to compare to antihydrogen

# Think like a precision measurer



What properties do we want in a transition?

- 
- 
- 

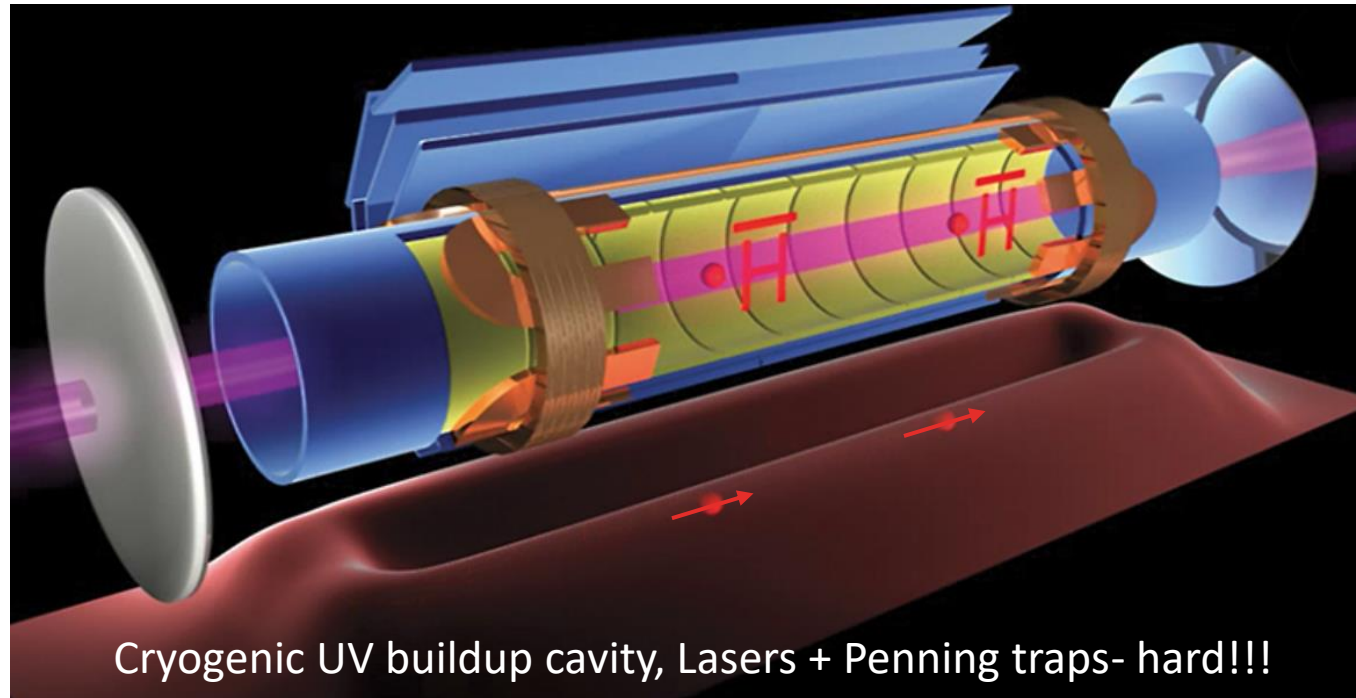
What do we want to control about the atom?

- 
- 
- 

What do we want to control about the environment?

- 
- 
-

# Laser spectroscopy of Antihydrogen 1S-2S



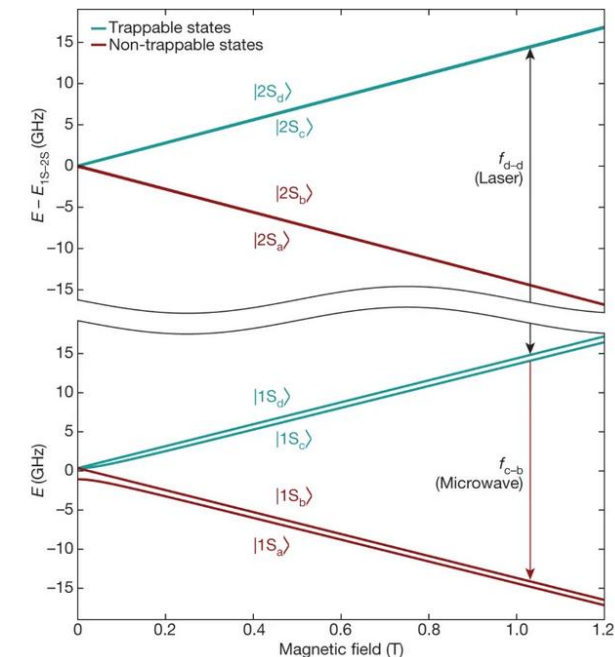
ALPHA collaboration

60 hr antihydrogen storage

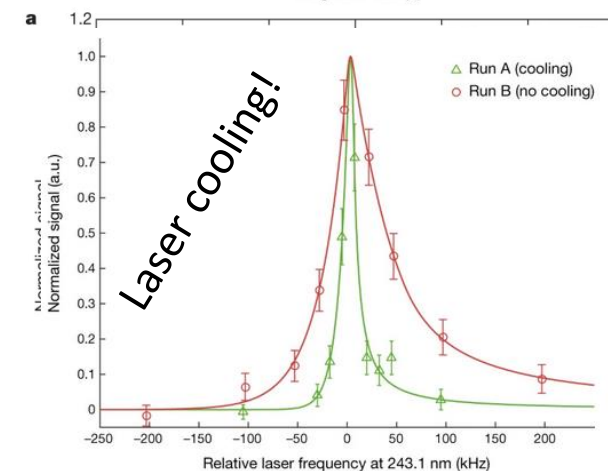
$f_{d-d} = 2,466,061,103,079.4(5.4)$  kHz (measured)

$f_{d-d} = 2,466,061,103,080.3(0.6)$  kHz (predicted)

2 ppt

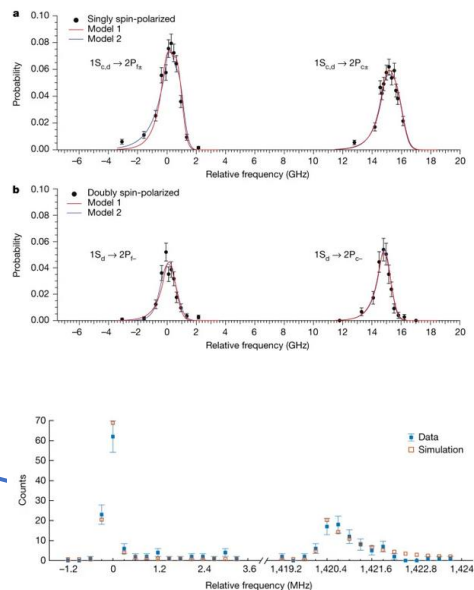
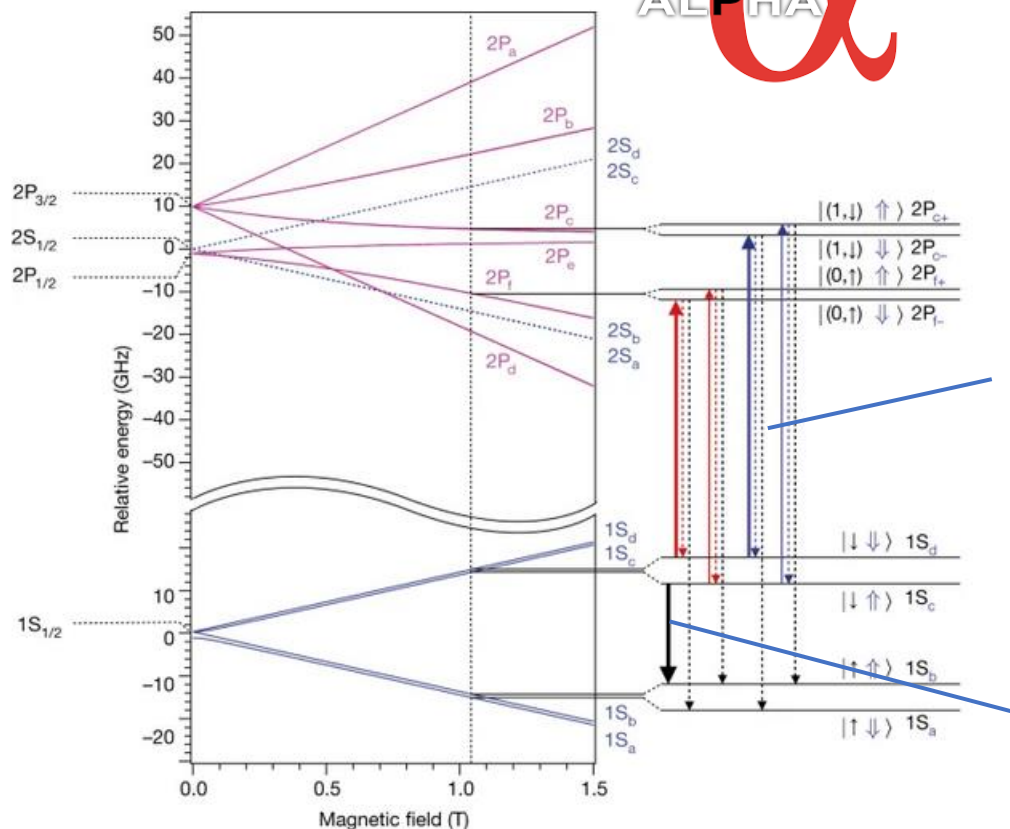


2 photons  
at 243 nm  
cancels  
Doppler  
shift

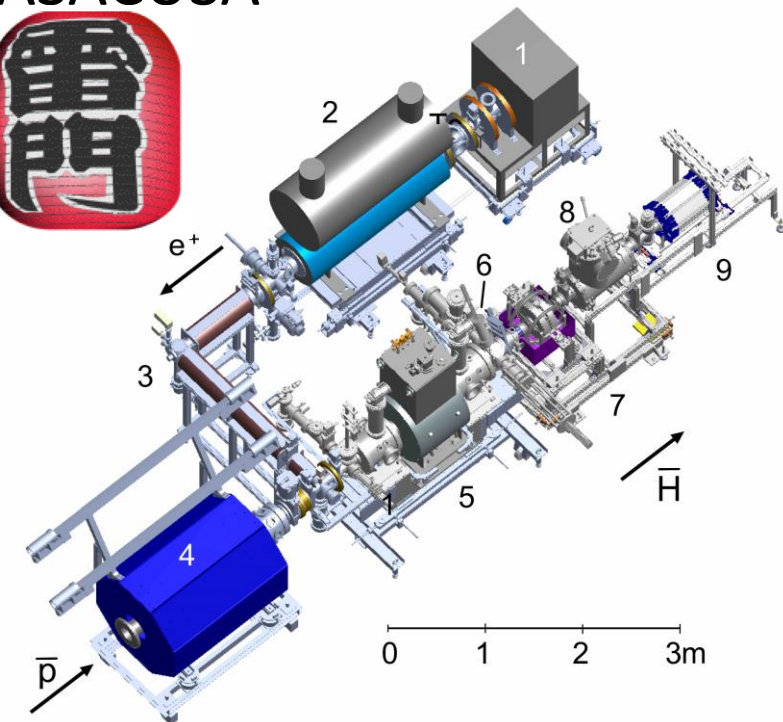


# RF spectroscopy hyperfine splitting

## ALPHA



## ASACUSA



$$\Delta\nu = 1420405748.4(3.4)(1.6) \text{ Hz}$$

- 2.7 ppb in Hydrogen

Lamb shift  $2S_{1/2} - 2P_{1/2}$   $\bar{H}$   $0.99 \pm 0.11$  GHz,  $H$   $0.9098717(32)$  GHz  
 Ground state splitting:  $\bar{H}$   $1,420.4 \pm 0.5$  MHz,  $H$   $1\,420\,405.751\,766\,7(9)$

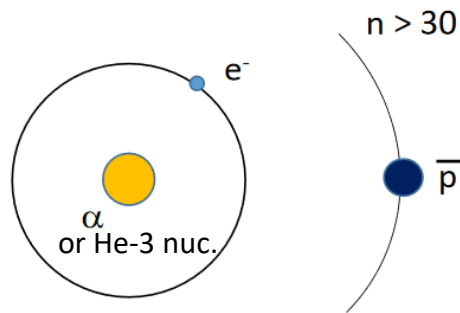
M. Ahmadi, Nature **548**, 66-69 (2017)  
 M. Ahmadi, Nature **578**, 375-380 (2020)  
 ASACUSA Collaboration. Report No. SPSC-P-307 Add. 1 CERN-SPSC-2005-002 (2005)  
 N. Ramsey, Hyp. Interactions **81** (1993)



# Antiprotonic helium



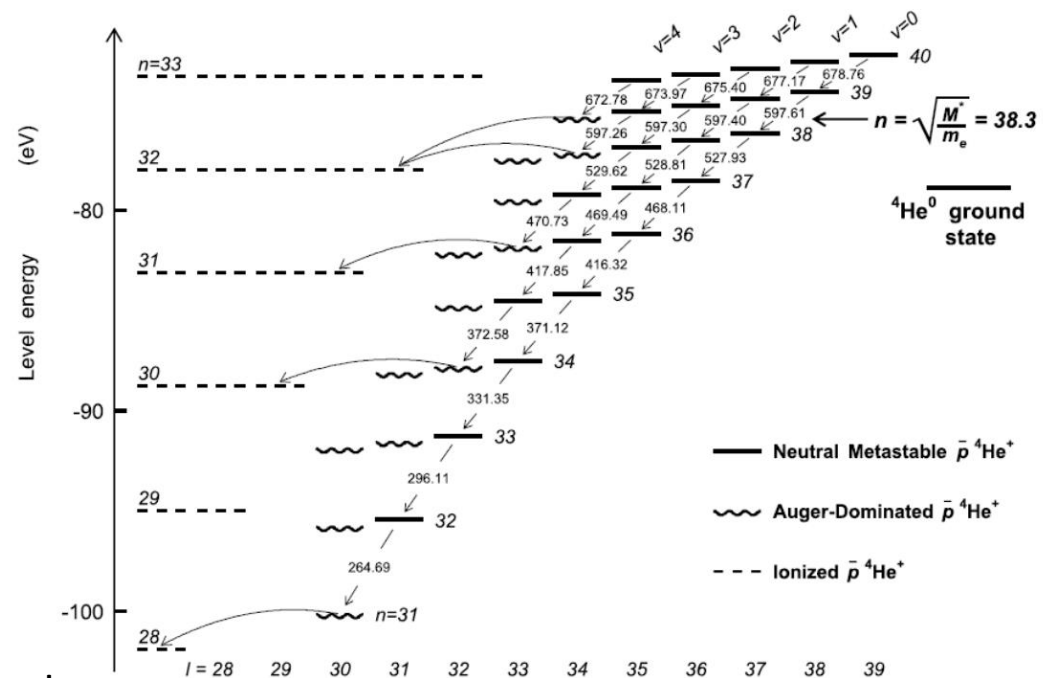
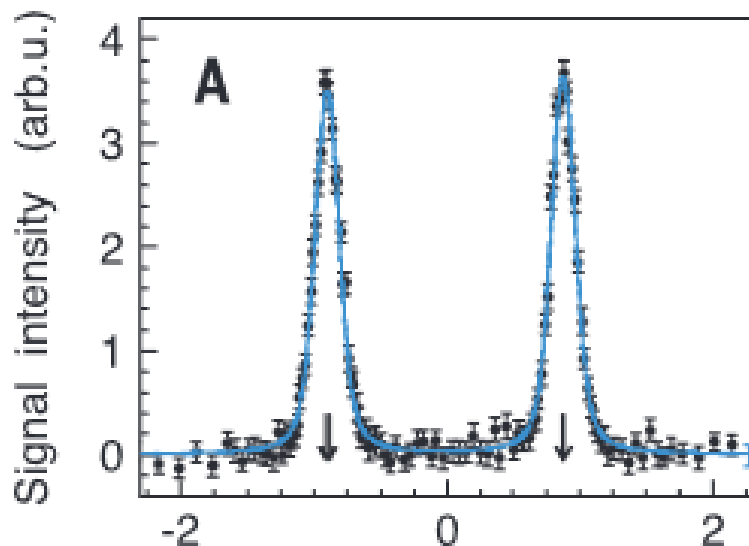
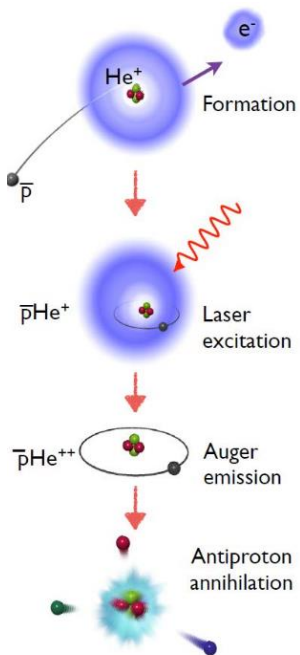
Antiprotonic Helium



$$E_n = -hcR \frac{Z^2}{n^2} \quad R = R_\infty \frac{m_{\bar{p}}}{m_e} \frac{1}{\left(\frac{m_{\bar{p}}}{m_e} + 1\right)}$$

Measure energy levels, determine  $\frac{m_{\bar{p}}}{m_e}$

Ground state lifetime: 100 ns  
Lifetime  $n \sim 38 \sim 1-2$  us or  $\sim$ ns

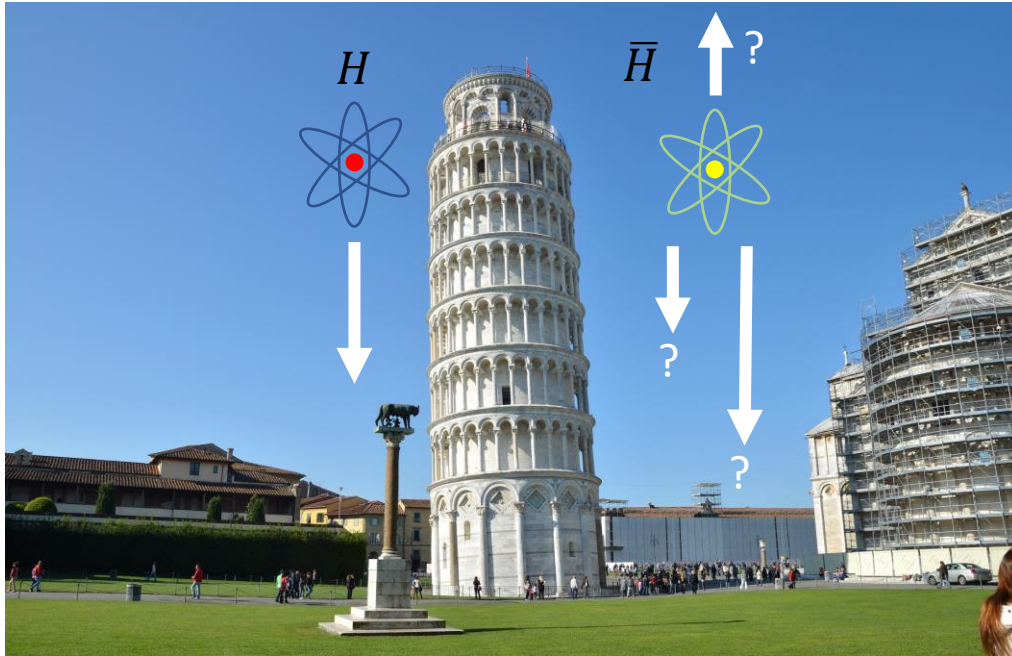


Laser resonance leads to electron ejection and rapid  $\bar{p}He^{2+}$  decay emitting pions, detected via Cherenkov detectors

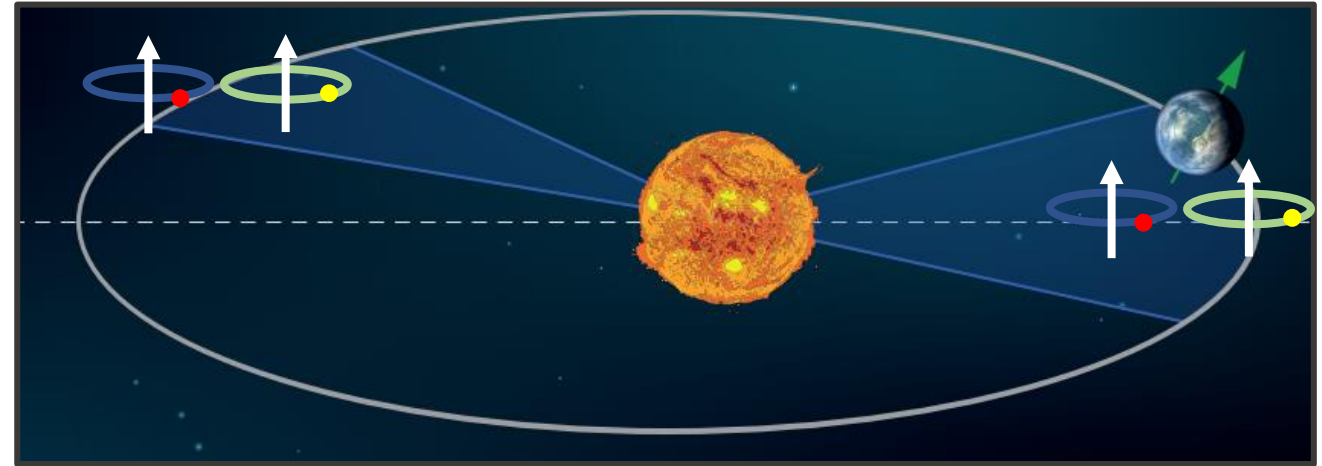
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# Effect of gravity on antihydrogen

# Types of measurement



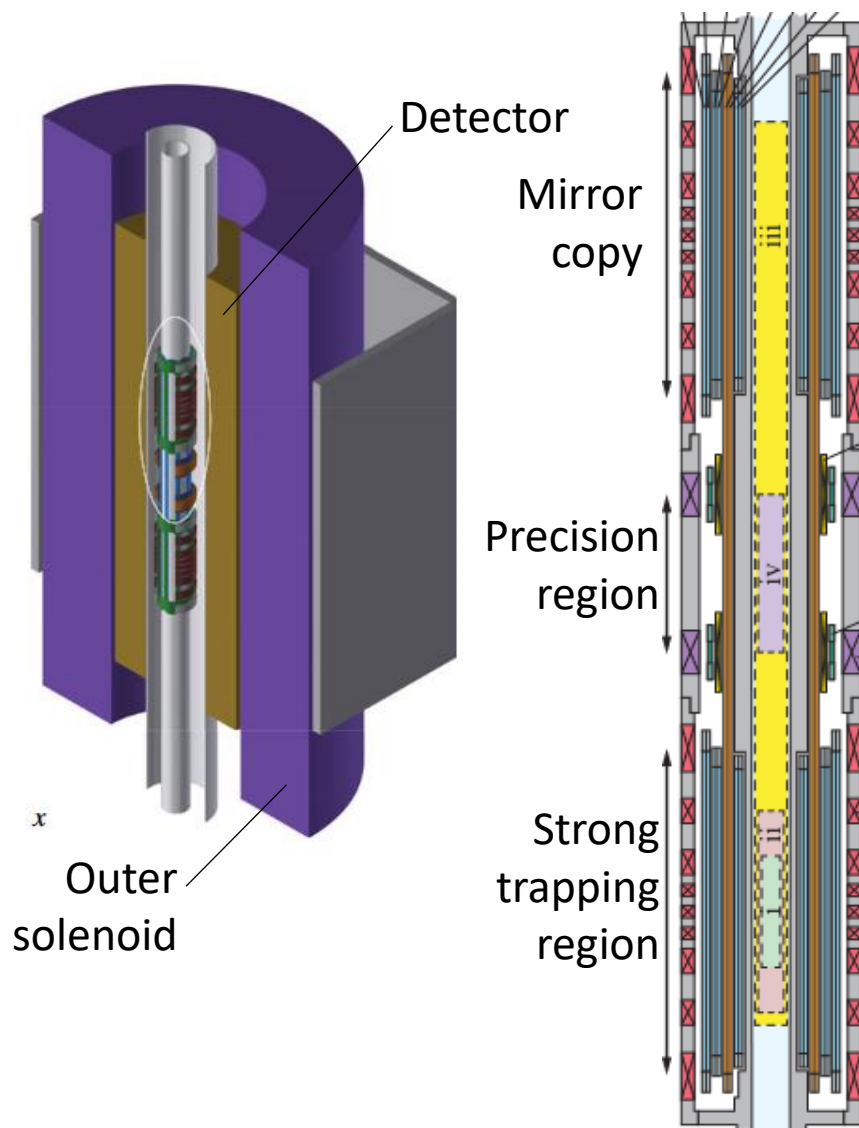
Freefall



Clock comparison

High precision needed- If proton is any guide, antiquark masses only  $\sim 1\%$  of the antiproton

# ALPHA-g

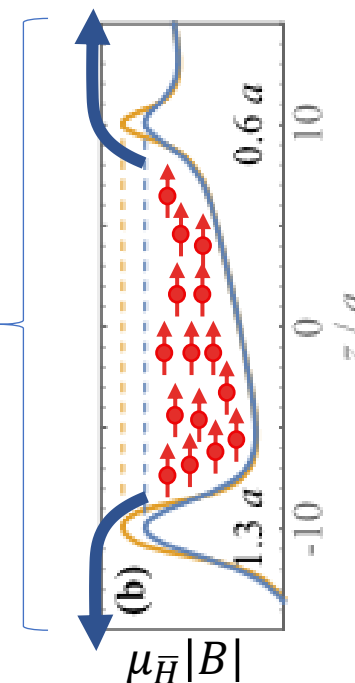


Mirror copy of lower region to keep fields symmetric

Region optimized for gravity measurement

Region optimized for  $\bar{H}$

$$V = \mu_{\bar{H}}|B| - m_{\bar{H}}gh$$



Slowly ramp magnetic fields until equal numbers escape up and down, Infer  $m_{\bar{H}}$

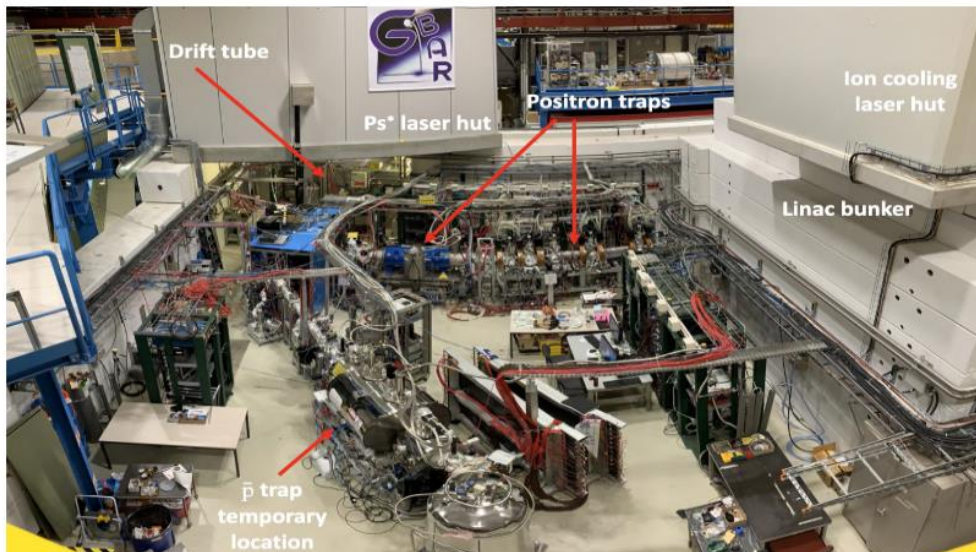
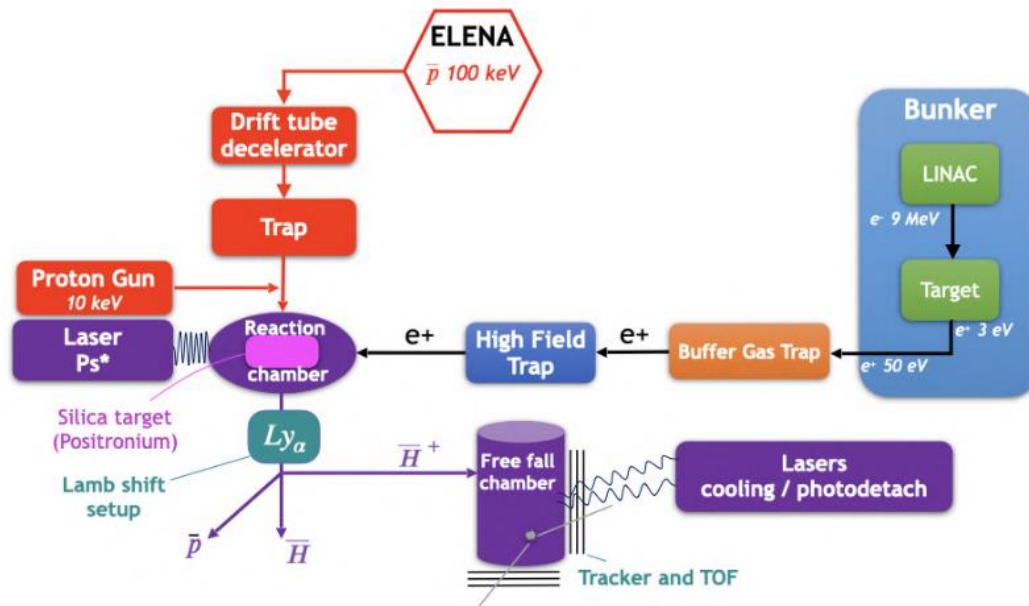
Colder the better!  
Initially <0.54 mK  
With laser cooling  
Initially <0.05 mK

Target 5-1% measurement on  $m_{\bar{H}}$

W. A. Bertsche, Phil. Trans. R. Soc. A **376** (2018)

C. So et al., IEEE Trans. Appl. Super. **30** 4 (2020)

# GBAR



1. Make  $\bar{H}^+$  by reacting  $\bar{H} + e^+$
2. Sympathetically laser cool  $\bar{H}^+$  with  $\text{Be}^+$  to  $20 \mu\text{K}$
3. Photoionise  $\bar{H}^+$  to  $\bar{H}$
4. Drop and measure effect of gravity

Initial goal 1%, final goal 0.1% with quantum measurement

Also, long term possibility to produce  $\bar{H}_2^+$  molecules and do antimolecular spectroscopy!

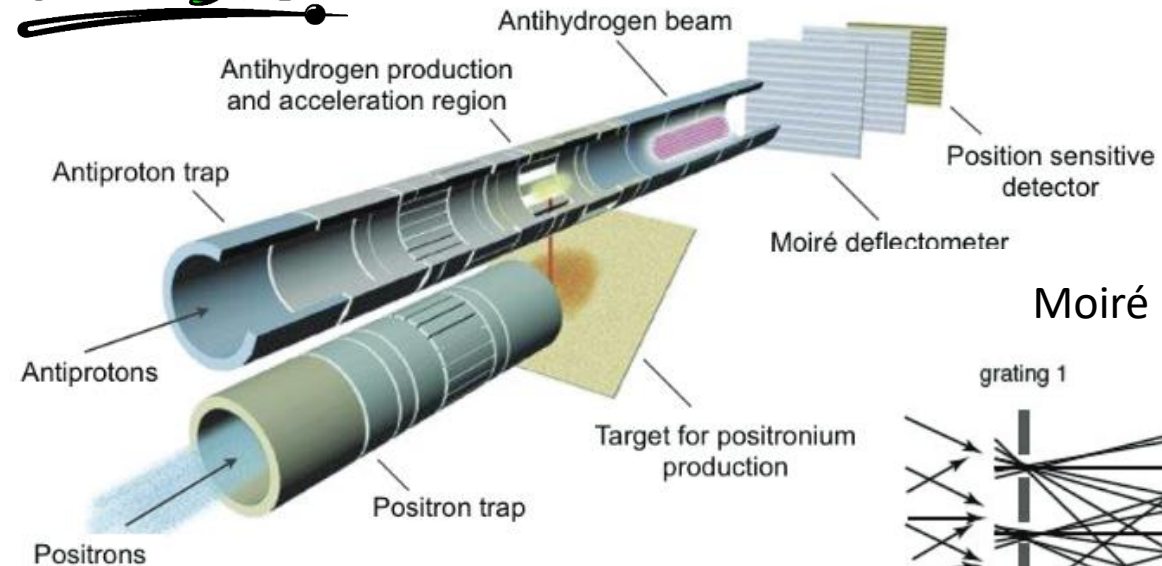


D. P. van der Werf, Antimatter and Gravity (WAG 2013) **30** (2014)  
 GBAR status report CERN-SPSC-2022-003 / SPSC-SR-302 (2022)  
[arXiv:2306.15801](https://arxiv.org/abs/2306.15801) [hep-ex]

# AEgIS

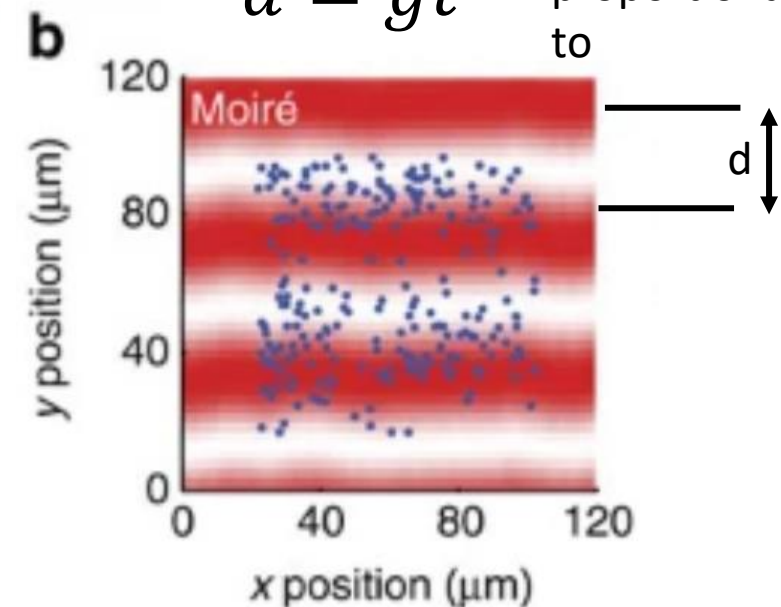
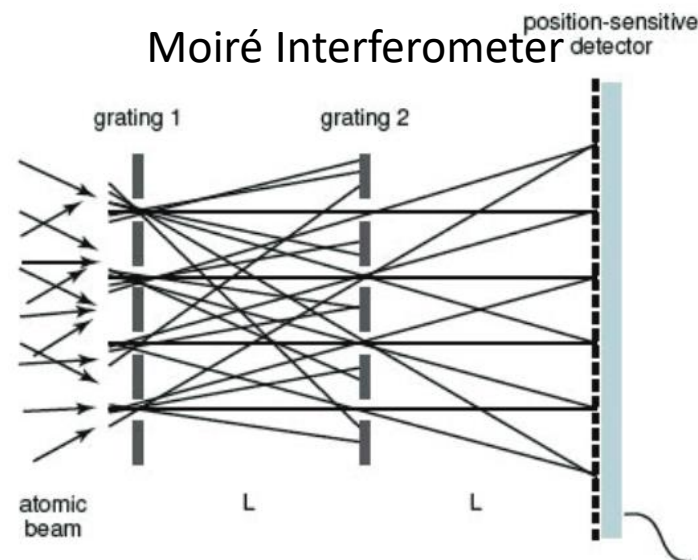
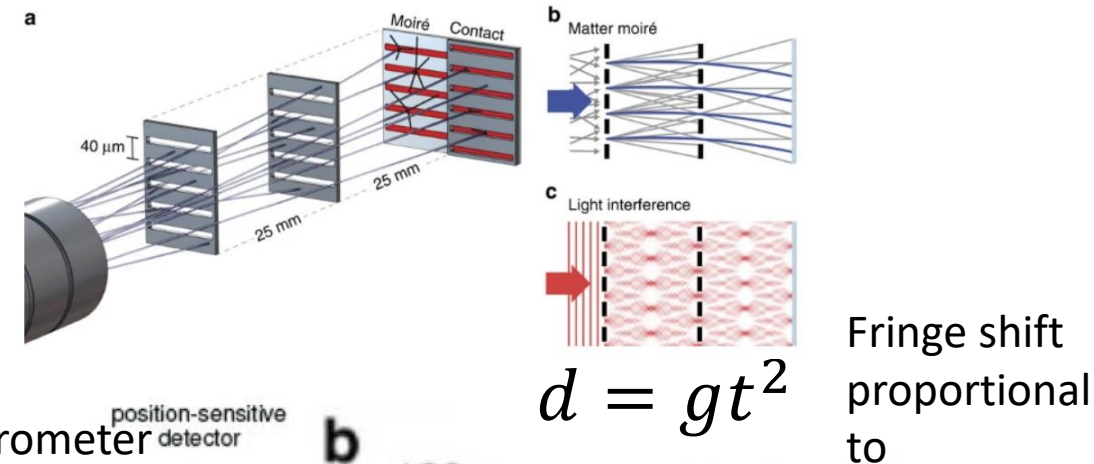
Use beam of  $\bar{H}$  for gravity measurement

**AEgIS**



First used to measure force on antiprotons  
 $530 \pm 50$  aN (stat.)  $\pm 350$  aN (syst.) in 2014  
 Next antihydrogen

100 mK required, 1% accuracy sought



S. Aghion et al., *Nature Communications* **5** 4538 (2014)  
 P. Scampoli et al., *Modern Physics Letters A* **29** 17 (2014)  
 A. Kellerbauer et al., *NIM B* **226** **3** (2008)

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Taking antimatter out of the lab

# PUMA

Take  $10^9$  antiprotons from the antimatter factory to ISOLDE

Some nuclei at the limits of  $N > Z$  have a neutron halo where one or more neutrons are found far outside the nucleus.

Others have neutron skins, where the density of neutrons is larger than protons at the nuclear surface – antiproton annihilation study these effects

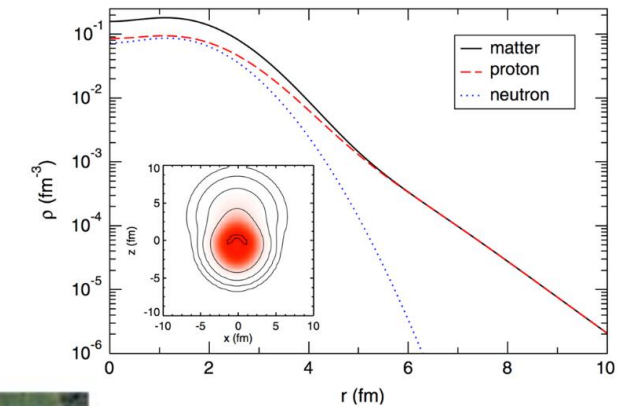
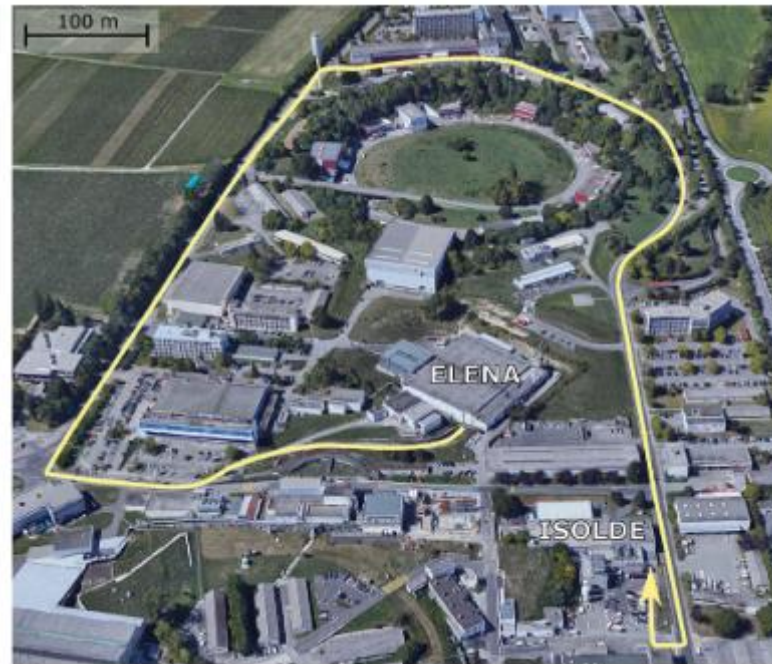
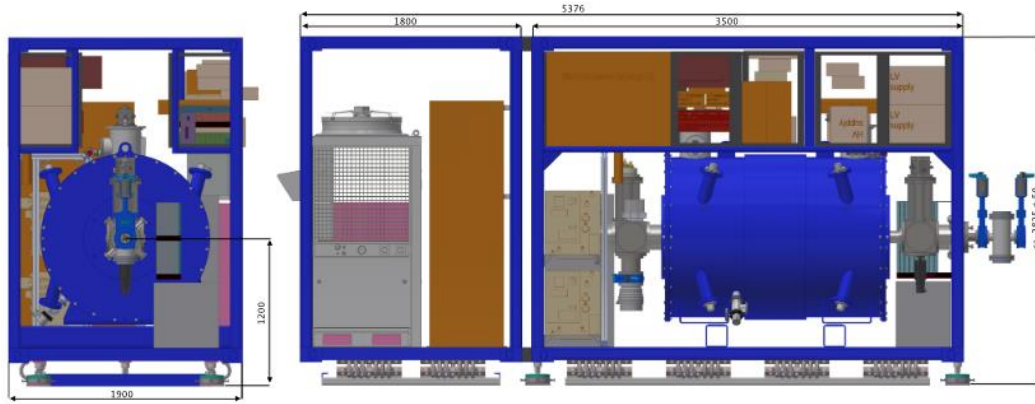
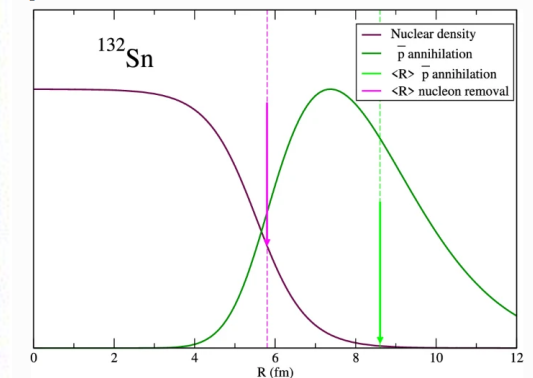


Fig. 6



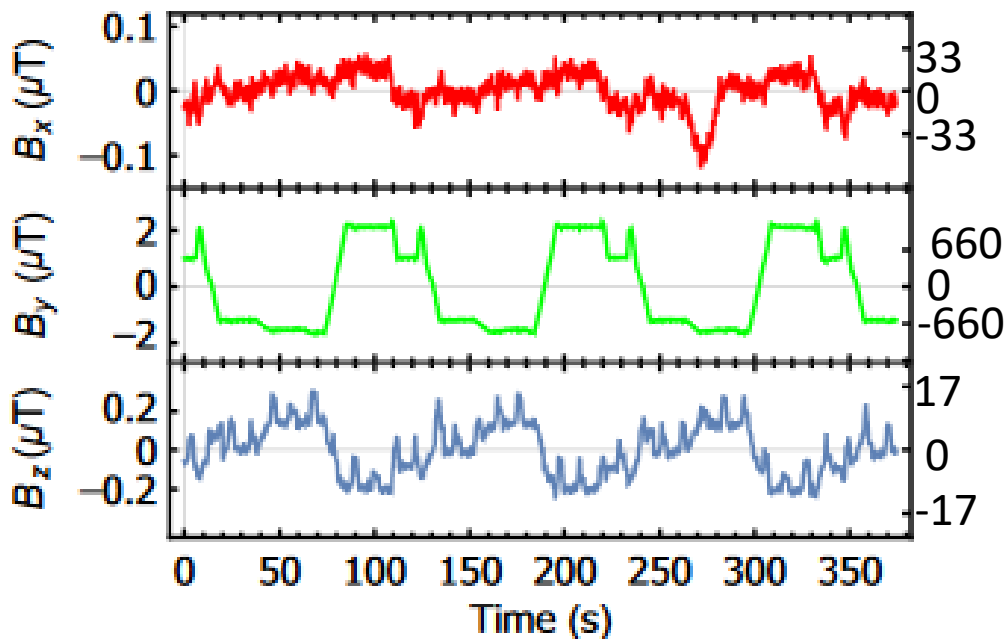


# BASE-STEP

BASE trying to measure frequencies to parts-per-trillion level



Take the antimatter somewhere quiet



Magnetic field fluctuating in the background up to one million times more strongly

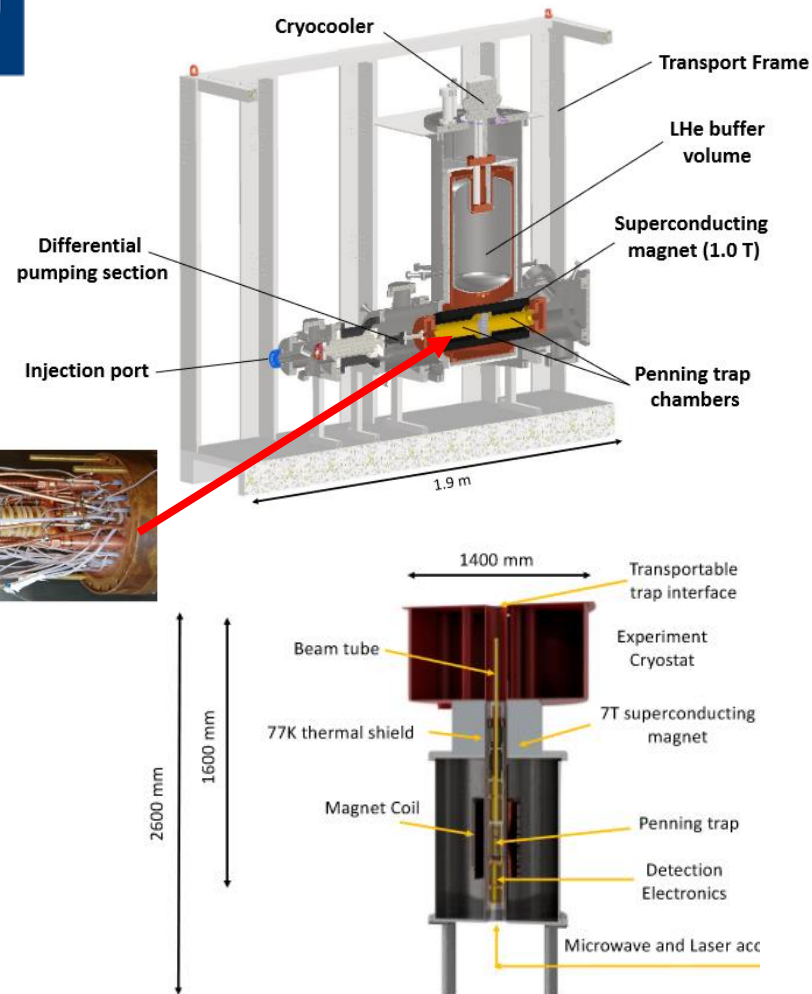
Hard to push the limits in this environment



Fractional magnetic field fluctuations (ppb)



Inject into a separate magnet in a quiet lab



# Should we be worried?

**EXPRESS** 

**Antimatter bombs: Could antimatter weaponry wipe out all life on Earth? Expert weighs in**

Wed 21 Jul 2021

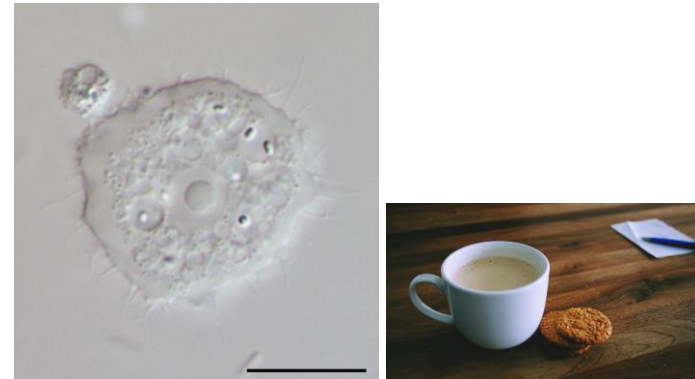
# NO!

Professor Robson said: "The idea you can produce masses of antimatter and make a bomb from it or something is not realistic. It's not something anyone needs to worry about."

One billion antiprotons annihilating

$$E = mc^2 = (2 \times 1 \times 10^9 \times 1.6 \times 10^{-27})c^2 = 1 \text{ nJ}$$

1nJ can heat 3 picogram of water from 20-→100 °C



About enough to make an espresso for an amoeba

(2015). "An update on *Acanthamoeba* keratitis: diagnosis, pathogenesis and treatment". *Parasite* **22**: 10.

# Thank you

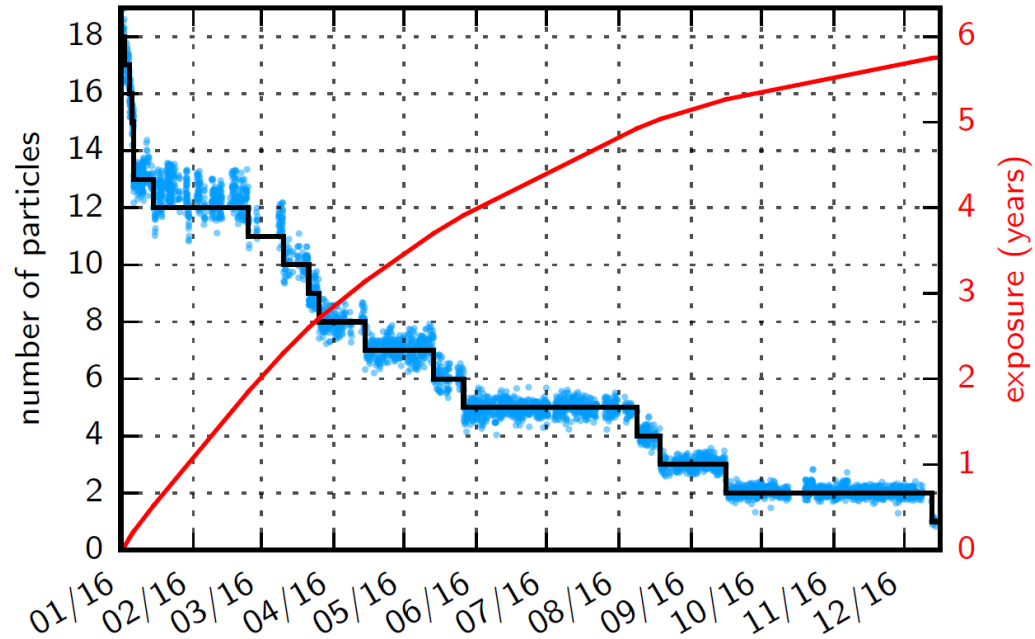
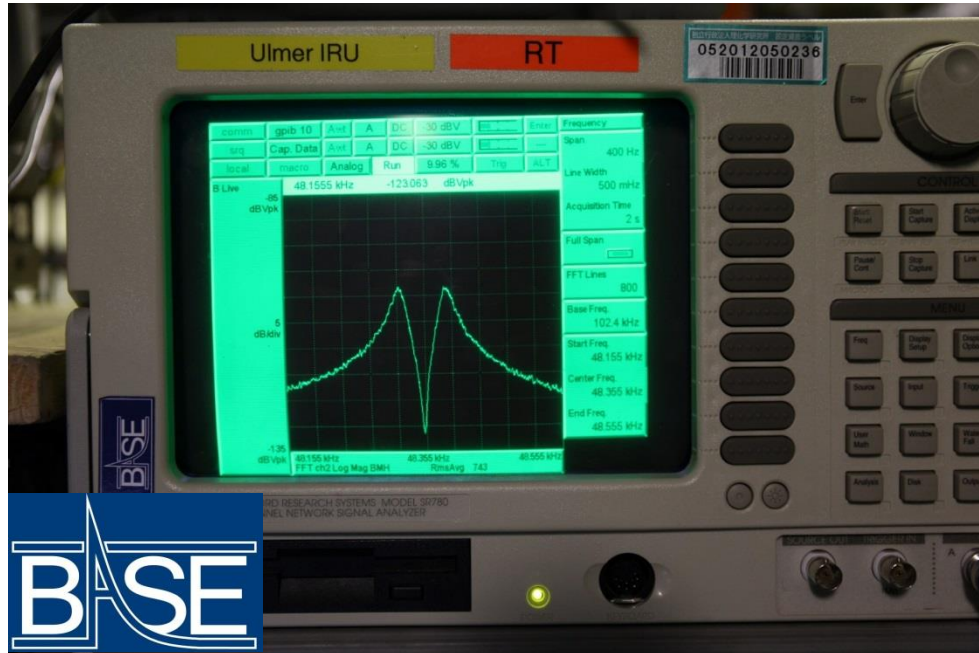
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Thanks to Stefan Ulmer, Christian Smorra & Andi Mooser for providing slides and materials for these lectures

And thank you for listening

# Storing antiprotons

BASE holds record for antiprotons stored from 03.11.2015 – 22.12.2016



- Storage of antiprotons for more than one year: **405.5 days**
- Extraction of single particles by a potential tweezer scheme

Inversion of the baryon asymmetry:

Antibaryon density:  $\sim 10^8/\text{cm}^3$   $V < (50 \mu\text{m})^3$

Baryon density:  $\sim 1 / \text{cm}^3$   $p < 10^{-16}$  Pa