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Crystal Chemistry and Structural Complexity of the Uranyl Carbonate Minerals and Synthetic Compounds

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Abstract: Uranyl carbonates are one of the largest groups of secondary uranium(VI)-bearing natural phases being represented by 40 minerals approved by the International Mineralogical Association, overtaken only by uranyl phosphates and uranyl sulfates. Uranyl carbonate phases form during the direct alteration of primary U ores on contact with groundwaters enriched by CO₂, thus playing an important role in the release of U to the environment. The presence of uranyl carbonate phases has also been detected on the surface of "lavas" that were formed during the Chernobyl accident. It is of interest that with all the importance and prevalence of these phases, about a quarter of approved minerals still have undetermined crystal structures, and the number of synthetic phases for which the structures were determined is significantly inferior to structurally characterized natural uranyl carbonates. In this work, we review the crystal chemistry of natural and synthetic uranyl carbonate phases. The majority of synthetic analogs of minerals were obtained from aqueous solutions at room temperature, which directly points to the absence of specific environmental conditions (increased P or T) for the formation of natural uranyl carbonates. Uranyl carbonates do not have excellent topological diversity and are mainly composed of finite clusters with rigid structures. Thus the structural architecture of uranyl carbonates is largely governed by the interstitial cations and the hydration state of the compounds. The information content is usually higher for minerals than for synthetic compounds of similar or close chemical composition, which likely points to the higher stability and preferred architectures of natural compounds.

Keywords: uranyl; carbonate; mineral; crystal structure; topology; structural complexity



Citation: Gurzhiy, V.V.; Kalashnikova, S.A.; Kuporev, I.V.; Plášil, J. Crystal Chemistry and Structural Complexity of the Uranyl Carbonate Minerals and Synthetic Compounds. *Crystals* **2021**, *11*, 704. https://doi.org/10.3390/cryst11060704

Academic Editor: Duncan H. Gregory

Received: 18 May 2021 Accepted: 15 June 2021 Published: 19 June 2021

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1. Introduction

Uranyl carbonate phases play a very important role in all processes related to the nuclear fuel cycle. This conjunction starts from U deposits, where uranyl carbonate minerals form during the direct alteration of primary U-bearing rocks (containing uraninite, etc.) under the influence of groundwaters enriched with CO₂, which can be derived from the dissolution of host carbonate rocks or from the atmosphere [1–5]. In dissolved form, uranyl carbonates can play an important role in U release to the environment. And of course, it should not be forgotten that uranyl-carbonate mineralization has been described among the alteration products of the "lavas" that were formed during the accident at the fourth reactor of the Chernobyl nuclear power plant in 1986 [6,7].

There are 40 uranyl carbonate mineral species approved by the International Mineralogical Association as of 1 November 2020, thus making this group one of the most representative among secondary uranium minerals, coming third only after phosphates and sulfates [8,9]. Despite a fairly large number of known compounds, the structural diversity is not as great as one might expect. It is also of interest that about a quarter of approved minerals still have their crystal structures undetermined. The amount of synthetic structurally characterized uranyl carbonates is inferior to natural phases but can give an idea of the crystallization conditions present in the environment.

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Current work is devoted to reviewing the topological diversity and growth conditions of natural uranyl carbonates and their synthetic analogs. Information-based complexity measures have been performed to determine contributions of various substructural building blocks and particular topological types into the complexity of the whole structure, which is related to the stability of a crystalline compound.

2. Materials and Methods

2.1. Structural Data

For the current review, all structural data deposited in the Inorganic Crystal Structure Database (ICSD; version 4.5.0; release February 2020) were selected and supplemented by the data reported in the most recent publications of the author of the current paper (J.P.). Chemical formulae, mineral names, and the basic crystallographic characteristics for all inorganic uranyl carbonates of both natural and synthetic origin are listed in Table 1. In addition, Table 1 contains information on the proposed symmetry and unit cell parameters for the uranyl carbonate minerals with yet undefined crystal structures listed in the IMA Database of Mineral Properties [10].

Table 1. Crystallographic characteristics of natural and synthetic uranyl carbonates.

No.	Chemical Formula	Mineral Name	Sp.Gr.	a, Å/ α, °	b, Å/ β, °	c, Å/ γ, °	Ref.
			Finite C	lusters			
			cc0-1	:2-9			
1	$K_4[(UO_2(CO_3)_2(O_2)](H_2O)$		P2 ₁ /n	6.9670(14)/90	9.2158(18)/91.511(3)	18.052(4)/90	[11]
2	$K_4[(UO_2(CO_3)_2(O_2)](H_2O)_{2.5}$		P2 ₁ /n	6.9077(14)/90	9.2332(18)/91.310(4)	21.809(4)/90	[12]
3	$(\text{CN}_3\text{H}_6)_4[\text{UO}_2(\text{CO}_3)_2(\text{O}_2)]\cdot\text{H}_2\text{O}$		Pca2 ₁	15.883(1)/90	8.788(2)/90	16.155(1)/90	[13]
			cc0-1	:3-2			
4	$Na_4(UO_2)(CO_3)_3$	Čejkaite	Cc	9.2919(8)/90	16.0991(11)/91.404(5)	6.4436(3)/90	[14]
4a	$Na_4(UO_2)(CO_3)_3$		P-3c	9.3417/90	9.3417/90	12.824/120	[15-17]
4b	$Na_4(UO_2)(CO_3)_3$	Cejkaite old model	P-1	9.291(2)/90.73(2)	9.292(2)/90.82(2)	12.895(2)/120.00(1)	[18]
5	K_3 Na(UO ₂)(CO ₃) ₃		P-62c	9.29(2)/90	9.29(2)/90	8.26(2)/120	[19]
6	$K_3Na(UO_2)(CO_3)_3(H_2O)$	Grimselite	P-62c	9.2507(1)/90	9.2507(1)/90	8.1788(1)/120	[20-23]
6a	$Rb_6Na_2((UO_2)(CO_3)_3)_2(H_2O)$	Rb analogue of Grimselite	P-62c	9.4316(7)/90	9.4316(7)/90	8.3595(8)/120	[24]
7	$K_4(UO_2)(CO_3)_3$	Agricolaite	C2/c	10.2380(2)/90	9.1930(2)/95.108(2)	12.2110(3)/90	[25]
7a	K ₄ UO ₂ (CO ₃) ₃		C2/c	10.247(3)/90	9.202(2)/95.11(2)	12.226(3)/90	[26]
7b	$K_4(UO_2)(CO_3)_3$		C2/c	10.240(7)/90	9.198(4)/95.12(4)	12.222(12)/90	[27]
58	$Rb_4(UO_2)(CO_3)_3$		C2/c	10.778(5)/90	9.381(2)/94.42(3)	12.509(3)/90	[28]
8	$Cs_4UO_2(CO_3)_3(H_2O)_6$		$P2_1/n$	11.1764(4)/90	9.5703(4)/ 96.451(2)	18.5756(7)/90	[29]
8a	$Cs_4(UO_2(CO_3)_3)(H_2O)_6$		P2 ₁ /n	18.723(3)/90	9.647(2)/96.84(1)	11.297(2)/90	[30]
9	$Cs_4(UO_2(CO_3)_3)$		C2/c	11.5131(9)/90	9.6037(8)/93.767(2)	12.9177(10)/90	[31]
10	$(NH_4)_4(UO_2(CO_3)_3)$		C2/c	10.679(4)/90	9.373(2)/96.43(2)	12.850(3)/90	[32]
11	$\text{Tl}_4((\text{UO}_2)(\text{CO}_3)_3)$		C2/c	10.684(2)/90	9.309(2)/94.95(2)	12.726(3)/90	[33]
12	$Mg_2(UO_2)(CO_3)_3(H_2O)_{18}$	Bayleyite	$P2_1/a$	26.560(3)/90	15.256(2)/92.90(1)	6.505(1)/90	[34,35]
13	$CaMg(UO_2)(CO_3)_3(H_2O)_{12}$	Swartzite	$P2_1/m$	11.080(2)/90	14.634(2)/99.43(1)	6.439(1)/90	[34,36,37]
14	$Ca_2(UO_2)(CO_3)_3(H_2O)_{11}$	Liebigite	Bba2	16.699(3)/90	17.557(3)/90	13.697(3)/90	[34,38-40]
15	$\text{Ca}_{9}(\text{UO}_{2})_{4}(\text{CO}_{3})_{13} \cdot 28\text{H}_{2}\text{O}$	Markeyite	Pmmn	17.9688(13)	18.4705(6)	10.1136(4)	[41]
16	$Ca_8(UO_2)_4(CO_3)_{12} \cdot 21H_2O$	Pseudomarkeyite	P2 ₁ /m	17.531(3)	18.555(3)	9.130(3)/103.95(3)	[42]
17	$Sr_2UO_2(CO_3)_3)(H_2O)_8$		$P2_1/c$	11.379(2)/90	11.446(2)/93.40 (1)	25.653(4)/90	[43]
18	$Na_6Mg(UO_2)_2(CO_3)_6 \cdot 6H_2O$	Leószilárdite	C2/m	11.6093(21)/90	6.7843(13)/91.378(3)	15.1058(28)/90	[44]
19	$Na_2Ca(UO_2)(CO_3)_3(H_2O)_{5.3}$	Andersonite	R-3m	17.8448(4)/90	17.8448(4)/90	23.6688(6)/120	[20,34,38,45-5
20	$Na_2Ca_8(UO_2)_4(CO_3)_{13} \cdot 27 H_2O$	Natromarkeyite	Pmmn	17.8820(13)	18.3030(4)	10.2249(3)	[42]
21	$\substack{\text{Ca}_{3}\text{Na}_{1.5}(\text{H}_{3}\text{O})_{0.5}(\text{UO}_{2}(\text{C}\\\text{O}_{3})_{3})_{2}(\text{H}_{2}\text{O})_{8}}$		Pnnm	18.150(3)/90	16.866(6)/90	18.436(3)/90	[56]
22	K ₂ Ca(UO ₂)(CO ₃) ₃ ·6H ₂ O	Braunerite	P2 ₁ /c	17.6725(12)/90	11.6065(5)/101.780(8)	29.673(3)/90	[57]
23	$K_2Ca_3[(UO_2)(CO_3)_3]_2 \cdot 8(H_2O)$	Linekite	Pnnm	17.0069(5)/90	18.0273(5)/90	18.3374(5)/90	[58]
23a	$K_2Ca_3((UO_2(CO_3)_3)_2(H_2O)_6$		Pnnm	17.015(2)/90	18.048(2)/90	18.394(2)/90	[59]
24	SrMg(UO ₂)(CO ₃) ₃ (H ₂ O) ₁₂	Swartzite-(Sr)	$P2_1/m$	11.216(2)/90	14.739(2)/99.48(1)	6.484(1)/90	[34,36]
25	Na _{0.79} Sr _{1.40} Mg _{0.17} (UO ₂ (C O ₃) ₃)(H ₂ O) _{4.66}		Pa-3	20.290(3)/90	20.290(3)/90	20.290(3)/90	[60]
26	$\substack{\text{MgCa}_{5}\text{Cu}_{2}(\text{UO}_{2})_{4}(\text{CO}_{3})_{12}\\ (\text{H}_{2}\text{O})_{33}}$	Paddlewheelite	Pc	22.052(4)/90	17.118(3)/90.474 (2)	19.354(3)/90	[61]

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Table 1. Cont.

No.	Chemical Formula Mineral Name		Sp.Gr.	a, Å/ α, °	b, Å/ β, °	c, Å/ γ, °	Ref.
27	$Na_{8}[(UO_{2})(CO_{3})_{3}](SO_{4})_{2}\cdot 3H_{2}O$	Ježekite	P-62m	9.0664(11)/90	9.0664(11)/90	6.9110(6)/120	[62]
28	$NaCa_3(UO_2)(CO_3)_3 (SO_4)F(H_2O)_{10}$	Schröckingerite	P-1	9.634(1)/91.41(1)	9.635(1)/92.33(1)	14.391(2)/120.26(1)	[34,63-66]
29	$\begin{array}{c} {\rm MgCa_4F_2[UO_2(CO_3)_3]_2} \\ {\rm (H_2O)_{17.29}} \end{array}$	Albrechtschraufite	P-1	13.569(2)/115.82(1)	13.419(2)/107.61(1)	11.622(2)/92.84(1)	[67,68]
30	$\text{Ca}_{5}(\text{UO}_{2}(\text{CO}_{3})_{3})_{2}(\text{NO}_{3})_{2} \ (\text{H}_{2}\text{O})_{10}$		P2 ₁ /n	6.5729(9)/90	16.517(2)/90.494(3)	15.195(2)/90	[69]
31	$Ca_6(UO_2(CO_3)_3)_2C_{14}(H_2O)_{19}$		P4/mbm	16.744(2)/90	16.744(2)/90	8.136(1)/90	[69]
32	$Ca_{12}(UO_2(CO_3)_3)_4C_{18}(H_2O)_{47}$		Fd-3	27.489(3)/90	27.489(3)/90	27.489(3)/90	[69]
33	Nd ₂ Ca[(UO ₂)(CO ₃) ₃](CO ₃) ₂ (H ₂ O) _{10.5}	Shabaite-(Nd)	P-1	8.3835(5)/90.058(3)	9.2766(12)/89.945(4)	31.7519(3)/90.331(4)	[70,71]
34	$[C(NH_2)_3]_4[UO_2(CO_3)_3]$		R3	12.3278(1)/90	12.3278(1)/90	11.4457(2)/120	[72]
35	(C ₄ H ₁₂ N) ₄ [UO ₂ (CO ₃) ₃]·8H ₂ O		P2 ₁ /n	10.5377(18)/90	12.358(2)/99.343(4)	28.533(5)/90	[73]
36	[C(NH ₂) ₃] ₆ [(UO ₂) ₃ (CO ₃) ₆]		P-1	6.941(2)/95.63(2)	14.488(2)/98.47(2)	22.374 (2)/101.88(2)	[74]
	(H ₂ O) _{6.5}		Nanoclu				
37	Mg ₈ Ca ₈ (UO ₂) ₂₄ (CO ₃) ₃₀ O ₄ (OH) ₁₂ (H ₂ O) ₁₃₈	Ewingite	I4 ₁ /acd	35.142(2)/90	35.142(2)/90	47.974(3)/90	[75]
			Layer				
	CaU(UO ₂) ₂ (CO ₃)O ₄ (OH)	***	5 ⁴ 4 ² 3 ⁴ (β-			20.007(5) (55	r
38	(H ₂ O) ₇	Wyartite	P2 ₁ 2 ₁ 2 ₁	11.2706(8)/90	7.1055(5)/90	20.807(1)/90	[76–78]
38a	Ca(U(UO ₂) ₂ (CO ₃) _{0.7} O ₄ (OH) _{1.6}) (H ₂ O) _{1.63}	Wyartite dehydrated	Ртсп	11.2610(6)/90	7.0870(4)/90	16.8359(10)/90	[79]
			$6^{1}5^{2}4^{2}3^{2}$ (phos	ohuranylite)			
39	Ca(UO ₂) ₃ (CO ₃) ₂ O ₂ (H ₂ O) ₆	Fontanite	$P2_1/n$	6.968(3)/90	17.276(7)/90.064(6)	15.377(6)/90	[80,81]
			6 ¹ 5 ² 4 ² 3 ⁶ (ro	ubaultite)			
40	$\text{Cu}_2(\text{UO}_2)_3(\text{CO}_3)_2\text{O}_2(\text{OH})_2 \ (\text{H}_2\text{O})_4$	Roubaultite	P-1	7.767(3)/92.16(4)	6.924(3)/90.89(4)	7.850(3)/93.48(4)	[82,83]
			6 ¹ 3 ² -I (ruthe	rfordine)			
41	(UO ₂)(CO ₃)	Rutherfordine	Imm2	4.840(1)/90	9.273(2)/90	4.298(1)/90	[20,84-87]
42	Ca(H ₂ O) ₃ [(UO ₂) ₃ (CO ₃) _{3.6} O _{0.2}]	Sharpite	Стст	4.9032(4)	15.6489(11)	22.0414(18)	[88]
42a	Ca(UO ₂) ₆ (CO ₃) ₅ (OH) ₄ ·6H ₂ O	Sharpite	Orth	21.99(2)	15.63(2)	4.487(4)	[89,90]
			6 ¹ 3 ² -II (wide	ımannite)			
43	Pb ₂ [(UO ₂)(CO ₃) ₂]	Widenmannite	Pmmn	4.9350(7)/90	9.550(4)/90	8.871(1)/90	[21,91–93]
			Layers of Miscellar				
44	Y ₂ (UO ₂) ₄ (CO ₃) ₃ O ₄ ·14H ₂ O	Kamotoite-(Y)	P2 ₁ /n	12.3525(5)	12.9432 (5)/99.857(3)	19.4409(7)	[94,95]
45	$\substack{ [(Y_{4.22}Nd_{3.78})(H_2O)_{25}(UO_2)_{16}O_8\\ (OH)_8(CO_3)_{16}](H_2O)_{14} }$	Bijvoetite-(Y)	B2 ₁	21.234(3)/90	12.958(2)/90.00(2)	44.911(7)/90	[96,97]
46	Ca(UO ₂)(CO ₃) ₂ ·5H ₂ O	Meyrowitzite	P2 ₁ /n	12.376(3)	16.0867(14)/107.679(13)	20.1340(17)	[98]
			Minerals with Unde	fined Structures			
47	Cu ₂ (Ce,Nd,La) ₂ (UO ₂)(CO ₃) ₅ (OH) ₂ ·1.5H2O	Astrocyanite-(Ce)	Hex	14.96(2)/90	14.96(2)/90	26.86(4)/120	[99]
48	(UO ₂)(CO ₃)·H ₂ O	Blatonite	Hex or Trig	15.79(1)/90	15.79(1)/90	23.93(3)/120	[100]
49	$(UO_2)(CO_3) \cdot nH_2O$	Joliotite	Orth	8.16	10.35	6.32	[21]
50	CaGd ₂ (UO ₂) ₂₄ (CO ₃) ₈ Si ₄ O ₂₈ · 60H ₂ O	Lepersonnite-(Gd)	Pnnm or Pnn2	16.23(3)/90	38.74(9)/90	11.73(3)/90	[96]
51	Ca(UO ₂)(CO ₃) ₂ ·3H ₂ O	Metazellerite	Pbn2 ₁ or Pbnm	9.718(5)	18.226(9)	4.965(4)	[101]
52	$(UO_2)_2(CO_3)(OH)_2 \cdot 4H_2O$	Oswaldpeetersite	P2 ₁ /c	4.1425(6)	14.098(3)/103.62(1)	18.374(5)	[102]
53	Ca ₃ Mg ₃ (UO ₂) ₂ (CO ₃) ₆ (OH) ₄ · 18H ₂ O	Rabbitite	Mon	32.6(1)	23.8(1)/~90	9.45(5)	[103]
54	Ca(UO ₂) ₃ (CO ₃)(OH) ₆ ·3H ₂ O	Urancalcarite	Pbnm or Pbn2 ₁ ,	15.42(3)	16.08(4)	6.970(6)	[104]
55	$Ca_2Cu(UO_2)(CO_3)_4\cdot 6H_2O$	Voglite	P2 ₁ or P2 ₁ /m	25.97	24.50/104.0	10.70	[105,106]
56	Ca(UO ₂)(CO ₃) ₂ ·5H ₂ O	Zellerite	Pmn2 ₁ or Pmnm	11.220(15)	19.252(16)	4.933(16)	[101,107]
57	CaZn ₁₁ (UO ₂)(CO ₃) ₃ (OH) ₂₀ · 4H ₂ O	Znucalite	Orth	10.72(1)	25.16(1)	6.325(4)	[108]

2.2. Graphical Representation and Anion Topologies

The crystal structures of uranyl carbonate minerals and synthetic compounds discussed in the current review are based on the finite clusters, chains, layers, and even nanoclusters built by the linkage of U-centered coordination polyhedra with each other and carbonate groups. U(VI) atoms make two short $U^{6+} \equiv O^{2-}$ bonds to form approximately

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linear UO_2^{2+} uranyl cations (Ur), which are in turn surrounded in the equatorial plane by other four-to-six O atoms, resulting in the formation of a tetra-, penta-, or hexagonal bipyramid, as a coordination polyhedron of U(VI) atoms. The carbonate group is the simplest oxocarbon anion with C atom arranged in the center of a flat triangle and O atoms occupying all three of its vertices.

Topological analysis of the uranyl carbonate structural complexes is based on the description of *Ur* and CO₃ interpolyhedral linkage. The topology of the uranyl carbonate finite clusters and chains can be described using the theory of graphical (nodal) representation, which was first proposed by Hawthorne [110], and subsequently modified by Krivovichev [111,112], in which black and white nodes correspond to *Ur* and CO₃ groups, respectively; and the single or double line between the nodes corresponds to a vertex- or edge-sharing way of polyhedra polymerization, respectively (Figure 1a-c). Anion topology approach was proposed by Burns and co-authors [113,114] to describe the U-bearing crystal structures that are based upon sheets with edge-sharing linkage. To obtain anion topology of the layer, all cations, O_{Ur} , and O atoms coordinating only one cation should be removed, while the rest of O atoms should be linked via single lines up to c.a. 3.5 Å length (Figure 1d-f). The black-and-white graph is labeled with a special index ccD-U:CO₃-#, where cc means "cation-centered", D specifies dimensionality (0—finite clusters, 1—chains and 2—sheets), U:CO₃ ratio, #—registration number of the unit. Sheet-anion topology is indicated by the ring symbol, $p_1^{r1}p_2^{r2}\dots$, where p is the number of vertices in a topological cycle, and *r* is the amount of the respective cycle in the reduced section of the sheet.

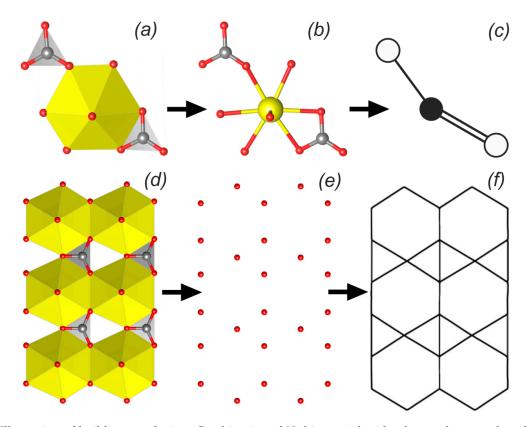


Figure 1. Illustration of building topologies. Combination of *Ur* bipyramid with edge- and vertex-shared triangular carbonate groups in polyhedral (a), ball-and-stick (b) representations, and respective black-and-white graph (c). Fragment of the dense uranyl-carbonate layer with edge-sharing interpolyhedral linkage (d), O atoms that are involved in linkage with more than one cation (e), and the resulted anion topology built on them (f). Legend: U-bearing coordination polyhedra = yellow; U atoms = yellow; C atoms = grey; O atoms = red; black nodes = U atoms, white nodes = C atoms; CO₃ groups are shown in a ball-and-stick model with grey filling; see Section 2.2 for details.

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2.3. Complexity Calculations

Structural complexity calculations allow to compare the structures and quantitatively characterize the impact of each substructural unit (i.e., U-bearing complex, interstitial cations, hydration state, etc.) in terms of their information content on the formation of a particular architecture. This approach was recently developed by Krivovichev [115–119], successfully implemented in a number of works (e.g., [120–123]), and is based on the Shannon information content calculations of per atom (I_G) and per unit cell ($I_{G,total}$) using the following equations:

$$I_G = -\sum_{i=1}^k p_i \log_2 p_i \quad \text{(bits/atom)} \tag{1}$$

$$I_{G,total} = -v I_G = -v \sum_{i=1}^{k} p_i \log_2 p_i \text{ (bits/cell)}$$
 (2)

where k is the number of different crystallographic orbits (independent sites) in the structure and p_i is the random choice probability for an atom from the i-th crystallographic orbit, that is:

$$p_i = m_i / v \tag{3}$$

where m_i is a multiplicity of a crystallographic orbit (i.e., the number of atoms of a specific Wyckoff site in the reduced unit cell), and v is the total number of atoms in the reduced unit cell.

The direct comparison of complexity parameters is possible only for the structures with identical or very close chemical composition (e.g., polymorphs), while changes in hydration state or interstitial complexes could significantly affect the overall complexity behavior. Thus, the structural complexity parameters of various building blocks (uranyl carbonate units, interstitial structure, H-bonding system) were calculated according to the recently suggested algorithm [124–127], so-called "ladders of information", to analyze their contributions into the complexity of the whole structure, and to distinguish which of the blocks plays the most important role, and which has the most influence on symmetry preservation or reduction.

3. Results

3.1. Uranyl Carbonate Minerals

Uranyl carbonates are one of the most abundant U(VI)-containing minerals at the Earth's surface or near the surface. Their crystallization is possible due to ubiquitous CO_2 dissolved in percolating aqueous solutions and can also be amplified by the dissolution of the carbonate minerals in the rock or hydrothermal veins (such as calcite or dolomite). Uranyl-carbonate aqueous species can be important constituents of groundwater under neutral to alkaline conditions as being thermodynamically favored [128,129]. Under such pH conditions, the dominating aqueous species are uranyl monocarbonate, $(UO_2)(CO_3)^0$, uranyl dicarbonate, $(UO_2)(CO_3)^2$, and uranyl tricarbonate, $(UO_2)(CO_3)^4$, with pK values of 5.5, 7, and 9, respectively [128]. The precipitation of solid phases from the solutions is usually connected with a higher evaporation rate or local oversaturation. Abandoned mining tunnels and adits can serve us as a model for such a situation. Efflorescences of uranyl carbonate minerals precipitating on the mining walls are typical indicators of uranium mineralization in closer or larger distances. Such precipitates have been found hundreds of meters far from the primary U mineralization in the mines (as e.g., in Jáchymov, Czech Republic).

In general, from a genetical point of view and considering the processes that led to the uranyl carbonate formation, we can distinguish among the two groups of uranyl carbonate minerals. The first comprises primary uranyl carbonates, or those that are connected genetically somewhat more with the primary mineralization. The second then comprises a group of uranyl carbonates of the recent or sub-recent origin, usually formed

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as the precipitates on the walls of the mining adits. Minerals are present, such as sharpite, $Ca[(UO_2)_3O_{0.2}(CO_3)_{3.6}](H_2O)_3$ [88,89], roubaultite, $Cu_2[(UO_2)_3(CO_3)_2(OH)_2](H_2O)_4$ [83] or fontanite, $Ca[(UO_2)_3(CO_3)_2O_2](H_2O)_6$ [81,96]. These minerals are usually tightly spatially connected either with primary minerals (even in relics) or other U(VI) non-carbonate supergene minerals, such as silicates of uranyl-oxides hydroxy-hydrate minerals. As the second, distinctive group, we can consider uranyl carbonate minerals such as grimselite, $K_3Na(UO_2)(CO_3)_3(H_2O)$ [22,23,130], bayleyite, $Mg_2[(UO_2)(CO_3)_3](H_2O)_{18}$ [34,35], or paddlewheelite, $MgCa_5Cu_2[(UO_2)(CO_3)_3]_4(H_2O)_{33}$ [61]. These are usually higher-hydrates oxysalts, tending to appear in powdery aggregates, efflorescence, or curved uneven crystals.

The first uranyl carbonate minerals were discovered in the 19th century. One of the first discovered was mineral liebigite, Ca₂[UO₂)(CO₃)₃](H₂O)_{~11} [40,131], reported in 1848 from Turkey by J.B. Smith and named after German chemist Justus von Liebig. Subsequently, this mineral was more precisely described and characterized from Jáchymov in Czechia (those times a part of the Austro-Hungarian Empire) under the name Uran-calc-carbonat, or Uranothallite, and then all were described to be the same mineral equal to liebigite [132]. Jáchymov became the famous and rich locality for many uranyl-carbonates. Many have been found there for the first time and thus Jáchymov remains one of the richest localities, even for the type uranyl carbonate minerals (from approximately 96 U(VI) supergene minerals, 19 are uranyl carbonates, thus 20% and 10 of them are type-minerals).

Until ca. 2015, there were only U-carbonates from the hydrothermal Variscan-type of U-deposits studied more in detail. Since extensive sampling campaigns at the Red Canyon area (San Juan County, UT, USA) several new particularly interesting U-carbonates with novel structural features and topologies have been discovered [42,98]. As current studies document that at the more detailed scale (micro- to nano-sized), the mineralogy of the localities is of course more diverse than thought, new uranyl carbonates are likely to be discovered. Furthermore, the discovery of U-nano-cages-containing the mineral ewingite [75], has brought up questions about the possible role of nano-scale clusters and cages in the processes of dissolution and formation of uranyl carbonates and uranyl minerals in general. It may be necessary to account for such nano-cages in the geochemical models of particular uranium-bearing systems.

3.2. Synthetic Uranyl Carbonates

First of all, it should be noted that the number of synthetic phases for which the structures were determined is significantly inferior to the structurally characterized natural uranyl carbonates in the ratio of 19:32. Whereas for other groups of U(VI)-bearing compounds this proportion is usually opposite [8,127,133]. The first structurally characterized synthetic uranyl carbonate, to our knowledge, was one of the simplest phases 4a, sodium-bearing Na₄(UO₂)(CO₃)₃ [17]. It is of interest that the first crystal structure of the natural uranyl carbonate, rutherfordine (41), was reported the year before [85]. The papers of K. Mereiter from the TU Wien (Austria) should be certainly noted in the first row among the works devoted to the synthesis and structural studies of synthetic uranyl carbonates. Then, the studies carried out by the A.M. Fedoseev and I.A. Charushnikova from the Frumkin Institute of Physical chemistry and Electrochemistry RAS (Russian Federation) and by V.N. Serezhkin from the Samara State University (Russian Federation) should be mentioned. A substantial portion of the synthetic uranyl carbonate compounds was synthesized and studied by P. C. Burns and his colleagues from the University of Notre Dame (USA), who significantly contribute to the studies of uranyl carbonate minerals as well.

All synthetic experiments can be roughly divided into two groups. Moreover, the majority of inorganic uranyl carbonates were synthesized by evaporation at room temperature and only a few of them were obtained from hydrothermal conditions. Uranyl nitrate hexahydrate was usually used as the source of U. But in some experiments, more specific reagents were used: UO_2 powder (for 1 and 2), $UO_2(CO_3)$ (for 7a), $Ag_4[UO_2(CO_3)_3]$ (for 8a), α - $UO_2MoO_4(H_2O)_2$ (for 10), and $Na_4UO_2(CO_3)_3$ (for 21). Potassium, sodium, cesium, or thallium carbonates were used as the source of CO_3 ions within the synthetic

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experiments. Compounds 36 and 10 can be considered as exceptions due to the usage of guanidine carbonate and carbamide in the respective syntheses. Several protocols of synthetic experiments deserve special attention. Thus, compound 1 [11] was formed as the result of the dissolution of UO₂ powder in the solution of K₂CO₃ and H₂O₂ at room temperature. Later it was filtered through a 0.45 µm polyamide syringe filter, and an additional 1.5 mL of 35 wt% H₂O₂ was added. Afterward it was transferred to a borosilicate scintillation vial and layered with methanol. The compound 2 [12] was obtained similarly, except for the scintillation vial step. The crystals of 4a [16] were obtained by hydrothermal synthesis at 135 °C in a sealed silica glass tube at about 20 MPa. The compound 7a [27] was synthesized by evaporation at room temperature, but before being left to evaporate, the dissolution of the precipitate was achieved via heating the solution over a steam bath. The crystals of 7b [28] were obtained from the solution that was stirred for five days. The compound 11 [33] was synthesized by slow addition of uranyl nitrate solution to the solution of $Tl_2(CO_3)_2$ at the temperature of c.a. 57 °C. The solvent was removed in a vacuum desiccator for two months from the resulting yellow-green solution, and crystals were then taken from the precipitate. To obtain the crystals of 36 [74], the initial solution was stirred vigorously for several days, afterwards, it was centrifuged and the supernatant was removed via pipet. The crystals were obtained from the precipitate, which was slowly cooled to 5 °C under a CO₂ atmosphere.

Nine of uranyl carbonate minerals have synthetic analog, which was also obtained mostly by evaporation at room temperature, except for the crystals of 7 [26], which were formed during the two months of evaporation at vacuum-desiccator. The compound 4a [15] was synthesized by hydrothermal reaction at $220\,^{\circ}$ C. The crystals of 41 [20] were obtained by purging the solution of UO_3 with $70\,kPa$ CO_2 at the glove box for $24\,h$.

Very special attention can be paid to compound **4a** [15], which may be the same sodium uranyl carbonate that was found among alteration products of the "lavas" resulting from the nuclear accident of the Chernobyl nuclear power plant [6,7].

3.3. Topological Analysis

The majority of uranyl carbonate crystal structures are based on finite clusters, which are represented by only two topological types (Table 1). The topological variety of layered uranyl carbonate complexes is significantly larger; however, the amount of compounds, which structures are based on the 2D units, is much lower. There are only ten uranyl carbonate compounds known with a layered structure, and all of them are natural phases.

The crystal structures of two synthetic K-bearing uranyl carbonates 1 [11] and 2 [12] differing only in the hydration state and one uranyl carbonate, templated by guanidinium molecules 3 [13], are based on the finite clusters of the cc0-1:2-9 topological type (Figure 2a,b). In terms of polyhedral representation, these clusters can be described as a hexagonal bipyramid that shares two of its equatorial edges with CO₃ groups spaced by one non-shared equatorial edge. There is a peroxide molecule arranged in the equatorial plane spaced from a carbonate group by another non-shared edge. Such topological type was also described in the structures of two uranyl nitrate compounds, pure inorganic [134] and organically templated [135], in which the peroxide group was replaced by two H₂O molecules. It should be noted that this topological type has an isomer, if two equatorial CO₃ groups are *trans*-arranged, being spaced by two non-shared edges, in contrast to the *cis*-arrangement in the structures of 1–3. The *trans*-isomer is one of the most common types of uranyl nitrate finite clusters [136], while it has not been observed in the structures of uranyl carbonates at all.

Uranyl tricarbonate cluster (UTC), which is shown in Figure 2c, is the most common structural unit among the natural and synthetic uranyl carbonate phases. There are 39 compounds known (Table 1), whose structures are based on these finite clusters, and is in sum 2.5 times more than the amount of all other structurally characterized uranyl carbonates (15). The topology of UTC belongs to the *cc*0-1:3-2 type (Figure 2d). This topology can be obtained from the previous *cis-cc*0-1:2-9 type by the replacement of the peroxide molecule

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by the third CO₃ group, resulting in the formation of a triangular cluster with the uranyl hexagonal bipyramid arranged in its core and ideal -6*m*2 point group symmetry.

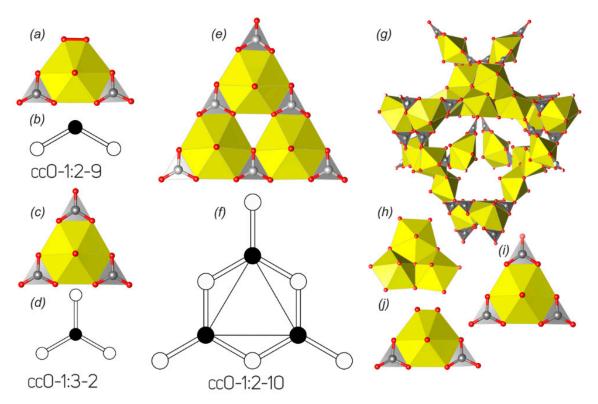


Figure 2. Finite clusters in the crystal structures of natural and synthetic uranyl carbonates and their graphical representations (see Table 1 and text for details). Legend: see Figure 1; peroxide molecule is indicated by red bond (a); see Section 3.3 for details.

Compound 36 [74], to our knowledge, is the only compound whose structure is based on the triuranyl hexacarbonate finite cluster (Figure 2e). The cluster is built by three vertex-sharing in a cyclic manner uranyl hexagonal bipyramids. Each cavity at the exterior side of such a cycle is occupied by a CO_3 group to form a large triangle, each side of which is built by alternating two bipyramids and three carbonate groups. The topology of the uranyl carbonate cluster (Figure 2f) in the structure of 36 belongs to the cc0-1:2-10 type. The architecture of this cluster can be also described as trebling of the UTC cluster with keeping triangular motif and ideal -6m2 point group symmetry.

Probably the most remarkable structure not only among the uranyl carbonate compounds but among all known minerals, was described in ewingite (37) [75]. Ewingite is a calcium-magnesium oxo-hydroxy-hydrate uranyl carbonate natural phase, whose structure is built by 24 uranyl pentagonal and hexagonal bipyramids interlinked with each other and $\rm CO_3$ groups, to form nanoclusters 2.3 nm in diameter (Figure 2g). Three fundamental building units can be distinguished within the uranyl carbonate cluster in ewingite. These are 4 trimers of edge-sharing pentagonal bipyramids, 6 cis-isomer of the uranyl bicarbonate unit (cc0-1:2-9), and 6 UTC complex (Figure 2h–j). Moreover, linkage of all building units occurs only through the carbonate groups. Mg and Ca ions as well as $\rm H_2O$ molecules are arranged both inside and in between the U-bearing nanoclusters.

The crystal structures of wyartite (38) [76–79] and its dehydrated form are based on the similar layered complexes that belong to the so-called β -U₃O₈-sheet anion topology (Figure 3a,b). Topology has the $5^44^23^4$ ring symbol and consists of infinite chains of edge-sharing pentagons that are linked with the neighbor chains through the common vertices and separated by the chains of squares and triangles. The crystal structures of 38 and 38a are remarkable for being the only U(V)-bearing natural phases. Pentagons are occupied by the U⁶⁺ ions, squares correspond to the irregular U⁵⁺O₇ polyhedra, whereas triangles are

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vacant. Carbonate groups share edges with the U⁵⁺-centered polyhedra and are arranged towards the interlayer space.

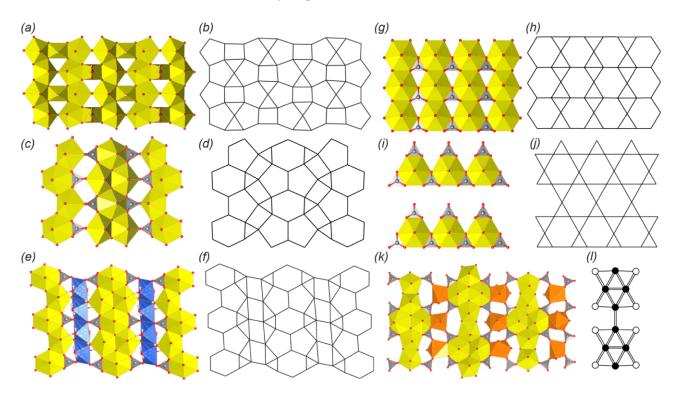


Figure 3. 2D complexes in the crystal structures of natural and synthetic uranyl carbonates and their anion topologies or graphical representation (see Table 1 and text for details). Legend: see Figure 1; Cu polyhedra = blue, Nd or Y polyhedra = orange; see Section 3.3 for details.

The crystal structure of fontanite (39) [80,81] is based on the layered uranyl carbonate complexes, which correspond to the, so-called, phosphuranylite anion topology [137] (Figure 3c,d) with the $6^15^24^23^2$ ring symbol. The topology consists of two types of alternating infinite chains. The first type of chains is formed by edge-sharing dimers of pentagons that are interlinked by edge-sharing hexagons. The second type of chain is formed by alternating edge-sharing triangles and squares. All hexagons and pentagons are occupied by the uranyl ions, all triangles are occupied by carbonate groups, while all squares are vacant. It should be noted that phosphuranylite anion topology is very common among the U-bearing natural and synthetic phases and is represented by a wide variety of isomers, which differ in the occupancy of polygons. Thus, hexagons may be vacant, and triangles may be occupied by tetrahedral, trigonal pyramidal, or planar trigonal oxyanions (e.g., [8,127]).

Another anion topology that consists of hexagons, pentagons, squares and triangles with the $6^15^24^23^6$ ring symbol (Figure 3e,f) was described in the structure of roubaultite (40) [82,83]. Roubaultite anion topology contains the same infinite chains of edge-sharing pentagon dimers linked by edge-sharing hexagons that were observed in the phosphuranylite topology. But in the structure of 40, these chains are separated by infinite chains of edge-sharing squares decorated with trimers of edge-sharing triangles on the sides. All hexagons and pentagons are also occupied by the uranyl ions, as I was realized in the phosphuranylite topology. Squares are occupied by Cu-centered slightly distorted octahedra. The middle triangle from each trimer is occupied by the carbonate group, leaving the other two triangles vacant.

The simplest uranyl carbonate, at least according to the chemical composition, ruther-fordine $(UO_2)(CO_3)$ [20,84–87], has a layered structure. The anion topology is also rather simple; it consists of parallel chains of edge-sharing hexagons separated by hourglass

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dimers of edge-sharing triangles (Figure 3g,h). All hexagons are occupied by the uranyl ions, and one triangle from each dimer is occupied by the CO₃ group, keeping the second triangle vacant. The crystal structure of sharpite (42) is also based on the layered complexes that belong to the same rutherfordine anion topology. However, the polyhedral representation appeared to be much more complex. Thus, the layer can be described as being formed by the 1D modules of rutherfordine topology. Each module represents a triple band of edge-sharing uranyl hexagonal bipyramids, a part of the triangular spaces between which are occupied by carbonate groups. These modules are arranged in the structure at approximate right angles to each other and are linked by the Ca-centered polyhedra, which are arranged on the crests of sawtooth waves (Figure 4a,b). Despite the curvature of such zigzag layers (in contrast to flat layered structure in rutherfordine) and the arrangement of Ca ions in the centers of square antiprisms, projection of such corrugated layers onto the (010) plane corresponds to the rutherfordine topology, with the equatorial arrangement of Ca polyhedra ligands having hexagon shape.

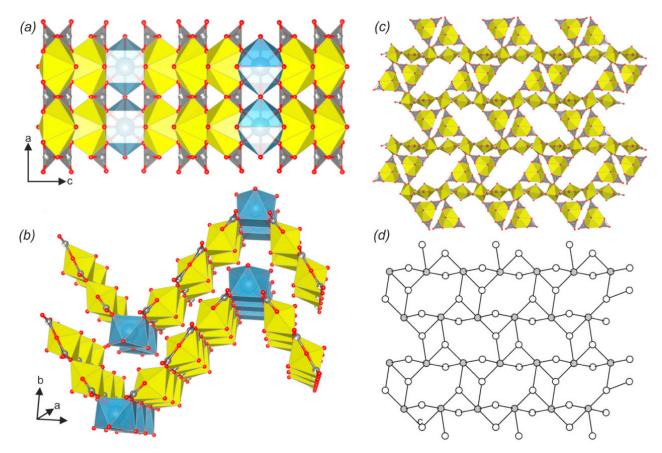


Figure 4. The crystal structures of sharpite (a,b) and meyrowitzite (c) with simplified topological representation (d). Legend: see Figure 1; Ca polyhedra = light blue.

The crystal structure of widenmannite (43) [21,91–93] is based on layered complexes, the topology of which consists of hexagons and triangles with the same 6^13^2 ring symbol as was found in the structure of rutherfordine. However, the arrangement of polygons in both structures is different. Widenmannite anion topology is built by the hexagons linked by vertex-sharing to other six hexagons, while all of its six edges are shared with triangles, thus forming trihexagonal tiling, which was used by Johannes Kepler in his book [138] and is also known under the kagome pattern name. In the ideal structure of the widenmannite (Figure 3i,j) each second row of hexagonal bipyramids should be vacant, but in the real structure the disorder with partial occupancy of the U sites takes place, which results in

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the occupation of all hexagons by the uranyl ions and half of the triangles oriented in the same direction are occupied by carbonate groups, keeping another half vacant.

The crystal structures of two *REE*-bearing minerals kamotoite-(Y) (44) [94,95] and bijvoetite-(Y) (45) [96,97] are based on highly remarkable and very rare layered complexes that have not been observed in any other natural or synthetic compound. The topology of the 2D complex is based on infinite chains of alternating dimers of edge-sharing uranyl hexagonal and pentagonal bipyramids (Figure 3k,l). Dimers of pentagonal bipyramids are arranged along the chain's extension, while dimers of hexagonal bipyramids are arranged perpendicularly. Each hexagonal bipyramid shares two of its oblique equatorial edges, not taking part in the linkage between U polyhedra, with CO_3 groups. These chains are linked into the 2D structure via irregular Y^{3+} - or Nd^{3+} -centered coordination polyhedra through the 6th non-shared equatorial edge from one chain and two O atoms of two carbonate groups from the neighbor chain. It should be noted that the resulting U- and *REE*-bearing layers are electroneutral, so the 3D structure formation is provided by the H-bonding system, which involves H_2O molecules from the coordination sphere of *REE* atoms and from the interlayer space.

The final to date topological type, which has been described in the structures of natural and synthetic uranyl carbonates, is observed in the structure of calcium uranyl carbonate mineral meyrowitzite (46) [98]. The structure of the layered complex is composed of UTC clusters sharing apical vertices of CO₃ groups with uranyl pentagonal bipyramids (Figure 4c). This structural type, unlike the rest of the topologies described herein, is the least dense in terms of the interconnection of U coordination polyhedra, and its topology will become clearer if graphical representation is used for illustration (Figure 4d). Thus, if uranyl pentagonal bipyramid is represented by grey nods, U hexagonal bipyramids by white nods, and the line between nods appearing if pentagonal bipyramid shares an equatorial O atom with the CO₃ group from the UTC cluster, the resulting graph of the complex will correspond to one of the most common *cc*1-1:2-4 topological type among the U(VI) bearing structures in general (e.g., [8,127]). Since the concept of graphical representation is violated, this description is more appropriate to use not as a direct interpretation of the topology, but as an approximate model.

3.4. Structural and Topological Complexity

Structural complexity measures have been implemented in several stages and the results of calculations are listed in Figures 5 and 6 and Table 2. At the first stage, the topological complexity (TI), according to the maximal point (for finite clusters) or layer symmetry group has been determined, as these are the basic structure building units. At the second stage, the structural complexity (SI) of the U-bearing complexes has been calculated taking into account its real symmetry. The next informational contribution comes from the stacking (LS) of finite clusters and layered complexes (if more than one complex is within the unit cell). The fourth contribution to the total structural complexity is derived by the interstitial structure (IS). The last portion of information comes from the interstitial H bonding system (H). It should be noted that the H atoms related to the U-bearing clusters and layers were considered as a part of those complexes, but not within the contribution of the H-bonding system. Complexity parameters for the whole structure have been determined using *ToposPro* software [139].

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 Table 2. Structural and topological complexity parameters for the uranyl carbonate compounds.

	Formula	T 1	Complexity Parameters of the Crystal Structure				Structural Co U-C Unit	mplexity of	f the		Topological (U-C Unit	ogical Complexity of the nit			
No.		Topology	Sp. Gr.	ν	I_G	$I_{G,total}$	Point, Rod or Layer Sym. Gr.	ν	I_G	$I_{G,total}$	Point, Rod or Layer Sym. Gr.	ν	I_G	$I_{G,total}$	
	Finite clusters														
1 2 3	$\begin{array}{l} K_4(UO_2(O_2)(CO_3)_2)(H_2O) \\ K_4(U(CO_3)_2)O_2(O_2)(H_2O)_{2.5} \\ (CN_3H_6)_4[UO_2(CO_3)_2(O_2)]\cdot H_2O \end{array}$	cc0-1:2-9	P2 ₁ /n P2 ₁ /n Pca2 ₁	80 100 204	4.322 4.644 5.672	345.750 464.390 1157.175	1	13	3.700	48.106	2mm	13	2.777	36.101	
4	$Na_4(UO_2)(CO_3)_3$ /Čejkaite		Cc	38	4.248	161.420									
4b *	Na ₄ (UO ₂)(CO ₃) ₃ / Cejkaite old model		P-1	76	5.274	400.840									
8 8a 12 14 16 17 21 22 23 23a 25 26 28 29 30 33 35	Cs ₄ UO ₂ (CO ₃) ₃ (H ₂ O) ₆ Cs ₄ (UO ₂ (CO ₃) ₃)(H ₂ O) ₆ Mg ₂ (UO ₂)(CO ₃) ₃ (H ₂ O) ₁₈ /Bayleyite Ca ₂ (UO ₂)(CO ₃) ₃ (H ₂ O) ₁₁ /Liebigite Ca ₈ (UO ₂) ₄ (CO ₃) ₁₂ ·21H ₂ O/Pseudomarkeyite Sr ₂ UO ₂ (CO ₃) ₃ (H ₂ O) ₈ Ca ₃ Na _{1.5} (H ₃ O) _{0.5} (UO ₂ (CO ₃) ₃) ₂ (H ₂ O) ₈ K ₂ Ca(UO ₂)(CO ₃) ₃ ·6H ₂ O/Braunerite K ₂ Ca ₃ [(UO ₂)(CO ₃) ₃) ₂ ·8(H ₂ O)/Linekite K ₂ Ca ₃ ((UO ₂)(CO ₃) ₃) ₂ (H ₂ O) ₆ Na _{0.79} Sr _{1.40} Mg _{0.17} (UO ₂ (CO ₃) ₃)(H ₂ O) _{4.66} MgCa ₅ Cu ₂ (UO ₂) ₄ (CO ₃) ₁₂ (H ₂ O) ₁₀ /Schröckingerite NaCa ₃ (UO ₂)(CO ₃) ₃ (SO ₄)F(H ₂ O) ₁₀ /Schröckingerite MgCa ₄ F ₂ [UO ₂ (CO ₃) ₃] ₂ (H ₂ O) _{17.29} /Albrechtschraufite Ca ₅ (UO ₂ (CO ₃) ₃) ₂ (NO ₃) ₂ (H ₂ O) ₁₀ Nd ₂ Ca[(UO ₂)(CO ₃) ₃](CO ₃) ₂ (H ₂ O) _{10.5} /Shabaite-(Nd) (C ₄ H ₁₂ N) ₄ [UO ₂ (CO ₃) ₃](SO ₃) ₂ (H ₂ O)	cc0-1:3-2	P2 ₁ /n P2 ₁ /n P2 ₁ /a Bba2 P2 ₁ /m P2 ₁ /c Pnnm P2 ₁ /c Pnnm Pnnm Pa-3 Pc P-1 P-1 P2 ₁ /n P-1	148 5.209 771.000 148 5.209 771.000 276 6.123 1689.950 200 5.664 1132.770 262 6.148 1610.760 324 6.34 2054.110 484 6.059 2932.730 1 15 472 6.883 3248.610 474 6.049 2867.260 462 5.99 2767.510 752 5.048 3795.880 616 8.267 5092.340 110 5.781 635.950 179 6.489 1161.600 146 5.204 759.710 230 6.845 1574.460	3.907	58.603	-6 <i>m</i> 2	15	2.106	31.584					
7 7 7a 7b 9 10 11	$\begin{array}{l} K_4(UO_2)(CO_3)_3/Agricolaite \\ K_4UO_2(CO_3)_3 \\ K_4(UO_2)(CO_3)_3 \\ Cs_4(UO_2(CO_3)_3) \\ (NH_4)_4(UO_2(CO_3)_3) \\ Tl_4((UO_2)(CO_3)_3) \end{array}$	-	C2/c C2/c C2/c C2/c C2/c C2/c C2/c	- 428 - 38 - 38 - 38 - 70 - 38 - 106	6.741 3.406 3.406 3.406 3.406 4.215 3.406	$\begin{array}{r} -2885.348 \\ 1\overline{29.420} \\ 129.420 \\ 129.420 \\ 129.420 \\ 295.050 \\ 129.420 \\ -527.\overline{160} \end{array}$	2	15	3.107	46.603	-				
13 15 19 20 24	$\begin{array}{l} CaMg(UO_2)(CO_3)_3(H_2O)_{12}/\textbf{Swartzite} \\ Ca_9(UO_2)_4(CO_3)_{13}\cdot 28H_2O/\textbf{Markeyite} \\ Na_2Ca(UO_2)(CO_3)_3(H_2O)_{5,3}/\textbf{Andersonite} \\ Na_2Ca_8(UO_2)_4(CO_3)_{13}\cdot 27H_2O/\textbf{Natromarkeyite} \\ SrMg(UO_2)(CO_3)_3(H_2O)_{12}/\textbf{Swartzite-(Sr)} \end{array}$	_	P2 ₁ /m Pmmn R-3m Pmmn P2 ₁ /m	300 203 310 106	4.973 5.495 4.461 5.599 4.973	1648.650 905.490 1735.600 527.160	m	15	3.240	48.600					
18	$Na_6Mg(UO_2)_2(CO_3)_6 \cdot 6H_2O/Le\'oszil\'ardite$		C2/m	55	4.363	239.980		15	3.774	56.610	_				
$-\frac{31}{4}$	$ \begin{array}{c} Ca_{6}(UO_{2}(CO_{3})_{3})_{2}C_{14}(H_{2}O)_{19} \\ Na_{4}(UO_{2})(CO_{3})_{3} \end{array} $		$-\frac{\overline{P4/mbm}}{\overline{P-3c}}$	$-\frac{174}{76}$	$-\frac{4.282}{3.049}$	745.070 231.750	mm2 	15	3.107	46.603	-				
4a 32	$Ca_{12}(UO_2(CO_3)_3)_4C_{18}(H_2O)_{47}$		F-3c Fd-3	438	4.397	1925.710	3	15	2.639	39.585					
34	[C(NH ₂) ₃] ₄ [UO ₂ (CO ₃) ₃]		R3	45	4.013	180.565									
5	$-\overline{K_3Na(UO_2)(CO_3)_3}$	-	P-62c	38	2.891	109.870					-				
6	$K_3Na(UO_2)(CO_3)_3(H_2O)/Grimselite$		P-62c	44	3.197	140.670	-6	15	2.506	37.584					

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 Table 2. Cont.

No.	r. I	pology	Complexity Parameters of the Crystal Structure				Structural Co U-C Unit	omplexity of	the		Topological Complexity of the U-C Unit			
	Formula	pology	Sp. Gr.	ν	I_G	$I_{G,total}$	Point, Rod or Layer Sym. Gr.	ν	I_G	$I_{G,total}$	Point, Rod or Layer Sym. Gr.	ν	I_G	$I_{G,total}$
6a	$Rb_6Na_2((UO_2)(CO_3)_3)_2(H_2O)$		P-62c	44	3.197	140.670	,				•			
27	$Na_8[(UO_2)(CO_3)_3](SO_4)_2 \cdot 3H_2O/Ježekite$		P-62m	42	3.498	146.930	-6m2	15	2.106	31.584	-			
36	$[C(NH_2)_3]_6[(UO_2)_3(CO_3)_6](H_2O)_{6.5}$ cc()-1:2-10	P-1	225	6.818	1534.100	1	33	5.044	166.452	-6m2	33	2.914	96.162
	Nanoclusters													
37	$Mg_{8}Ca_{8}(UO_{2})_{24}(CO_{3})_{30}O_{4}(OH)_{12}(H_{2}O)_{138}/\textbf{Ewingite}$		I4 ₁ /acd	2508	7.311	18,335.988	-4	220	5.781	1271.820	-4	220	5.781	1271.820
	Layers													
	$5^44^23^4~(\beta$ - $U_3O_8)$													
38 38a	$\begin{array}{l} CaU(UO_2)_2(CO_3)O_4(OH)(H_2O)_7/\textbf{Wyartite} \\ Ca(U(UO_2)_2(CO_3)_{0.7}O_4(OH)_{1.6})(H_2O)_{1.63} \end{array}$		P2 ₁ 2 ₁ 2 ₁ Pmcn	156 84	5.285 3.821	824.52 320.964	p2 ₁ p2 ₁ mn	40 36	4.322 3.614	172.880 130.103	p2 ₁ mn	40 36	3.822 3.614	152.880 130.103
	6 ¹ 5 ² 4 ² 3 ² (phosphuranylite)													
39	Ca(UO ₂) ₃ (CO ₃) ₂ O ₂ (H ₂ O) ₆ /Fontanite		P2 ₁ /n	152	5.248	797.685	p11n	38	4.248	161.424	сттт	19	2.880	54.720
	$6^15^24^23^6$ (roubaultite)													
40	$Cu_2(UO_2)_3(CO_3)_2O_2(OH)_2(H_2O)_4/\textbf{Roubaultite}$		P-1	37	4.236	156.750	p-1	23	3.567	82.042	p _a mmm	23	1.837	42.239
	Finite clusters													
	6 ¹ 3 ² -I (rutherfordine)													
41	UO ₂)(CO ₃)/Rutherfordine		Imm2	7	2.236	15.651	р2тт	7	2.236	15.651	р2тт	7	2.236	15.651
42	$Ca(H_2O)_3[(UO_2)_3(CO_3)_{3.6}O_{0.2}]/Sharpite$		Стст	72	3.837	276.235	p2/m11	24	3.335	80.040	p _b mmm	24	3.168	76.032
	6 ¹ 3 ² -II (widenmannite)													
43	Pb ₂ [(UO ₂)(CO ₃) ₂]		Pmmn	34	3.382	114.974	p2mm	11	2.914	32.054	p _b 2mm	11	2.914	32.054
	Layers of miscellaneous topology													
44	$Y_2(UO_2)_4(CO_3)_3O_4 \cdot 14H_2O/$ Kamotoite-(Y)		P2 ₁ /n	282	6.147	1733.353	p11a	64	5.000	320.000	p _b mmm	32	3.250	104.000
45	$[(Y_{4.22}Nd_{3.78})(H_2O)_{25}(UO_2)_{16}O_8(OH)_8(CO_3)_{16}](H_2O)_{14}/$ Bijvo (Y)	etite-	$B2_1$	522	8.028	4190.567	p1	68	6.087	413.916	10	34	3.382	114.988
46	$\overline{Ca(UO_2)(CO_3)_2} \cdot \overline{5H_2O/Meyrowitzite}$		$-P\overline{2}_1/n$	320	6.322		$\bar{p}2_{1}/\bar{b}$		5.044	665.808	$-p\overline{2}_{1}/b^{-}$		5.044	665.808

^{*—}although the old model of čejkaite is erroneous from the structural point of view, it was decided to keep complexity calculations for it due to presence of structural data in the database.

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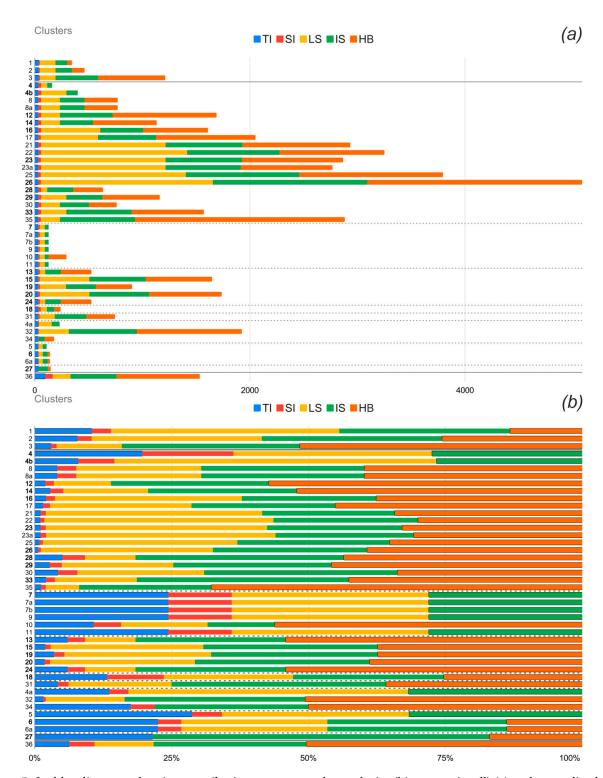


Figure 5. Ladder diagrams showing contributions to structural complexity (bits per unit cell) (**a**) and normalized contributions (in %) (**b**) for the structures based on uranyl carbonate finite clusters. Legend: TI = topological information; SI = structural information; LS = layer stacking; IS = interstitial structure; HB = hydrogen bonding. See Table 2 and text for details.

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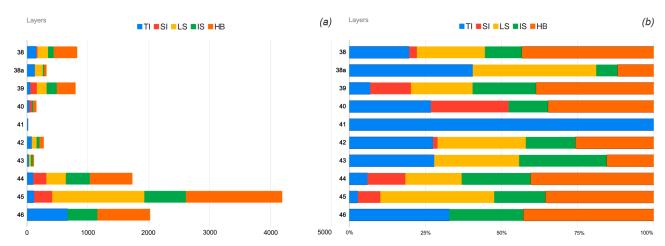


Figure 6. Ladder diagrams showing contributions to structural complexity (bits per unit cell) (**a**) and normalized contributions (in %) (**b**) for the structures based on uranyl carbonate layers. Legend: see Figure 5. See Table 2 and text for details.

4. Discussion

All three synthetic compounds, whose structures are based on finite clusters of the cc0-1:2-9 topological type (Table 2), demonstrate low real (structural) symmetry of the uranyl bicarbonate cluster that corresponds to the point symmetry group 1. However, the topological symmetry of the cluster is much higher and is described by the orthorhombic point symmetry group 2mm (Figure 7a). It should be noted that all three compounds have similar Z = 4, and thus have equal contribution not only of TI and SI domains, but also from the LS. Complexity of these compounds largely depends on the nature of the interstitial component and hydration state. Substitution of inorganic K⁺ ions (in 1 and 2) by the guanidinium cations (in 3) transfer compound in terms of complexity from intermediate to very complex group.

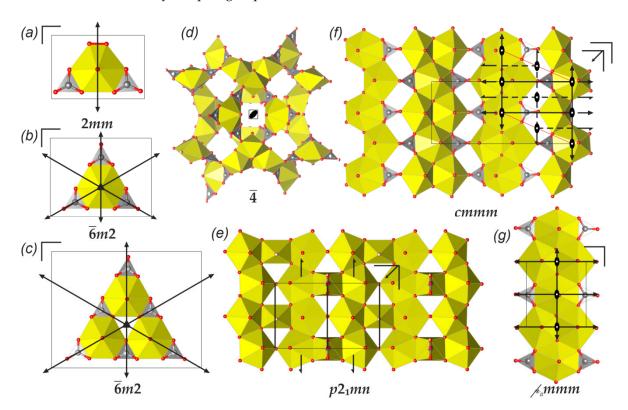


Figure 7. Uranyl carbonate complexes and their highest (topological) symmetry groups. Legend: see Figure 1. See text for details.

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Topological symmetry of the uranyl tricarbonate cluster (cc0-1:3-2 type) is described by the -6m2 point group (Figure 7b), and mineral ježekite, 27 [62], and is the only compound whose topological symmetry preserves in a real structure. Another six compounds 4a, 5, 6a, 32, 34, including mineral grimselite, 6 [20–23], have rather high structural symmetry of the UTC: trigonal point group 3 (4a, 32, 34) or hexagonal point group -6 (5, 6, 6a), which results in a slight increase of SI contribution after TI portion. It should be noted that the cubic symmetry of the whole structures of 4a and 32 is higher than the topological symmetry of the cluster, which demonstrates that interstitial cations and H₂O molecules can act as symmetry breaking agents, and not only symmetry reducing. It is of interest that all six compounds that have the structural symmetry of the UTC equal to point group m are minerals. Moreover, compounds with structural symmetry of the UTC equal to point group 2 are also represented by mineral agricolaite, 7 [25], and its synthetic analogs. Thus, all compounds with monoclinic structural symmetry of the uranyl tricarbonate clusters are related to natural phases. Nearly half of all compounds, whose structures are based on the UTC have the lowest structural symmetry of the cluster, described by the triclinic non-centrosymmetric point group 1, and the distribution between minerals and synthetic compounds here is almost uniform. Second, the most complex compound among the uranyl carbonates is paddlewheelite, 26 [61], whose structure is also based on the UTC units, and information content is 8.267 bits/atom and 5092.340 bits/cell. It should be however mentioned that paddlewheelite has one of the largest information contents per atom among the uranyl carbonate compounds, which is achieved due to a large amount of interstitial cations and H₂O molecules along with the rather high density of their framework arrangement.

The crystal structure of synthetic compound 36 [74] is based on the large triangular triuranyl hexacarbonate clusters of cc0-1:2-10 topological type, which has the same topological symmetry -6m2 as UTC cluster (Figure 7c). But at the same time the structural symmetry of this cluster is the lowest and corresponds to the triclinic point group 1. The unit cell of 36 contains two triuranyl hexacarbonate clusters but their contribution (TI + SI + LS) is comparable with a contribution of four UTC clusters of the same structural symmetry.

Ewingite, 37 [75], is a mineral with the most complex crystal structure known nowadays (Table 2; Figure 7d). According to the structure reported by Olds and coauthors [75], the structural model of ewingite contains 12,684.860 bits/cell, but considering an additional estimated amount of H₂O molecules and respective H atoms in complexity calculations, the total information amount will be presumably equal to c.a. 23,000 bits/cell. Our attempts to get rid of disordered sites and to assign H atoms to H₂O molecules and OH groups resulted in the value of 18,335.988 bits/cell. However, it should be kept in mind that the imperfect quality of measured crystals didn't allow to assign all disordered sites of H₂O molecules in the structural model. Thus, to reach the value of 23,000 bits/cell, an additional 12 fully occupied H₂O sites (48 molecules per formula unit) should appear in the structure, which is somewhat doubtful. Most likely, one could expect the structural complexity of ewingite to be in the range of 19,500–21,500 bits/cell, depending on the variable hydration state. The contribution of TI and SI into the total information content is the smallest (6.9%), stacking is giving another 20.8%, while the contribution of interstitial structure (24.7%) and H-bonding system (47.6%) gives nearly $\frac{3}{4}$ (72.3%) of the total complexity of ewingite crystal structure. Complexity parameters for ewingite are listed in Table 2, but omitted from Figure 5 for clarity.

The crystal structures of wyartite, 38 [76–78], and its dehydrated analog 38a [79] are based on the layers of β -U₃O₈ anion topology, whose topological symmetry is described by the orthorhombic layer symmetry group $p2_1mn$ (Figure 7e). The presence of a significant amount of H₂O molecules in the coordination sphere of interstitial cations reduces the layer's structural symmetry in wyartite, while the release of H₂O and subsequent linkage of U-bearing layers directly through the Ca-centered polyhedra keeps the topological symmetry and breaks the symmetry of the whole structure of 38a, which results in a decrease of information content by 2.5 times in comparison with the structure of natural compound 38.

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U-bearing layers with phosphuranylite anion topology play an important role in the mineralogy of uranyl selenites as has been recently shown [127]. There is only one uranyl carbonate, mineral fontanite, 39 [80,81], whose structure is based on the layers of this topological type (Figure 7f). However, the structure of uranyl carbonate layers in fontanite differs from that in uranyl selenite minerals and synthetic compounds (Figure 8). Pyramidal selenite groups with lone electron pairs make chains of edge-sharing *Ur* polyhedra arranged as stepped [127] or zig-zag layers (Figure 8c). In the structure of marthozite, as an example of zig-zag layers, equatorial planes of *Ur* bipyramids are arranged parallel to the mean plane of the layer. In the structure of fontanite, uranyl carbonate layer has also a *zig-zag* manner, but equatorial planes of *Ur* bipyramids make an angle of c.a. 135° at the linkage with the neighbor chain of edge-sharing *Ur* polyhedra. Topological symmetry of uranyl carbonate layer (*cmmm*) is higher than that in uranyl selenite marthozite (*pmmm* [127]) because of the flat carbonate groups in comparison to selenite pyramids, but the structural symmetry (*p11n*) and complexity parameters of U-bearing layers in fontanite are the same as were reported for marthozite [127].

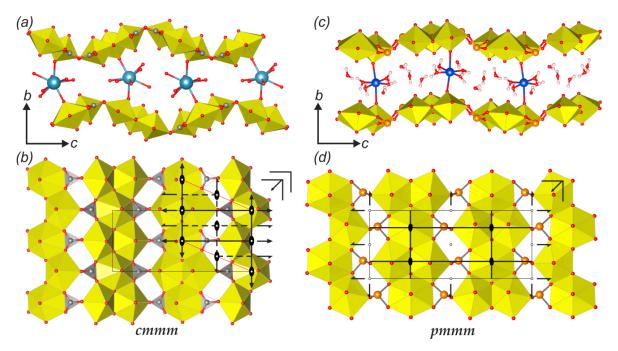


Figure 8. The crystal structures of fontanite (**a**) and marthozite (**c**), uranyl carbonate (**b**) and uranyl selenite (**d**) layers of phosphuranylite topology in their structures, and respective topological symmetry groups. Legend: see Figures 1 and 7.

The crystal structure of rutherfordine, 41 [20,84–87], is the simplest among natural and synthetic uranyl carbonates. It is also of special interest because the total amount of information is equal to the topological symmetry contribution (Table 2; Figure 9a). It happens because there is no interstitial structure in rutherfordine, and the body-centered cell is reduced to a single layer.

U-bearing layers of rutherfordine anion topology are also found in the structure of sharpite, **42** [88–90]. However, from a structural point of view, this topology is obtained from uranyl carbonate chains linked by the Ca-centered polyhedra, whose topological symmetry is described by the p_bmmm rod symmetry group (Figure 9b). A similar situation is observed in the structure of roubaultite, **40** [82,83], in which the U-bearing layer can be described in terms of anion topology, but actually is built by the chains of p_ammm topological symmetry (Figure 7g) similar to those found in phosphuranylite topology, and linked not directly to each other, but through Cu-centered octahedra. Similarly, and as it was described in the Section 3.3, each second row of hexagonal bipyramids in the structure

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of widenmannite, **43** [93] should ideally be vacant, so the structure can be described as built by chains of the p_b2mm rod symmetry group (Figure 9c).

Bijvoetite-(Y), **45** [96,97], is the most complex compound among the layered uranyl carbonates (Table 2) with a structure based on the uranyl carbonate chains (Figure 9d) linked through the *REE*-centered polyhedra. While meyrowitzite, **46** [98], has the largest TI and SI complexity parameters (Table 2; Figure 9e) among the uranyl carbonate compounds.

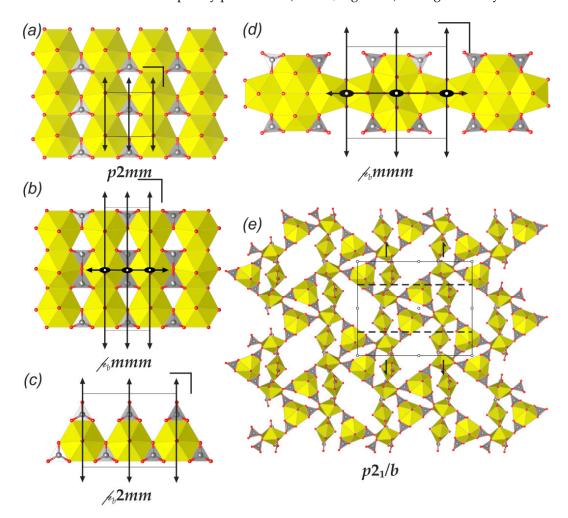


Figure 9. Uranyl carbonate complexes and their topological symmetry groups. Legend: see Figure 7. See text for details.

5. Conclusions

Comparison of crystal–chemical characteristics of isotypic natural and synthetic compounds can give an answer to the environmental conditions of mineral growth. For instance, the majority of synthetic analogs of minerals were obtained from aqueous solutions at room temperature. This observation allows us to assume that the formation of natural uranyl carbonates does not need any specific environmental conditions (increased P or T), which was recently suggested for uranyl selenites [127] and uranyl sulfates [126].

Structural and topological complexity calculations demonstrate that information content, in general, is usually higher for minerals than for synthetic compounds of similar or close chemical composition, which is likely to point to the higher stability and preferred architectures of natural compounds. However, one interesting feature that was not observed during recent complexity studies of uranyl selenite and sulfate compounds should be noted. A significant portion of compounds have the real symmetry of the structure higher than the structural symmetry of the uranyl carbonate complex. It should be also kept in mind that uranyl carbonate substructural units have average topographical diversity, and mainly include the finite clusters with rigid, edge-sharing manner, of coordination polyhedra

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polymerization. Thus the structural architecture of uranyl carbonates is largely governed by the interstitial cations and the hydration state of the compounds, while uranyl carbonate complexes play the role of flexible structural skeleton or stone aggregates in concrete.

Author Contributions: Conceptualization, V.V.G. and J.P.; Methodology, V.V.G., S.A.K., I.V.K. and J.P.; Investigation, V.V.G., S.A.K., I.V.K. and J.P.; Writing-Original Draft Preparation, V.V.G., S.A.K., I.V.K. and J.P.; Writing-Review & Editing, V.V.G. and J.P.; Visualization, V.V.G. and I.V.K. All authors have read and agreed to the published version of the manuscript.

Funding: This research was funded by the Russian Science Foundation (grant 18-17-00018 to V.V.G. and I.V.K.), by the President of Russian Federation grant to leading scientific schools (grant NSh-2526.2020.5 to S.A.K.) and through the Czech Science foundation (project 20-11949S to J.P.).

Acknowledgments: We are grateful to reviewers for useful comments.

Conflicts of Interest: The authors declare no conflict of interest.

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