



# Center for Advanced Multimodal Mobility Solutions and Education

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## **DETERMINATION OF FREEWAY ACCELERATION LANE LENGTH FOR SMOOTH AND SAFE TRUCK MERGING**

### **Final Report**

by

Yi Qi, Ph.D., P.E. (ORCID ID: <https://orcid.org/0000-0002-6314-2626>)

Professor and Chair, Department of Transportation Studies, Texas Southern University

Phone: 1-713-313-6809; Email: [Yi.Qi@tsu.edu](mailto:Yi.Qi@tsu.edu)

Qun Zhao (ORCID ID: <https://orcid.org/0000-0003-3760-9234>)

Research Associate, Department of Transportation Studie, Texas Southern University

Phone: 1-713-313-1854; Email: [qun.zhao@tsu.edu](mailto:qun.zhao@tsu.edu)

Shaojie Liu (ORCID ID: <https://orcid.org/0000-0001-5330-3871>)

Graduate Research Assistant, Department of Transportation Studies, Texas Southern University

Phone: 1-713-313-1854; Email: [liushaojie03051994@gmail.com](mailto:liushaojie03051994@gmail.com)

Wenrui Qu (ORCID ID: <https://orcid.org/0000-0003-4139-3544>)

School of Mathematics and Statistic,

Qilu University of Technology (Shandong Academy of Sciences)

City of Jinan, Shandong Province, P.R. China, E-mail: [quwenrui601@163.com](mailto:quwenrui601@163.com)

Juan Li (ORCID ID: <https://orcid.org/0000-0003-2416-5013>)

Graduate Research Assistant, Department of Transportation Studies, Texas Southern University

Phone: 1-713-313-1854; Email: [seija1026@gmail.com](mailto:seija1026@gmail.com)

for

Center for Advanced Multimodal Mobility Solutions and Education

(CAMMSE @ UNC Charlotte)

The University of North Carolina at Charlotte

9201 University City Blvd

Charlotte, NC 28223

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## **EXECUTIVE SUMMARY**

Freeway entrance ramp has intensive vehicle merging activities that lead to delay and potentially high risk of collision between merging and freeway vehicles, especially for the ramps with a high percentage of heavy truck volume. Sufficient length of acceleration lane is critical for the traffic operations at the ramp merging sections. Currently, most DOTs employ the guidelines provided in the American Association of State Highway and Transportation Officials (AASHTO) Green Book, “A Policy on Geometric Design of Highways and Streets” (AASHTO 2011). However, AASHTO’s acceleration lane length design guideline was developed based on passenger cars and hasn’t been updated for years since 1965. In addition, AASHTO other design guidelines and previous studies mainly considered the speed differential between the on-ramp and freeway vehicles on determining freeway acceleration lane length. Only a few of them considered traffic volume, and even less gave special considerations on the heavy trucks that need more time to accelerate and find larger gaps to merge.

This research developed an analytical model for estimating the required freeway acceleration lane lengths for both heavy trucks and passenger cars. The model considers both the acceleration and gap searching needs of the merging vehicles. As a result, it can take account of the impacts of the freeway traffic volume into the estimation of the required acceleration lane length. A case study was conducted in Houston, TX to demonstrate the model application. Finally, this research provides a chart and a lookup table for estimating required acceleration lane lengths for both heavy trucks and passenger cars under different traffic volume conditions for different combinations of the freeway and entrance ramp design speeds.

# Chapter 1. Introduction

## 1.1 Problem Statement

Freeway entrance ramp locations have intensive vehicle merging activities that lead to delay and potentially high risk of collision between merging and freeway vehicles, especially for the locations where high truck volume present. Sufficient length of acceleration lane is critical for traffic safety at the ramp merging sections. Currently, the existing roadway design guidelines, such as American Association of State Highway and Transportation Officials Green Book (AASHTO, 2011), determine the required acceleration lane length mainly based on the design speeds of the freeway and the on-ramps. Actually, for the freeways with high traffic volume, the acceleration lane should also provide sufficient time and space for drivers to find an acceptable gap prior to merging. Therefore, the length of the acceleration lane should be sufficient for both vehicle acceleration and gap searching purposes. Figure 1.1 shows the elements that should be considered in the design of freeway acceleration lanes.

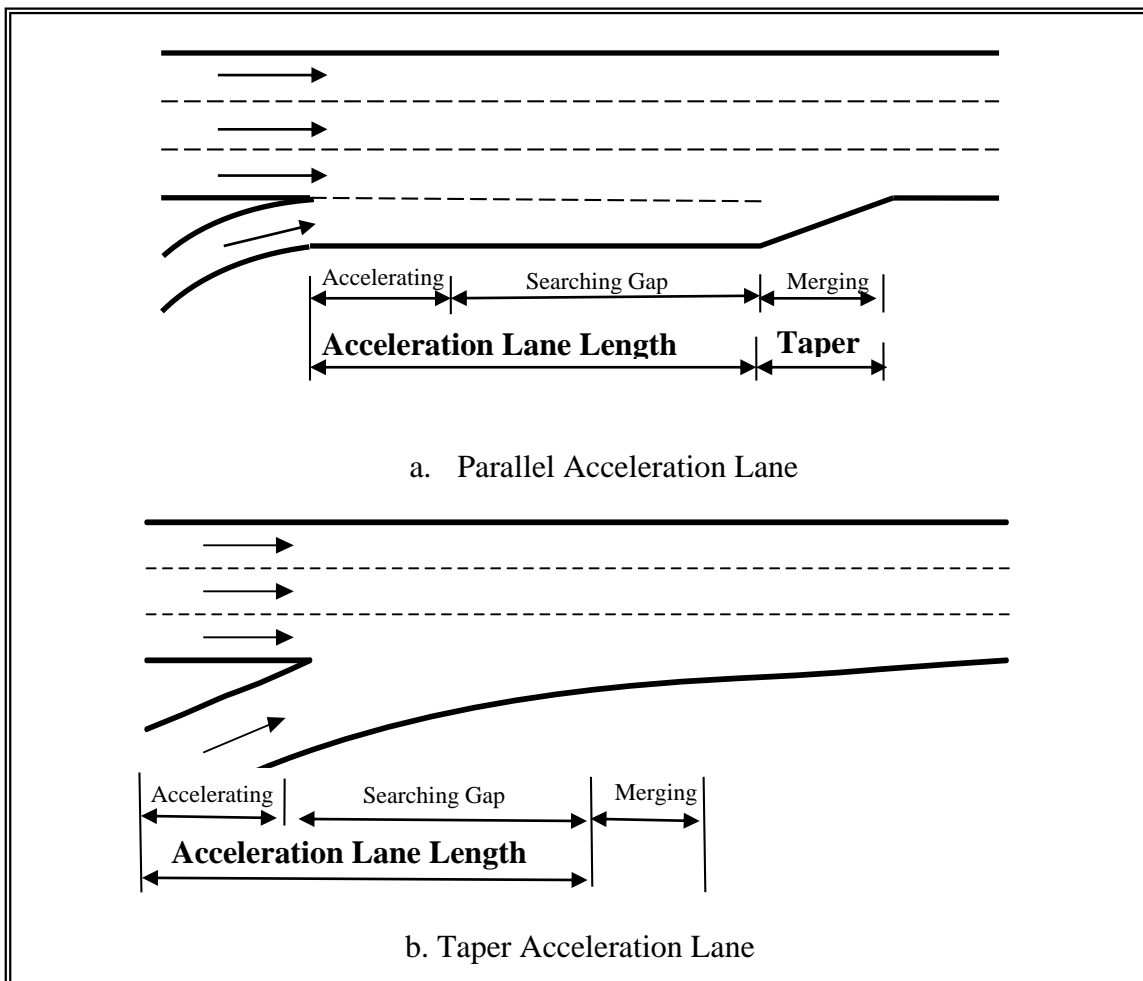


Figure 1. 1: Freeway Acceleration Lane Design Elements

For the freeways with higher traffic volumes, the on-ramp vehicles often need longer times to find an acceptable gap and, thereby need a longer merging distance. Therefore, longer acceleration lanes should be provided at locations with higher traffic volumes. However, the existing guidelines and studies on freeway acceleration lane length rarely consider the impacts of freeway traffic volume and are mainly based on the speed differential between the freeway and the on-ramp. As a result, the required length of the acceleration lane is often underestimated, especially for the locations with high freeway traffic volumes.

In addition, a few existing studies gave special considerations on the heavy trucks that need more time to accelerate and to find a larger gap to merge. Nowadays, over 70% of the freight tonnage is moved by heavy trucks in the United States. For roadways where a high percentage of truck volume present, it is necessary to consider the effects of heavy trucks in the roadway design to ensure the efficiency of freight transportation. With the increase of the overall traffic volume and freight transportation, there is a need to update AASHTO and other freeway acceleration lane design guidelines by considering heavy trucks' characteristics.

To fill the gaps in the existing studies, this research developed an analytical model for estimating the length of freeway acceleration lanes according to the merging distance required by the on-ramp vehicles. This model considers both the acceleration and gap searching needs of the merging vehicles. As a result, it can consider the impact of the freeway traffic volume on the required acceleration lane length. In addition, to ensure the safe merging of heavy trucks, this model takes account of the operational characteristics of heavy trucks into the estimation of the freeway acceleration lane length. The developed model was validated by a case study at an on-ramp location in Houston, Texas. The results of the case study showed that the model can produce reasonable estimates of the acceleration lane lengths under different traffic volume conditions. The results of this research will complement the provisions in existing roadway design guidelines in designing freeway auxiliary lanes.

## **1.2 Objectives**

The goal of this project is to conduct an in-depth study on freeway acceleration lane length for large trucks and develop an analytical model to estimate the freeway acceleration lane lengths under different traffic conditions. The research is developed based on the CAMMSE theme of addressing the FAST Act research priority area of "Improving Mobility of People and Goods." The research is relevant to the CAMMSE research thrust, "Develop data modeling and analytical tools to optimize passenger and freight movements." Specific project objectives include:

- 1) Collect field data using Houston TranStar cameras;
- 2) Extract traffic information for developing and validating the model. Information extracted include freeway design speed, ramp design speed, traffic volume, large truck merging behaviors (merging ahead vehicles or merging behind vehicles, and average gap accepted by different types of merging trucks);
- 3) Develop a model to determine acceleration lane length whether or not considering large trucks;

- 4) Conduct a case study to demonstrate the application of the developed model;
- 5) Recommend adequate freeway acceleration lane lengths under different traffic conditions.

### **1.3 Report Overview**

The rest of this paper is organized as follows: first, a thorough literature review is presented including the existing design guidelines, previous studies of determining freeway acceleration lane length, as well as research on estimating freeway acceleration lane length. Next, the methodology to develop the proposed model is introduced and utilized with real data collected by a field study in Houston, TX. In the end, by analyzing the results, conclusions and recommendations on further acceleration lane length design are provided.

## Chapter 2. Literature Review

The literature review includes two parts: 1) the existing design guidelines on freeway acceleration lane and 2) the existing methods for estimating the freeway acceleration lane length.

### 2.1 Design Guidelines and Research on Freeway Acceleration Lane Length

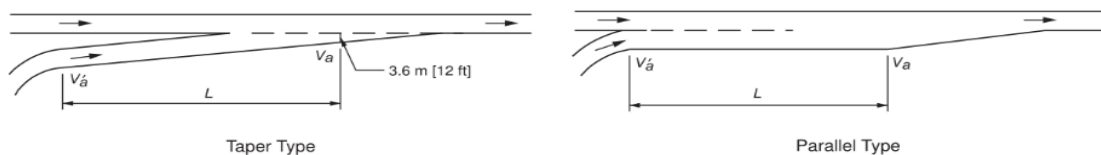
#### 2.1.1 The AASHTO Green Book (2011)

The AASHTO Green Book (2011) provided acceleration lane design guidelines used by many state transportation agencies. Three factors were considered in the determination of minimum acceleration lane length: (1) the speed at which vehicles enter the acceleration lane, (2) the acceleration behavior of vehicles at the entrance ramp, and (3) the speed at which vehicles start to merge into freeway traffic. The minimum length of an acceleration lane was presented in Table 1. The two columns listed the design speed of the freeway ( $V$ ) and the speed reached by the vehicles on the highway ( $V_a$ ). Note that  $V_a$  is around 75% of  $V$ . For the row indexes, the initial speed ( $V'_a$ ) was the speed at which vehicles just enter the acceleration lane, which was little less than the on-ramp design speed. AASHTO used the term “entrance curve” instead of “on-ramp.” Thus, the term “entrance curve design speed” was equivalent to “on-ramp design speed.” According to the AASHTO Green Book (2011) guideline, it could be seen that freeway acceleration lanes mainly depended on the design speed of the freeway ( $V$ ) and the “entrance curve design speed”, and the impact of freeway traffic volume on the vehicle merging maneuver was not considered in the design of acceleration lanes.

**Table 2. 1: Minimum Length of Acceleration Lane by AASHTO Green Book (2011).**

U.S. Customary										
Acceleration Length, $L$ (ft) for Entrance Curve Design Speed (mph)										
Highway		Stop Condition	15	20	25	30	35	40	45	50
Design Speed, $V$ (mph)	Speed Reached, $V_a$ (mph)	and Initial Speed, $V'_a$ (mph)								
		0	14	18	22	26	30	36	40	44
30	23	180	140	—	—	—	—	—	—	—
35	27	280	220	160	—	—	—	—	—	—
40	31	360	300	270	210	120	—	—	—	—
45	35	560	490	440	380	280	160	—	—	—
50	39	720	660	610	550	450	350	130	—	—
55	43	960	900	810	780	670	550	320	150	—
60	47	1200	1140	1100	1020	910	800	550	420	180
65	50	1410	1350	1310	1220	1120	1000	770	600	370
70	53	1620	1560	1520	1420	1350	1230	1000	820	580
75	55	1790	1730	1630	1580	1510	1420	1160	1040	780

Note: Uniform 50:1 to 70:1 tapers are recommended where lengths of acceleration lanes exceed 1,300 ft.



### 2.1.2 Deen (1957)

Thomas Deen (1957) studied the acceleration behavior of heavy commercial vehicles in a real-world scenario. The author conducted field study at the Lincoln Tunnel Interchange on the New Jersey Turnpike, where all vehicles entering the roadway were required to stop at a toll booth, and then accelerated and entered the turnpike via an acceleration lane. With the time data and speed data collected, the vehicle accelerations were able to be calculated. All of the data are concerned with vehicle accelerations on a level or nearly level grade.

The data set was divided into four categories of vehicles: 51 buses, 59 single-unit trucks, 55 single trailer axle semi-trailer trucks, and 39 tandem trailer axle semi-trailer trucks. Only loaded vehicles were included in the sample.

After data analysis, it was noted that semi-trailer trucks with single trailer axles and ones with tandem trailer axles had approximately the same acceleration characteristics. The two categories were not statistically significantly different, so the data from the two categories were combined into a single semi-trailer truck category.

It was found that: 1) single unit trucks accelerate at a higher rate than other heavy commercial vehicles at speeds below 29 miles per hour; 2) buses accelerate at a greater rate above 29 miles per hour; 3) semi-trailer trucks accelerate at the lowest rate of the commercial vehicles studied.

In addition, the author found acceleration lanes designed under current length standards are adequate for single unit trucks for all highway design speeds of 50 miles per hour or less and are adequate for semitrailer trucks for all highway design speeds of 30 miles per hour or less. Design of acceleration lanes based on the acceleration characteristics of the assumed SU or C-50 design vehicles as determined from the society of automotive engineers truck ability prediction procedure does not appear justified, nor are they required to accommodate most heavy commercial vehicles. Therefore, following table was recommended to determine acceleration lane length required for these vehicles (see Table 2.2). Comparing with the AASHTO Green Book (2011) recommendations in Table 2.1, it could be seen that, at the same freeway and ramp design speeds, a longer acceleration lane was recommended by this study because the acceleration behavior of heavy trucks was considered.

**Table 2. 2: Acceleration Lane Lengths for Semi-Trailer Trucks.**

Design speed(mph)	Assumed truck running speed(mph)	Entrance curve design speed(mph)									
		0	5	10	15	20	25	30	35	40	
		Assumed actual entrance speed(mph)									
		0	5	10	14	18	22	26	30	34	
30	22	290	275	240	190	110	-	-	-	-	
40	29	700	685	650	600	520	410	210	-	-	
50	35	1240	1225	1190	1140	1160	950	750	460	100	
60	40	1820	1805	1770	1720	1640	1530	1330	1040	680	

Source: Thomas Deen (1957)

### 2.1.3 NCHRP REPORT 505 (2003)

In NCHRP Report 505, the research team reviewed the range of dimensions and performance characteristics of trucks currently used on U.S. highways and predicted how these characteristics may change in response to current political, economic, and technological trends. The objective of this research is to evaluate whether the proposed geometric design (Table 2.1) in AASHTO Green Book (2001) was capable of accommodating heavy trucks.

The evaluation of the recommendation table in Green Book, was conducted using the truck speed profile model (TSPM) to determine the weight-to-power ratios implied by the design values. Table 2.3 shows the maximum weight-to-power ratio of a truck capable of achieving the given conditions as specified in Table 2.1, assuming a 0 percent grade.

**Table 2. 3: Maximum weight-to-power ratios for minimum acceleration lengths (0 percent grades)**

Maximum weight-to-power ratio (lb/hp) capable of reaching $V_a$ given $V'_a$ for 0 percent grades over acceleration lengths as specified in Table 62										
Highway	Stop condition	15	20	25	30	35	40	45	50	
Design speed, $V$ (mph)	Speed reached, $V_a$ (mph)	And initial speed, $V'_a$ (mph)								
		0	14	18	22	26	30	36	40	44
30	23	105	140	–	–	–	–	–	–	–
35	27	110	120	130	–	–	–	–	–	–
40	31	105	115	120	125	120	–	–	–	–
45	35	120	120	125	135	135	135	–	–	–
50	39	120	120	120	120	120	125	145	–	–
55	43	120	120	115	120	120	120	120	130	–
60	47	110	115	115	115	110	115	110	120	130
65	50	110	110	110	110	110	115	110	110	110
70	53	105	105	105	105	105	105	105	105	105
75	55	105	105	100	100	105	105	105	105	100

Table 2.3 indicates that trucks with weight-to-power ratios in the range of 100 to 145 lb/hp have sufficient acceleration capabilities to achieve the given speeds within the minimum acceleration lengths, assuming a 0 percent grade. However, the 2001 Green Book used a 200-lb/hp truck to represent of the size and type of vehicle normally used for design control of major highways and that current field data indicate that on the freeways the 85th percentile weight-to-power ratios of trucks fall within a fairly narrow range around 170 to 210 lb/hp, this analysis indicates that the underlying assumptions for estimating the minimum acceleration lengths in Table 2.1 do not necessarily account for the performance capabilities of heavily loaded vehicles. It appears that the 2001 Green Book criteria can accommodate an average truck, but not a heavily loaded truck. Although it was not recommended to update the AASHTO guideline at that point, further research on this issue was recommended.

Finally, the NCHRP report provides guidance for roadway geometric designers on how best to accommodate large trucks on the U.S. highway system.



**Table 2. 4: Minimum acceleration lengths for a 180 lb/hp truck**

Acceleration length, L (ft), necessary for entrance curve to enable a 180 lb/hp truck to reach $V_a$ given $V'_a$ for a 0 percent grade										
Highway Design speed, V (mph)	Stop condition Speed reached, $V_a$ (mph)	And initial speed, $V'_a$ (mph)								
		0	15	20	25	30	35	40	45	50
30	23	275	160	–	–	–	–	–	–	–
35	27	400	300	230	–	–	–	–	–	–
40	31	590	475	400	310	170	–	–	–	–
45	35	800	700	630	540	400	240	–	–	–
50	39	1100	1020	950	850	720	560	200	–	–
55	43	1510	1400	1330	1230	1100	920	580	240	–
60	47	2000	1900	1830	1740	1600	1430	1070	760	330
65	50	2490	2380	2280	2230	2090	1920	1560	1220	800
70	53	3060	2960	2900	2800	2670	2510	2140	1810	1260
75	55	3520	3430	3360	3260	3130	2960	2590	2290	1850

(Source: NCHRP Report 505, 2003)

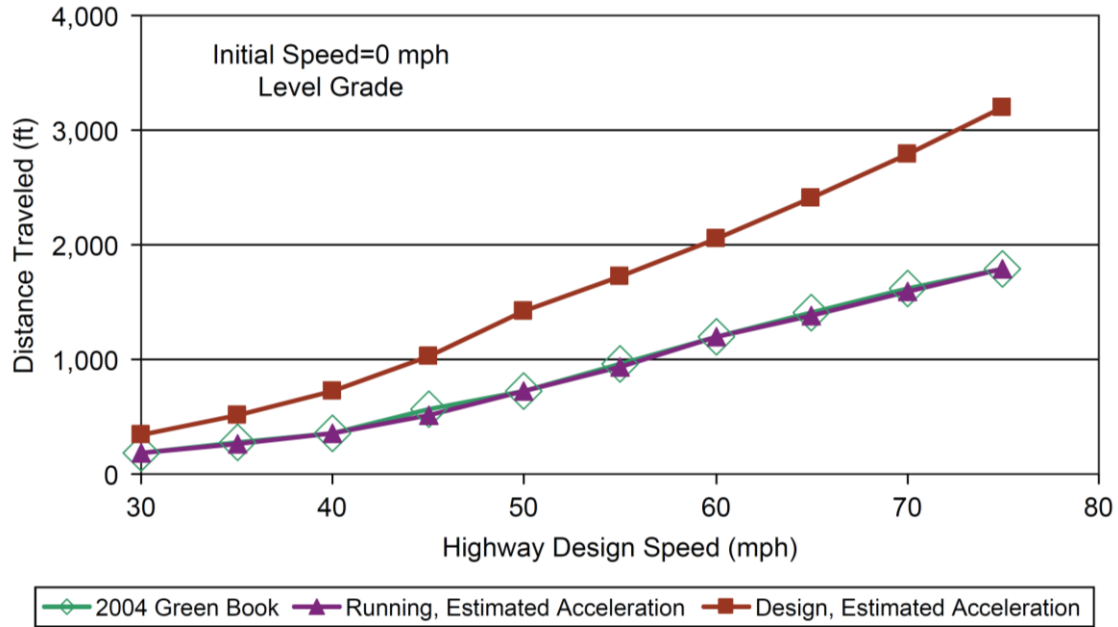
#### 2.1.4 Fitzpatrick and Zimmerman (2007)

Fitzpatrick and Zimmerman (2007) examined and reproduced the design guidance for the acceleration lane length provided by the AASHTO Green Book 2004. The 2004 Green Book provides design criteria for entrance ramp acceleration lengths, which are similar to the values included in A Policy on Geometric Design of Rural Highways (*the Blue Book*) published by AASHTO in 1965. The procedure used to generate the acceleration lengths included in the 1965 Blue Book is based upon speeds on ramps, acceleration behavior, and speeds on limited-access roads. The assumptions are outdated and need more current information.

Moreover, the authors provided a summary of how acceleration lane length could be calculated using several different existing methodologies. The methodologies to calculate acceleration lane lengths include:

##### Calculated Through Use of Design Speed

When design speed is used rather than running speed within the methodology identified from the Blue Book, the acceleration lengths increase significantly. As shown in Figure 2.1, for a highway design speed of 70 mph (113 km/h), the acceleration lengths would change from 1,600 to 2,800 ft (488 to 854 m). The use of acceleration performance that is more representative of current vehicles may offset some of the increase caused by using design speed rather than running speed.



**Figure 2. 1: Acceleration lengths from use of design speed or running speed and Blue Book procedure**  
(Source: Fitzpatrick and Zimmerman, 2007)

Calculated Through Use of Equations That Produce Second-to-Second Acceleration

Another potential source for the determination of distance traveled while accelerating is vehicle performance equations. NCHRP Report 505 (2003) discussed truck characteristics with respect to critical length of grade. In addition, it also provided a spreadsheet that could be used to determine distance traveled from an assumed ramp curve speed to highway speed. A TxDOT report (2007) also investigated vehicle performance on highway facility design. A spreadsheet (5544) was generated to compare between different assumptions. This spreadsheet was used to determine potential acceleration lengths for passenger cars.

Acceleration Lengths Calculated Through Use of Constant Acceleration

The constant acceleration rate is also widely used to provide a reasonable approximation of the needed acceleration length. The authors also listed several sources with available constant acceleration rate. Figure 2.2 described the acceleration lengths calculated with different constant rates.

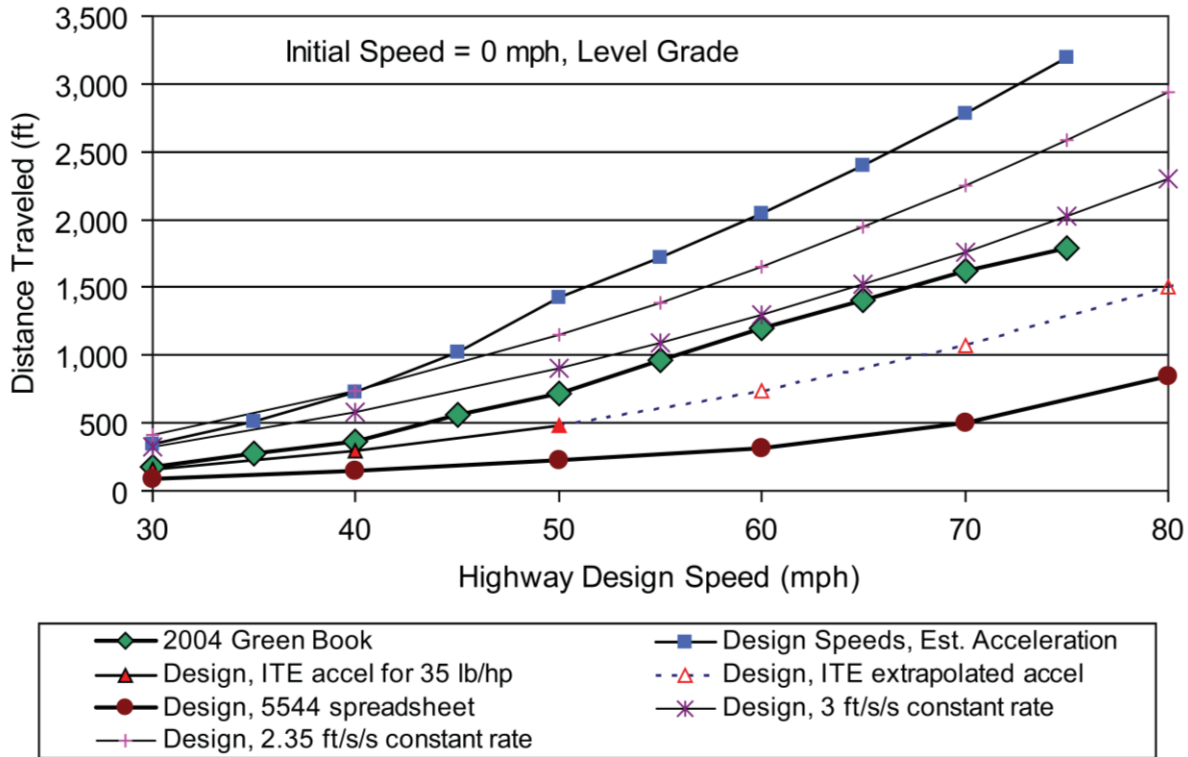


Figure 2. 2: Acceleration lengths from a stop through use of constant acceleration compared with results from 2004 Green Book (1) and 5544 spreadsheets.  
 (Source: Fitzpatrick and Zimmerman, 2007)

Finally, based on a Canadian study (Hassan, Y et al., 2006), the authors recommended an average constant acceleration rate of 2.5 ft/s<sup>2</sup> to calculate potential acceleration length. By using the updated acceleration rate, minimum acceleration lane lengths longer than that suggested by the AASHTO Green Book 2004 were recommended (see Table 2.2).

Table 2. 5: Minimum Acceleration Lane Length Recommended by Fitzpatrick and Zimmerman (2007).

Highway design speed(mph)	Entrance curve design speed(mph)								
	0	15	20	25	30	35	40	45	50
30	389	292	216	-	-	-	-	-	-
35	529	432	357	259	-	-	-	-	-
40	691	594	519	421	303	-	-	-	-
45	875	778	702	605	486	346	-	-	-
50	1080	983	908	810	691	551	389	-	-
55	1301	1210	1134	1037	918	778	616	432	-
60	1556	1459	1383	1286	1167	1026	864	681	475
65	1826	1729	1653	1556	1437	1297	1134	951	746
70	2118	2020	1945	1848	1729	1588	1426	1243	1037
75	2431	2334	2258	2162	2042	1902	1740	1556	1351

### 2.1.5 Hunter and Machemehl (1997), Hunter et al. (2001)

In their report, Hunter and Machemehl (1997) evaluated the appropriateness of AASHTO minimum allowable ramp design speed, as well as the adequacy of high-speed ramp lengths designed by AASHTO criteria. In order to evaluation of freeway entry ramp design speed criteria, an examination of assumptions regarding ramp vehicle acceleration and deceleration rates, as well as of gap seeking and acceptance behavior are important.

In this study, the videotaping method was used to conduct field data collection. Twenty sites were selected along freeways in Houston, San Antonio, Dallas and Austin, Texas. After processing data collected, authors presented several approaches to modeling ramp driver acceleration/deceleration behavior. By analyzing results, authors determined that observed ramp driver acceleration rate and AASHTO values were comparable. However, it was suggested that acceleration lengths for taper-type entry ramps should include only the lane portions from which ramp drivers can clearly view the freeway right-lane traffic, which leads to a recommendation that AASHTO acceleration lane length measurement model should be modified for taper type ramps.

Another study by Hunter et al. (2001) also indicated that the design length of acceleration lanes should fully consider drivers' views of the freeway right-lane traffic. This is because most drivers on a ramp with adequate sight distance tend to travel to the end of the speed change lane before merging; for ramps where drivers' views are obstructed, drivers are more likely to aggressively merge from any location beyond the gore to avoid being trapped at the end of the acceleration lane.

### 2.1.6 Gattis et. al (2008)

Gattis et. al (2008) examined attributes associated with tractor-trailer trucks accelerating on freeway entry ramps and entering the main traffic lanes. The authors studied the acceleration behavior of tractor-trailer trucks in actual operating conditions, and based on the observations evaluate the adequacy of current acceleration lane lengths and determine if longer lengths are needed to accommodate these larger trucks. Other attributes examined included truck speeds at various distances from the scales, freeway volumes, and freeway grades.

Data used in this research were collected at four separate commercial vehicle weigh stations in Arkansas and one in southwest Missouri using weigh-in-motion systems, static scales, video cameras, and lidar guns. This equipment provided speed and distance data that were correlated to the weight of each measured truck. The weights of the majority of the tractor-trailer trucks measured during this research project ranged from 40,000 to 80,000 pounds. The percentage of trucks present in the freeway traffic flow ranged from 14% to 52%. These percentages were based on traffic counts performed by the Arkansas Highway and Transportation Department in 2006 and the Missouri Department of Transportation in 2007.

The data for this project were analyzed using both graphical and statistical techniques including data distribution graphs and statistical significance tests. The effects that truck weight, freeway volume, and roadway grade had on the speeds of the measured truck were examined and compared among the data collection sites. From the data, mathematical models

that predicted the average and 10th percentile speeds for tractor-trailer trucks at each of three grade-groups (slight downgrade, nearly level, slight upgrade) were developed.

With the model developed in this research project, the authors proposed acceleration lane lengths considering tractor-trailer trucks.

Table 2.6 compares the acceleration lane lengths recommended in other literature with the models from this research project. It can be seen that the acceleration lane lengths proposed by Deen, NCHRP Report 505, and the model developed during this research are substantially longer than those proposed by both the AASHTO Green Book and Fitzpatrick and Zimmerman. One possible reason may be both the AASHTO and the Fitzpatrick and Zimmerman recommendations were based on passenger cars, not heavy trucks.

**Table 2. 6: Acceleration Lane Lengths from Reviewed Sources and the Proposed Acceleration Lane Lengths from Research Project**

	Deen 1957	AASHTO Green Book 2004	NCHRP Rept. 505 2003	Fitzpatrick and Zimmerman 2006	This study 2008
assumed initial speed (mph)	22	22	22	20	17
distance (ft) to reach	39 mph 40 mph 50 mph 55 mph 60 mph	- 1530 - 1020 - - - - -	- - 850 2230 3260 -	- 908 1383 1653 1945	- 1203 2119 2731 3655

NOTES:

1. Deen distances stated for semi-trailer trucks
2. AASHTO 2004 distances are not specifically for trucks; are similar to 1965 distances stated for passenger cars
3. NCHRP 505 distances are for a 180 lb/hp truck on a 0% grade
4. Fitzpatrick and Zimmerman distances are for passenger cars. The values listed in each row of this table for Fitzpatrick and Zimmerman are their values for a design speed that is 10 mph above the speed in the row in this table.
5. 2008 distances were calculated with the revised "level" unimpeded average truck speed model

### 2.1.7 Bareket & Fancher (1993)

In their study, Bareket & Fancher (1993) simulated the operation of various longer combination vehicles (LCV) on roadways and highways that are typical in Michigan. By analyzing the simulation results, necessary highway design modifications to accommodate each truck combination were identified, including highway acceleration lane length.

To investigate the acceleration related performance levels for different LCVs, two situations were considered in this study: 1) an actual roadway section from the drawings provided by Michigan Department of Transportation (MDOT), and 2) a generic situation which involving hypothetical long continuous grades and trucks that are represented by mere weight-to-power ratios.

Actual situation

For the actual roadway section, two sites were studied: the first site was departing Lakeview Drive from Jackson Road, merging with the eastbound traffic on I-94, and the second site was departing ramp I from Whittaker Road, merging with the westbound traffic on I-94. Calculation results for each site were plotted as an accumulative portrayal of speed vs. distance for the combinations studied.

Figure 2.3 shows the calculation results of Jackson Roan as an accumulative portrayal of speed vs. distance. It can be seen when concerning the acceleration from speed, the tractor-semitrailer (TST) configurations (both 48 ft and 57 ft) perform best, while the triple is the slowest combination. When the specific-power values are considered, this observation can be rationalized: the semitrailers have 232 lb/hp, while the other combinations all have higher values.

Another finding from Figure 2.3 is all the trucks perform similarly during the initial stages of the acceleration (up to about 1,000ft). As the progress, there is an approximately 5 mph difference between the fastest combinations (semitrailers) and the slowest combination(triple). Therefore, to reach a speed of 45 mph, the triple needs an additional 1,000 ft.

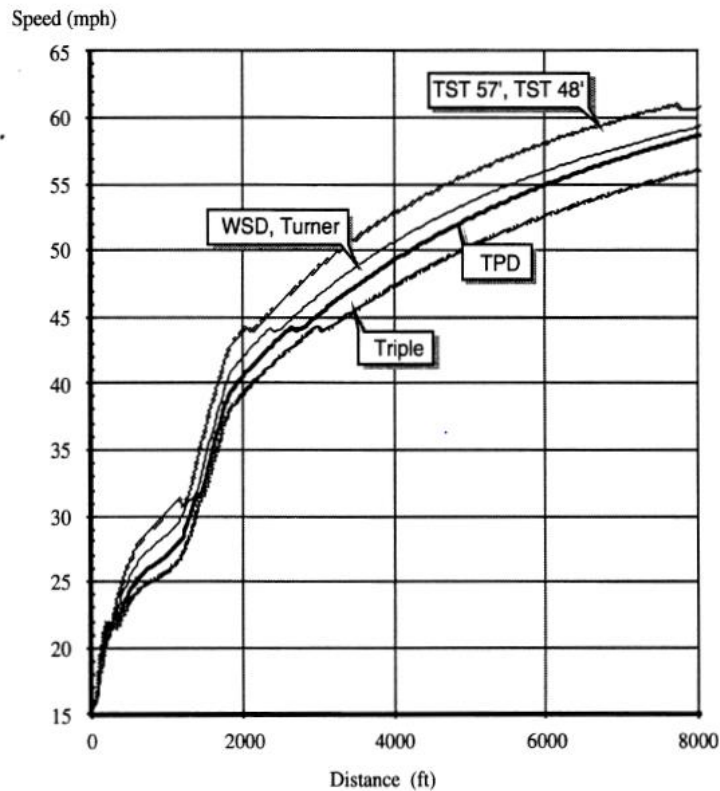


Figure 2. 3: Acceleration from Speed – Jackson Road to I-94 eastbound

With the results from the actual roadway situation, authors concluded that on average, an additional 1,000 ft of merging lanes should be provided to maintain the current speed differential between merging and highway traffic.

### Generic Situation

Generic situation simulated trucks with different weight-to-power values. For the purpose of this analysis, LCVs were represented as three groups: 230, 265 and 300 lb/hp. Performance levels of these generic trucks were evaluated on level roads and roads that had 2% and 4% grades. Calculation results were tabulated and then plotted as distances it took to reach certain final speeds from different initial speeds.

Figure 2.4 shows the acceleration results from an initial speed of 22 mph on a 2% grade. It indicates that if trucks with 300 lb/hp are to perform at the level of trucks with 230 lb/hp, then the merging/acceleration lanes need to be extended.

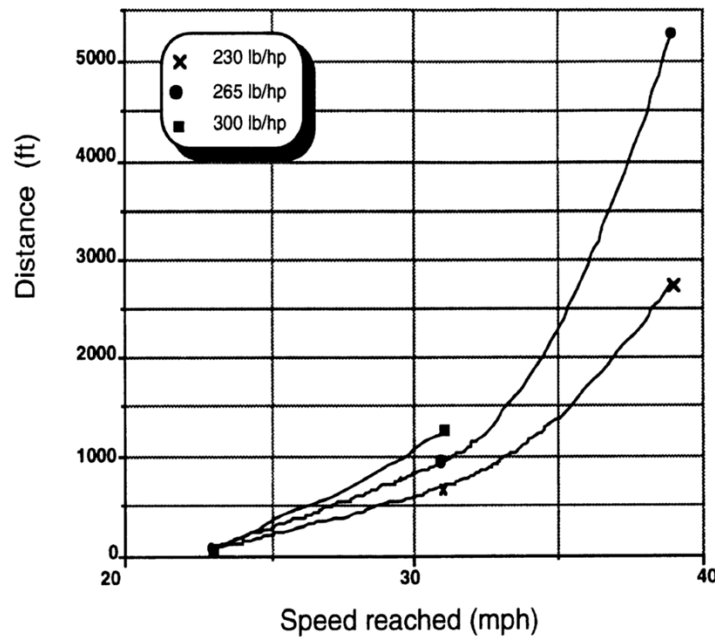


Figure 2. 4 Acceleration from 22 mph on a 2% grade

The authors further concluded that there is a linear relationship between the required lane extension and the current length. An equation representing the linear relationship between existing acceleration lanes length and an extension in length for LCVs was proposed:

$$\Delta L = 0.31 L$$

where:

L is the length of the existing acceleration lane

$\Delta L$  is the required extension for the acceleration lane

#### 2.1.8 Long (2000)

Long (2000) did a study on the acceleration characteristics of starting vehicles. The design accelerations in the AASHTO acceleration values were found to deviate substantially from observed accelerations. At the start of motion, observed accelerations were about 15% faster for passenger cars and 45% faster for single unit trucks than design accelerations. As speed increased, observed accelerations dropped three to four times faster than design accelerations

for these vehicles. In the study, the linearly decreasing design acceleration rates for different classes of vehicles in different design situations are recommended, and revisions for Green Book parameters and charts are suggested. For normal passenger cars, the average acceleration of  $4.72 \text{ ft/s}^2$  over a speed range of 0 to 25 mph is recommended. For loaded trucks, an average acceleration of  $0.47 \text{ ft/s}^2$  is recommended.

### 2.1.9 Other Studies

Many studies have found that the current design guidelines of the acceleration lane are not sufficient for heavy trucks.

In a research conducted by TTI (2003), it was found that “merge areas and acceleration lanes” were the most challenging driving circumstances voted by truck drivers. Drivers had perceived that many freeway acceleration lanes don’t provide adequate space for a large truck to accelerate and merge with the freeway traffic stream. Furthermore, in a recent study on truck safety conducted by Qi et al. (2018), freeway short merging distance was also identified as one of the top ten risk factors contributing to large truck crashes.

## 2.2 Methods for Estimating the Freeway Acceleration Lane Length

As shown in Figure 1.1, a freeway acceleration lane would include two sections, acceleration section, and gap searching section. The acceleration section provides the necessary lane length required by the ramp vehicles to accelerate until the desired speed is reached, which can be obtained directly by the inputs of initial speed, acceleration rate, and desired speed. The merging section is, however, more complicated than the acceleration section for it has to involve studies on gap acceptance and driving behaviors.

In the merging process, the merging maneuver is a process of rejecting and accepting different gaps. Greenshields et al. (1947) defined the critical gap as the “acceptable average-minimum time gap”. Different drivers would have different critical gaps depending on their driving behavior. Usually, an aggressive driver is more likely to accept a smaller gap than a vigilant driver who expects a longer gap to merge safely. Moreover, even for the same driver, the critical gap can vary according to geometry features of ramps, traffic volumes and weather conditions.

Liu and Wang (2012) provided an analytic framework for calculating the on-ramp acceleration length integrating human factors, vehicle dynamic characteristics, roadway surface condition and on-ramp weaving design. Two driver behaviors, merging ahead (vehicles move at a speed higher than the average freeway speed to search for an acceptable gap to merge) and merging behind (vehicles keep moving at a speed a little lower than the freeway average speed to wait for an acceptable gap to merge) were separated for analysis in this study. The relationship between the acceleration lane length and the speed differential between on-ramp and freeway vehicles were investigated. This is the first study that investigated the required acceleration lane length from a vehicle merging behavior point of view. However, it did not consider the distance caused by searching for an acceptable gap prior to merging.

Song (2010) derived a model to determine both acceleration and deceleration lane length on Urban Expressway. In his study, the acceleration lane length consists of three sections,



acceleration length, merging length and width transition length. By combining the probability theory and differential methods, a model of calculating the length of the waiting merging section was established. However, the model developed in this paper did not consider the characteristics of large vehicles and the different driving behaviors during the merging process.

### Chapter 3. Methodology

In this study, the length of a freeway acceleration lane was estimated according to the merging distance required by on-ramp vehicles (including both passenger cars and heavy trucks) during the merging process.

As indicated in Figure 3.1, the total acceleration lane length ( $L$ ) includes two parts: 1) acceleration length ( $L_1$ ), which enables a vehicle to accelerate from the ramp speed to near freeway speed prior to merging and 2) gap searching length ( $L_2$ ), which provides the moving vehicle the distance to find an acceptable gap prior to merging. After that, the vehicle will adjust its speed to merge to the freeway traffic flow. This part of merging could also be accomplished by using the taper at the end of the acceleration lane or on the freeway main lane. In this study, only the acceleration length and gap searching length were considered in determining the acceleration lane length. Note that the “gap searching length” is only applicable to a freeway location with substantial traffic volume. If the freeway traffic volume is always very light and vehicles can merge easily without waiting for any gaps, this part of the length could be zero. The required acceleration lane lengths by heavy trucks and passenger cars were estimated as follows.

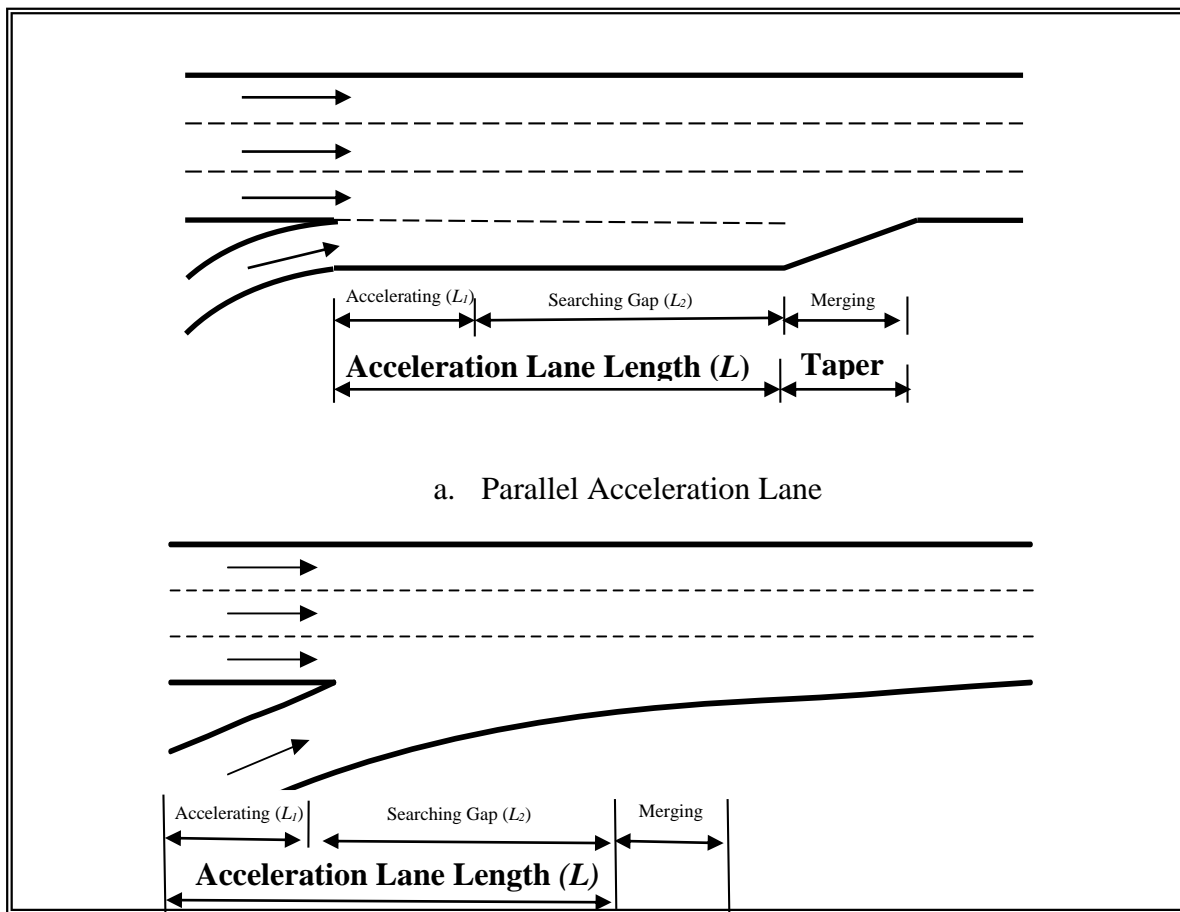


Figure 3. 1: Freeway Acceleration Lane Design Length

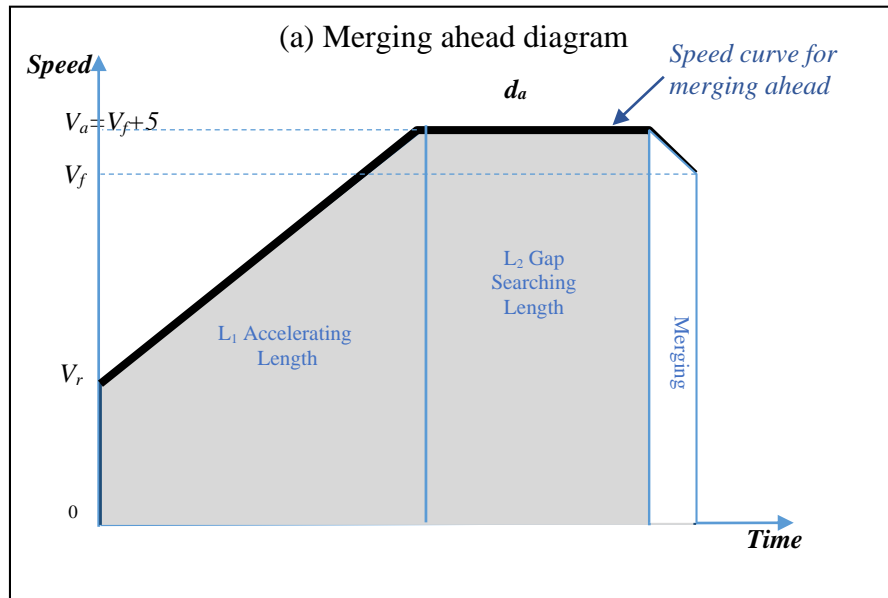
### 3.1 Model for Freeway Acceleration Lane Length

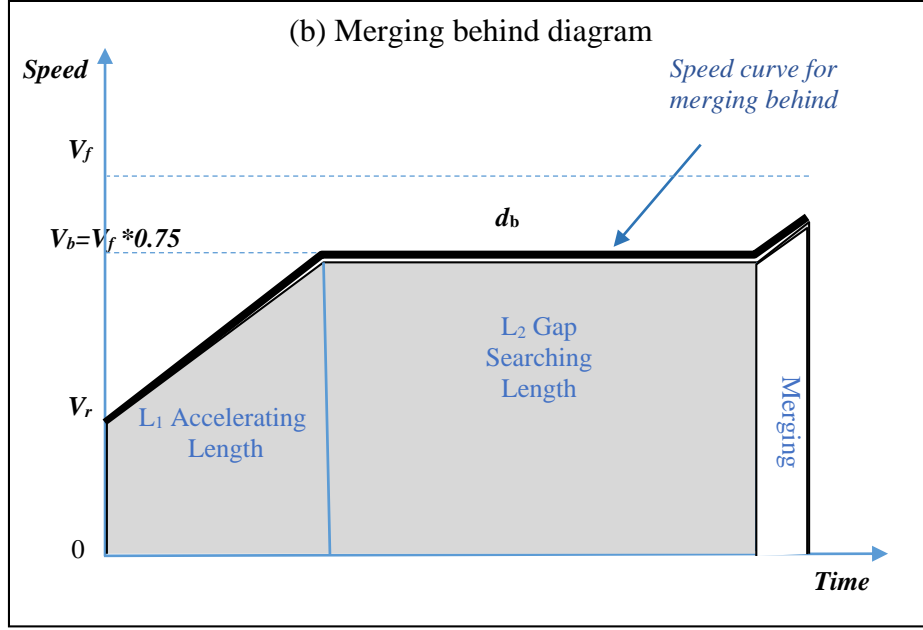
Since the acceleration lane length ( $L$ ) is defined as the sum of acceleration ( $L_1$ ) and gap searching ( $L_2$ ), we have

$$L = L_1 + L_2 \quad (1)$$

As mentioned before, two merging behaviors, merging ahead and merging behind were considered in developing the model. Because the speeds are different for these two merging behaviors, the required acceleration lane lengths are different. In this research, the speed for merging ahead behavior ( $V_a$ ) is assumed as the freeway design speed ( $V_f$ ) plus 5 mph and the speed for merging behind behavior ( $V_b$ ) is assumed as the 75% of the freeway design speed according to the actual speed reached by vehicles suggested by AASHTO green book (see Table 2.1 ).

For both merging ahead and behind situations, there are two stages in the process. (1)  $L_1$ , vehicles accelerate from the ramp speed ( $V_r$ ) to speed ( $V_a$ ) or speed ( $V_b$ ) (2)  $L_2$ , vehicles keep searching for an acceptable gap while moving at the constant speed  $V_a$  or  $V_b$ , where the searching time (also referred to as merging delay) is noted as  $d_a$  or  $d_b$ . This overall merging process can be presented by the speed and time diagram in Figure 3.2.





$V_r$  is ramp design speed;  $V_f$  is freeway design speed;  
 $V_a$  is gap searching speed,  $V_a = V_f + 5\text{mph}$  for merging ahead;  
 $d_a$  is gap searching time or merging delay for merging ahead;  
 $V_b$  is gap searching speed,  $V_b = V_f * 0.75\text{mph}$  for merging behind;  
 $d_b$  is gap searching time or merging delay for merging behind.

**Figure 3. 2: Speed and time diagram for merging ahead and merging behind cases**

According to Figure 3.1, the total distance traveled by the merging vehicle can be calculated as the area below the speed curve (the shaded area in Figure 2), which is the minimum required length for the acceleration lane in both situations and can be mathematically expressed by Equation 2 and Equation 3, respectively

$$L_a = L_{1a} + L_{2a} = \frac{V_a^2 - V_r^2}{2a} + V_a d_a \quad (2)$$

$$L_b = L_{1b} + L_{2b} = \frac{V_b^2 - V_r^2}{2a} + V_b d_b \quad (3)$$

Where

$L_a$  is the acceleration lane length for merging ahead (m),

$L_b$  is acceleration lane length for merging behind (m),

$L_{1a}$  is the length for merging ahead vehicle to accelerate to the desired speed(m)

$L_{2a}$  is the length for merging ahead vehicles to find an available gap to merge(m)

$L_{1b}$  is the length for merging behind vehicles to accelerate to the desired speed(m)

$L_{2b}$  is the length for merging behind vehicles to find an available gap(m)

$V_r$  is the ramp design speed (mps),

$V_f$  is freeway design speed (mps),

$V_a$  is the speed during gap searching for merging ahead situation (mps), which is assumed as  $V_f + 5$  mph,

$V_b$  is gap searching speed (mps) for the merging behind situation (mps), which is assumed as  $V_f * 0.75$  mph,

$a$  is the accelerate rate (ftps<sup>2</sup>), which is different for different types of vehicles and different merging behaviors. In this study,  $a$  for merging ahead is set as the maximum acceleration rate for a given type of vehicle and  $a$  for merging behind is set as the average accelerate rate for a given type of vehicle. According to Bokare and Maurya (2017),  $a$  for merging ahead passenger cars is the 2.28 m/s<sup>2</sup>;  $a$  for merging passenger cars is 0.62 m/s<sup>2</sup>;  $a$  for merging ahead heavy trucks is 0.9 m/s<sup>2</sup>, and  $a$  for merging behind heavy trucks is 0.26 m/s<sup>2</sup>.

From Equation 2 and Equation 3, it can be seen that merging delay (or gap searching time) is a critical element in estimating the length of a freeway acceleration lane.

### 3.2 Merging Delay

Drew (1965) developed a model for estimating the merging delay. The basic idea for estimating the merging delay is that the average merging delay is the product of the average number of rejected gaps and the average length of rejected gaps, which can be mathematically expressed as follows:

$$\text{Merging Delay} = \text{Average Number of Rejected Gaps} \times \text{Average Length of Rejected Gaps} \quad (4)$$

It is important to know the gap distribution to calculate the merging delay. According to Rod J. Troutbeck (1997), a negative exponential distribution is the most common distribution and would be employed in this study.

$$f(t) = qe^{-qt} \quad (5)$$

where,

$t$  is the time gap (s) in the freeway traffic flow,

$f(t)$  is the distribution of time gaps on freeway traffic flow,

$q$  is the freeway traffic volume (vps).

Assuming that the critical gap accepted by a merging vehicle for a safe merge is  $T$ , the probability of rejecting a gap can be calculated by the following equation:

$$p = p(t < T) = \int_0^T f(t)dt = 1 - e^{-qT} \quad (6)$$

Then, the probability for a driver rejecting  $n$  gaps before finding an acceptable gap to merge is

$$P_n = p^n(1 - p), n = 1, 2, \dots \quad (7)$$

The average number of gaps for which a driver has to wait is given by

$$E(n) = \sum_{n=0}^{\infty} nP_n = \frac{p}{1-p} = \frac{\int_0^T f(t)dt}{\int_T^{\infty} f(t)dt} \quad (8)$$

The average length of the rejected gaps can be calculated by the following equation:

$$E(t | t < T) = \frac{\int_0^T tf(t)dt}{\int_0^T f(t)dt} \quad (9)$$

Therefore, according to Equations 4 and 5, the average merging delay can be estimated by

$$d' = E(n) \times E(t | t < T) = \frac{\int_0^T tf(t)dt}{\int_T^{\infty} f(t)dt} = \frac{e^{qT} - qT - 1}{q} \quad (10)$$

Furthermore, some vehicles will be able to merge directly without rejecting any gaps because the first gap that they encounter is acceptable. According to Equation 7, such a proportion of vehicles is  $1 - p$  ( $n=0$  in Equation 7). Thus, the probability for a vehicle rejecting at least one gap is  $p$ . Then the average delay for the proportion of vehicles that will actually suffer delays is

$$d = \frac{d'}{p} = \frac{e^{qT} - qT - 1}{q(1 - e^{-qT})} \quad (11)$$

According to Equation 11, to derive the average merging delay, the critical gap ( $T$ ) accepted by merging drivers for a safe merging needs to be estimated first.

### 3.3 Critical Gap

According to Drew (1965), the critical gap is defined as the time gap that is just as likely to be accepted as it is to be rejected. In other words, a critical gap is the gap size where the probability of accepting such gap is equal to the probability of rejecting such a gap. Many different methods for estimating critical gap have been present (Brilon et al., 1999; Bunker and Troutbeck, 2003; Hewitt, 1983). Drew (1965) conducted a study for estimating the critical gap for freeway ramp merging. In this study, the number of rejected gaps and accepted gaps of on-ramp vehicles were collected from the field. The relationships of accepted gaps and rejected gaps with a length of gaps were drawn, respectively. Then, the critical gap was determined by the intersection point of these two curves (see Figure 3.3 as an example). In this study, the same method was used for estimating the critical gaps for both passage cars and heavy trucks that have different merging behaviors at the selected study site. Note that, heavy truck in this study refers to Class 7 and Class 8 trucks defined by FHWA [7]. The details about the estimation of the critical gaps are introduced in the case study section.

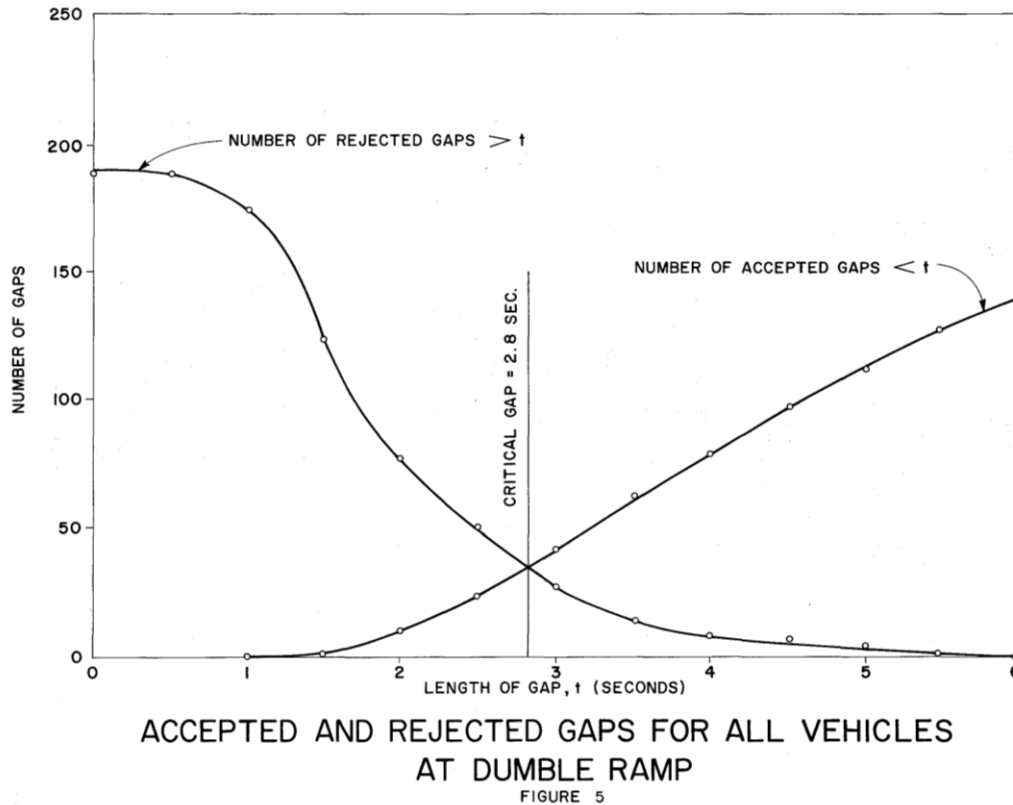


Figure 3. 3: Determination of critical gap (source: Drew, 1965)

### 3.4 The Overall Procedure for Determining Freeway Acceleration Lane Length

Overall, for the proposed method, the freeway acceleration lane length can be determined by the following 4 steps.

*Step 1. Estimate the following 4 critical gaps according to the method given in Drew (1965) as presented in Figure 3.*

- $T_a^{HT}$ : the critical gap for merging ahead heavy trucks
- $T_b^{HT}$ : the critical gap for merging behind heavy trucks
- $T_a^{PC}$ : the critical gap for merging ahead passage cars
- $T_b^{PC}$ : the critical gap for merging behind passage cars

Note that, in the case that a field study is not conducted for collecting the required data for critical gap estimation, the critical gaps estimated by this study are recommended to use as default values.

*Step 2. Estimate the following 4 merging delays based on the 4 estimated critical gaps by using Equation 11.*

- $d_a^{HT}$ : the merging delay for merging ahead heavy trucks
- $d_b^{HT}$ : the merging delay for merging behind heavy trucks
- $d_a^{PC}$ : the merging delay for merging ahead passage cars
- $d_b^{PC}$ : the merging delay for merging behind passage cars

*Step 3. Estimate the following 4 freeway acceleration lane lengths based on the 4 estimated merging delays by using Equation 2 and Equation 3.*

- $L_a^{HT}$ : the acceleration lane length for merging ahead heavy trucks
- $L_b^{HT}$ : the acceleration lane length for merging behind heavy trucks
- $L_a^{PC}$ : the acceleration lane length for merging ahead passage cars
- $L_b^{PC}$ : the acceleration lane length for merging behind passage cars

*Step 4. Determine the required freeway acceleration lane lengths*

The required acceleration lane should be able to accommodate vehicles with different merging behaviors. In other words, it will allow both merging ahead and merging behind vehicles to safely merge to the freeway. Therefore, the required freeway acceleration lane lengths for the locations with different traffic conditions (in term of heavy truck volume) can be determined as follows:

- $L^{HT} = \text{Max} (L_a^{HT}, L_b^{HT})$  for locations where heavy trucks need to be considered in the design of freeway acceleration lane
- $L^{PC} = \text{Max} (L_a^{PC}, L_b^{PC})$  for locations where heavy trucks do not need to be considered in the design of freeway acceleration lane
- Note that, since the critical gap for heavy trucks usually is larger than that of the passage cars, and the acceleration rate of heavy trucks is lower than that of the passage cars, it can be approved that  $L^{HT}$  will be greater than  $L^{PC}$ , which means if the freeway acceleration lane is long enough for merging heavy trucks, then it can also safely accommodate the merging passage cars. It depends on the traffic engineer's judgments to choose  $L^{HT}$  or  $L^{PC}$  as the final recommended freeway acceleration lane lengths for a particular location according to the truck volume or the truck safety problem at this location.



## Chapter 4. Case Study

To demonstrate the application of the developed model, a case study was conducted based on the data collected from a real-world study site. The chapter covers three parts: 1) study site and data collection, 2) determine the acceleration lane length by applying the proposed method, and 3) provide updated acceleration lane length recommendation charts and tables for different volumes based on the developed model.

### 4.1 Study Site and Data Collection

The study site is an on-ramp location on freeway SH288 southbound at exit McHard RD in Houston, Texas (Figure 4.1). At this location, the ramp speed is 40 mph and the freeway speed is 60 mph. Time periods to collect the number of accepted and rejected gaps are in the midday during 9-12 am and 2-5 pm when the traffic condition at this location is at near-congestion condition (at LOS C). It means that the safe gaps are still available for the merging vehicle, however, drivers must be very vigilant in searching gaps to merge.



Figure 4. 1: A video snapshot of the study site

In total, 76 hours of traffic video was collected. The collected traffic videos were then processed in the lab using an Excel-based tool and software called time machine, a virtual clock to derive the different type of gaps with different sizes. The following information was extracted from the video:

- Traffic volume
- Percentage of heavy trucks
- Number of accepted and rejected gaps for a particular gap size for heavy trucks (HT) and passenger cars (PC) with different merging behaviors.

Based on the observation on the recorded videos, the average traffic volume was 740 vehicles per hour per lane, the truck percentage at this location ranged from 8.9% to 14.4% during the observed time periods. Merging ahead and merging behind events were collected for both heavy trucks and passenger cars. The collected gaps for different types of merging events for heavy trucks and passenger cars are presented in Table 4.1 and Table 4.2, respectively.

**Table 4. 1: Collected Accepted and Rejected Gaps for Heavy Trucks at SH288@ McHard**

Length of Gap t (Seconds)	Merging Ahead		Merging Behind	
	No. Accept Gaps<t	No. Reject Gaps>t	No. Accept Gaps<t	No. Reject Gaps>t
$\Delta t = 1$	0	250	0	250
2	8	161	7	144
3	54	60	29	64
4	110	17	72	33
5	145	7	108	18
6	185	3	138	12
7	202	0	162	8
8	218	0	183	5
9	231	0	197	4
10	240	0	212	2
11	245	0	217	1
12	247	0	225	1
13	249	0	233	0
14	250	0	237	0
15	250	0	243	0
16	250	0	248	0
17	250	0	249	0
19	250	0	250	0

**Table 4. 2: Collected Accepted and Rejected Gaps for Passenger Cars at SH288@ McHard**

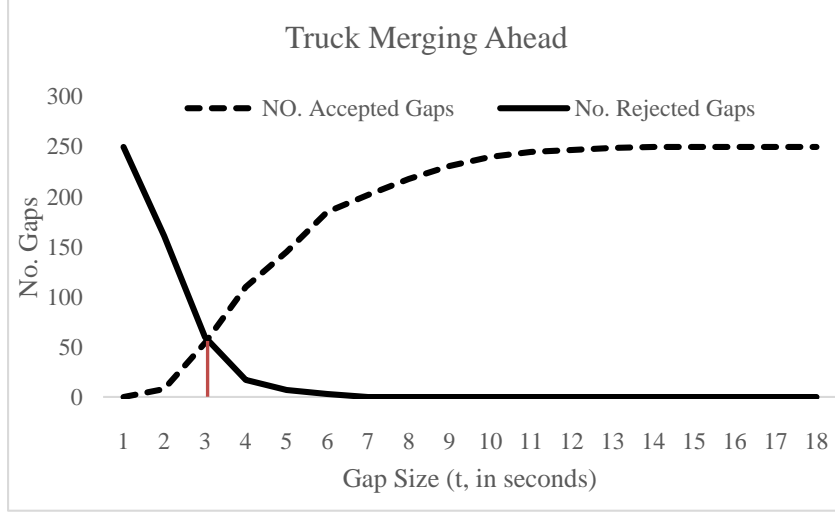
Length of Gap t (Seconds)	Merging Ahead		Merging Behind	
	No. Accept Gaps<t	No. Reject Gaps>t	No. Accept Gaps<t	No. Reject Gaps>t
0	0	250	0	250
$\Delta t = 1$	0	249	1	248
2	50	149	40	160
3	120	47	125	54
4	164	25	187	22
5	197	11	224	4
6	220	4	236	0
7	239	2	241	0
8	244	1	245	0
9	248	0	249	0
10	250	0	250	0

## 4.2 Acceleration Lane Length Determination

To determine the acceleration lane length at this study site, the 4-step procedure introduced in the methodology section was used.

### 4.2.1 Estimate the Four Types of Critical Gaps

Based on the collected accepted and rejected gaps at the study site, the four critical gaps for two different types of vehicles with different merging behaviors can be estimated. As we mentioned before, a critical gap is a gap where the probability of accepting such gap is equal to the probability of rejecting such gap. Using the truck merging ahead event as an example, Figure 4.2 can be developed based on the collected accepted and rejected gaps for the “truck merging ahead” event presented in Table 4.1. In Figure 4.2, the two curves represent the numbers of accepted and rejected gaps at different sizes. The critical gap for merging ahead heavy truck ( $T_a^{HT}$ ) can be determined according to the intersection point of these two curves as shown in Figure 4.2.



**Figure 4. 2: Estimation of critical gaps for study location**

Using this method, the critical gaps for merging ahead heavy truck, merging behind heavy truck, merging ahead passenger car, merging behind passenger car can be obtained and are listed as follows.

- $T_a^{PC}$  (the critical gap for merging ahead passage cars): 2.58s
- $T_b^{PC}$  (the critical gap for merging behind passage cars): 2.63s
- $T_a^{HT}$  (the critical gap for merging ahead heavy trucks): 3.06s
- $T_b^{HT}$  (the critical gap for merging behind heavy trucks): 3.47s

#### 4.2.2 Estimate Merging Delay

Based on the estimated critical gaps and the observed average freeway traffic volume at this location, i.e. 740vph/ln ( $q = 0.21$ vps/ln), the merging delays for different types of merging events (merging ahead and merging behind) and different types of vehicles (heavy trucks and passage cars) can be estimated by using Equation 11 as follows:

$$d_a^{HT} = \frac{e^{q \times 3.06} - q \times 3.06 - 1}{q(1 - e^{-q \times 3.06})} = \frac{e^{0.21 \times 3.06} - 0.21 \times 3.06 - 1}{0.21 \times (1 - e^{-0.21 \times 3.06})} = 2.60s$$

$$d_b^{HT} = \frac{e^{q \times 3.47} - q \times 3.47 - 1}{q(1 - e^{-q \times 3.47})} = \frac{e^{0.21 \times 3.47} - 0.21 \times 3.47 - 1}{0.21 \times (1 - e^{-0.21 \times 3.47})} = 3.16s$$

$$d_a^{PC} = \frac{e^{q \times 2.58} - q \times 2.58 - 1}{q(1 - e^{-q \times 2.58})} = \frac{e^{0.21 \times 2.58} - 0.21 \times 2.58 - 1}{0.21 \times (1 - e^{-0.21 \times 2.58})} = 2.01s$$

$$d_b^{PC} = \frac{e^{q \times 2.63} - q \times 2.63 - 1}{q(1 - e^{-q \times 2.63})} = \frac{e^{0.21 \times 2.63} - 0.21 \times 2.63 - 1}{0.21 \times (1 - e^{-0.21 \times 2.63})} = 2.07s$$

#### 4.2.3 Estimate Freeway Acceleration Lane Length

As we mentioned before, at this location, the ramp design speed  $V_r$  is 17.8mps (40mph) and freeway design speed  $V_f$  is 26.7mps (60mph). Then, according to the estimated merging delays, the acceleration lane length for different types of merging behaviors (merging ahead and merging behind) and different types of vehicles (heavy trucks and passage cars) can be estimated by using Equation 2 and 3 as follows:

$$L_a^{HT} = L_{1a}^{HT} + L_{2a}^{HT} = \frac{V_a^2 - V_r^2}{2a} + V_a d_a = \frac{29.1^2 - 17.8^2}{2 \times 0.9} + 29.1 \times 2.60 = 370m$$

$$L_b^{HT} = L_{1b}^{HT} + L_{2b}^{HT} = \frac{V_b^2 - V_r^2}{2a} + V_b d_b = \frac{20.11^2 - 17.8^2}{2 \times 0.26} + 20.11 \times 3.16 = 231m$$

$$L_a^{PC} = L_{1a}^{PC} + L_{2a}^{PC} = \frac{V_a^2 - V_r^2}{2a} + V_a d_a = \frac{29.1^2 - 17.8^2}{2 \times 2.28} + 29.1 \times 2.01 = 175m$$

$$L_b^{PC} = L_{1b}^{PC} + L_{2b}^{PC} = \frac{V_b^2 - V_r^2}{2a} + V_b d_b = \frac{20.11^2 - 17.8^2}{2 \times 0.62} + 20.11 \times 2.07 = 112m$$

#### 4.2.4 Estimate Freeway Acceleration Lane Length

Finally, the recommended acceleration lane length for this location should be discussed in two separate situations, considering heavy trucks and without considering heavy trucks. If heavy trucks are considered in the design of acceleration lane, then

$$L^{HT} = \max(L_a^{HT}, L_b^{HT}) = 370m$$

If heavy trucks are not considered in the design of acceleration lane, then

$$L^{PC} = \max(L_a^{PC}, L_b^{PC}) = 175m$$

Both estimated freeway acceleration lane lengths, i.e.  $L^{HT}$  and  $L^{PC}$ , are longer than the recommended acceleration lane length provided by the AASHTO Green Book (2011) for the freeway and ramp at the given design speeds ( $V_f = 60\text{mph}$ ,  $V_r = 40\text{mph}$ ), which is 168m (550ft). This result is reasonable because the required distance for searching for an acceptable gap and the operation characteristics of heavy trucks were not considered in the current AASHTO guidelines. Thus, it tends to underestimate the required length for the freeway acceleration lanes.

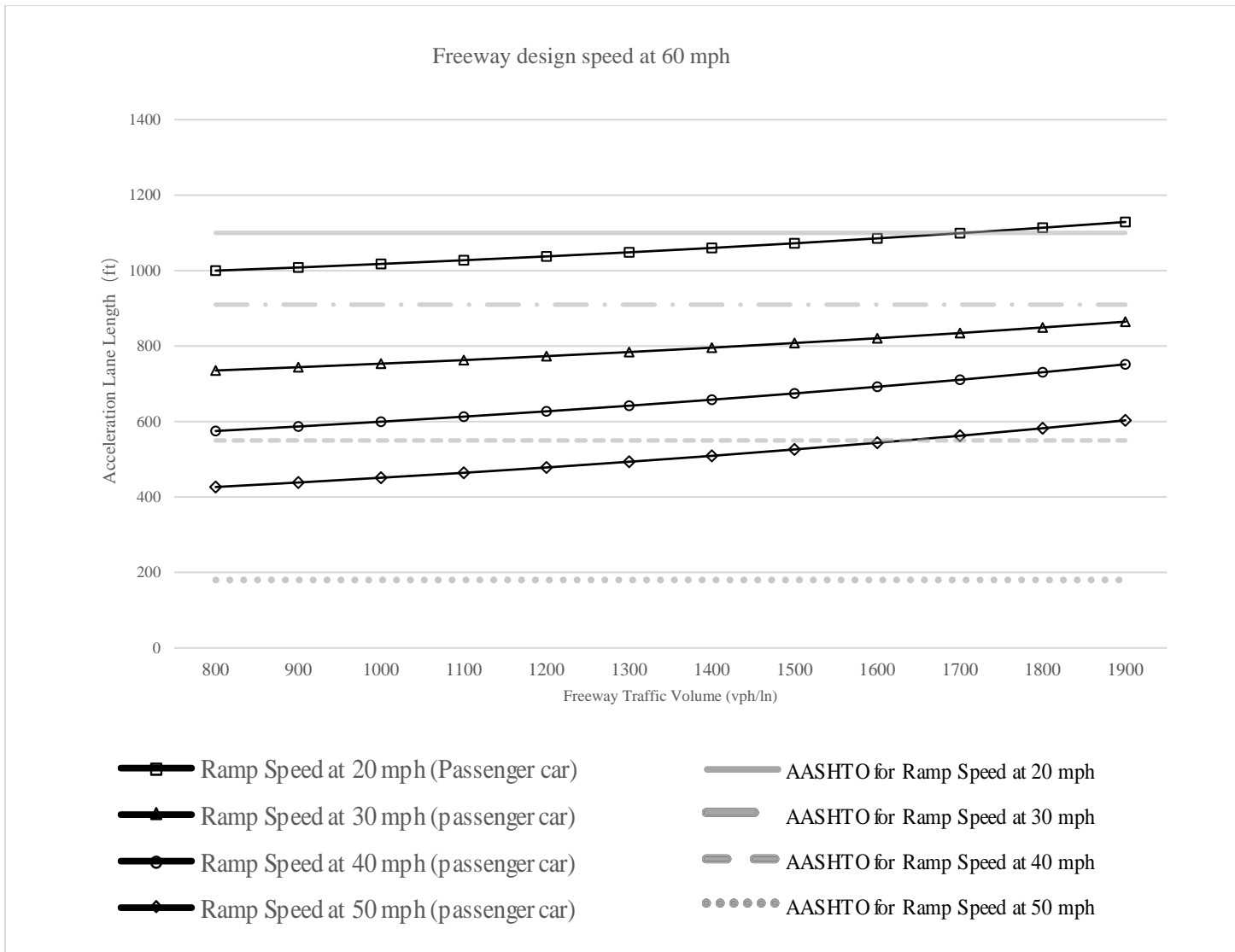
## Chapter 5. Guidelines on Freeway Acceleration Lane Lengths under Different Traffic Volume Conditions

As mentioned before, most of the existing methods, including the AASHTO Green Book (2011) guidelines, did not consider the effects of the traffic volume on determining the required lengths of freeway acceleration lanes. Based on the model developed by this research, new guidelines on the required freeway acceleration lane lengths under different traffic volume conditions were developed and presented in Figure 4. Note that, a special set of guidelines on the required freeway acceleration lane lengths for the safe merging of heavy trucks was provided for the locations where heavy truck safety need to be considered in the freeway design. In developing these guidelines, the four critical gaps ( $T_a^{PC}$ ,  $T_b^{PC}$ ,  $T_a^{HT}$  and  $T_b^{HT}$ ) collected by this study was used for calculating the required freeway acceleration lane lengths.

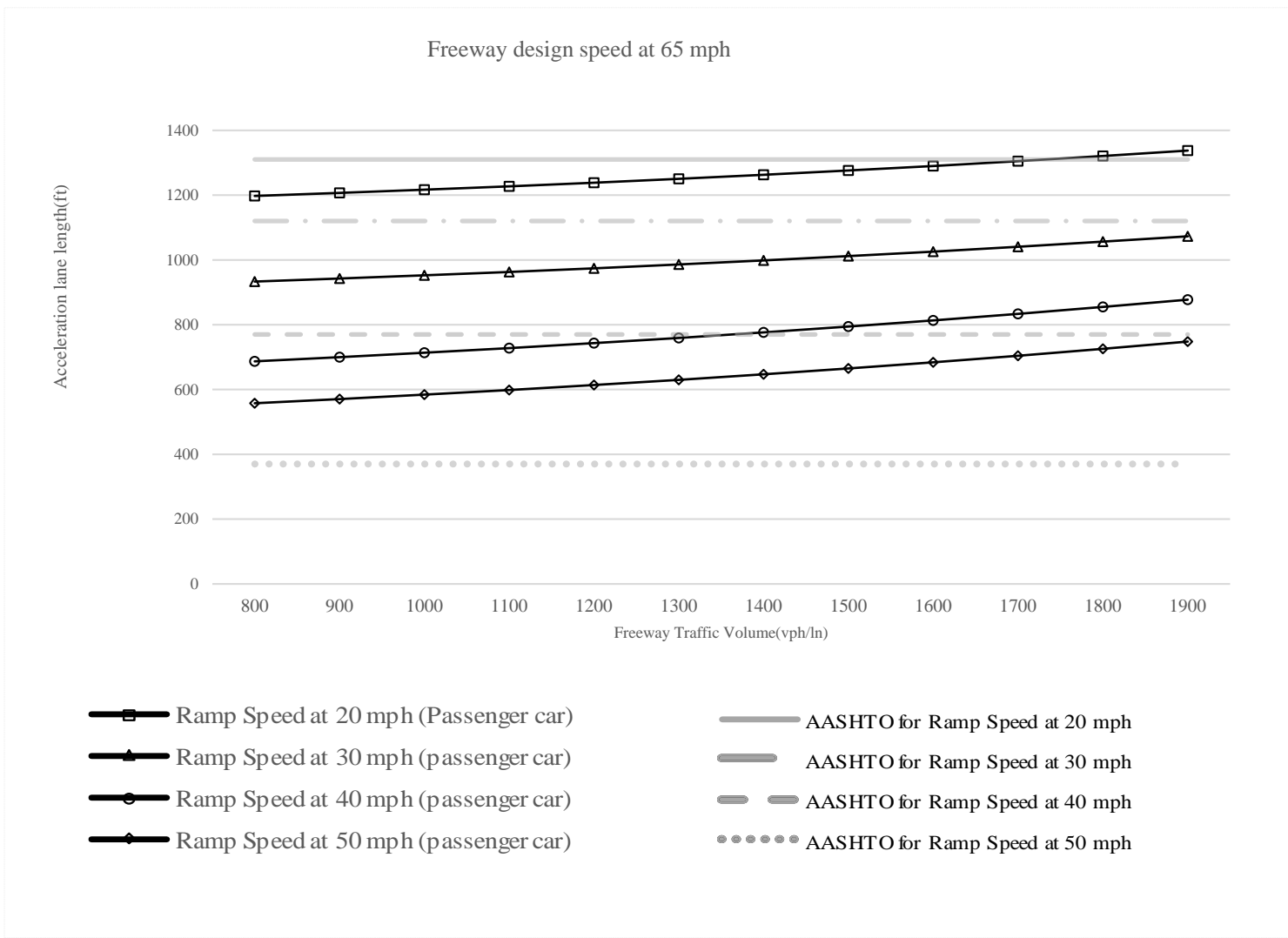
From Figure 4, it can be seen that for all the cases, there is at least 10 percent increase of acceleration lane length as traffic volume increases from 800 vph/ln to 1900 vph/ln. These results indicated that the required acceleration lane length is sensitive to the change in traffic volume. It is reasonable because higher traffic volume on a freeway will result in fewer numbers of acceptable gaps and longer merging distance for the on-ramp merging vehicles. Therefore, a longer acceleration lane should be provided at the locations with higher traffic volumes.

In addition, longer acceleration lane lengths are required for accommodating the merging of the heavy truck. This is also reasonable because heavy trucks need more time to accelerate and to find a larger gap to merge comparing with passenger cars. Furthermore, the speed differential between the freeway and the on-ramp also has a significant impact on the required acceleration lane length. As the speed differential increases, the required acceleration lane length also increases because a longer time is needed for merging vehicles to accelerate to the designed freeway speed. Overall, the developed guidelines can reasonably reflect the impacts of traffic volume, heavy vehicle operation characteristics and other influencing factors on the determination of the required lengths of freeway acceleration lanes. Finally, by comparing the developed guidelines with the existing guidelines, i.e. AASHTO guidelines, it was found that overall, the developed guidelines are comparable with the AASHTO guidelines when only considering passenger cars. The recommended acceleration lane length is higher than what recommended by AASHTO guidelines when the traffic volume is high and it becomes significantly higher than what recommended by AASHTO guidelines when considering heavy trucks.

To facilitate the implementation of the developed guidelines, a lookup table that summarized the recommended freeway acceleration lane lengths under different traffic volume conditions (Table 5.1 and Table 5.2) were also developed based on the results presented in Figure 5.1 and Figure 5.2.

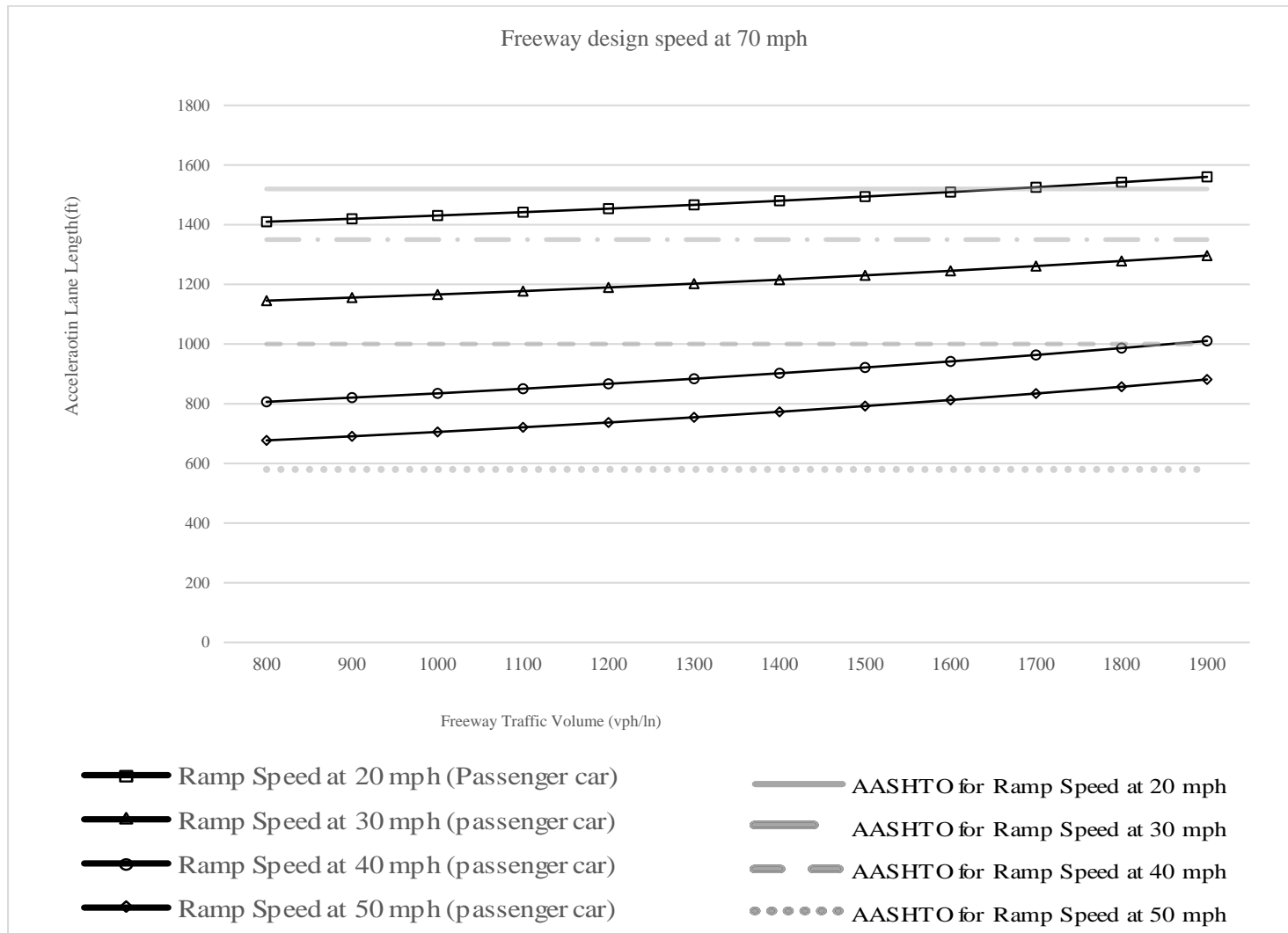


**Figure 5. 1: Recommended freeway acceleration lane lengths when only considering passenger cars ( $L^{PC}$ ) for freeway design speed at 60 mph**



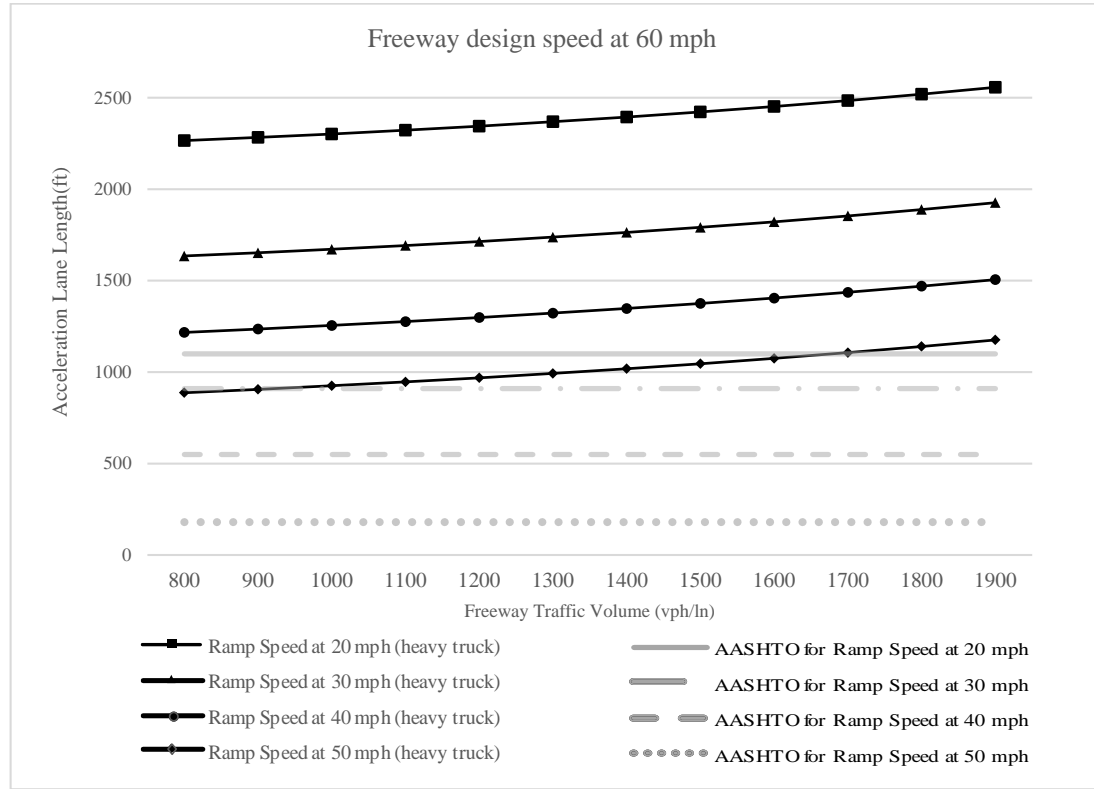
**Figure 5. 2: Recommended freeway acceleration lane lengths when only considering passenger cars ( $L^{PC}$ ) for freeway design speed at 65 mph**





**Figure 5. 3: Recommended freeway acceleration lane lengths when only considering passenger cars ( $L^{PC}$ ) for freeway design speed at 70 mph**

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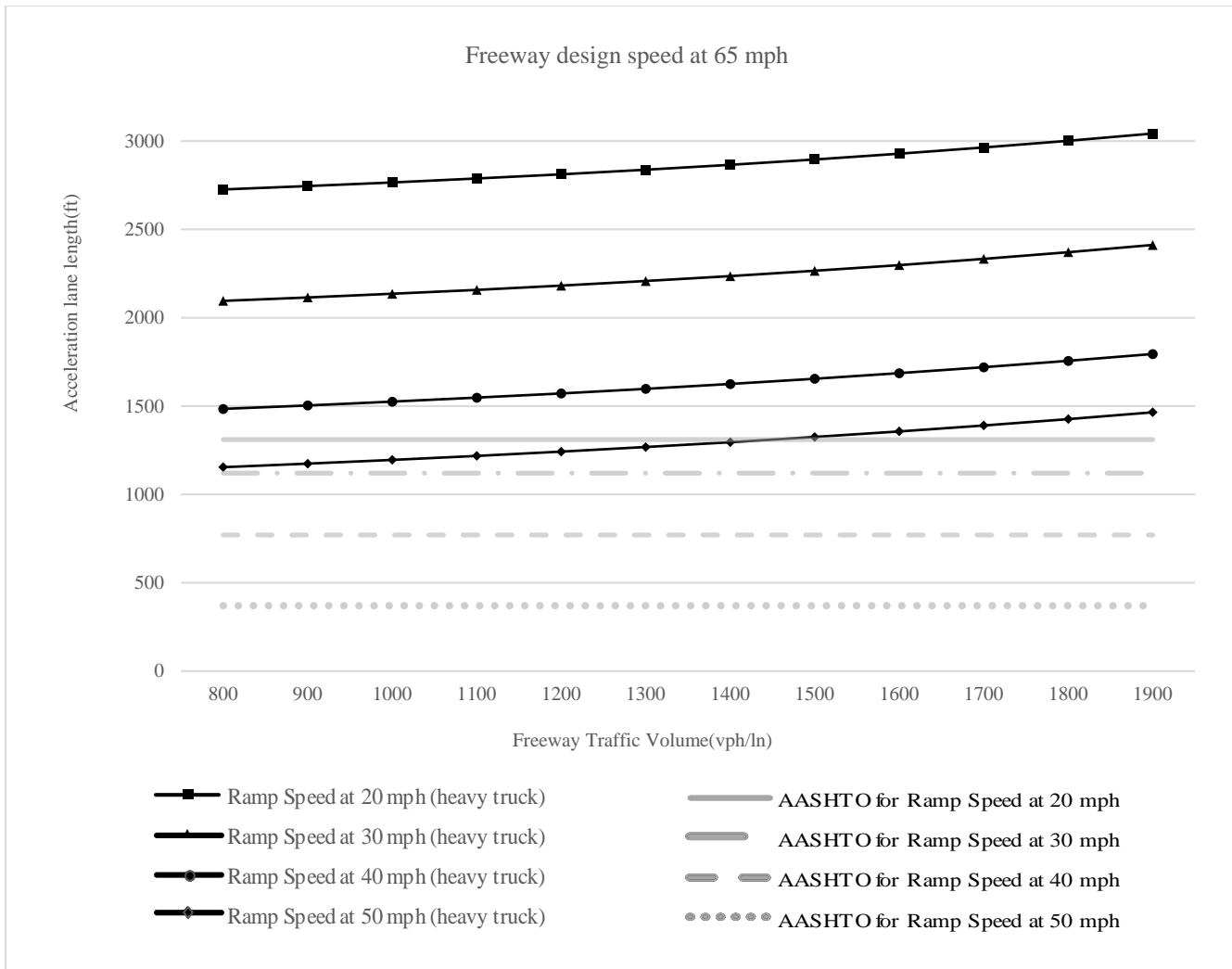


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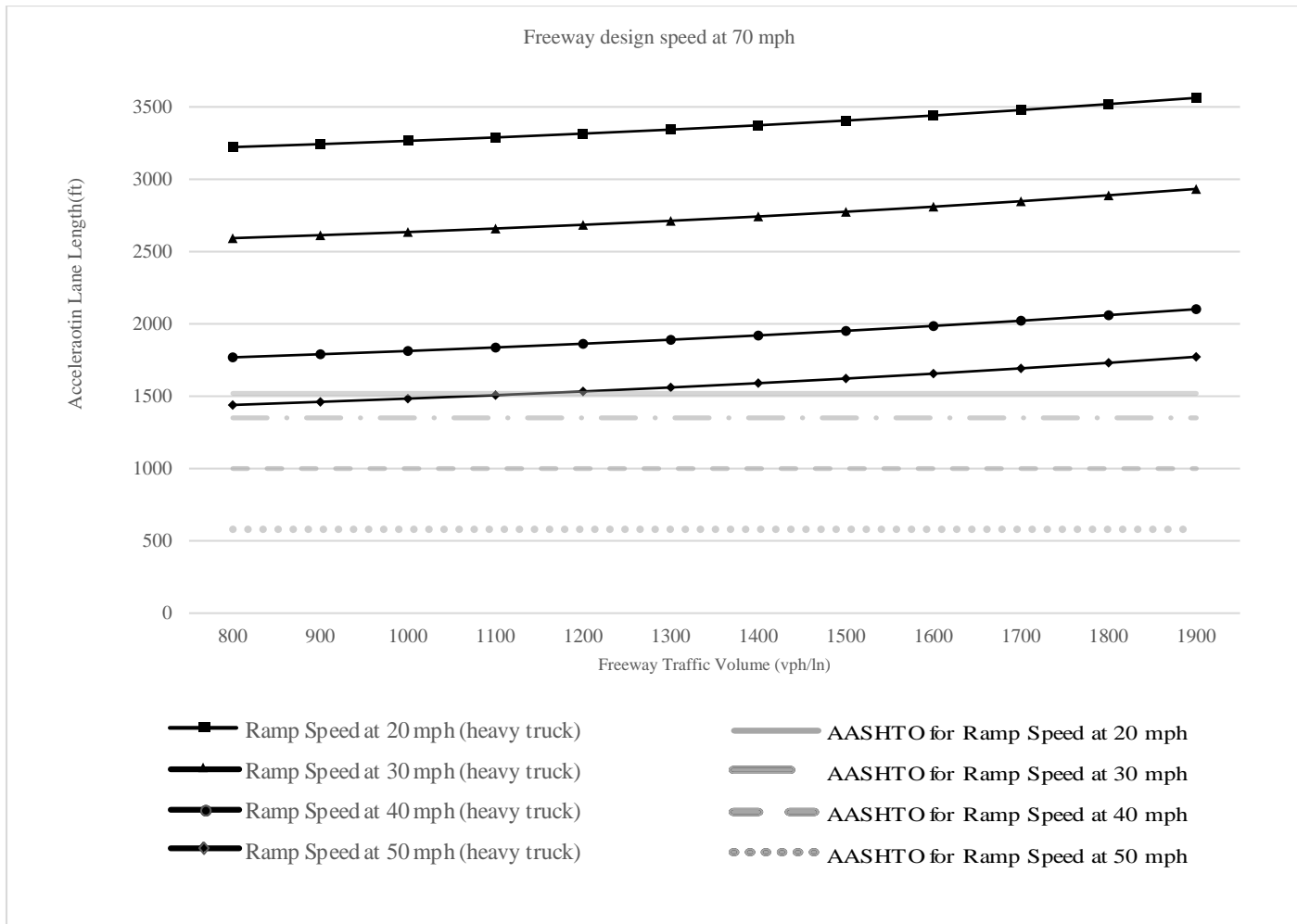
Figure 5. 4: Recommended freeway acceleration lane lengths when considering heavy trucks ( $L^{HT}$ ) for freeway design speed at 60 mph



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Figure 5. 5: Recommended freeway acceleration lane lengths when considering heavy trucks ( $L^{HT}$ ) for freeway design speed at 65 mph



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Figure 5. 6: Recommended freeway acceleration lane lengths when considering heavy trucks ( $L^{HT}$ ) for freeway design speed at 70 mph

**Table 5. 1: Recommended Freeway Acceleration Lane Lengths for Passenger Cars (in ft)**

Freeway Speeds	Volume (vph/ln)	Ramp Speeds			
		20 mph	30 mph	40 mph	50 mph
<b>60 mph</b>	<b>800</b>	1000	735	575	426
	<b>900</b>	1009	744	587	438
	<b>1000</b>	1018	753	599	451
	<b>1100</b>	1027	763	613	464
	<b>1200</b>	1038	773	627	478
	<b>1300</b>	1049	784	642	493
	<b>1400</b>	1060	796	658	509
	<b>1500</b>	1072	808	674	526
	<b>1600</b>	1085	821	692	544
	<b>1700</b>	1099	835	711	562
	<b>1800</b>	1114	849	731	582
<b>1900</b>	1129	865	752	603	
<b>65 mph</b>	<b>800</b>	1197	933	687	558
	<b>900</b>	1207	942	700	571
	<b>1000</b>	1217	952	714	584
	<b>1100</b>	1227	963	728	599
	<b>1200</b>	1238	974	743	614
	<b>1300</b>	1250	986	759	630
	<b>1400</b>	1263	998	776	647
	<b>1500</b>	1276	1012	794	665
	<b>1600</b>	1290	1026	813	684
	<b>1700</b>	1305	1041	834	704
	<b>1800</b>	1321	1056	855	726
<b>1900</b>	1337	1073	878	748	
<b>70 mph</b>	<b>800</b>	1410	1146	807	677
	<b>900</b>	1420	1156	820	691
	<b>1000</b>	1431	1166	835	705
	<b>1100</b>	1442	1178	850	721
	<b>1200</b>	1454	1190	867	737
	<b>1300</b>	1467	1202	884	754
	<b>1400</b>	1480	1216	902	773
	<b>1500</b>	1495	1230	921	792
	<b>1600</b>	1510	1245	942	812
	<b>1700</b>	1526	1261	963	834
<b>1800</b>	1543	1278	986	857	

	<b>1900</b>	1561	1296	1011	881
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**Table 5. 2: Recommended Freeway Acceleration Lane Lengths for Heavy Trucks (in ft)**

Freeway Speeds	Volume (vph/ln)	Ramp Speeds			
		20 mph	30 mph	40 mph	50 mph
<b>60 mph</b>	<b>800</b>	2265	1635	1217	887
	<b>900</b>	2283	1652	1235	906
	<b>1000</b>	2301	1671	1255	925
	<b>1100</b>	2322	1692	1276	946
	<b>1200</b>	2344	1714	1298	968
	<b>1300</b>	2368	1738	1322	993
	<b>1400</b>	2394	1764	1348	1018
	<b>1500</b>	2422	1791	1375	1046
	<b>1600</b>	2452	1821	1405	1075
	<b>1700</b>	2484	1854	1436	1106
	<b>1800</b>	2519	1889	1470	1140
<b>1900</b>	2557	1926	1506	1176	
<b>65 mph</b>	<b>800</b>	2726	2096	1484	1154
	<b>900</b>	2745	2115	1504	1174
	<b>1000</b>	2766	2136	1525	1195
	<b>1100</b>	2788	2158	1547	1218
	<b>1200</b>	2812	2182	1572	1242
	<b>1300</b>	2838	2208	1597	1268
	<b>1400</b>	2866	2236	1625	1295
	<b>1500</b>	2896	2266	1655	1325
	<b>1600</b>	2929	2298	1686	1356
	<b>1700</b>	2964	2333	1720	1390
	<b>1800</b>	3002	2371	1756	1426
<b>1900</b>	3042	2412	1795	1465	
<b>70 mph</b>	<b>800</b>	3223	2593	1769	1439
	<b>900</b>	3244	2613	1790	1461
	<b>1000</b>	3266	2635	1813	1483
	<b>1100</b>	3290	2659	1837	1507
	<b>1200</b>	3316	2685	1863	1533
	<b>1300</b>	3343	2713	1891	1561
	<b>1400</b>	3374	2743	1920	1591
	<b>1500</b>	3406	2776	1952	1622
	<b>1600</b>	3441	2811	1986	1656
	<b>1700</b>	3479	2848	2022	1692
<b>1800</b>	3520	2889	2061	1731	

	<b>1900</b>	3564	2933	2102	1772
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## Chapter 6. Conclusions

In this study, an analytical model was developed for estimating the freeway acceleration lane length for vehicle safe merging. To develop this model, a thorough literature review was conducted, which includes two parts: 1) the existing design guidelines on freeway acceleration lane and 2) the existing methods for estimating the freeway acceleration lane length. The model developed by this study considers both the acceleration and the gap searching needs of the vehicles during the merging process. Thus, it can take account of the impacts of freeway traffic volume on the required acceleration lane lengths, which fills a gap in the existing studies. In addition, heavy trucks and passenger vehicles are treated differently in the developed model since they have significantly different operational characteristics. Beside the developed model, this study also had the following key findings:

- There are two types of merging behaviors: merging ahead and merging behind. The critical gaps for different types of merging behaviors and different types of vehicles are very different. According to the conducted field study, for heavy trucks, the critical gap for merging ahead is about 3.06s and the critical gap for merging behind is about 3.47s; for passenger vehicles, the critical gap for merging ahead is 2.58s and the critical gap for merging behind is 2.63s.
- Freeway traffic volume is an important factor to be considered when determining freeway acceleration lane length. In the case study, with the traffic volume increasing from 800 vph to 1900 vph, the required acceleration lane length increase for more than 10 % for all the cases.

A case study was conducted in Houston, TX to demonstrate the model application. This research provides a chart and a lookup table for estimating required acceleration lane lengths for both heavy trucks and passenger cars under different traffic volume conditions for different combinations of the freeway and entrance ramp design speeds. The results of this research complement the provisions in current roadway design manuals/guidelines in implementing and designing freeway auxiliary lanes.

Note that, the model was developed based on the field study conducted at one typical on-ramp location in Texas. In the future, more field studies with different combinations of ramp speed and freeway speed need to be conducted to further validate the results of this study.

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