

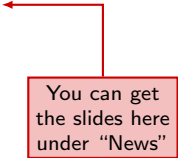
Subregular Syntax

The What, How, and Why

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You can get
the slides here
under "News"

A Mathematical Distinctness Theorem

- ▶ From a computational perspective, there is a split between “P-side” and “S-side”.

regular < context-free < mildly context-sensitive < ...

Phonology

Morphology

Syntax

- ▶ Matches linguistic practice (despite attempts at unification, e.g. DM)
- ▶ Why is syntax the outlier?

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Kaplan and Kay (1994)

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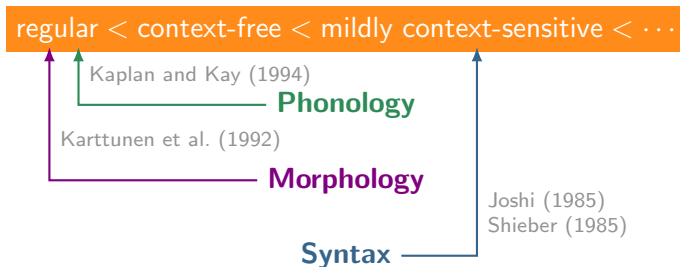
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An Alternative: Simple Syntax

- ▶ The postulated split is misleading.
- ▶ If we probe deeper, we find that
 - ▶ syntax is just as simple,
 - ▶ phonology, morphology, and syntax are weaker than regular \Rightarrow **subregular**
 - ▶ relativized locality plays a major role,
 - ▶ and is approximated by the formal class **TSL**.
- ▶ This has repercussions for
 - ▶ cognitive architecture of language,
 - ▶ learning,
 - ▶ processing.

Outline

- 1** Locality and Tiers in Phonology
 - Tier-Based Strictly Local (TSL)
 - The Cognitive Picture
- 2** c-Command Constraints in Syntax
 - c-Strings
 - The Cognitive Picture
- 3** Syntax
 - Minimalist Grammars
 - Merge is TSL
 - Move is TSL

The Subregular Program

- ▶ **Received view:** class of regular (= finite-state) string languages maximally complex
- ▶ **Subregular hierarchy:** even weaker/simpler subclasses
- ▶ The **tier-based strictly local (TSL)** languages have emerged as particularly important.



**Jeff
Heinz**



**Jane
Chandlee**



**Adam
Jardine**



**Kevin
McMullin**

Example: Word-Final Devoicing

- ▶ Captured by forbidding voiced segments at the end of a word
- ▶ **German**: Don't have **z**\$ or **v**\$ or **d**\$ (where \$ = word edge).

Example: German

*\$ r a d \$

*z\$

*v\$

*d\$

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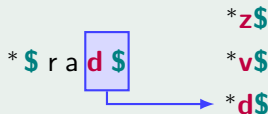
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- ▶ Captured by forbidding voiceless segments between vowels
- ▶ **Suppose:**
 - ▶ $[-\text{voice}] = \{s, f\}$
 - ▶ $V = \{a, i, u\}$
- ▶ **Then:** don't have **asa**, **ajfa**, **asi**, **ajfi**, ...

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A Problem: Samala Sibilant Harmony

- ▶ If multiple sibilants occur in the same word, they must all be +anterior (**s,z**) or –anterior (**ʃ,ʒ**).
- ▶ In other words: Don't mix **purple** and **teal**.

*sʃ *sʒ *zʃ *zʒ
 *ʃs *ʒs *ʃz *ʒz

- ▶ **But:** Sibilants can be arbitrarily far away from each other!

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Making Long-Distance Dependencies Local

- ▶ Let's take a clue from phonology:
create locality with **tiers**.
(Goldsmith 1985; Heinz et al. 2011)
- ▶ Enforce constraints on tier,
rather than string



Jeff Heinz

Example: Samala Revisited

1 Project sibilant tier

2 *sʃ, *sʒ, *zʃ, *zʒ, *ʃs, *ʒs, *ʃz, *ʒz

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			ʃ	l	a	w	a	ʃ
			\$					\$

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*	\$	h	a
	s	x	i
	n	t	i
	l	a	w
	a	ʃ	\$

\$	ʃ	ʃ	\$
\$	h	a	ʃ
	x	i	n
	t	i	l
	a	w	a
	ʃ	\$	\$

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Tier projection controlled by

- 1 label of segment
- 2 local context
- 3 symbols already on tier

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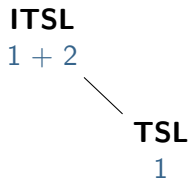
TSL

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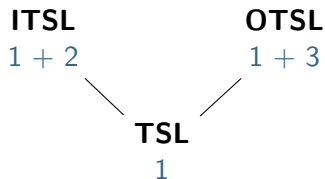
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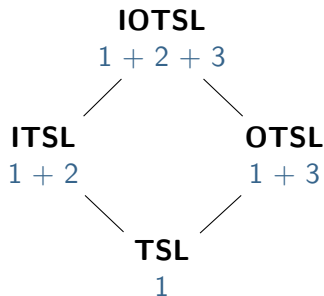
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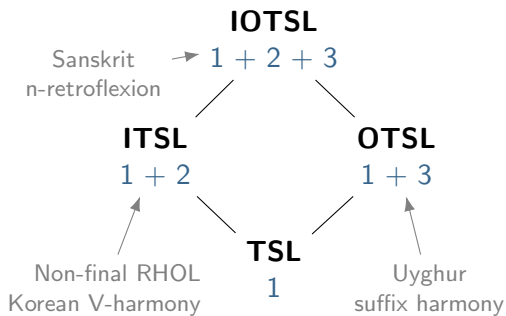
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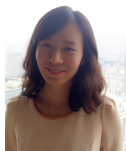
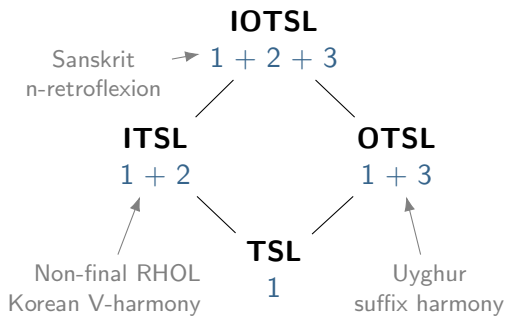
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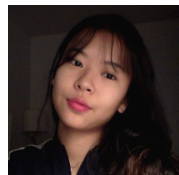
**Hyunah
Baek**



**Aniello
De Santo**



**Connor
Mayer**



**Suji
Yang**

TSL Across Language Modules

- ▶ Phonological dependencies fall within the TSL region.
- ▶ Morphological dependencies do, too.
(Aksënova et al. 2016; Aksënova and De Santo 2017; Chandlee 2017)
- ▶ Phonology and morphology are **computationally similar**.



**Alëna
Aksënova**



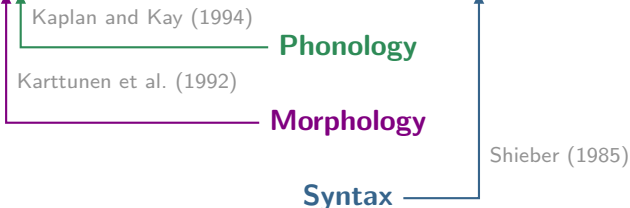
**Sophie
Moradi**

Why is TSL Relevant?

- ▶ Linguistically natural
- ▶ Captures wide range of phonotactic dependencies
- ▶ Correct and efficient learning algorithms
(I/O-TSL work in progress)
(Jardine and McMullin 2017)
- ▶ Low resource demand
 - ▶ remember the last n symbols of a specific type
 - ▶ requires little working memory
 - ▶ no complex memory architecture
- ▶ Rules out unattested patterns
 - ▶ center embedding
 - ▶ harmony only if separated by even number of segments

Could Syntax Also be Subregular?

TSL < regular < context-free < mildly context-sensitive < ...



- ▶ Syntax seems even more like an outlier...
- ▶ Don't look at strings!
What about **syntactic dependencies**?



Nazila Shafiei

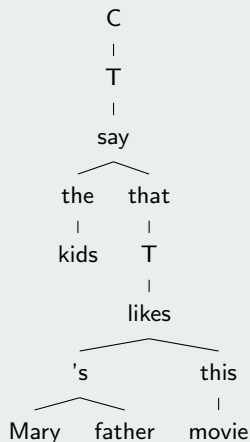
c-Strings

Command-Strings

The **c[ommand]-string** of a node n contains

- ▶ n and
 - ▶ every node that commands n .
-
- ▶ easily computed from dependency trees
 - ▶ c-command constraints seem to be largely **IOTSL over c-strings**

Example



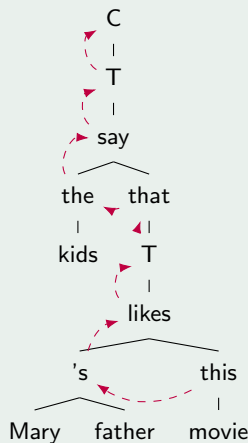
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Example



this 's likes T that the say T C

Principle A

Principle A (as a distributional constraint)

Every reflexive must be c-commanded by a DP in the same TP.

Equivalent c-String Constraint

If the c-string starts with a reflexive,
then at least one D must occur before the first T.

TSL Strategy for Principle A

- 1 Always project first symbol (ITSL)
- 2 Project D/T if previous symbol is Refl (OTSL)
- 3 Constraint: ***Refl** T (bigram)

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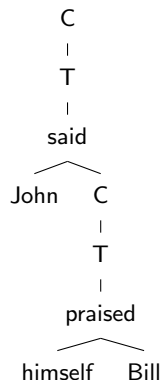
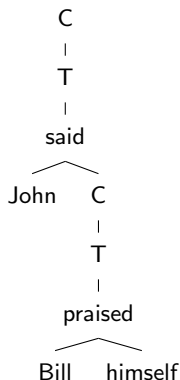
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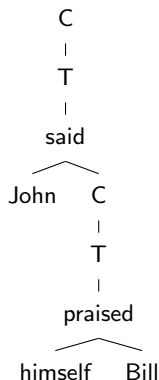
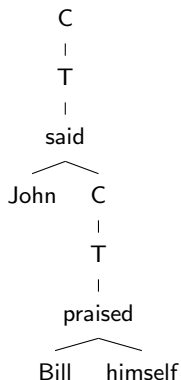
Example of Principle A as a TSL Constraint



\$ **himself** **Bill** \$
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himself **Bill** praised T C ...

\$ **himself** T \$
 | |
himself praised T C ...

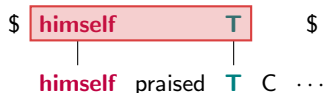
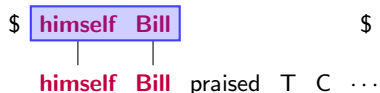
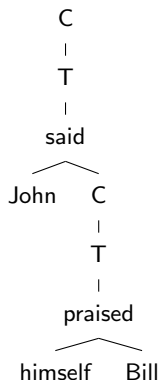
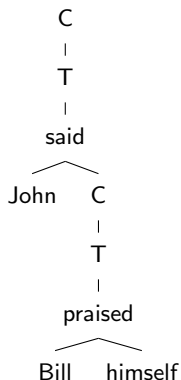
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Another Example: Swedish *sig*

- ▶ Swedish *sig* must be non-locally bound.

- (1) a. John said Bill praised *sig*.
 b. *Bill praised *sig*.

TSL Strategy for *sig*

- 1 Always project first symbol (ITSL)
- 2 Project T if previous symbol is *sig* (OTSL)
- 3 Project D if previous symbol is T (OTSL)
- 4 Constraint: ***sig T \$** (trigram)

\$	sig			T	John	\$		\$	sig			T	\$
	sig	Bill	praised	T	C	John	...		sig	Bill	praised	T	C

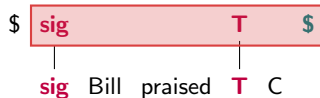
Another Example: Swedish *sig*

- ▶ Swedish *sig* must be non-locally bound.

- (1) a. John said Bill praised *sig*.
 b. *Bill praised *sig*.

TSL Strategy for *sig*

- 1 Always project first symbol (ITSL)
- 2 Project T if previous symbol is *sig* (OTSL)
- 3 Project D if previous symbol is T (OTSL)
- 4 Constraint: ***sig T \$** (trigram)



Comparison to Phonology and Morphology

Similarities

- ▶ mostly bigram and trigram constraints
- ▶ simple structural contexts
- ▶ dependencies in phonology are also c-command-like (Graf 2018a)

Differences

- ▶ OTSL seems more common in syntax

A Typological Prediction

Formal typology of syntactic constraints should mirror phonology and morphology.

Connection to Parsing

- ▶ A tree is well-formed only if each node has a well-formed c-string.
- ▶ verifiable by deterministic top-down tree automaton with finite look-ahead
⇒ **efficient incremental parsing**

An Intriguing Hypothesis

- ▶ Why c-command (rather than, say, precedence)?
 - ▶ Because it allows for more efficient processing!
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- ▶ But syntax isn't just c-command.
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Minimalist Grammars



Ed Stabler

- ▶ Minimalist grammars (MGs) are a formalization of Minimalist syntax. (Stabler 1997, 2011)
- ▶ Operations: **Merge** and **Move**
- ▶ Adopt Chomsky-Borer hypothesis: Grammar is just a finite list of feature-annotated lexical items

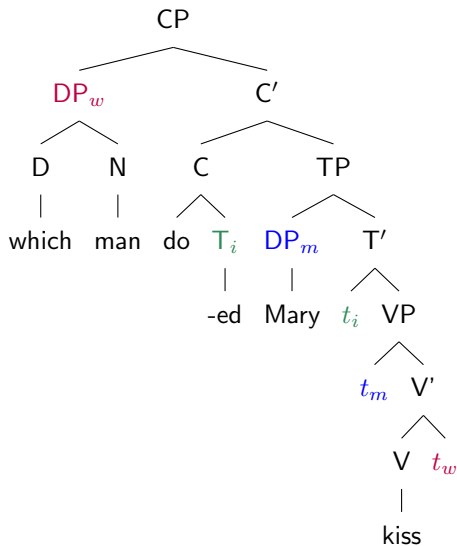
Chemistry

atoms
electrons
molecules

Syntax

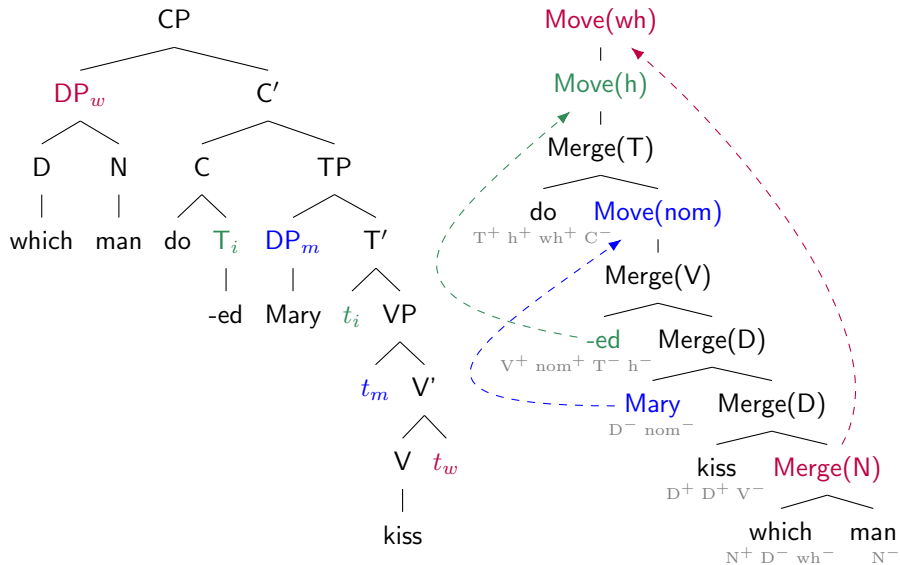
words
features
sentences

MG Syntax in Action



Phrase Structure Tree

MG Syntax in Action



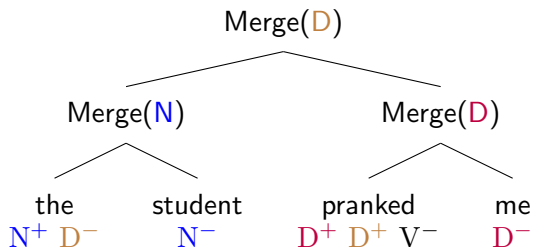
Phrase Structure Tree

Derivation Tree

The Central Role of Derivation Trees

- ▶ Derivation trees are rarely considered in generative syntax.
(but see Epstein et al. 1998)
- ▶ Satisfy Chomsky's structural desiderata:
 - ▶ no linear order
 - ▶ label-free
 - ▶ extension condition
 - ▶ inclusiveness condition
- ▶ Contain all information to produce phrase structure trees
⇒ **central data structure** of Minimalist syntax

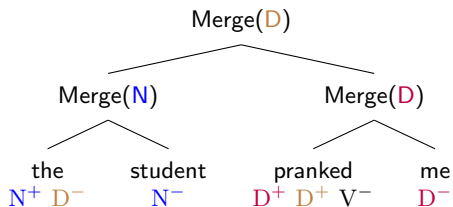
Merge is TSL



- ▶ The selector features of the head have to match the category features of the arguments.
- ▶ 1-to-1 match between selector features and category features.
- ▶ This is naturally expressed as **TSL over trees**.

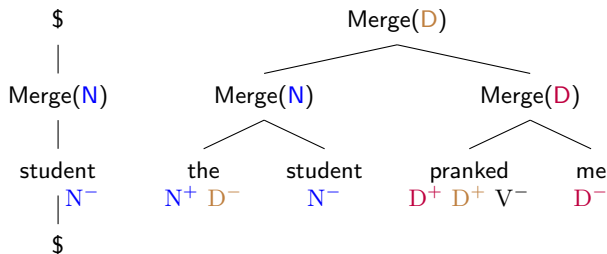
Category Tiers for Merge

- ▶ Project tree tier for each category X .
- ▶ Every X^- has a Merge node as its mother.
- ▶ Every Merge node has exactly one X^- among its daughters.



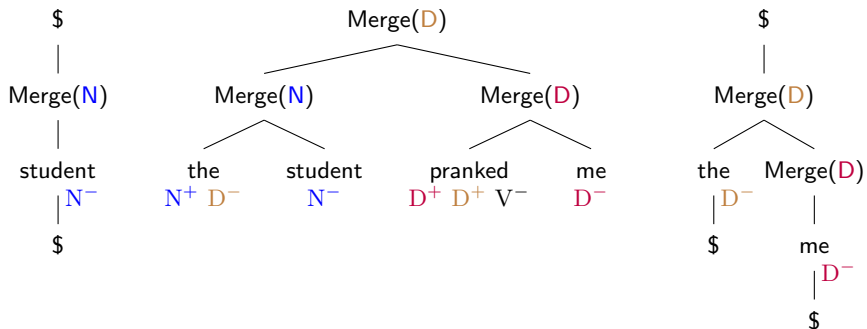
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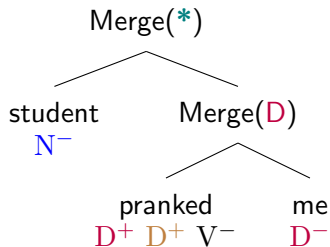


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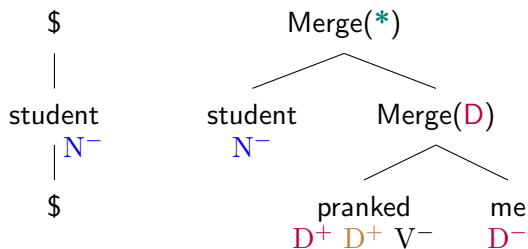


Illicit Merge Yields Ill-Formed Tiers



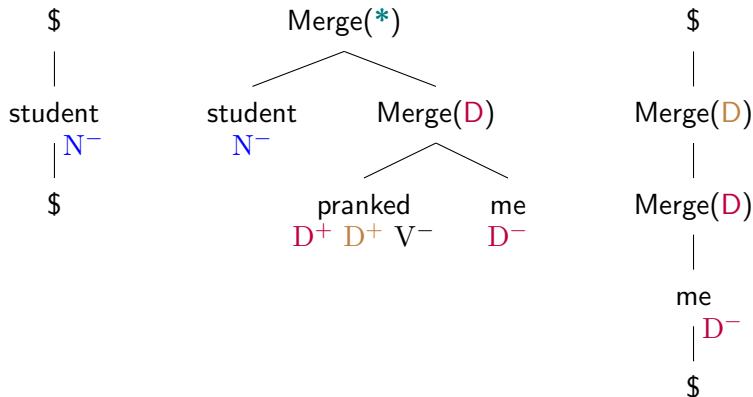
- ▶ This handles Merge.
- ▶ Moving on to Move...

Illicit Merge Yields Ill-Formed Tiers



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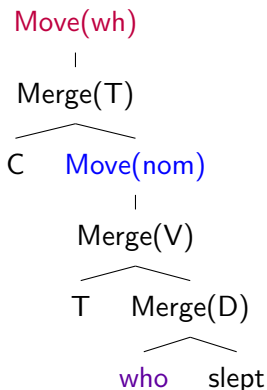
Illicit Merge Yields Ill-Formed Tiers



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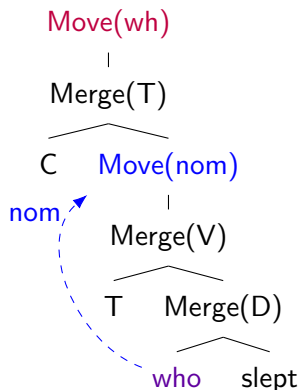
Move: Single Movement Normal Form

- ▶ **Assumption:** every phrase at most one movement feature
- ▶ Intermediate landing sites not feature-triggered
(Graf et al. 2016)



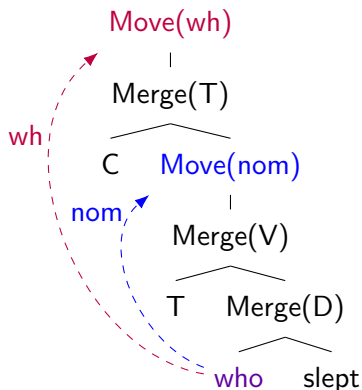
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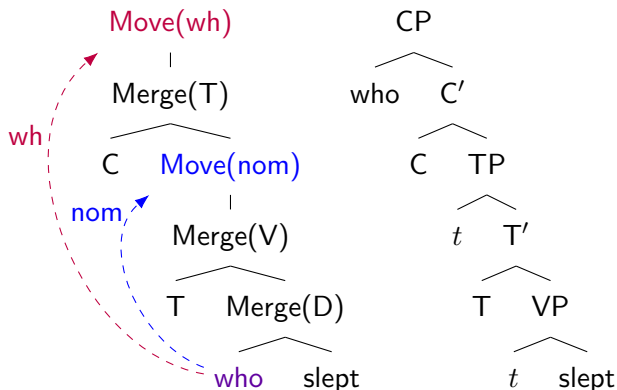
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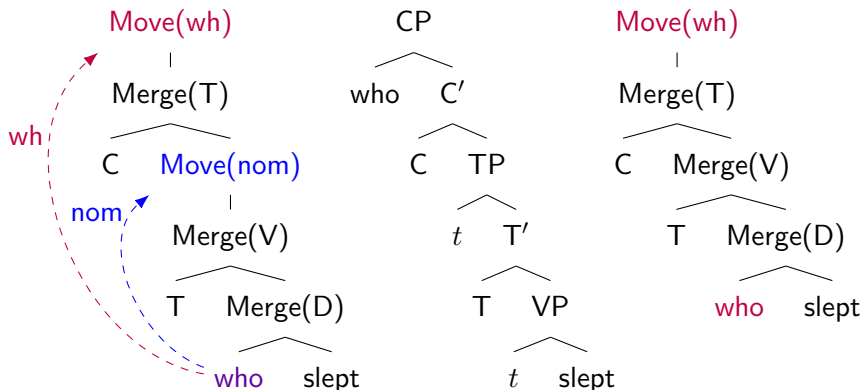
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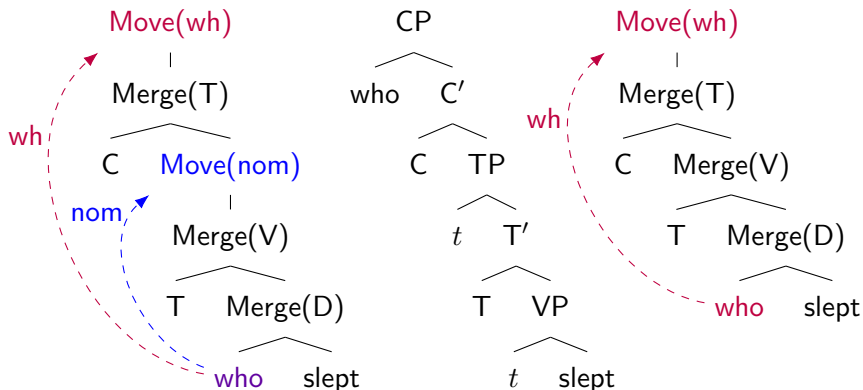
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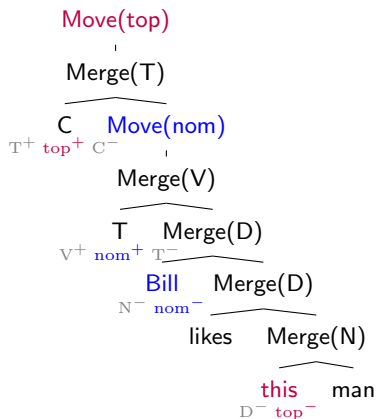
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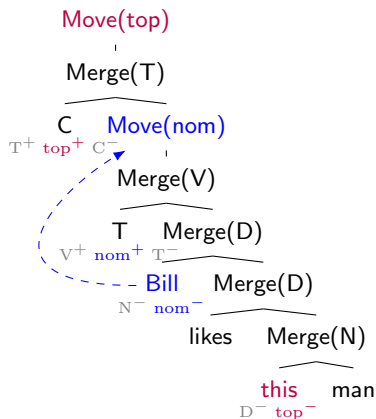
Movement Tiers for Move

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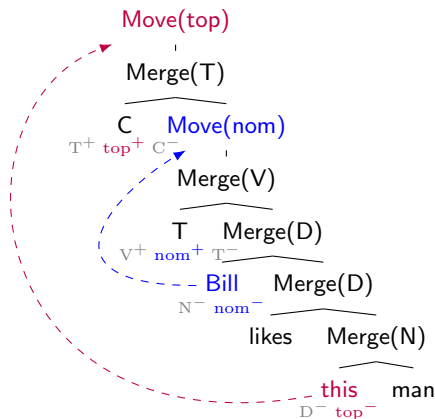
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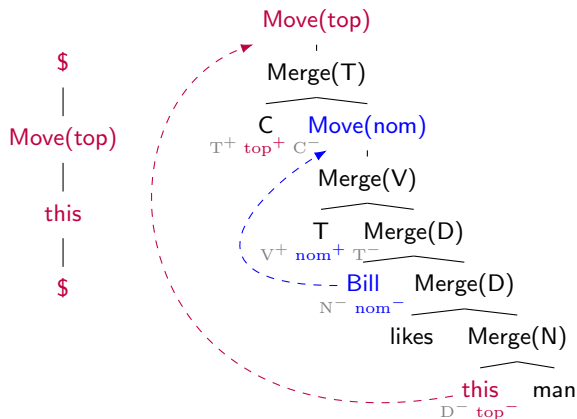
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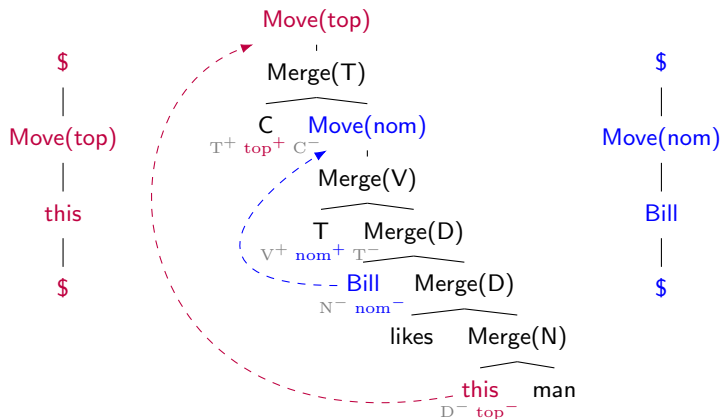
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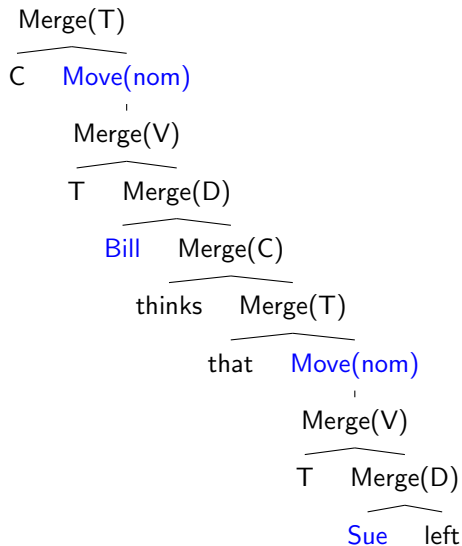


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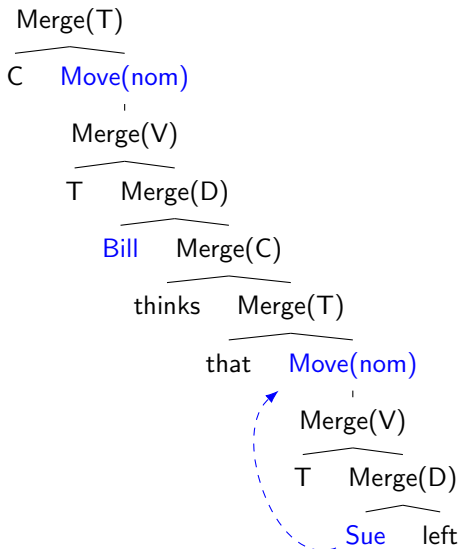
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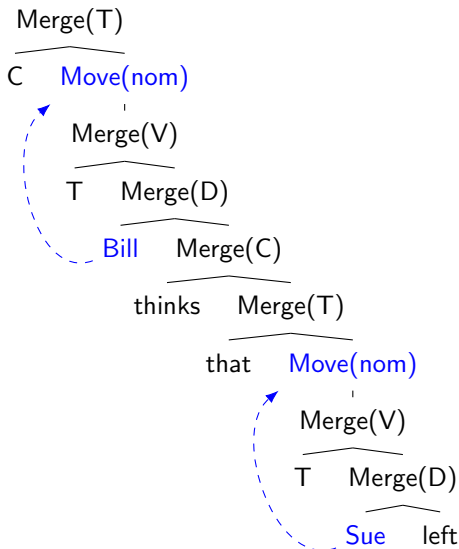
A Tier With Multiple Movers



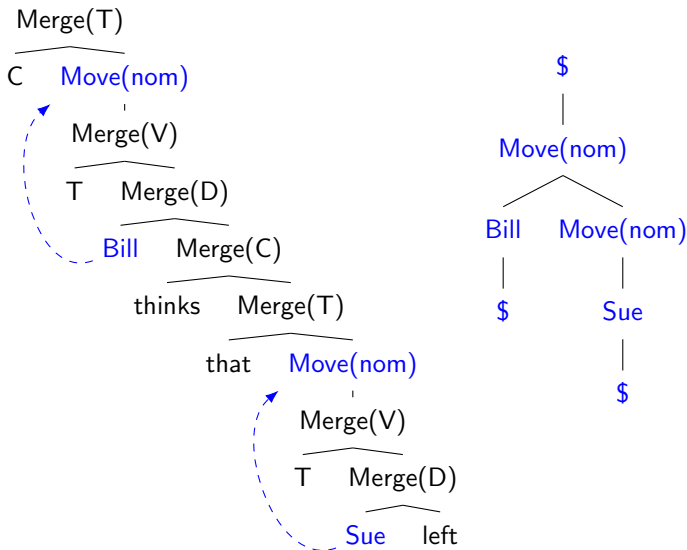
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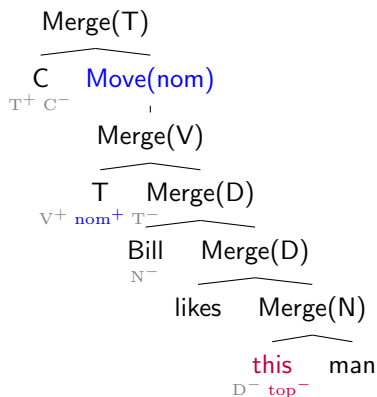
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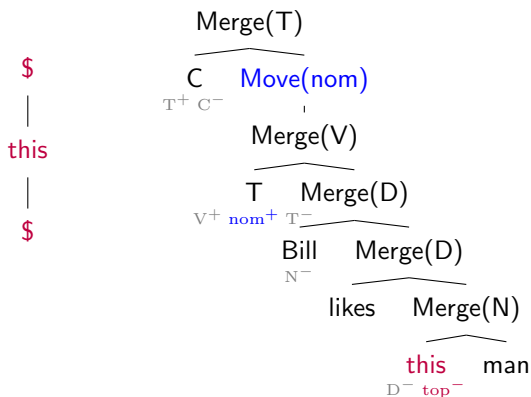
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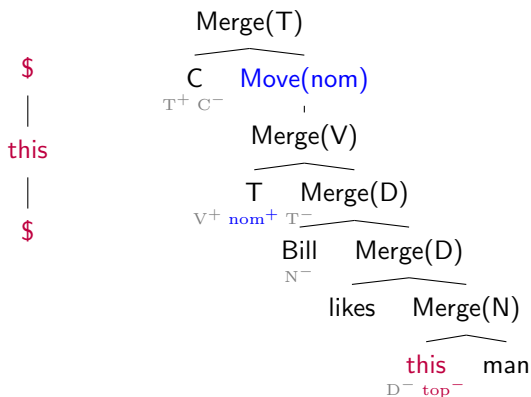
Blocking Simple Cases of Illicit Movement



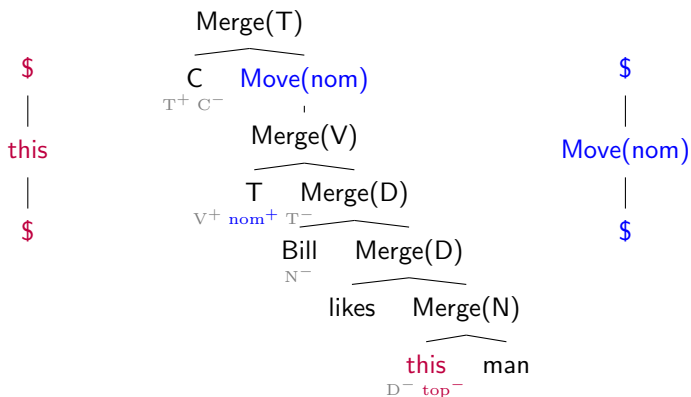
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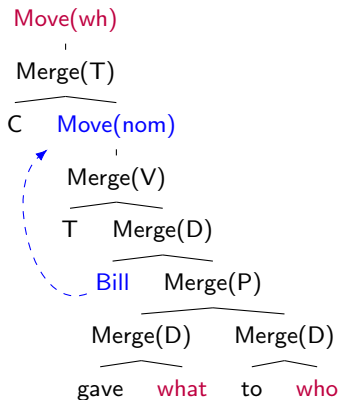
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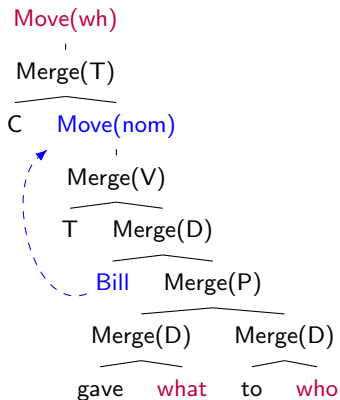
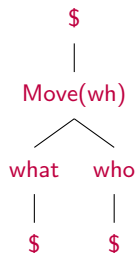
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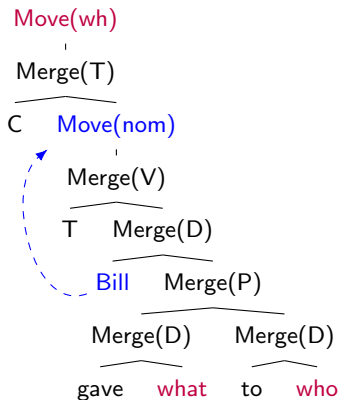
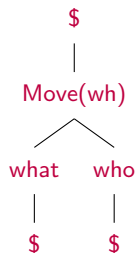
Blocking Many-to-One Movement



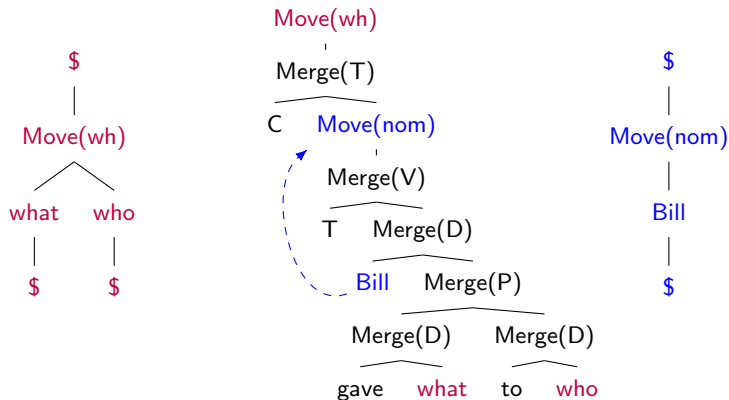
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Blocking Many-to-One Movement



The Common Core of Merge and Move

TSL Strategy for Merge

- ▶ Project tree tier for each **category** X .
- ▶ Every X^- has a **Merge** node as its mother.
- ▶ Every **Merge** node has exactly one X^- among its daughters.

TSL Strategy for Move

- ▶ Project tree tier for each **movement type** x .
- ▶ Every x^- has a **Move** node as its mother.
- ▶ Every **Move** node has exactly one x^- among its daughters.

Note: constraints again **highly local**

Summary

- ▶ Syntax looks like a complex outlier.
- ▶ But not if we choose appropriate representations:
 - ▶ c-command dependencies are TSL over c-strings
 - ▶ Merge and Move are TSL over derivation trees
- ▶ **Computational parallelism:**
 - ▶ phonology is TSL
 - ▶ morphology is TSL
 - ▶ syntax is TSL

Work In Progress

- ▶ **Movement**
 - ▶ Interaction of movement and c-command
 - ▶ Complexity without Single Movement Normal Form
- ▶ **Empirical work**
 - ▶ limits of c-string constraints
 - ▶ unified treatment of island constraints
 - ▶ modeling specific phenomena (e.g. case assignment)
- ▶ **Processing & Learning**
 - ▶ compiling c-string constraints into MG parser
 - ▶ learning via semantic bootstrapping



Sabine Laszakovits



Mai Ha Vu

Open Issues

- ▶ experimental evidence for computational parallelism
- ▶ even tighter subclasses of TSL
- ▶ full predicted typology
- ▶ model concrete aspects of acquisition

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Join the program!

Resources and Readings

- 1 Survey papers:** Pullum and Rogers (2006); Heinz (2011a,b, 2018); Rogers and Pullum (2011); Chandlee and Heinz (2016)
- 2 TSL and its extensions:** Heinz et al. (2011); McMullin (2016); Baek (2017); De Santo (2017); De Santo and Graf (2017); Graf (2017c); Graf and Mayer (2018); Mayer and Major (2018); Yang (2018)
- 3 TSL morphology:** Aksënova et al. (2016); Graf (2017b)
- 4 TSL morpho-semantics:** Graf (2017d)
- 5 TSL syntax:** Graf (2012a, 2018b); Graf and Shafiei (2019); Vu (2018); Vu et al. (2019)
- 6 Mappings:** Courcelle and Engelfriet (2012); Chandlee (2014, 2017); Jardine (2016)
- 7 Learnability:** Heinz (2010); Kasprzik and Kötzing (2010); Heinz et al. (2012); Jardine et al. (2014); Lai (2015); Jardine and Heinz (2016); Jardine and McMullin (2017)

Appendix

Psychological Reality of Derivation Trees

Central role of derivation trees backed up by **processing data**:

- ▶ Derivation trees can be parsed top-down (Stabler 2013)
- ▶ Parsing models update Derivational Theory of Complexity, make correct processing predictions for
 - ▶ right < center embedding (Kobele et al. 2013)
 - ▶ crossing < nested dependencies (Kobele et al. 2013)
 - ▶ SC-RC < RC-SC (Graf et al. 2017)
 - ▶ SRC < ORC in English (Graf et al. 2017)
 - ▶ SRC < ORC in East-Asian (Graf et al. 2017)
 - ▶ quantifier scope preferences (Pasternak 2016)
 - ▶ stacked relative clauses (Zhang 2017)
 - ▶ Korean attachment ambiguities

Technical Fertility of Derivation Trees

Derivation trees made it easy for MGs to accommodate the full syntactic toolbox:

- ▶ sideways movement (Stabler 2006; Graf 2013)
- ▶ affix hopping (Graf 2012b, 2013)
- ▶ clustering movement (Gärtner and Michaelis 2010)
- ▶ tucking in (Graf 2013)
- ▶ ATB movement (Kobele 2008)
- ▶ copy movement (Kobele 2006)
- ▶ extraposition (Hunter and Frank 2014)
- ▶ Late Merge (Kobele 2010; Graf 2014a)
- ▶ Agree (Kobele 2011; Graf 2012a)
- ▶ adjunction (Fowlie 2013; Graf 2014b; Hunter 2015)
- ▶ TAG-style adjunction (Graf 2012c)

Even More MG Extensions

- ▶ local and global constraints (Kobele 2011; Graf 2012a, 2017a)
- ▶ transderivational constraints (Graf 2010, 2013)
- ▶ Principle A and B (Graf and Abner 2012)
- ▶ GPSG-style feature percolation (Kobele 2008)
- ▶ idioms (Kobele 2012)
- ▶ grafts (multi-rooted multi-dominance trees) (Graf in progress)

Long Story Short

Derivation trees are a more useful and fertile data structure than phrase structure trees.

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